

<b>termvar</b> , $x, y, d$	Term-level variable	
<i>label</i> , $l$	$::=$	Label
<b>mode</b> , $m$	$::=$ <ul style="list-style-type: none"> <li>  <math>-</math></li> <li>  <math>L</math></li> <li>  <math>F</math></li> <li>  <math>G</math></li> <li>  <math>\text{max\_mode}(\Gamma)</math></li> <li>  <math>\text{if mode\_cond then } m_3 \text{ else } m_4</math></li> </ul>	Mode <ul style="list-style-type: none"> <li>Placeholder for any mode</li> <li>Local</li> <li>Foreign</li> <li>Global</li> </ul>
mode_cond	$::=$ <ul style="list-style-type: none"> <li>  <math>m_1 = m_2</math></li> <li>  <math>m_1 \leq m_2</math></li> <li>  <math>m \in \text{suprmodes}(\Gamma)</math></li> <li>  <math>\exists m \in \text{suprmodes}(\Gamma)</math></li> </ul>	Mode statement
<b>type</b> , $A, B$	$::=$ <ul style="list-style-type: none"> <li>  <math>1</math></li> <li>  <math>A_1 \oplus A_2</math></li> <li>  <math>A_1 \otimes A_2</math></li> <li>  <math>A_1 \ltimes A_2</math></li> <li>  <math>m_1 A_1 \multimap A_2</math></li> <li>  <math>A^\perp</math></li> <li>  <math>(A)</math></li> </ul>	Type <ul style="list-style-type: none"> <li>Unit</li> <li>Sum</li> <li>Product</li> <li>Ampar type (consuming <math>A_1</math> yields <math>A_2</math>)</li> <li>Linear function</li> <li>Destination</li> </ul>
dynamic_value, $v$	$::=$ <ul style="list-style-type: none"> <li>  <math>l</math></li> <li>  <math>@l</math></li> <li>  <math>()</math></li> <li>  <math>\text{Inl } v</math></li> <li>  <math>\text{Inr } v</math></li> <li>  <math>\langle v_1, v_2 \rangle</math></li> <li>  <math>\langle v_1, v_2 \rangle</math></li> <li>  <math>\lambda x. t</math></li> <li>  <math>(v)</math></li> </ul>	Dynamic value <ul style="list-style-type: none"> <li>Hole</li> <li>Destination</li> <li>Unit</li> <li>Left variant for sum</li> <li>Right variant for sum</li> <li>Product</li> <li>Ampar (<math>v_2</math> is the root of the structure)</li> <li>Linear function</li> </ul>
term, $t, u$	$::=$ <ul style="list-style-type: none"> <li>  <math>v</math></li> <li>  <math>x</math></li> <li>  <math>t \ u</math></li> <li>  <math>t ; u</math></li> <li>  <math>\text{case } t \text{ of } \{ \text{Inl } x_1 \mapsto u_1, \text{Inr } x_2 \mapsto u_2 \}</math></li> <li>  <math>\text{case } t \text{ of } \{ \langle x_1, x_2 \rangle \mapsto u \}</math></li> <li>  <math>\text{mapL } t \text{ with } \{ x \mapsto u \}</math></li> <li>  <math>\text{to}_x</math></li> <li>  <math>\text{from}_x</math></li> <li>  <math>\text{alloc}</math></li> <li>  <math>t \triangleleft ()</math></li> <li>  <math>t \triangleleft \text{Inl}</math></li> <li>  <math>t \triangleleft \text{Inr}</math></li> </ul>	Term <ul style="list-style-type: none"> <li>Dynamic value</li> <li>Variable</li> <li>Application</li> <li>Pattern-match on unit</li> <li>Pattern-match on sum</li> <li>Pattern-match on product</li> <li>Map over the left side of the ampar</li> <li>Wrap <math>t</math> into a trivial ampar</li> <li>Extract value from trivial ampar</li> <li>Return a fresh "identity" ampar object</li> <li>Fill destination with unit</li> <li>Fill destination with left variant</li> <li>Fill destination with right variant</li> </ul>

	$ \begin{array}{ l} t \triangleleft \langle , \rangle \\ t \triangleleft \cdot u \\ (t) \\ t[e] \end{array} $	Fill destination with product constructor Fill destination with root of ampar u S M
sub	$ \begin{array}{ l} \\ x \mapsto v \end{array} $	variable or label substitution
subs	$ \begin{array}{ l} \text{sub} \\ \text{sub}, \text{subs} \end{array} $	variable or substitutions
effect, e	$ \begin{array}{ l} \varepsilon \\ \text{subs} \end{array} $	empty effect
type_affect, ta	$ \begin{array}{ l} x :_m A \\ +l : A \\ -l : A \end{array} $	type affectation Hole Destination
type_affects	$ \begin{array}{ l} \text{ta} \\ \text{ta}, \text{type\_affects} \end{array} $	type affectations
typing_context, $\mathcal{U}, \Gamma$	$ \begin{array}{ l} \{\} \\ \{\text{type\_affects}\} \\ \Gamma_1 \sqcup \Gamma_2 \\ \Gamma_1 \uplus \Gamma_2 \\ \Gamma[m_1 \mapsto m_2] \end{array} $	typing context
terminals	$ \begin{array}{ l} \text{---} \circ \\ \times \\ \mapsto \\ () \\ \text{Inl} \\ \text{Inr} \\ \langle , \rangle \\ \odot \\ \triangleleft \\ \triangleleft \cdot \\ ; \\ \sqcup \\ \uplus \\ \{\} \\ \exists \\ \neq \end{array} $	

	$\leq$ $\in$ $\notin$ $\subset$ $\mathcal{N}$ $\vdash$ $\longrightarrow$ $\rightsquigarrow$
formula	$::=$ judgement
Ctx	$::=$ $x \in \mathcal{N}(\Gamma)$ $l \in \mathcal{N}(\Gamma)$ $x \notin \mathcal{N}(\Gamma)$ $l \notin \mathcal{N}(\Gamma)$ fresh $x$ fresh $l$ type_affect $\in \Gamma$ mode_cond
Eq	$::=$ $A_1 = A_2$ $A_1 \neq A_2$ $t = u$ $t \neq u$ $\Gamma_1 = \Gamma_2$ $\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset$
Ty	$::=$ $\Gamma \vdash t : A$
judgement	$::=$ Ctx Eq Ty
user_syntax	$::=$ termvar label mode mode_cond type dynamic_value term sub subs effect

| type\_affect  
 | type\_affects  
 | typing\_context  
 | terminals

$x \in \mathcal{N}(\Gamma)$
$l \in \mathcal{N}(\Gamma)$
$x \notin \mathcal{N}(\Gamma)$
$l \notin \mathcal{N}(\Gamma)$
fresh $x$
fresh $l$
type_affect $\in \Gamma$
mode_cond
$A_1 = A_2$
$A_1 \neq A_2$
$t = u$
$t \neq u$
$\Gamma_1 = \Gamma_2$
$\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset$
$\Gamma \vdash t : A$

$\overline{\{+l : A\} \vdash l : A}$	TYTERM_HOLE
$\overline{\{-l : A\} \vdash @l : A^\perp}$	TYTERM_DEST
$\overline{\{\}} \vdash () : 1$	TYTERM_UNIT
$\frac{\Gamma \vdash v : A_1}{\Gamma \vdash \text{Inl } v : A_1 \oplus A_2}$	TYTERM_INL
$\frac{\Gamma \vdash v : A_2}{\Gamma \vdash \text{Inr } v : A_1 \oplus A_2}$	TYTERM_INR
$\frac{\Gamma_1 \vdash v_1 : A_1 \quad \Gamma_2 \vdash v_2 : A_2}{\Gamma_1 \sqcup \Gamma_2 \vdash \langle v_1, v_2 \rangle : A_1 \otimes A_2}$	TYTERM_PROD
$\frac{\Gamma_1 \vdash v_1 : A_1 \quad \Gamma_2 \vdash v_2 : A_2 \quad \Gamma_3 = \Gamma_1 \uplus \Gamma_2}{\Gamma_3 \vdash \langle v_1, v_2 \rangle : A_1 \times A_2}$	TYTERM_AMPAR
$\frac{\Gamma \sqcup \{x :_{m_1} A_1\} \vdash t : A_2}{\Gamma \vdash \lambda x. t :_{m_1} A_1 \multimap A_2}$	TYTERM_LAMBDA
$\frac{\Gamma_1 \vdash t :_{m_1} A_1 \multimap A_2 \quad \Gamma_2 \vdash u : A_1 \quad m_1 \in \text{suprmodes}(\Gamma_2)}{\Gamma_1 \sqcup \Gamma_2 \vdash tu : A_2}$	TYTERM_APP

$$\begin{array}{c}
\frac{\Gamma_1 \vdash t : \mathbf{1} \quad \Gamma_2 \vdash u : \mathbf{B}}{\Gamma_1 \sqcup \Gamma_2 \vdash t ; u : \mathbf{B}} \quad \text{TYTERM\_PATUNIT} \\
\\
\frac{\begin{array}{l} \Gamma_1 \vdash t : \mathbf{A_1 \oplus A_2} \\ \exists m \in \text{suprmodes}(\Gamma_1) \\ \Gamma_2 \sqcup \{x_1 :_m \mathbf{A_1}\} \vdash u_1 : \mathbf{B} \\ \Gamma_2 \sqcup \{x_2 :_m \mathbf{A_2}\} \vdash u_2 : \mathbf{B} \end{array}}{\Gamma_1 \sqcup \Gamma_2 \vdash \text{case } t \text{ of } \{ \text{Inl } x_1 \mapsto u_1, \text{Inr } x_2 \mapsto u_2 \} : \mathbf{B}} \quad \text{TYTERM\_PATSUM} \\
\\
\frac{\begin{array}{l} \Gamma_1 \vdash t : \mathbf{A_1 \otimes A_2} \\ \exists m \in \text{suprmodes}(\Gamma_1) \\ \Gamma_2 \sqcup \{x_1 :_m \mathbf{A_1}, x_2 :_m \mathbf{A_2}\} \vdash u : \mathbf{B} \end{array}}{\Gamma_1 \sqcup \Gamma_2 \vdash \text{case } t \text{ of } \{ \langle x_1, x_2 \rangle \mapsto u \} : \mathbf{B}} \quad \text{TYTERM\_PATPROD} \\
\\
\frac{\begin{array}{l} \Gamma_1 \vdash t : \mathbf{A_1 \times A_2} \\ \exists m' \in \text{suprmodes}(\Gamma_1 \sqcup \Gamma_2) \\ m = \text{if } F \in \text{suprmodes}(\Gamma_1) \text{ then } F \text{ else } L \\ \Gamma_2[L \mapsto F] \sqcup \{x :_m \mathbf{A_1}\} \vdash u : \mathbf{B} \end{array}}{\Gamma_1 \sqcup \Gamma_2 \vdash \text{mapL } t \text{ with } \{x \mapsto u\} : \mathbf{B \times A_2}} \quad \text{TYTERM\_MAPAMPAR} \\
\\
\frac{}{\{\} \vdash \text{alloc} : \mathbf{A^\perp \times A}} \quad \text{TYTERM\_ALLOC} \\
\\
\frac{\Gamma \vdash t : \mathbf{A}}{\Gamma \vdash \text{to}_\times : \mathbf{1 \times A}} \quad \text{TYTERM\_TOAMPAR} \\
\\
\frac{\Gamma \vdash t : \mathbf{1 \times A}}{\Gamma \vdash \text{from}_\times : \mathbf{A}} \quad \text{TYTERM\_FROMAMPAR} \\
\\
\frac{\Gamma \vdash t : \mathbf{1^\perp}}{\Gamma \vdash t \triangleleft () : \mathbf{1}} \quad \text{TYTERM\_FILLUNIT} \\
\\
\frac{\Gamma \vdash t : (\mathbf{A_1 \oplus A_2})^\perp}{\Gamma \vdash t \triangleleft \text{Inl} : \mathbf{A_1^\perp}} \quad \text{TYTERM\_FILLINL} \\
\\
\frac{\Gamma \vdash t : (\mathbf{A_1 \oplus A_2})^\perp}{\Gamma \vdash t \triangleleft \text{Inr} : \mathbf{A_2^\perp}} \quad \text{TYTERM\_FILLINR} \\
\\
\frac{\Gamma \vdash t : (\mathbf{A_1 \otimes A_2})^\perp}{\Gamma \vdash t \triangleleft \langle \rangle : \mathbf{A_1^\perp \otimes A_2^\perp}} \quad \text{TYTERM\_FILLPROD} \\
\\
\frac{\begin{array}{l} \Gamma_1 \vdash t : \mathbf{A_2^\perp} \\ \Gamma_2 \vdash u : \mathbf{A_1 \times A_2} \\ L \in \text{suprmodes}(\Gamma_1) \\ F \in \text{suprmodes}(\Gamma_2) \end{array}}{\Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft \cdot u : \mathbf{A_1}} \quad \text{TYTERM\_FILLCOMPL} \\
\\
\frac{\begin{array}{l} \Gamma_1 \vdash t : \mathbf{A_2^\perp} \\ \Gamma_2 \vdash u : \mathbf{A_1 \times A_2} \\ F \in \text{suprmodes}(\Gamma_1) \\ G \in \text{suprmodes}(\Gamma_2) \end{array}}{\Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft \cdot u : \mathbf{A_1}} \quad \text{TYTERM\_FILLCOMPF}
\end{array}$$

Definition rules: 22 good 0 bad  
 Definition rule clauses: 60 good 0 bad