

Supplementary Statistical Methods

Genetic Disruption of WASHC4 Drives Endo-lysosomal Dysfunction and Cognitive-Movement Impairments in Mice and Humans

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Summary

Here we address concerns about the statistical validity of our previous approach to assess differential protein abundance in the **WASH-iBioID** and **SWIP-TMT** proteomics datasets. Our previous approach depended upon the R package edgeR. We used edgeR to perform both protein- and module-level inference—assessing differential abundance of individual proteins as well as protein groups in SWIP^{P1019R} mouse brain. edgeR utilizes a negative binomial (NB) statistical framework originally developed for analysis of RNA-Seq read count data. Previously, we failed to fully consider the validity of edgeR's NB assumption for proteomics data. We evaluate the goodness-of-fit of the negative binomial model for our TMT dataset and find evidence of a lack-of-fit. Thus, we revise our statistical approach and reanalyze our data, making use of *Huang et al. (2020)*'s recently published R package MSstatsTMT. MSstatsTMT uses a flexible linear mixed-model (LMM) statistical framework which we extend to re-evaluate both protein- and module-level statistical comparisons in our SWIP-TMT spatial proteomics dataset.

Goodness-of-fit of the NB Model for TMT MS

Our previous method can be summarized as the *Sum + IRS* approach (*Huang et al., 2020*). Following protein summarization and internal reference scaling (IRS) normalization (*Plubell et al., 2017*), we applied edgeR (*McCarthy et al., 2012*) to assess differential abundance of individual proteins and protein-groups. The use of edgeR for protein-level comparisons was based on work by *Plubell et al. (2017)* who describe IRS normalization and the use of edgeR for statistical testing in TMT MS experiments (*Plubell et al., 2017*). We failed however, to consider the overall adequacy of edgeR's NB GLM model for our TMT proteomics data.

Statistical inference in edgeR is performed for each gene or protein using a negative binomial, generalized linear model framework. The data are assumed to be adequately described by a NB distribution parameterized by a dispersion parameter, ϕ . The dispersion parameter ϕ accounts for mean-variance relationships in proteomics and transcriptomics data. As signal intensity in protein MS is fundamentally related to the number of ions generated from an ionized, fragmented protein, we incorrectly inferred that TMT mass spectrometry data can be modeled as NB count data. Based on this assumption, we justified our use of edgeR.

To evaluate the overall adequacy of the negative binomial model for TMT proteomics data, we plot the residual protein deviance statistics of all proteins fit with edgeR's NB GLM against their theoretical normal quantiles in a quantile-quantile (QQ) plot (FIG:gof). The QQ plot addresses the question of how similar the observed data are to the theoretical distribution given by the NB model. A linear relationship between the observed and theoretical values is a goodness-of-fit indicator. Deviation from this linear trend is evidence of a lack-of-fit.

Following protein summarization and normalization with MSstatsTMT, the SWIP-TMT data were fit with a NB GLM using edgeR::glmFit. **Figure 2** illustrates the divergence of the observed and theoretical quantiles for our SWIP-TMT dataset fit with edgeR's NB GLM. Given our experimental design, MSstatsTMT fits an appropriate linear-mixed model to the data. The quantile-quantile plot in **Figure 2** indicates that the data are well described by MSstatsTMT's LMM, which does not depend upon the negative binomial assumption.

Protein-wise Linear Mixed-Models

Huang et al. (2020) created MSstatsTMT, an R package for data normalization and hypothesis testing in multiplex TMT proteomics experiments. MSstatsTMT performs statistical inference in two steps. First, each protein in the dataset is fit with a LMM expressing the major sources of variation in the experimental design. Second, given the fitted model, a model-based comparison is made between pairs of treatment conditions. Using LMMs we can untangle the variance attributable to the biological effect we are interested in from the experimental and biological

covariates which mask this response.

Huang et al. (2020) outline a common vocabulary for describing TMT MS experimental design. An experiment consists of $m = 1 \dots M$ concatenations of isobarically labeled samples or Mixtures. This mixture is then analyzed by the mass spectrometer in a single MS Run. This mixture is often fractionated into multiple liquid chromatography Fractions to decrease sample complexity, and thereby increase the depth of proteome coverage. Within a mixture, each of the unique TMT channels is dedicated to the analysis of $c = 1 \dots C$ individual biological or treatment Conditions. There may then be $b = 1 \dots B$ biological replicates or Subjects. Finally, a single TMT mixture may be repeatedly analyzed in $t = 1 \dots T$ technical replicate mass spectrometry runs.

Equation 1 is a LMM describing protein abundance as a function of the major sources of variation in a general TMT experiment composed of M mixtures, T technical replicates of mixture, C conditions, and B biological subjects.

$$Y_{mcbt} = \mu + Condition_c + Mixture_m + TechRep(Mixture)_{m(t)} + Subject_{mcb} + \epsilon_{mcbt} \quad (1)$$

$$\begin{aligned} \sum_{c=1}^C Condition_c &= 0 \\ Mixture_m &\overset{iid}{\sim} N(0, \sigma_M^2) \\ TechRep(Mixture)_{t(m)} &\overset{iid}{\sim} N(0, \sigma_T^2) \\ Subject_{mcb} &\overset{iid}{\sim} N(0, \sigma_S^2) \\ \epsilon_{mcbt} &\overset{iid}{\sim} N(0, \sigma^2) \end{aligned} \quad (2)$$

The model's constraints 2 distinguish fixed- and mixed-effect components of variation in the response, Y_{mcbt} . Mixture is a mixed-effect and represents variation between different TMT mixtures. By definition mixed-effects are assumed to be normally and independently distributed (iid). The term TechRep(Mixture) represents random variation between replicates of a single MS Run. Subject corresponds to each unique biological replicate and represents biological variation among the levels of the fixed-effect term Condition. The term ϵ_{mcbt} is a mixed-effect representing both biological and technical variation, quantifying any remaining error. If a component of the model is not estimable, then it is removed. For example, if there is no technical replication of mixture ($T=0$), then the model is reduced to equation 3.

$$Y_{mcbt} = \mu + Condition_c + Mixture_m + Subject_b + \epsilon_{mcb} \quad (3)$$

SWIP-TMT Spatial Proteomics

We analyzed the brains of mice with the SWIP^{P1019R} mutation by subcellular fractionation and TMT MS profiling. We aimed to reveal how this pathogenic

mutation may perturb the organization of the subcellular proteome. We adapted the subcellular fractionation method of *Geladaki et al. (2019)* to prepare seven subcellular fractions from the brains of control and SWIP^{P1019R} mutant mice. Our experimental design is summarized in *Figure 7*.

Each 16-plex TMT Mixture was composed of fourteen biological fractions or BioFractions obtained from subcellular fractionation of a control and SWIP^{P1019R} mutant mouse brain. We refer to these subcellular preparations as a BioFractions to distinguish them from an MS Fraction. The term Condition of equation 3 represents these fourteen combinations of Genotype and BioFraction.

In our design, Mixture is confounded with Subject. We analyzed all seven BioFractions from a single control and mutant mouse in the same Mixture. We choose to model the effect of Mixture and not Subject based on the assumption that the experimental batch effect represented by the term Mixture is greater than the error inherent in the repeated measures of each Subject. We omit the unestimable terms TechRep(Mixture) and Subject from equation (1). The reduced linear mixed-model describing our experimental design is given by equation 4.

$$Y_{mcbt} = \mu + Condition_c + Mixture_m + \epsilon_{mcb} \quad (4)$$

Statistical Inference with MSstatsTMT

MSstatsTMT performs protein-wise comparisons between pairs of Conditions by comparing the estimates obtained from the LMM fit by restricted maximum likelihood (*Bates et al., 2015*). We are interested in testing the hypothesis:

$$H_0 : l^T * \beta = 0 \quad (5)$$

Where l^T is a vector of $\sum = 1$ specifying the positive and negative coefficients of a contrast. β is the model-based estimates of Condition. The null hypothesis (5) is that the fold change, $l^T * \beta$, is 0. A test statistic for such a two-way contrasts is given by *Kuznetsova et al. (2017)*:

$$t = \frac{l^T \hat{\beta}}{\sqrt{l^T \sigma^2 \hat{V} l}} \quad (6)$$

We obtain the model's estimates, $\hat{\beta}$, error, σ^2 , and variance-covariance matrix, \hat{V} , from the fit LMM. Given a contrast, l^T , the numerator of equation (6) is the fold change of a comparison. The product of σ^2 and \hat{V} is the scaled variance-covariance matrix describing error estimates of the model's fixed- and mixed-effect parameters. Together the denominator represents the standard error of the comparison. The degrees of freedom for the contrast are derived using the Satterthwaite moment of approximation method (*Kuznetsova et al., 2017*). Finally, a p-value is calculated given the t-statistic and degrees of freedom. P-values for

the protein-wise tests are adjusted using the Benjamini-Hochberg FDR method (*Huang et al., 2020*).

We used MSstatsTMT to assess two types of contrasts. Intra-BioFraction comparisons are the seven pairwise comparisons of control and mutant protein abundance for each BioFraction. We also assessed the overall Mutant–Control comparison. Each of these contrasts is represented by a vector, I^T , which specifies a contrast between coefficients of Condition in the LMM (4). **Figure 8** illustrates the two types of protein-level statistical comparisons we implement with MSstatsTMT.

Module-level Inference with Mixed-Models

The strength of linear mixed-models lies in their flexibility. In a mixed-model the response variable is taken to be a function of both fixed- and random-effects. If the set of possible levels of a covariate is fixed and reproducible, then the factor is modeled as a fixed-effect parameter. In contrast, if the levels of an observation reflect a sampling of the set of all possible levels, then the covariate is modeled as a random-effect. Random or mixed-effects represent categorical variables that reflect experimental or observational units within the dataset. As such, mixed-effect parameters account for the variation occurring among lower levels of an upper level unit in the data (*Bates et al., 2015*).

We wish to extend the LMM framework developed by MSstatsTMT to perform inference at the level of protein groups. Given a map partitioning the proteome into modules of covarying proteins, we wish to assess the module-level difference between control and SWIP^{P1019R} conditions. We fit the data for each module in the dataset with a LMM. We represent the proteins within each module as the mixed-effect term Protein, capturing variation among a module’s constituent proteins.

$$Y_{mcbt} = \mu + Condition_c + Mixture_m + Protein_p + \epsilon_{mcb} \quad (7)$$

$$Protein_p \stackrel{iid}{\sim} N(0, \sigma_p^2)$$

The term Protein in equation 7 quantifies the variance σ_p attributable to heterogeneity among a modules proteins.

LMM Goodness-of-fit

It is useful to consider the goodness-of-fit of our models. A straight forward measure of a LMM’s quality is the Nakagawa coefficient of determination (*Nakagawa and Schielzeth, 2012*). *Nakagawa and Schielzeth (2012)*’s conditional R_c^2 is interpreted as the total variance explained by a LMM (R_{total}^2). The marginal R_m^2 is interpreted as the variance explained by the LMM’s fixed-effects (R_{fixed}^2). We implement *Nakagawa and Schielzeth (2012)*’s coefficient of determination using

the `r.squaredGLMM` function taken from the `MuMin` package (*Wang and Merkle, 2018*).

In addition to considering the total variance explained by a module, it is helpful to consider the variance explained by each of its factors. The R package `variancePartition` enables us to calculate the percent variance explained by a LMM's parameters `cite(variancePartition)`.

Spatial Proteomics Network Construction

Using our SWIP-TMT dataset, we aim to identify modules or groups of proteins that covary together across subcellular space. Prior to building the co-variation network, other sources of variation should be removed. Although `MSstatsTMT` handles the batch effect inherent in experiments with multiple TMT mixtures, it is necessary to remove this effect prior to building the network. We removed the effect of `Mixture` using `limma::RemoveBatchEffect`. These adjusted data are used for network construction and plotting, but not statistical modeling.

Prior to network construction, we removed protein models with poor fit ($R^2_{total} < 0.7$; $n=791$ proteins). Removing this noisy proteins facilitation module identification and improves overall module quality.

The final network was constructed using data from both Control and Mutant samples after adjusting for batch (`Mixture`). The final dataset included 42 samples and 6,119 proteins. The protein covariation network was build by calculating the Pearson correlation for all pairwise comparisons of proteins.

We performed network enhancement to remove biological noise from the network prior to clustering. This step is essential in large, and dense networks for module detection. Network enhancement reweights the network's edges and has the overall effect of making the network sparse. Conceptually this step is related to the soft-thresholding approach taken by WGCNA or WPCNA analysis workflows (REFS), but has the benefit of not assuming that the network has an overall scale-free topology. Without reweighting or enhancing the network, most extant clustering algorithms fail to detect communities in the dataset. Network enhancement has the effect of making the network sparse and facilitates the identification of network structure.

Community Detection with Leidenalg

To reveal the structure of our spatial proteomics network we used the recently published Leiden algorithm (*Traag et al., 2019*).

Implementation

In order to understand and extend the function of `MSstatsTMT`, we extracted `MSstatsTMT`'s core model-fitting and statistical testing steps. At the core of the model fitting-step is the R package `lme4` which implements mixed-effects models with its function `lme4::lmer` (*Bates et al., 2015*). The package `lmerTest` extends `lme4`'s functionality and enables the computation of Satterthwaite degrees of freedom (*Kuznetsova et al., 2017*).

Fit WASHC4

As a means of example, we demonstrate the model fitting statistical testing steps for both and protein- and module-level statistical comparisons. First, we fit the LMM in (4) the normalized protein level data from `MSstatsTMT` for WASHC4.

```
## fit the protein-level model to WASHC4

# load dependencies
library(dplyr)
library(lmerTest)

# load SwipProteomics
data(swip)
data(msstats_prot)

# LMM formula
fx0 <- 'Abundance ~ 0 + Genotype:BioFraction + (1|Mixture)'

# fit the model
fm0 <- lmer(fx0, data = msstats_prot %>% subset(Protein == swip))

# examine the model's summary
summary(fm0, ddf = "Satterthwaite")
```

'MutantF7-ControlF7'

We assess the contrast between `BioFraction` seven (F7) mutant and control conditions.

```
## compare 'Mutant:F7' and 'Control:F7' conditions

# create a contrast
coeff <- lme4::fixef(fm0)
```

```
contrast7 <- setNames(rep(0,length(coeff)), nm = names(coeff))
contrast7["GenotypeMutant:BioFractionF7"] <- +1 # positive coeff
contrast7["GenotypeControl:BioFractionF7"] <- -1 # negative coeff

# evaluate contrast
lmerTestContrast(fm0, contrast7)
```

'Mutant-Control'

Provided the correct contrast, we easily evaluate the overall difference between mutant and control mice.

```
# create a contrast to compare 'Mutant' versus 'Control'
contrast8 <- getContrast(fm0, "Mutant","Control")

# evaluate contrast
lmerTestContrast(fm0, contrast8)
```

Fit WASH Complex

Next we fit a LMM to the five WASH complex proteins.

```
# the module-level formula to be fit:
fx1 <- 'Abundance ~ 0 + Condition + (1|Mixture) + (1|Protein)'

# load WASH Complex proteins
data(washc_prots)

fm1 <- lmer(fx1, data=msstats_prot %>% subset(Protein %in% washc_prots))

# assess 'Mutant-Control' comparison
lmerTestContrast(fm1, contrast8)
```

We evaluate the goodness of fit of our module-level model.

```
# assess gof with Nakagawa coefficient of determination
r.squaredGLMM.merMod(fm0)

r.squaredGLMM.merMod(fm1)
```


variancePartition

We compute the variance explained using variancePartition.

```
# load variancePartition
suppressPackageStartupMessages({
  library(variancePartition)
})

# calculate partitioned variance
form <- "Abundance ~ (1|Genotype) + (1|BioFraction) + (1|Mixture) + (1|Protein)"
fit <- lmer(form, data = msstats_prot %>% filter(Protein %in% washc_prots))

calcVarPart(fit)
```

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Coefficient	Estimate	SE	DF	t value	p value
Mutant:F4	5.40	0.121	17.31	44.62	2.59e-19
Control:F4	6.71	0.121	17.31	55.40	6.26e-21
Mutant:F5	5.57	0.121	17.31	45.96	1.56e-19
Control:F5	6.95	0.121	17.31	57.34	3.47e-21
Mutant:F6	5.64	0.121	17.31	46.56	1.24e-19
Control:F6	7.24	0.121	17.31	59.77	1.7e-21
Mutant:F7	5.63	0.121	17.31	46.49	1.28e-19
Control:F7	7.32	0.121	17.31	60.44	1.4e-21
Mutant:F8	5.49	0.121	17.31	45.35	1.96e-19
Control:F8	7.13	0.121	17.31	58.86	2.21e-21
Mutant:F9	5.78	0.121	17.31	47.73	8.15e-20
Control:F9	6.95	0.121	17.31	57.42	3.39e-21
Mutant:F10	5.78	0.121	17.31	47.76	8.07e-20
Control:F10	7.62	0.121	17.31	62.90	7.04e-22

Figure 1. This is a caption.

Supplemental Tables

Supplemental Figures

- gof
- design
- contrasts
- ...

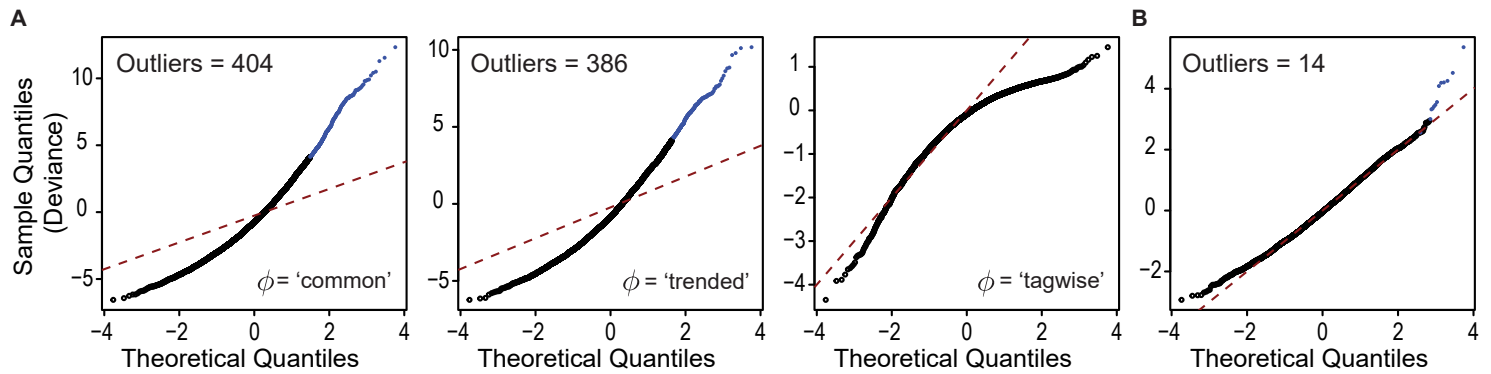


Figure 2. Goodness-of-fit of edgeR (A), and MSstatsTMT (B) statistical approaches. The overall adequacy of the linear models fit to the data were assessed by plotting the residual deviance for all proteins as a quantile-quantile plot (McCarthy *et al.*, (2012)). **(A)** For analysis with edgeR, The normalized protein data from MSstatsTMT were fit with a negative binomial generalized linear model of the form: $\text{Abundance} \sim \text{Mixture} + \text{Condition}$. Where *Mixture* is an additive blocking factor that accounts for variability between experiments. The NB framework used by edgeR utilizes a dispersion parameter ψ to account for mean-variance relationships in the data. The dispersion parameter can take several forms including: 'common', 'trended', and 'tagwise'. We plot the deviance statistics for the data fit with each of the three dispersion parameters against their theoretical normal quantiles using the `edgeR::gof` function. **(B)** For analysis with MSstatsTMT, the normalized protein data were fit with a linear mixed-effects model (LMM) of the form: $\text{Abundance} \sim 0 + \text{Condition} + (1|\text{Mixture})$. Where *Mixture* represents the mixed-effect of *Mixture*. The residual deviance and degrees of freedom were extracted from the fitted models, z-score normalized, and plotted as in (A). Proteins with a significantly poor fit are indicated as outliers in blue (Holm-adjusted P-value < 0.05).

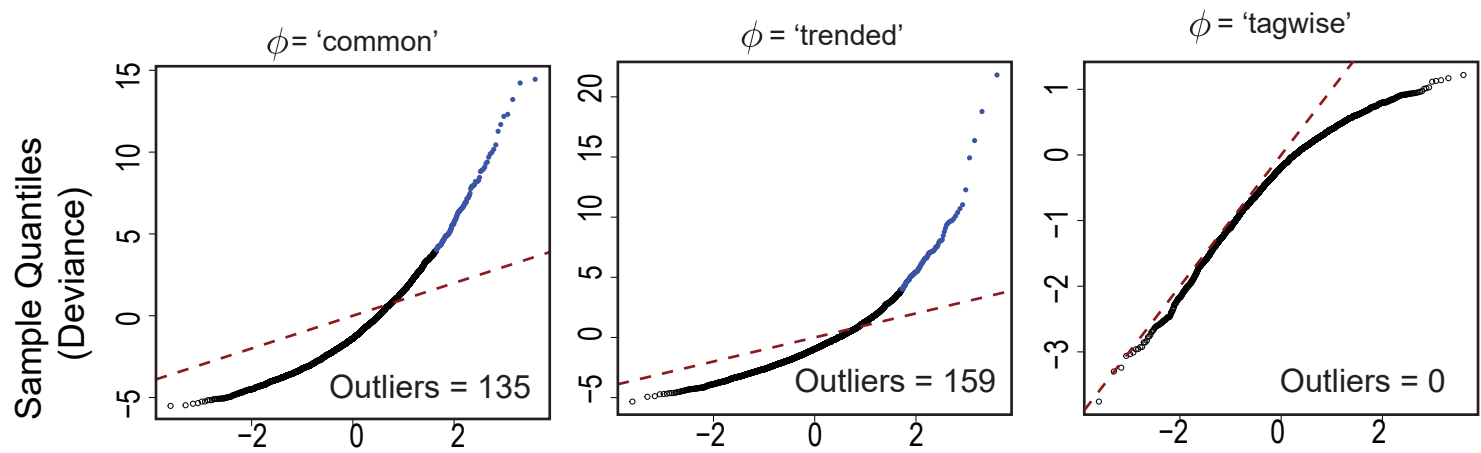


Figure 3. Goodness-of-fit for the edgeR NB GLM for the Khan *et al*, (2018) dataset.

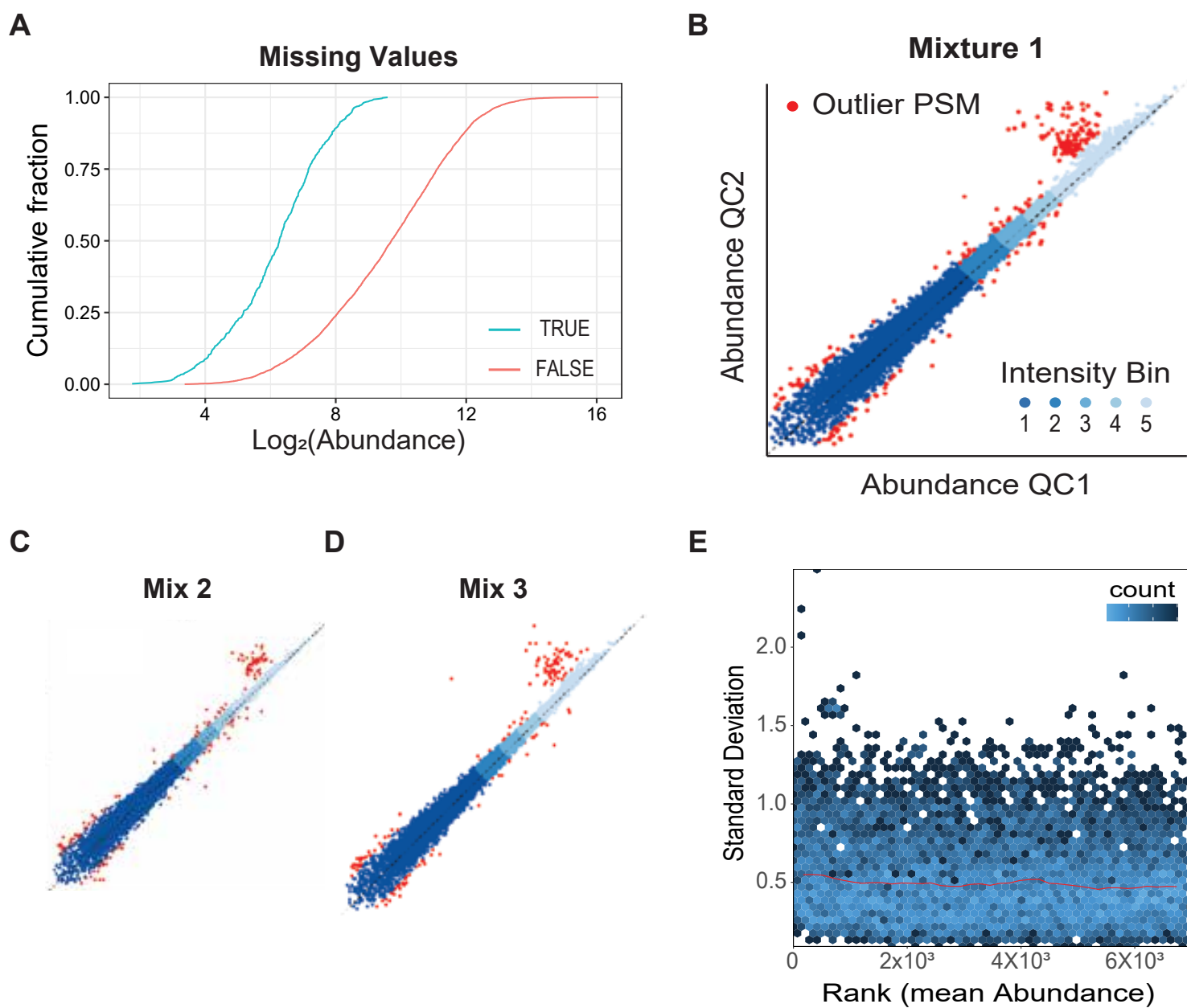


Figure 4. Missing value imputation and PSM outlier removal. A B C D

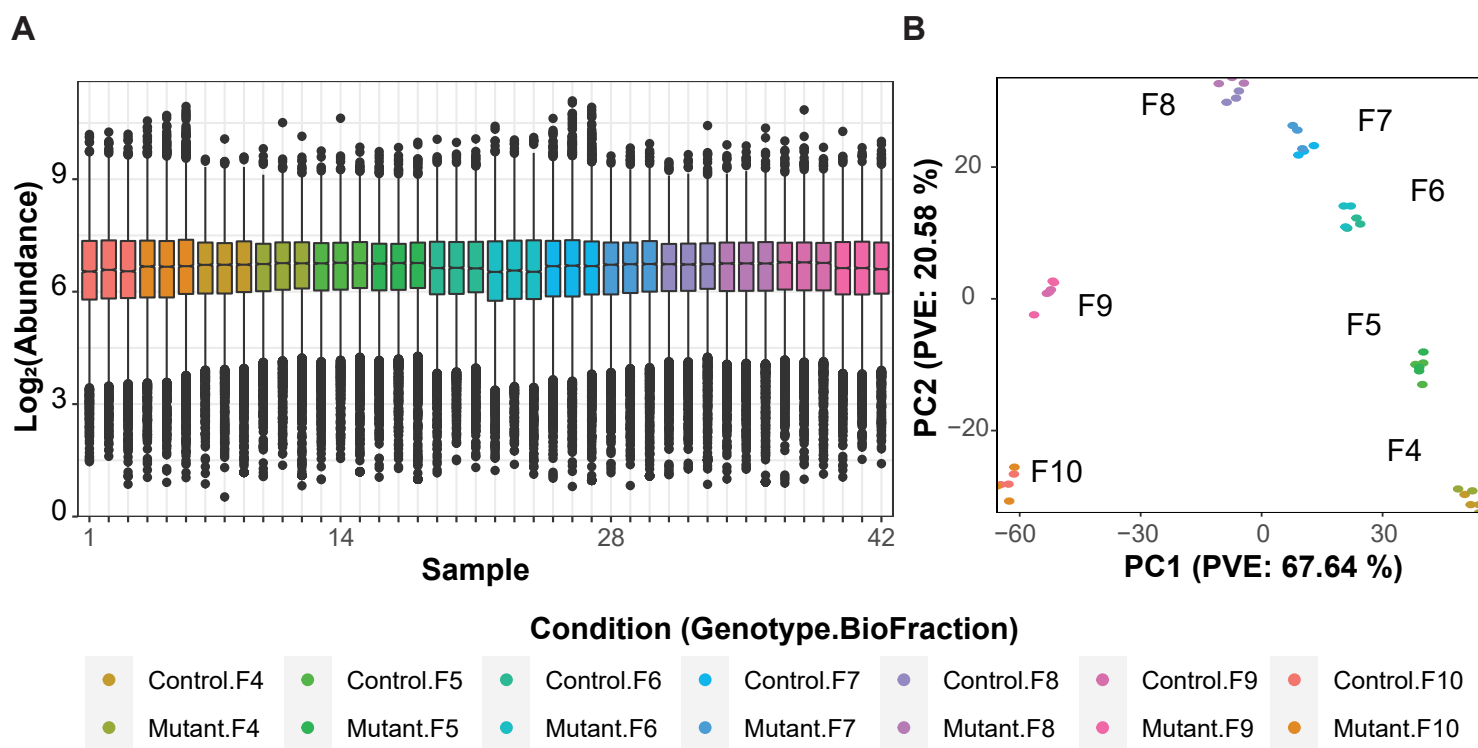


Figure 5. Data Normalization and PCA. A B

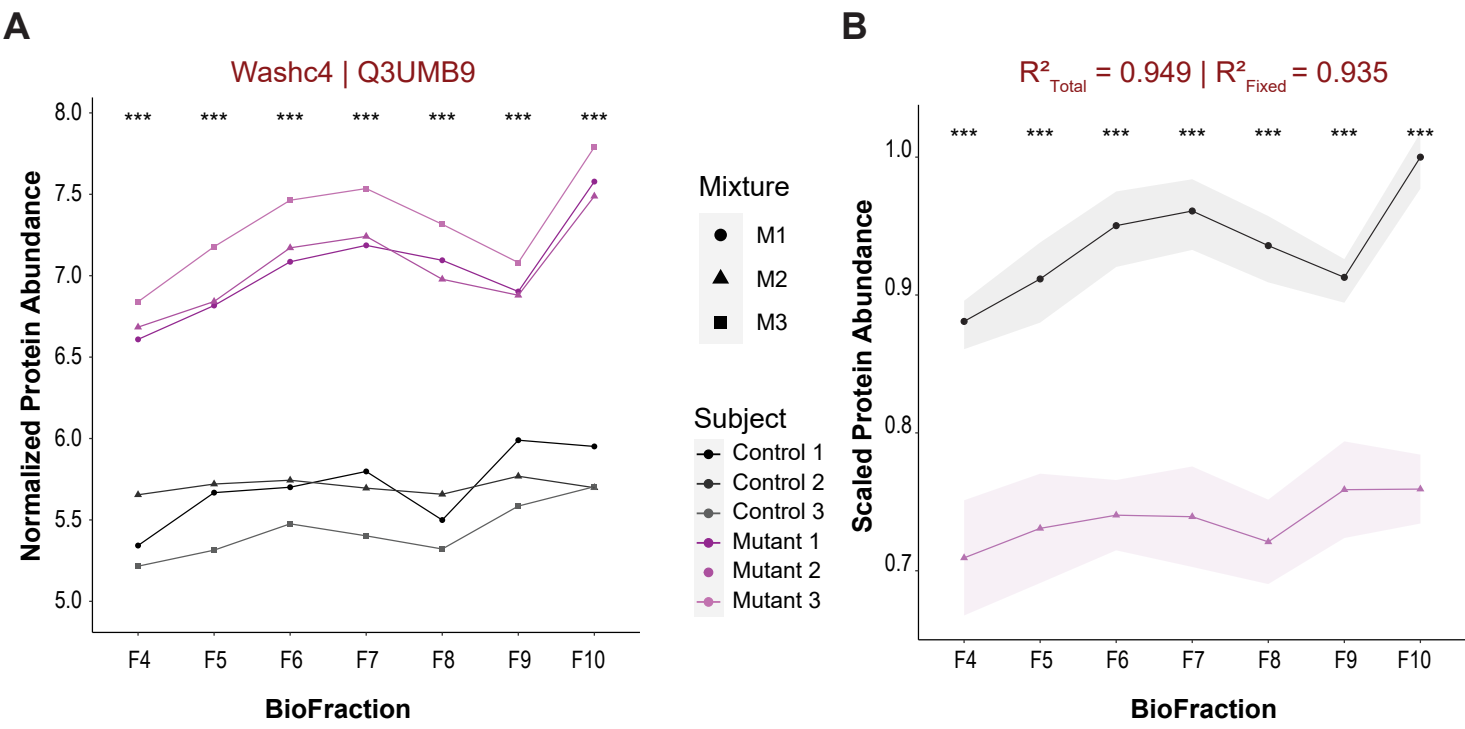


Figure 6. Data Normalization and PCA. A B

TMT Channel

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	C14	C15	C16
Mix1	WT-5K	WT-9K	WT-12K	WT-15K	WT-30K	WT-79K	WT-129K	QC1	MUT-5K	MUT-9K	MUT-12K	MUT-15K	MUT-30K	MUT-79K	MUT-129K	QC2
Mix2	WT-5K	WT-9K	WT-12K	WT-15K	WT-30K	WT-79K	WT-129K	QC1	MUT-5K	MUT-9K	MUT-12K	MUT-15K	MUT-30K	MUT-79K	MUT-129K	QC2
Mix3	WT-5K	WT-9K	WT-12K	WT-15K	WT-30K	WT-79K	WT-129K	QC1	MUT-5K	MUT-9K	MUT-12K	MUT-15K	MUT-30K	MUT-79K	MUT-129K	QC2

Figure 7. Experimental Design. We performed three 16-plex TMT experiments. Each TMT mixture is a concatenation of 16 labeled samples. In each experiment we analyzed seven subcellular BioFractions prepared from the brain of a single Control and 'Mutant' mouse. In all, we analyzed three Subjects from each Condition. Each Mixture includes two Channels dedicated to the analysis of a common quality control (QC) sample for normalization between MS runs.

		<div>Genotype</div> <div><div>Control (-1/7)</div><div>Mutant (+1/7)</div></div>													
		BioFraction													
Contrasts	l^T	F4	F5	F6	F7	F8	F9	F10	F4	F5	F6	F7	F8	F9	F10
L1	Mutant.F4-Control.F4	-1	0	0	0	0	0	0	+1	0	0	0	0	0	0
L2	Mutant.F5-Control.F5	0	-1	0	0	0	0	0	0	+1	0	0	0	0	0
L3	Mutant.F6-Control.F6	0	0	-1	0	0	0	0	0	0	+1	0	0	0	0
L4	Mutant.F7-Control.F7	0	0	0	-1	0	0	0	0	0	0	+1	0	0	0
L5	Mutant.F8-Control.F8	0	0	0	0	-1	0	0	0	0	0	0	+1	0	0
L6	Mutant.F9-Control.F9	0	0	0	0	0	-1	0	0	0	0	0	0	+1	0
L7	Mutant.F10-Control.F10	0	0	0	0	0	0	-1	0	0	0	0	0	0	+1
L8	Mutant-Control	-1/7	-1/7	-1/7	-1/7	-1/7	-1/7	-1/7	+1/7	+1/7	+1/7	+1/7	+1/7	+1/7	+1/7
		1	Coefficients						β	16					

Figure 8. Statistical Comparisons. We assessed two types of contrasts. Each row of the matrix specifies a contrast between positive and negative coefficients in the mixed-effects model fit to each protein. Contrasts 1-7 are intra-BioFraction contrasts that specify the pairwise comparisons of Control and Mutant groups for a single fraction. In Contrast 8 we compare Mutant-Control and assess the overall difference of Control and Mutant conditions. Each contrast is a vector of sum 1.

$$Y_{mtcb} = \mu + Mixture_m + Condition_{cb} + \epsilon_{mcb}$$

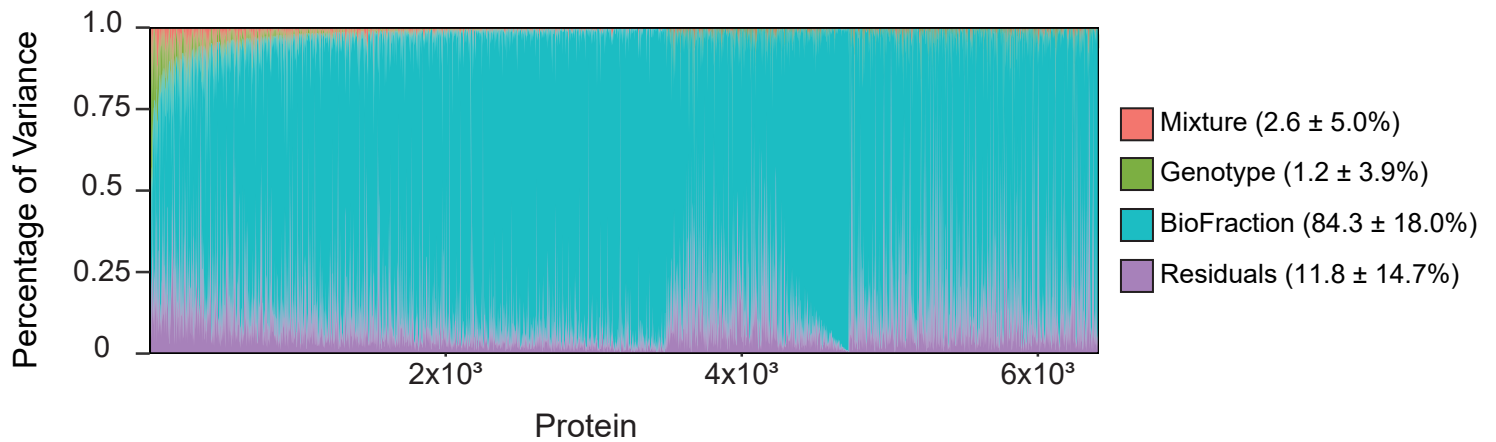


Figure 9. Analysis of Variance Components. The proportion of variance explained by Genotype, BioFraction, Mixture, and remaining residual error (subplot error) for all proteins. Note while the contribution of Mixture seems negligible, its average for all proteins is approximately twice the average percent variance explained by Genotype. BioFraction explains the majority of the variance for all proteins. Analysis done with `variancePartition::calcVarPart`.