# Reinforcement Leanring and Its Applications for NLP

Reporter: Li Guanlin, Li Xintong, Wang Zhi

Al Lab, Tencent

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- Actor-critic style
- Value function fitting

### RL for NLP

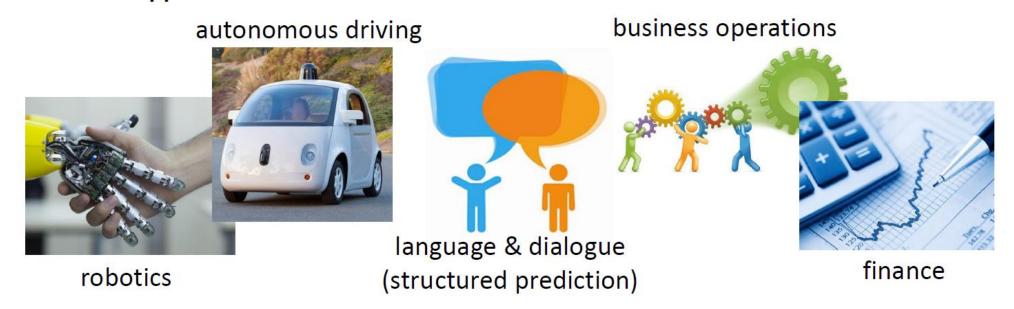
- An actor-critic algorithm for sequence prediction
- Decoding with value network for neural machine translation

## When RL needed?

Single isolated decision making: e.g., classification, regression. When the that decision does not affect future decisions.

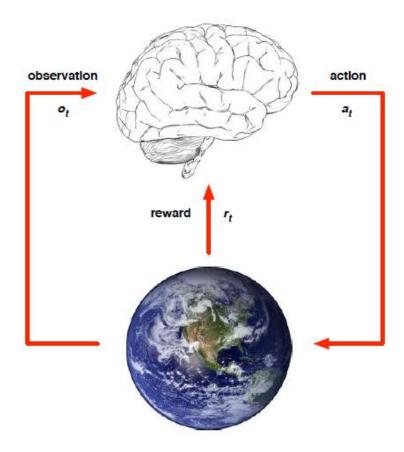
## **Sequential decsion making**

#### **Common Applications**



+ a key aspect of intelligence

# RL Problem Set-up



- ► At each step t the agent:
  - Executes action a<sub>t</sub>
  - Receives observation ot
  - Receives scalar reward r<sub>t</sub>
- ► The environment:
  - Receives action at
  - ightharpoonup Emits observation  $o_{t+1}$
  - ightharpoonup Emits scalar reward  $r_{t+1}$

# MDP and a RL problem

Markov decision process

$$\mathcal{M} = \{\mathcal{S}, \mathcal{A}, \mathcal{T}, r\}$$

 $\mathcal{S}$  – state space

states  $s \in \mathcal{S}$  (discrete or continuous)

 $\mathcal{A}$  – action space

actions  $a \in \mathcal{A}$  (discrete or continuous)

 $\mathcal{T}$  – transition operator (now a tensor!)

r – reward function

$$r: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$$

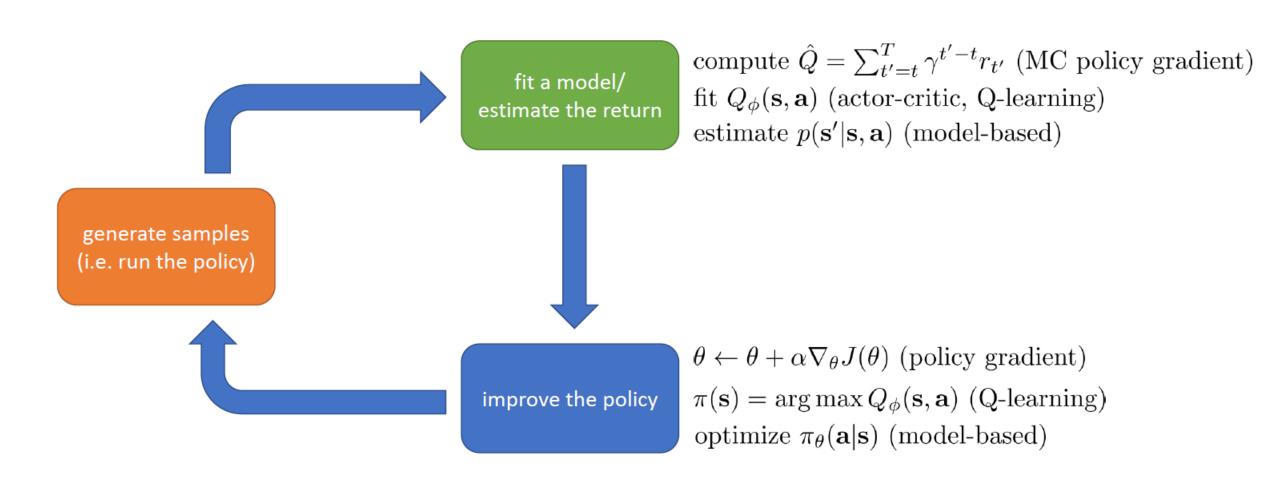
$$r(s_t, a_t)$$
 – reward

$$p_{\theta}(\mathbf{s}_1, \mathbf{a}_1, \dots, \mathbf{s}_T, \mathbf{a}_T) = p(\mathbf{s}_1) \prod_{t=1}^T \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t) p(\mathbf{s}_{t+1} | \mathbf{s}_t, \mathbf{a}_t)$$

$$\pi_{\theta}(\tau)$$

$$\theta^* = \arg\max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_t, \mathbf{a}_t) \right]$$

# The anatomy of a reinforcement learning algorithm

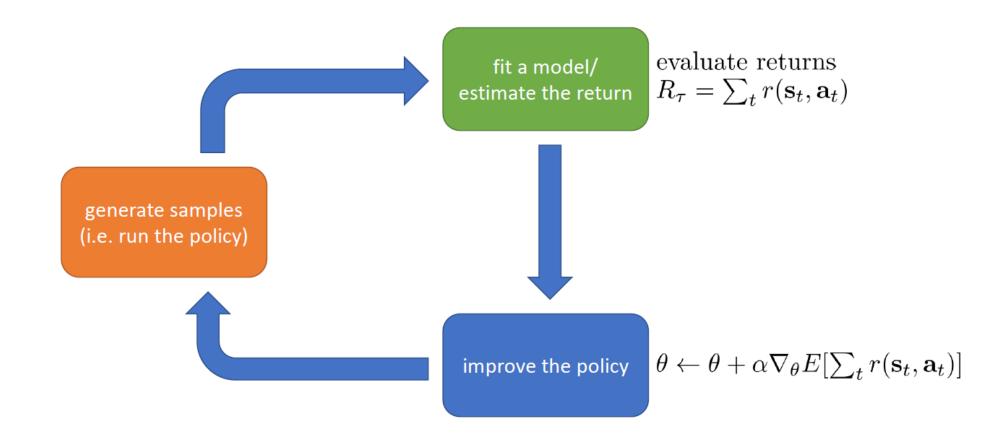


# Types of RL algorithms

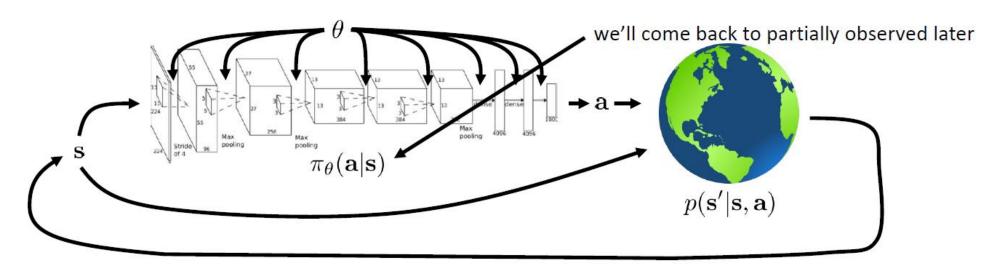
$$\theta^* = \arg\max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_t, \mathbf{a}_t) \right]$$

- Policy gradients: directly differentiate the above objective
- Value-based: estimate value function or Q-function of the optimal policy (no explicit policy)
- Actor-critic: estimate value function or Q-function of the current policy, use it to improve policy

# Direct policy gradients



# The goal of reinforcement learning



$$\underbrace{p_{\theta}(\mathbf{s}_1, \mathbf{a}_1, \dots, \mathbf{s}_T, \mathbf{a}_T)}_{\pi_{\theta}(\tau)} = p(\mathbf{s}_1) \prod_{t=1}^{T} \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t) p(\mathbf{s}_{t+1} | \mathbf{s}_t, \mathbf{a}_t)$$

$$\theta^* = \arg \max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_t, \mathbf{a}_t) \right]$$

# Direct policy differentiation

$$\theta^* = \arg\max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_t, \mathbf{a}_t) \right]$$

$$J(\theta)$$

$$J(\theta) = E_{\tau \sim \pi_{\theta}(\tau)}[r(\tau)] = \int \pi_{\theta}(\tau)r(\tau)d\tau$$
$$\sum_{t=1}^{T} r(\mathbf{s}_{t}, \mathbf{a}_{t})$$

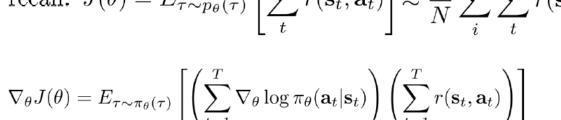
a convenient identity

$$\underline{\pi_{\theta}(\tau)\nabla_{\theta}\log \pi_{\theta}(\tau)} = \pi_{\theta}(\tau)\frac{\nabla_{\theta}\pi_{\theta}(\tau)}{\pi_{\theta}(\tau)} = \underline{\nabla_{\theta}\pi_{\theta}(\tau)}$$

$$\nabla_{\theta} J(\theta) = \int \underline{\nabla_{\theta} \pi_{\theta}(\tau)} r(\tau) d\tau = \int \underline{\pi_{\theta}(\tau)} \nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau) d\tau = E_{\tau \sim \pi_{\theta}(\tau)} [\nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau)]$$

# Evaluating the policy gradient

recall: 
$$J(\theta) = E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_{t}, \mathbf{a}_{t}) \right] \approx \frac{1}{N} \sum_{i} \sum_{t} r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t})$$



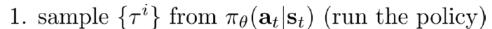
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \right) \left( \sum_{t=1}^{T} r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) \right)$$

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

generate samples (i.e. run the policy)

#### fit a model to estimate return





2. 
$$\nabla_{\theta} J(\theta) \approx \sum_{i} \left( \sum_{t} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}^{i} | \mathbf{s}_{t}^{i}) \right) \left( \sum_{t} r(\mathbf{s}_{t}^{i}, \mathbf{a}_{t}^{i}) \right)$$

3. 
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$



improve the policy

## **Policy Gradient**

v.s. Supervised Classification

$$\nabla_{\theta} J(\theta) = \nabla_{\theta} \log \pi_{\theta}(\tau) r(\tau)$$

$$\nabla_{\theta} J(\theta) = \nabla_{\theta} \log \pi_{\theta}(\tau) y$$

# What did we just do?

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \right) \left( \sum_{t=1}^{T} r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) \right)$$

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \nabla_{\theta} \log \pi_{\theta}(\tau_{i}) r(\tau_{i})$$
$$\sum_{t=1}^{N} \nabla_{\theta} \log_{\theta} \pi_{\theta}(\mathbf{a}_{i,t}|\mathbf{s}_{i,t})$$

maximum likelihood: 
$$\nabla_{\theta} J_{\text{ML}}(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \nabla_{\theta} \log \pi_{\theta}(\tau_i)$$

good stuff is made more likely

bad stuff is made less likely

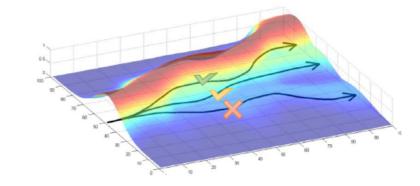
simply formalizes the notion of "trial and error"!

#### REINFORCE algorithm:

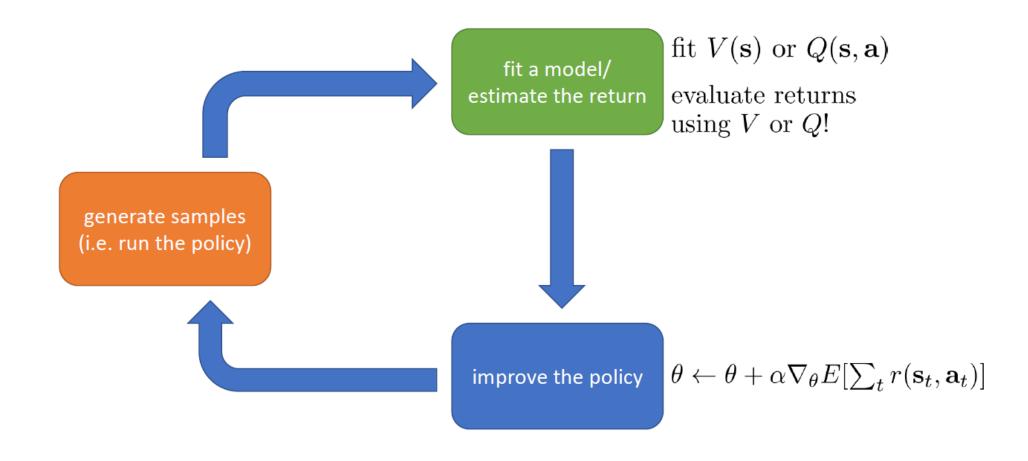


- 1. sample  $\{\tau^i\}$  from  $\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)$  (run it on the robot)
- 2.  $\nabla_{\theta} J(\theta) \approx \sum_{i} \left( \sum_{t} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}^{i} | \mathbf{s}_{t}^{i}) \right) \left( \sum_{t} r(\mathbf{s}_{t}^{i}, \mathbf{a}_{t}^{i}) \right)$ 3.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

3. 
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$



# Actor-critic: value functions + policy gradients



# Recap: policy gradients

#### REINFORCE algorithm:



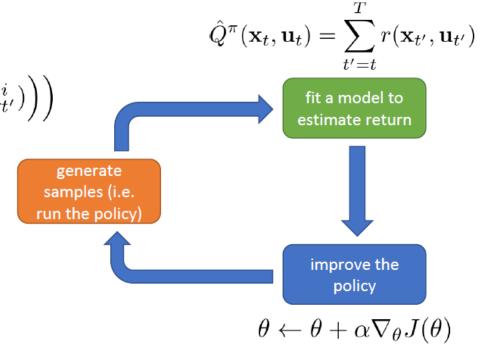
1. sample  $\{\tau^i\}$  from  $\pi_{\theta}(\mathbf{a}_t|\mathbf{s}_t)$  (run the policy)

2. 
$$\nabla_{\theta} J(\theta) \approx \sum_{i} \left( \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{t}^{i} | \mathbf{s}_{t}^{i}) \left( \sum_{t'=t}^{T} r(\mathbf{s}_{t'}^{i}, \mathbf{a}_{t'}^{i}) \right) \right)$$

3.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$ 

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \hat{Q}_{i,t}^{\pi}$$

"reward to go"



# Improving the policy gradient

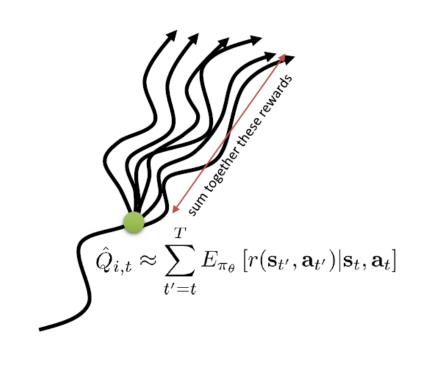
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \left( \sum_{t'=1}^{T} r(\mathbf{s}_{i,t'}, \mathbf{a}_{i,t'}) \right)$$
"reward to go"
$$\hat{Q}_{i,t}$$

 $\hat{Q}_{i,t}$ : estimate of expected reward if we take action  $\mathbf{a}_{i,t}$  in state  $\mathbf{s}_{i,t}$  can we get a better estimate?

$$Q(\mathbf{s}_t, \mathbf{a}_t) = \sum_{t'=t}^T E_{\pi_{\theta}} [r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_t, \mathbf{a}_t]$$
: true expected reward-to-go

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t}|\mathbf{s}_{i,t}) \left( Q(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) - V(\mathbf{s}_{i,t}) \right)$$

$$E[\nabla_{\theta} \log \pi_{\theta}(\tau)b] = \int \pi_{\theta}(\tau)\nabla_{\theta} \log \pi_{\theta}(\tau)b \, d\tau = \int \nabla_{\theta}\pi_{\theta}(\tau)b \, d\tau = b\nabla_{\theta} \int \pi_{\theta}(\tau)d\tau = b\nabla_{\theta}1 = 0$$



$$V(\mathbf{s}_t) = E_{\mathbf{a}_t \sim \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)}[Q(\mathbf{s}_t, \mathbf{a}_t)]$$

## State & state-action value functions

$$Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) = \sum_{t'=t}^{T} E_{\pi_{\theta}} \left[ r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_{t}, \mathbf{a}_{t} \right] : \text{ total reward from taking } \mathbf{a}_{t} \text{ in } \mathbf{s}_{t}$$
 fit  $Q^{\pi}, V^{\pi}, \text{ or } A^{\pi}$  
$$V^{\pi}(\mathbf{s}_{t}) = E_{\mathbf{a}_{t} \sim \pi_{\theta}(\mathbf{a}_{t} | \mathbf{s}_{t})} [Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t})] : \text{ total reward from } \mathbf{s}_{t}$$
 fit a model to estimate return 
$$A^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) = Q^{\pi}(\mathbf{s}_{t}, \mathbf{a}_{t}) - V^{\pi}(\mathbf{s}_{t}) : \text{ how much better } \mathbf{a}_{t} \text{ is }$$
 generate samples (i.e. run the policy) 
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) A^{\pi}(\mathbf{s}_{i,t}, \mathbf{a}_{i,t})$$
 improve the policy 
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$
 the better this estimate, the lower the variance

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \left( \sum_{t'=1}^{T} r(\mathbf{s}_{i,t'}, \mathbf{a}_{i,t'}) - b \right)$$

unbiased, but high variance single-sample estimate

# Value function fitting

$$Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}} \left[ r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_t, \mathbf{a}_t \right]$$

$$V^{\pi}(\mathbf{s}_t) = E_{\mathbf{a}_t \sim \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)}[Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t)]$$

$$A^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) - V^{\pi}(\mathbf{s}_t)$$

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) A^{\pi}(\mathbf{s}_{i,t}, \mathbf{a}_{i,t})$$

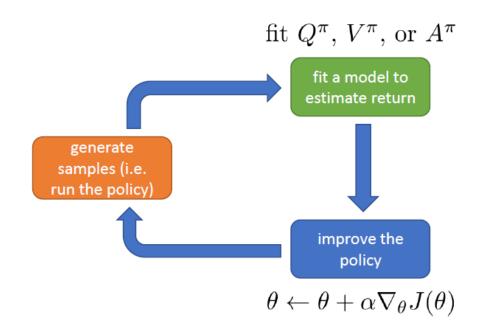
fit what to what?

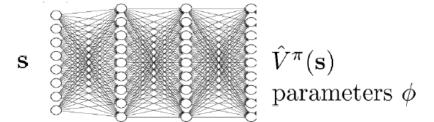
$$Q^{\pi}, V^{\pi}, A^{\pi}$$
?

$$Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = r(\mathbf{s}_t, \mathbf{a}_t) + E_{\mathbf{s}_{t+1} \sim p(\mathbf{s}_{t+1}|\mathbf{s}_t, \mathbf{a}_t)}[V^{\pi}(\mathbf{s}_{t+1})]$$

$$A^{\pi}(\mathbf{s}_t, \mathbf{a}_t) \approx r(\mathbf{s}_t, \mathbf{a}_t) + V^{\pi}(\mathbf{s}_{t+1}) - V^{\pi}(\mathbf{s}_{t+1})$$

let's just fit  $V^{\pi}(\mathbf{s})!$ 





# Policy evaluation

$$V^{\pi}(\mathbf{s}_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}} \left[ r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_t \right]$$

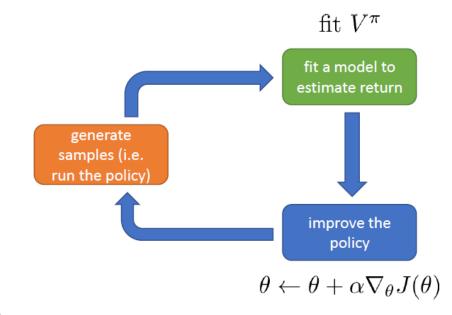
$$J(\theta) = E_{\mathbf{s}_1 \sim p(\mathbf{s}_1)}[V^{\pi}(\mathbf{s}_1)]$$

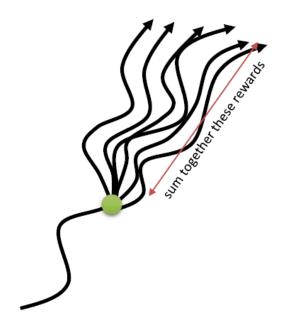
how can we perform policy evaluation?

Monte Carlo policy evaluation (this is what policy gradient does)

$$V^{\pi}(\mathbf{s}_t) pprox \sum_{t'=t}^{T} r(\mathbf{s}_{t'}, \mathbf{a}_{t'})$$

$$V^{\pi}(\mathbf{s}_t) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t'=t}^{T} r(\mathbf{s}_{t'}, \mathbf{a}_{t'})$$
 (requires us to reset the simulator)





# Monte Carlo evaluation with function approximation

$$V^{\pi}(\mathbf{s}_t) pprox \sum_{t'=t}^T r(\mathbf{s}_{t'}, \mathbf{a}_{t'})$$

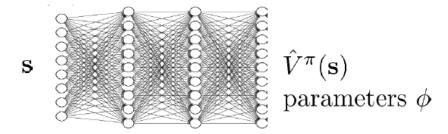
not as good as this:  $V^{\pi}(\mathbf{s}_t) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t'=t}^{T} r(\mathbf{s}_{t'}, \mathbf{a}_{t'})$ 

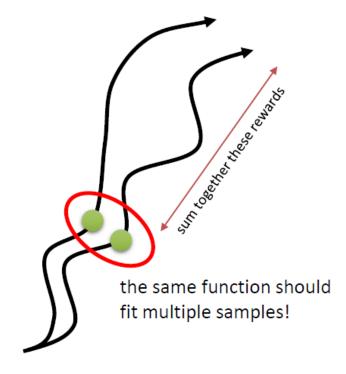
but still pretty good!

training data: 
$$\left\{ \left( \mathbf{s}_{i,t}, \sum_{t'=t}^{T} r(\mathbf{s}_{i,t'}, \mathbf{a}_{i,t'}) \right) \right\}$$

$$y_{i,t}$$

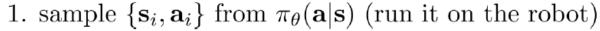
supervised regression: 
$$\mathcal{L}(\phi) = \frac{1}{2} \sum_{i} \left\| \hat{V}_{\phi}^{\pi}(\mathbf{s}_{i}) - y_{i} \right\|^{2}$$





# An actor-critic algorithm

batch actor-critic algorithm:



2. fit 
$$\hat{V}_{\phi}^{\pi}(\mathbf{s})$$
 to sampled reward sums

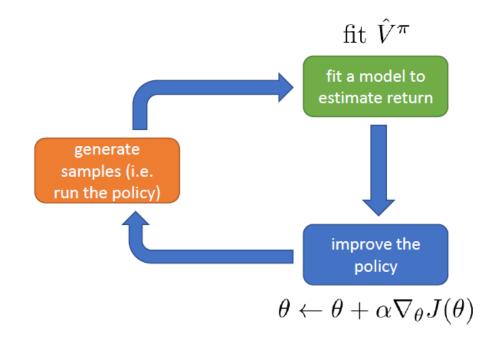
3. evaluate 
$$\hat{A}^{\pi}(\mathbf{s}_i, \mathbf{a}_i) = r(\mathbf{s}_i, \mathbf{a}_i) + \hat{V}_{\phi}^{\pi}(\mathbf{s}_i') - \hat{V}_{\phi}^{\pi}(\mathbf{s}_i)$$

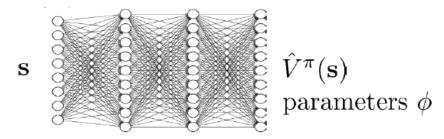
4. 
$$\nabla_{\theta} J(\theta) \approx \sum_{i} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i}|\mathbf{s}_{i}) \hat{A}^{\pi}(\mathbf{s}_{i},\mathbf{a}_{i})$$

5. 
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

$$y_{i,t} \approx r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) + \hat{V}_{\phi}^{\pi}(\mathbf{s}_{i,t+1})$$

$$\mathcal{L}(\phi) = \frac{1}{2} \sum_{i} \left\| \hat{V}_{\phi}^{\pi}(\mathbf{s}_{i}) - y_{i} \right\|^{2}$$





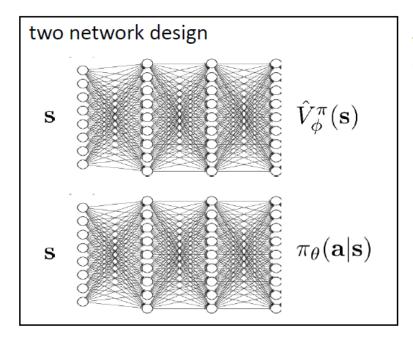
$$V^{\pi}(\mathbf{s}_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}} \left[ r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_t \right]$$

# Architecture design

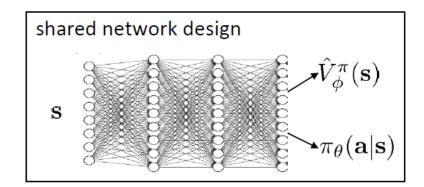
online actor-critic algorithm:



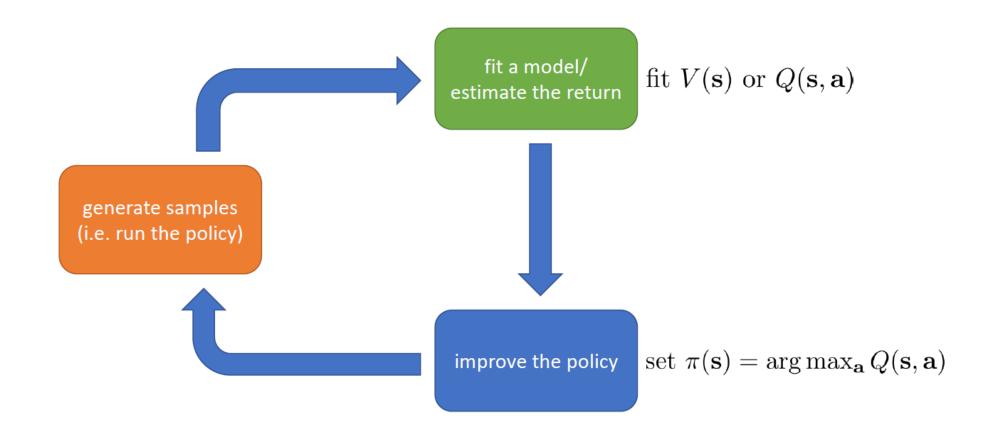
- 1. take action  $\mathbf{a} \sim \pi_{\theta}(\mathbf{a}|\mathbf{s})$ , get  $(\mathbf{s}, \mathbf{a}, \mathbf{s}', r)$
- 2. update  $\hat{V}_{\phi}^{\pi}$  using target  $r + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}')$
- 3. evaluate  $\hat{A}^{\pi}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}') \hat{V}_{\phi}^{\pi}(\mathbf{s})$
- 4.  $\nabla_{\theta} J(\theta) \approx \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}|\mathbf{s}) \hat{A}^{\pi}(\mathbf{s},\mathbf{a})$
- 5.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$



- + simple & stable
- no shared features between actor & critic

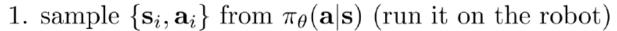


# Value function based algorithms

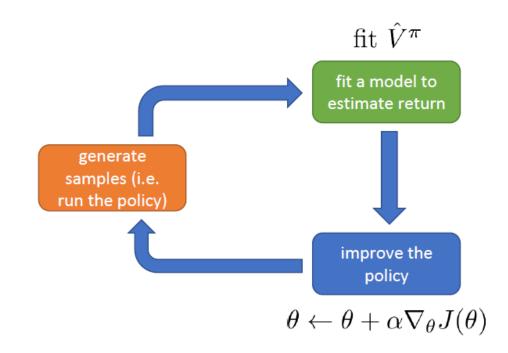


# Recap: actor-critic

#### batch actor-critic algorithm:



- 2. fit  $\hat{V}_{\phi}^{\pi}(\mathbf{s})$  to sampled reward sums
- 3. evaluate  $\hat{A}^{\pi}(\mathbf{s}_i, \mathbf{a}_i) = r(\mathbf{s}_i, \mathbf{a}_i) + \hat{V}_{\phi}^{\pi}(\mathbf{s}_i') \hat{V}_{\phi}^{\pi}(\mathbf{s}_i)$
- 4.  $\nabla_{\theta} J(\theta) \approx \sum_{i} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i}|\mathbf{s}_{i}) \hat{A}^{\pi}(\mathbf{s}_{i},\mathbf{a}_{i})$
- 5.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$



# Can we omit policy gradient completely?

 $A^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ : how much better is  $\mathbf{a}_t$  than the average action according to  $\pi$ 

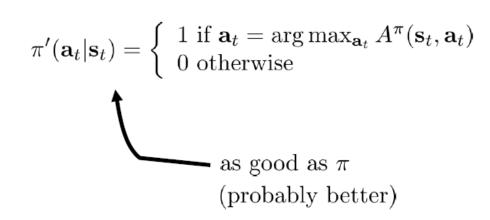
 $\arg\max_{\mathbf{a}_t} A^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$ : best action from  $\mathbf{s}_t$ , if we then follow  $\pi$ 

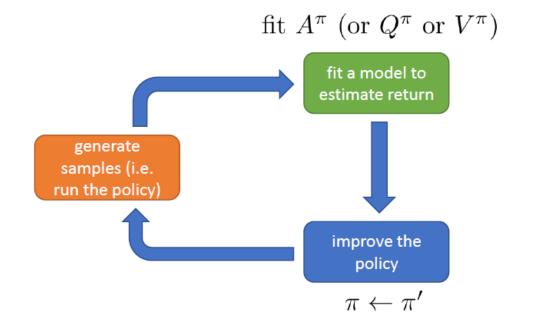


forget policies, let's just do this!

at least as good as any  $\mathbf{a}_t \sim \pi(\mathbf{a}_t|\mathbf{s}_t)$ 

regardless of what  $\pi(\mathbf{a}_t|\mathbf{s}_t)$  is!





# Policy iteration with dynamic programming

$$\pi'(\mathbf{a}_t|\mathbf{s}_t) = \begin{cases} 1 \text{ if } \mathbf{a}_t = \arg\max_{\mathbf{a}_t} A^{\pi}(\mathbf{s}_t, \mathbf{a}_t) \\ 0 \text{ otherwise} \end{cases}$$

$$A^{\pi}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma E[V^{\pi}(\mathbf{s}')] - V^{\pi}(\mathbf{s})$$

$$\arg\max_{\mathbf{a}_t} A^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = \arg\max_{\mathbf{a}_t} Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t)$$

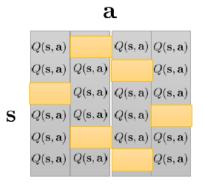
$$Q^{\pi}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma E[V^{\pi}(\mathbf{s}')]$$
 (a bit simpler)

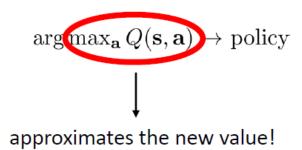
skip the policy and compute values directly!

value iteration algorithm:

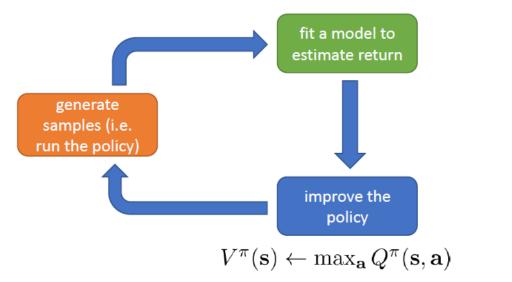


- 1. set  $Q(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + \gamma E[V(\mathbf{s}')]$ 2. set  $V(\mathbf{s}) \leftarrow \max_{\mathbf{a}} Q(\mathbf{s}, \mathbf{a})$





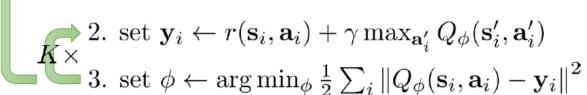
$$Q^{\pi}(\mathbf{s}, \mathbf{a}) \leftarrow r(\mathbf{s}, \mathbf{a}) + \gamma E_{\mathbf{s}' \sim p(\mathbf{s}' | \mathbf{s}, \mathbf{a})}[V^{\pi}(\mathbf{s}')]$$



# Fitted Q-iteration

#### full fitted Q-iteration algorithm:

1. collect dataset  $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i', r_i)\}$  using some policy



parameters

dataset size N, collection policy iterations Kgradient steps S

## **Bellman Equation**

$$Q^*(s, a) = r(s, a) + \gamma \max_{a'} Q^*(s', a')$$

## Minimizing Bellman Residual

$$Q(s,a) \leftarrow Q(s,a) + \alpha[r(s,a) + \gamma \max_{a'} Q(s',a') - Q(s,a)]$$

## Comparison

#### Policy gradient

- > The only one that actually performs gradient descent on true objective, but often the least efficient.
- Episodic learning

## Value function fitting

- > Fixed point iteration, not guaranteed to converge to anything in the nonlinear case.
- Assumption on full observability.

Actor-critic = Policy gradient + Value function fitting

## Examples of specific algorithms

- Value function fitting methods
  - Q-learning, DQN [1]
  - Temporal difference learning
  - Fitted value iteration
- Policy gradient methods
  - REINFORCE
  - Natural policy gradient
  - Trust region policy optimization [2]
- Actor-critic algorithms
  - Asynchronous advantage actor critic (A3C) [3]

- [1] Volodymyr Mnih, et al., "Human-level control through deep reinforcement learning," Nature 2015.
- [2] John Schulman, et al., "Trust Region Policy Optimization," ICML 2015.
- [3] Volodymyr Mnih, et al., "Asynchronous Methods for Deep Reinforcement Learning," ICML 2016.