

metavariable, x , xs , y , uf , f , d

term, t , u	$::=$ $ $ x $ $ v $ $ $t\ u$ $ $ $t ; u$ $ $ $\text{case } t \text{ of } \{() \mapsto u\}$ $ $ $\text{case } t \text{ of } \{ \text{Ur } x \mapsto u \}$ $ $ $\text{case } t \text{ of } \{ \text{inl } x_1 \mapsto u_1, \text{inr } x_2 \mapsto u_2 \}$ $ $ $\text{case } t \text{ of } \{ \langle x_1, x_2 \rangle \mapsto u \}$ $ $ $\text{case } t \text{ of } \{ \text{roll } x \mapsto u \}$ $ $ $\text{alloc } d . t$ $ $ $t \triangleleft ()$ $ $ $t \triangleleft u$ $ $ $t \triangleleft \text{Ur } u$ $ $ $t \triangleleft \text{inl } d . u$ $ $ $t \triangleleft \text{inr } d . u$ $ $ $t \triangleleft \langle d_1, d_2 \rangle . u$ $ $ $t \triangleleft \text{roll } d . u$ $ $ (t) $ $ $t [\text{var_subs}]$	term variable value application effect execution pattern-matching on unit pattern-matching on exponentiated value pattern-matching on sum pattern-matching on product unroll for recursive types allocate data fill destination with unit fill terminal-type destination fill destination with exponential fill sum-type destination with variant 1 fill sum-type destination with variant 2 fill product-type destination fill destination with recursive type
var_sub, vs	$::=$ $ $ $x := t$	variable substitution
var_subs	$::=$ $ $ vs $ $ $vs, \text{var_subs}$	variable substitutions
heap_val, h	$::=$ $ $ $()$ $ $ $\text{Ur } \ell$ $ $ $\text{inl } \ell$ $ $ $\text{inr } \ell$ $ $ $\langle \ell_1, \ell_2 \rangle$ $ $ $\text{roll } \ell$ $ $ $\text{C } \ell$	M generic for all the cases above
val, v	$::=$ $ $ \bullet $ $ $[\ell]$ $ $ $\lambda x:A . t$ $ $ h	unreducible value no-effect effect address of an allocated memory area lambda abstraction heap value
<i>label</i> , ℓ	$::=$	memory address
labels	$::=$ $ $ ℓ $ $ ℓ, labels $ $ ℓ	M

	$\bar{\ell}$, labels	M	
$label_set, L$	$::=$ \emptyset $\{labels\}$ $L_1 \sqcup L_2$		set of used labels
heap_affect, ha	$::=$ $\ell \triangleleft v$ $\bar{\ell} \triangleleft \bar{v}$	M	heap cell generic for multiple occurrences
heap_affects	$::=$ ha ha, heap_affects		heap cells
heap_context, \mathbb{H}	$::=$ \emptyset $\{heap_affects\}$ $\mathbb{H}_1 \sqcup \mathbb{H}_2$		heap contents
type, A, B	$::=$ \perp 1 R $A \otimes B$ $A \oplus B$ $A \multimap B$ $[A]$ $!A$ (A) $W[r := A]$	S M	bottom type unit type recursive type bound to a name product type sum type linear function type destination type exponential
type_with_hole, W	$::=$ r \perp 1 R $W_1 \otimes W_2$ $W_1 \oplus W_2$ $W_1 \multimap W_2$ $[W]$ $!W$ (W)	S	type hole in recursive definition bottom type unit type recursive type bound to a name product type sum type linear function type destination type exponential
rec_type_bound, R	$::=$		recursive type bound to a name
rec_type_def	$::=$ $\mu r. W$		

type_affect, ta

$$\begin{array}{l} ::= \\ | \quad x : A \\ | \quad \ell : A \\ | \quad \bar{\ell} : \bar{A} \end{array}$$

type_affects

$$\begin{array}{l} ::= \\ | \quad \text{ta} \\ | \quad \text{ta}, \text{type_affects} \end{array}$$

typing_context, Γ , \mathcal{U} , Φ , Ψ , Ψ^{\sharp} , Ψ^{\dagger}

$$\begin{array}{l} ::= \\ | \quad \emptyset \\ | \quad \{\text{type_affects}\} \\ | \quad \Gamma_1 \sqcup \Gamma_2 \end{array}$$

types, \bar{A}

$$\begin{array}{l} ::= \\ | \quad \cdot \\ | \quad A \\ | \quad A \text{ types} \end{array}$$

command

$$\begin{array}{l} ::= \\ | \quad L | \mathbb{H} | \mathfrak{t} \end{array}$$

heap_constructor, C

$$\begin{array}{l} ::= \\ | \quad () \\ | \quad \text{Ur} \\ | \quad \text{inl} \\ | \quad \text{inr} \\ | \quad \langle, \rangle \\ | \quad \text{roll } R \end{array}$$

judg

$$\begin{array}{l} ::= \\ | \quad \ell \in \mathcal{N}(\Phi) \\ | \quad \ell \notin \mathcal{N}(\Phi) \\ | \quad \text{type_affect} \in \Gamma \\ | \quad \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\ | \quad \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \wedge \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_3) = \emptyset \wedge \mathcal{N}(\Gamma_2) \cap \mathcal{N}(\Gamma_3) = \emptyset \\ | \quad \mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi) \subset L \\ | \quad \mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi^{\sharp}) \sqcup \mathcal{N}(\Psi^{\dagger}) \subset L \\ | \quad \ell \in L \\ | \quad \ell \notin L \\ | \quad \text{heap_affect} \in \mathbb{H} \\ | \quad A = B \\ | \quad \mathfrak{t} = u \\ | \quad \Gamma = D \\ | \quad \{\ell \triangleleft v', \bar{\ell} \triangleleft \bar{v}\} = \text{deepCopy}(L, [\ell], v) \\ | \quad R \stackrel{\text{fix}}{=} \text{rec_type_def} \\ | \quad A \text{ is destination-free} \\ | \quad C : \bar{A} \sqsubseteq A \\ | \quad \Phi ; \Psi^{\sharp} \cup \Psi^{\dagger} ; \mathcal{U} ; \Gamma \vdash \text{command} : A \end{array}$$

	$\Phi ; \Psi \vdash \mathbb{H}$ $\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash t : \mathcal{A}$ $\text{command} \Downarrow \text{command}'$
terminals	$::=$ $()$ \mapsto \oplus $\text{--}\circ$ $::=$ \vdash \sqcup \emptyset \neq \in \notin $\backslash n$ \langle \rangle inl inr Ur \triangleleft $ $ $\text{--}\hookrightarrow$ $=$ \Downarrow fix \equiv \perp \bullet \subset $;$ \mathcal{N} $\bar{\ell}$ \bar{v}
formula	$::=$ judgement
Ctx	$::=$ $\ell \in \mathcal{N}(\Phi)$ $\ell \notin \mathcal{N}(\Phi)$ $\text{type_affect} \in \Gamma$ $\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset$ $\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \wedge \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_3) = \emptyset \wedge \mathcal{N}(\Gamma_2) \cap \mathcal{N}(\Gamma_3) = \emptyset$
	Γ_1 and Γ_2 are disjoint Γ_1, Γ_2 and Γ_3 are pairwise disjoint
LabelSet	$::=$ $\mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi) \subset L$ $\mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi^{\mathbb{H}}) \sqcup \mathcal{N}(\Psi^t) \subset L$ $\ell \in L$

	$\ell = \text{fresh}(L)$	
Heap	$::=$ $\text{heap_affect} \in \mathbb{H}$	
Eq	$::=$ $A = B$ $t = u$ $\Gamma = D$	
Copy	$::=$ $\{\ell \triangleleft v', \bar{\ell} \triangleleft \bar{v}\} = \text{deepCopy}(L, [\ell], v)$	Deep-copy v into the memory tree with root ℓ and \bar{v} into the memory tree with root $\bar{\ell}$
Ty	$::=$ $R \stackrel{\text{fix}}{=} \text{rec_type_def}$ A is destination-free $C : \bar{A} \xrightarrow{c} A$ $\Phi ; \Psi^{\mathbb{H}} \sqcup \Psi^t ; \bar{U} ; \Gamma \vdash \text{command} : A$ $\Phi ; \Psi \vdash \mathbb{H}$ $\Phi ; \Psi ; \bar{U} ; \Gamma \vdash t : A$	A is destination-free Heap constructor C builds a value of type A given \bar{A}
Sem	$::=$ $\text{command} \Downarrow \text{command}'$	
judgement	$::=$ Ctx LabelSet Heap Eq Copy Ty Sem	
user_syntax	$::=$ <i>metavariable</i> term var_sub var_subs heap_val val <i>label</i> labels <i>label_set</i> heap_affect heap_affects heap_context type type_with_hole rec_type_bound	

| rec_type_def
 | type_affect
 | type_affects
 | typing_context
 | **types**
 | command
 | **heap_constructor**
 | judg
 | terminals

$$\ell \in \mathcal{N}(\Phi)$$

$$\ell \notin \mathcal{N}(\Phi)$$

$$\text{type_affect} \in \Gamma$$

$$\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \quad \Gamma_1 \text{ and } \Gamma_2 \text{ are disjoint typing contexts with no clashing variable names or labels}$$

$$\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \wedge \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_3) = \emptyset \wedge \mathcal{N}(\Gamma_2) \cap \mathcal{N}(\Gamma_3) = \emptyset \quad \Gamma_1, \Gamma_2 \text{ and } \Gamma_3 \text{ are fully disjoint typing contexts}$$

$$\mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi) \subset L$$

$$\mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi^{\mathbb{H}}) \sqcup \mathcal{N}(\Psi^t) \subset L$$

$$\ell \in L$$

$$\ell = \text{fresh}(L)$$

$$\text{heap_affect} \in \mathbb{H}$$

$$A = B$$

$$t = u$$

$$\Gamma = D$$

$$\{\ell \triangleleft v', \bar{\ell} \triangleleft \bar{v}\} = \text{deepCopy}(L, [\ell], v) \quad \text{Deep-copy } v \text{ into the memory tree with root } \ell \text{ and fresh labels } \bar{\ell}$$

$$R \stackrel{\text{fix}}{=} \text{rec_type_def}$$

$$A \text{ is destination-free} \quad A \text{ is destination-free}$$

$$C : \bar{A} \xrightarrow{\quad} A \quad \text{Heap constructor } C \text{ builds a value of type } A \text{ given arguments of type } \bar{A}$$

$$\frac{}{() : \cdot \xrightarrow{\quad} 1} \quad \text{TYCTOR_U}$$

$$\frac{}{\text{inl} : A \xrightarrow{\quad} A \oplus B} \quad \text{TYCTOR_INL}$$

$$\frac{}{\text{inr} : B \xrightarrow{\quad} A \oplus B} \quad \text{TYCTOR_INR}$$

$$\frac{}{\langle, \rangle : A \ B \xrightarrow{\quad} A \otimes B} \quad \text{TYCTOR_P}$$

$$\frac{}{\text{Ur} : A \xrightarrow{\quad} !A} \quad \text{TYCTOR_E}$$

$$\frac{R \stackrel{\text{fix}}{=} \mu r. W}{\text{roll } R : W[r := R] \xrightarrow{\quad} R} \quad \text{TYCTOR_R}$$

$$\Phi ; \Psi^{\mathbb{H}} \sqcup \Psi^t ; \bar{U} ; \Gamma \vdash \text{command} : A$$

$$\begin{array}{c}
\mathcal{N}(\Psi^{\mathbb{H}}) \cap \mathcal{N}(\Psi^{\mathbb{t}}) = \emptyset \\
\mathcal{N}(\Phi) \sqcup \mathcal{N}(\Psi^{\mathbb{H}}) \sqcup \mathcal{N}(\Psi^{\mathbb{t}}) \subset \textcolor{red}{L} \\
\Phi ; \Psi^{\mathbb{H}} \vdash \mathbb{H} \\
\Phi ; \Psi^{\mathbb{t}} ; \mathcal{U} ; \Gamma \vdash \mathbf{t} : \textcolor{blue}{A} \\
\hline
\Phi ; \Psi^{\mathbb{H}} \sqcup \Psi^{\mathbb{t}} ; \mathcal{U} ; \Gamma \vdash \textcolor{red}{L} | \mathbb{H} | \mathbf{t} : \textcolor{blue}{A} \quad \text{TYCOMMAND_DEF}
\end{array}$$

$$\boxed{\Phi ; \Psi \vdash \mathbb{H}}$$

$$\begin{array}{c}
\overline{\emptyset ; \emptyset \vdash \emptyset} \quad \text{TYHEAP_EMPTY} \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\Phi ; \Psi_1 \vdash \mathbb{H} \\
\Phi ; \Psi_2 ; \emptyset ; \emptyset \vdash \mathbf{v} : \textcolor{blue}{A} \\
\hline
\Phi \sqcup \{\textcolor{red}{\ell} : \textcolor{blue}{A}\} ; \Psi_1 \sqcup \Psi_2 \vdash \mathbb{H} \sqcup \{\textcolor{red}{\ell} \triangleleft \mathbf{v}\} \quad \text{TYHEAP_VAL}
\end{array}$$

$$\boxed{\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash \mathbf{t} : \textcolor{blue}{A}}$$

$$\begin{array}{c}
\overline{\Phi ; \emptyset ; \mathcal{U} ; \emptyset \vdash \bullet : \perp} \quad \text{TYTERM_NOEFF} \\
\frac{\textcolor{red}{\ell} \notin \mathcal{N}(\Phi)}{\Phi ; \{\textcolor{red}{\ell} : \textcolor{blue}{A}\} ; \mathcal{U} ; \emptyset \vdash \lfloor \textcolor{red}{\ell} \rfloor : \lfloor \textcolor{blue}{A} \rfloor} \quad \text{TYTERM_LDEST} \\
\frac{\Phi ; \Psi ; \mathcal{U} ; \Gamma \sqcup \{\textcolor{violet}{x} : \textcolor{blue}{A}\} \vdash \mathbf{t} : \textcolor{blue}{B}}{\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash \lambda \textcolor{violet}{x} : \textcolor{blue}{A} . \mathbf{t} : \textcolor{blue}{A} \multimap \textcolor{blue}{B}} \quad \text{TYTERM_LAM} \\
\frac{\mathbf{C} : \bar{\textcolor{blue}{A}} \sqsubseteq \textcolor{blue}{A}}{\Phi \sqcup \{\textcolor{red}{\ell} : \bar{\textcolor{blue}{A}}\} ; \emptyset ; \mathcal{U} ; \emptyset \vdash \mathbf{C} \textcolor{red}{\ell} : \textcolor{blue}{A}} \quad \text{TYTERM_HEAPVAL} \\
\frac{}{\Phi ; \emptyset ; \mathcal{U} ; \{\textcolor{violet}{x} : \textcolor{blue}{A}\} \vdash \textcolor{violet}{x} : \textcolor{blue}{A}} \quad \text{TYTERM_ID} \\
\frac{}{\Phi ; \emptyset ; \mathcal{U} \sqcup \{\textcolor{violet}{x} : \textcolor{blue}{A}\} ; \emptyset \vdash \textcolor{violet}{x} : \textcolor{blue}{A}} \quad \text{TYTERM_ID'} \\
\frac{\begin{array}{c} \Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash \mathbf{t} : \textcolor{blue}{A} \multimap \textcolor{blue}{B} \\ \Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \vdash \mathbf{u} : \textcolor{blue}{A} \\ \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\ \mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \end{array}}{\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \mathbf{t} \mathbf{u} : \textcolor{blue}{B}} \quad \text{TYTERM_APP} \\
\frac{\begin{array}{c} \Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash \mathbf{t} : \perp \\ \Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \vdash \mathbf{u} : \textcolor{blue}{B} \\ \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\ \mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \end{array}}{\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \mathbf{t} ; \mathbf{u} : \textcolor{blue}{B}} \quad \text{TYTERM_EFFTHEN} \\
\frac{\begin{array}{c} \Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash \mathbf{t} : \mathbf{1} \\ \Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \vdash \mathbf{u} : \textcolor{blue}{A} \\ \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\ \mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \end{array}}{\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \text{case t of } \{() \mapsto \mathbf{u}\} : \textcolor{blue}{A}} \quad \text{TYTERM_PATU} \\
\frac{\begin{array}{c} \Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash \mathbf{t} : !\textcolor{blue}{A} \\ \Phi ; \Psi_2 ; \mathcal{U} \sqcup \{\textcolor{violet}{x} : \textcolor{blue}{A}\} ; \Gamma_2 \vdash \mathbf{u} : \textcolor{blue}{B} \\ \mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\ \mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \end{array}}{\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \text{case t of } \{ \text{Ur } \textcolor{violet}{x} \mapsto \mathbf{u} \} : \textcolor{blue}{B}} \quad \text{TYTERM_PATE}
\end{array}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A}_1 \oplus \mathbf{A}_2 \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{x_1 : \mathbf{A}_1\} \vdash u_1 : \mathbf{B} \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{x_2 : \mathbf{A}_2\} \vdash u_2 : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \text{case } t \text{ of } \{\text{inl } x_1 \mapsto u_1, \text{inr } x_2 \mapsto u_2\} : \mathbf{B} \quad \text{TYTERM_PATs}
\end{array}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A}_1 \otimes \mathbf{A}_2 \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{x_1 : \mathbf{A}_1, x_2 : \mathbf{A}_2\} \vdash u : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \text{case } t \text{ of } \{\langle x_1, x_2 \rangle \mapsto u\} : \mathbf{B} \quad \text{TYTERM_PATP}
\end{array}$$

$$\begin{array}{c}
R \stackrel{\text{fix}}{=} \mu r . W \\
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{R} \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{x : W[r := R]\} \vdash u : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash \text{case } t \text{ of } \{\text{roll } x \mapsto u\} : \mathbf{B} \quad \text{TYTERM_PATR}
\end{array}$$

$$\frac{\Phi ; \Psi ; \mathcal{U} ; \Gamma \sqcup \{d : \mathbf{A}\} \vdash t : \perp}{\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash \text{alloc } d . t : \mathbf{A}} \quad \text{TYTERM_ALLOC}$$

$$\frac{\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash t : \mathbf{1}}{\Phi ; \Psi ; \mathcal{U} ; \Gamma \vdash t \triangleleft () : \perp} \quad \text{TYTERM_FILLU}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A} \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \vdash u : \mathbf{A} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft u : \perp \quad \text{TYTERM_FILLL}
\end{array}$$

$$\begin{array}{c}
\mathbf{A} \text{ is destination-free} \\
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma \vdash t : \mathbf{!A} \\
\Phi ; \emptyset ; \mathcal{U} ; \emptyset \vdash u : \mathbf{A} \\
\hline
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma \vdash t \triangleleft \text{Ur } u : \perp \quad \text{TYTERM_FILLE}
\end{array}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A}_1 \oplus \mathbf{A}_2 \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{d' : \mathbf{A}_1\} \vdash u : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft \text{inl } d' . u : \mathbf{B} \quad \text{TYTERM_FILLINL}
\end{array}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A}_1 \oplus \mathbf{A}_2 \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{d' : \mathbf{A}_2\} \vdash u : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma \vdash t \triangleleft \text{inr } d' . u : \mathbf{B} \quad \text{TYTERM_FILLINR}
\end{array}$$

$$\begin{array}{c}
\Phi ; \Psi_1 ; \mathcal{U} ; \Gamma_1 \vdash t : \mathbf{A}_1 \otimes \mathbf{A}_2 \\
\Phi ; \Psi_2 ; \mathcal{U} ; \Gamma_2 \sqcup \{d_1 : \mathbf{A}_1, d_2 : \mathbf{A}_2\} \vdash u : \mathbf{B} \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi ; \Psi_1 \sqcup \Psi_2 ; \mathcal{U} ; \Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft \langle d_1, d_2 \rangle . u : \mathbf{B} \quad \text{TYTERM_FILLP}
\end{array}$$

$$\begin{array}{c}
R \stackrel{\text{fix}}{=} \mu r. W \\
\Phi; \Psi_1; \mathcal{U}; \Gamma_1 \vdash t : [R] \\
\Phi; \Psi_2; \mathcal{U}; \Gamma_2 \sqcup \{d : [W[r := R]]\} \vdash u : B \\
\mathcal{N}(\Gamma_1) \cap \mathcal{N}(\Gamma_2) = \emptyset \\
\mathcal{N}(\Psi_1) \cap \mathcal{N}(\Psi_2) = \emptyset \\
\hline
\Phi; \Psi_1 \sqcup \Psi_2; \mathcal{U}; \Gamma_1 \sqcup \Gamma_2 \vdash t \triangleleft_{\text{roll } d}^R u : B \quad \text{TYTERM_FILLR}
\end{array}$$

$$\boxed{\text{command} \Downarrow \text{command}'}$$

$$\begin{array}{c}
\frac{}{L | \mathbb{H} | \bullet \Downarrow L | \mathbb{H} | \bullet} \text{SEMOP_NOEFF (value)} \\
\\
\frac{}{L | \mathbb{H} | [\ell] \Downarrow L | \mathbb{H} | [\ell]} \text{SEMOP_LDEST (value)} \\
\\
\frac{}{L | \mathbb{H} | \lambda x:A. t \Downarrow L | \mathbb{H} | \lambda x:A. t} \text{SEMOP_LAM (value)} \\
\\
\frac{}{L | \mathbb{H} | C \bar{\ell} \Downarrow L | \mathbb{H} | C \bar{\ell}} \text{SEMOP_HEAPVAL (value)} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | \lambda x:A. t' \\
L_1 | \mathbb{H}_1 | u \Downarrow L_2 | \mathbb{H}_2 | v_2 \\
L_2 | \mathbb{H}_2 | t' [x := v_2] \Downarrow L_3 | \mathbb{H}_3 | v_3
\end{array}
}{L_0 | \mathbb{H}_0 | t u \Downarrow L_3 | \mathbb{H}_3 | v_3} \text{SEMOP_APP} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | () \\
L_1 | \mathbb{H}_1 | u \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{() \mapsto u\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATU} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft v_1\} | \text{Ur } \ell \\
L_1 | \mathbb{H}_1 | u [x := v_1] \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{\text{Ur } x \mapsto u\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATE} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft v_1\} | \text{inl } \ell \\
L_1 | \mathbb{H}_1 | u_1 [x_1 := v_1] \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{\text{inl } x_1 \mapsto u_1, \text{inr } x_2 \mapsto u_2\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATINL} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft v_1\} | \text{inr } \ell \\
L_1 | \mathbb{H}_1 | u_2 [x_2 := v_1] \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{\text{inl } x_1 \mapsto u_1, \text{inr } x_2 \mapsto u_2\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATINR} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell_1 \triangleleft v_{11}, \ell_2 \triangleleft v_{12}\} | \langle \ell_1, \ell_2 \rangle \\
L_1 | \mathbb{H}_1 | u [x_1 := v_{11}, x_2 := v_{12}] \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{\langle x_1, x_2 \rangle \mapsto u\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATP} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft v_1\} | \text{roll } \ell \\
L_1 | \mathbb{H}_1 | u [x := v_1] \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | \text{case } t \text{ of } \{\text{roll } x \mapsto u\} \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_PATR} \\
\\
\frac{
\begin{array}{c}
L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | \bullet \\
L_1 | \mathbb{H}_1 | u \Downarrow L_2 | \mathbb{H}_2 | v_2
\end{array}
}{L_0 | \mathbb{H}_0 | t ; u \Downarrow L_2 | \mathbb{H}_2 | v_2} \text{SEMOP_EFFTHEN} \\
\\
\frac{
\begin{array}{c}
\ell = \text{fresh}(L_0) \\
L_0 \sqcup \{\ell\} | \mathbb{H}_0 | t [d := [\ell]] \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft v_1\} | \bullet
\end{array}
}{L_0 | \mathbb{H}_0 | \text{alloc } d. t \Downarrow L_1 | \mathbb{H}_1 | v_1} \text{SEMOP_ALLOC}
\end{array}$$

$$\begin{array}{c}
\frac{L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell]}{L_0 | \mathbb{H}_0 | t \triangleleft () \Downarrow L_1 | \mathbb{H}_1 \sqcup \{\ell \triangleleft ()\} | \bullet} \text{SEMOP_FILLU} \\
\\
\frac{\begin{array}{c} L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 | \mathbb{H}_1 | u \Downarrow L_2 | \mathbb{H}_2 | v_2 \\ \{\ell \triangleleft v_3, \bar{\ell} \triangleleft \bar{v}\} = \text{deepCopy}(L_2, [\ell], v_2) \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft u \Downarrow L_2 \sqcup \{\bar{\ell}\} | \mathbb{H}_2 \sqcup \{\ell \triangleleft v_3, \bar{\ell} \triangleleft \bar{v}\} | \bullet} \text{SEMOP_FILLL} \\
\\
\frac{\begin{array}{c} L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 | \mathbb{H}_1 | u \Downarrow L_2 | \mathbb{H}_2 | v_2 \\ \ell' = \text{fresh}(L_2) \\ \{\ell' \triangleleft v_3, \bar{\ell} \triangleleft \bar{v}\} = \text{deepCopy}(L_2 \sqcup \{\ell'\}, [\ell'], v_2) \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft \text{Ur } u \Downarrow L_2 \sqcup \{\ell', \bar{\ell}\} | \mathbb{H}_2 \sqcup \{\ell \triangleleft \text{Ur } \ell', \ell' \triangleleft v_3, \bar{\ell} \triangleleft \bar{v}\} | \bullet} \text{SEMOP_FILLE} \\
\\
\frac{\begin{array}{c} \ell' = \text{fresh}(L_1) \\ L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 \sqcup \{\ell'\} | \mathbb{H}_1 | u[d := [\ell']] \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell' \triangleleft v_1\} | v_2 \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft \text{inl } d \cdot u \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell \triangleleft \text{inl } \ell', \ell' \triangleleft v_1\} | v_2} \text{SEMOP_FILLINL} \\
\\
\frac{\begin{array}{c} \ell' = \text{fresh}(L_1) \\ L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 \sqcup \{\ell'\} | \mathbb{H}_1 | u[d := [\ell']] \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell' \triangleleft v_1\} | v_2 \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft \text{inr } d \cdot u \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell \triangleleft \text{inr } \ell', \ell' \triangleleft v_1\} | v_2} \text{SEMOP_FILLINR} \\
\\
\frac{\begin{array}{c} \ell_1 = \text{fresh}(L_1) \\ \ell_2 = \text{fresh}(L_1 \sqcup \{\ell_1\}) \\ L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 \sqcup \{\ell_1, \ell_2\} | \mathbb{H}_1 | u[d_1 := [\ell_1], d_2 := [\ell_2]] \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell_1 \triangleleft v_{11}, \ell_2 \triangleleft v_{12}\} | v_2 \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft \langle d_1, d_2 \rangle \cdot u \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell \triangleleft \langle \ell_1, \ell_2 \rangle, \ell_1 \triangleleft v_{11}, \ell_2 \triangleleft v_{12}\} | v_2} \text{SEMOP_FILLP} \\
\\
\frac{\begin{array}{c} \ell' = \text{fresh}(L_1) \\ L_0 | \mathbb{H}_0 | t \Downarrow L_1 | \mathbb{H}_1 | [\ell] \\ L_1 \sqcup \{\ell'\} | \mathbb{H}_1 | u[d := [\ell']] \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell' \triangleleft v_1\} | v_2 \end{array}}{L_0 | \mathbb{H}_0 | t \triangleleft \text{roll}_{\text{R}} d \cdot u \Downarrow L_2 | \mathbb{H}_2 \sqcup \{\ell \triangleleft \text{roll}_{\text{R}} \ell', \ell' \triangleleft v_1\} | v_2} \text{SEMOP_FILLR}
\end{array}$$

Definition rules: 50 good 0 bad

Definition rule clauses: 157 good 0 bad