Modern type-safe embedding of attribute grammars

An exercise with functional zippers in Haskell

João Paulo Fernandes¹, Pedro Martins², Alberto Pardo³, João Saraiva⁴, Marcos Viera³, and Tom Westerhout⁵

- CISUC Universidade de Coimbra, Portugal jpf@dei.uc.pt
 University of California, Irvine, USA pribeiro@uci.edu
- Universidad de la República, Uruguay, {pardo,mviera}@fing.edu.uy
 Universidade do Minho, Portugal, saraiva@di.uminho.pt
- ⁵ Radboud University, The Netherlands, t.westerhout@student.ru.nl

Abstract. Attribute grammars are a powerful, declarative formalism to implement and reason about programs which, by design, are conveniently modular. Although a full attribute grammar compiler can be tailored to specific needs, its implementation is highly non-trivial, and its long-term maintenance is a major endeavor. In fact, maintaining a traditional attribute grammar system is such a big effort that most systems that were proposed in the past are no longer active. Our approach to implementing attribute grammars is to write them as first-class citizens of a modern functional programming language. We improve a previous zipper-based attribute grammar embedding making it non-intrusive (i.e. no changes to the user-defined data types are required) and type-safe. On top of that, we achieve clearer syntax by using modern Haskell extensions. We believe that our embedding can be employed in practice to implement elegant, efficient, and modular solutions to real-life programming challenges.

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1 Introduction

Attribute Grammars (AGs) are a declarative formalism which was proposed by Knuth [8] in the late 60s and allows one to implement and reason about programs in a modular and convenient way. A concrete AG relies on a context-free grammar to define the syntax of a language, and on attributes associated with the productions of the grammar to define the semantics of that language. AGs have been used in practice to specify real programming languages, like for example Haskell [3], as well as powerful pretty printing algorithms [18], deforestation techniques [5], and powerful type systems [12].

When programming with AGs, modularity is achieved due to the possibility of defining and using different aspects of computations as separate attributes.

Attributes are distinct computation units, typically quite simple and modular, that can be combined into elaborated solutions to complex programming problems. They can also be analyzed, debugged, and maintained independently which eases program development and evolution.

AGs have proven to be particularly useful to specify computations over trees: given one tree, several AG systems such as [15, 4, 9, 20] take specifications of which values or attributes need to be computed and perform these computations. The design and coding efforts put into the creation, improvement, and maintenance of these AG systems, however, is tremendous which is often an obstacle to achieving the success they deserve.

An increasingly popular alternative approach to the use of AGs relies on embedding them as first-class citizens of general purpose programming languages [13, 10, 14, 16, 21, 2]. This avoids the burden of implementing a totally new language and associated system by hosting it in state-of-the-art programming languages. Following this approach one then exploits the modern constructions and infrastructure that are already provided by those languages and focuses on the particularities of the domain specific language being developed.

Functional zipper [7] is a powerful abstraction which greatly simplifies the implementation of traversal algorithms performing a lot of local updates. Functional zippers have successfully been applied to construct an AG embedding in Haskell [10, 11]. Despite its elegance, this solution had a major drawback which prevented its use in real-world applications: attributes were not cached, but rather repeatedly recomputed which severely hurt performance. Recently, this flaw has been eliminated [6] and replaced with a different one: the approach became intrusive, i.e. to benefit from the embedding user-defined data structures have to be adjusted.

In this paper we present an alternative mechanism to cache attributes based on a self-organising infinite grid. This graph is laid on top of the user-defined algebraic data type (ADT) and mirrors its structure. The used-defined data type itself remains untouched. The embedding is then based on two (rather than one) coherent zippers traversing the data structures in parallel. On top of being non-intrusive our solution is completely type-safe. Modern Haskell extensions such as ConstraintKinds allow us to propagate constraints down in the ADT completely eliminating run-time type casts present in the previous versions. Another side benefit of using modern Haskell features is a cleaner syntax with less code being generated by means of Template Haskell.

2 Functional Zippers

Zipper is a data structure commonly used in functional programming for traversal with fast local updates. The zipper data structure was originally conceived by Huet[7] in the context of trees. We will, however, first consider a simpler problem: a bidirectional list traversal.

Lists Suppose that we would like to update a list at a specific position:

Here modify takes an update action f^6 , an index i, and a list xs and returns a new list with the i'th element replaced with the result of f.First, we "unpack" the list into before = $[xs_0, \dots xs_{i-1}]$, $x = xs_i$, and after = $[xs_{i+1}, \dots]$. Then replace x by f(x) and finally "pack" the result back into a single list. If we do a lot of updates, we end up unpacking and packing the list over and over again – very time-consuming for long lists. We would thus like to benefit from fusion without explicitly working with the unpacked representation as it is bug-prone. A list zipper provides a way to achieve this.

A zipper consists of a focus (alternatively called a hole) and surrounding ${\rm context}^7$:

```
data Zipper a = Zipper { _hole :: a, _cxt :: !(Context a) }
data Context a = Context [a] [a]
```

where the *Context* keeps track of elements to the left (before in modify) and to the right (after in modify) of the focus. We can now define movements:

```
left (Zipper _ (Context [] _)) = Nothing
left (Zipper hole (Context (1 : ls) rs)) = Just $
    Zipper l $ Context ls (hole : rs)

right :: Zipper a \rightarrow Maybe (Zipper a)
right (Zipper _ (Context _ [])) = Nothing
right (Zipper hole (Context ls (r : rs))) = Just $
    Zipper r $ Context (hole : ls) rs
```

and functions for entering and leaving the zipper:

left :: $Zipper a \rightarrow Maybe (Zipper a)$

```
enter :: [a] \rightarrow Maybe (Zipper a)

enter [] = Nothing

enter (x : xs) = Just $ Zipper x (Context [] xs)

leave :: Zipper a \rightarrow [a]

leave (Zipper hole (Context ls rs)) = reverse ls ++ hole : rs
```

 $^{^6}$ f returns a list rather than a single element to prevent curious readers from suggesting to use a boxed array instead of a list.

⁷ '!' in front of the type of _cxt is a strictness annotation enabled by the BangPatterns extension. Context can be seen as a path from the to the current focus and is always finite, i.e. there is no reason for it to be lazy.

Finally, we define a local version of our modify function (**TODO:** Boy, is this function ugly...)

```
modify :: (a \rightarrow [a]) \rightarrow Zipper a \rightarrow Maybe (Zipper a) modify f (Zipper hole (Context ls rs)) = case f hole of (x : xs) \rightarrow Just $ Zipper x (Context ls (xs ++ rs)) [] \rightarrow case rs of (r : rs') \rightarrow Just $ Zipper r (Context ls rs') [] \rightarrow case ls of (1 : ls') \rightarrow Just $ Zipper l (Context ls' rs) \rightarrow Nothing
```

using which we can perform multiple updates efficiently and with minimal code bloat 8 :

Trees Consider now a binary tree data structure:

```
data Tree a = Leaf !a | Fork (Tree a) (Tree a)
```

A binary tree zipper is slightly more insteresting than the list zipper, because we can move up and down the tree as well as left and right. The zipper again consists of a hole (a subtree we are focused on) and its surrounding context (a path from the hole to the root of the tree):

To move the zipper down, we "unpack" the current hole:

```
down :: Zipper \ a \rightarrow Maybe \ (Zipper \ a)
down (Zipper \ (Leaf \_) \ \_) = Nothing
down (Zipper \ (Fork \ 1 \ r) \ cxt) = Just \ \ Zipper \ r \ (Right \ 1 \ cxt)
```

```
(>=>) :: Monad m => (a \rightarrow m b) \rightarrow (b \rightarrow m c) \rightarrow a \rightarrow m c
```

⁸ Operator >=> comes from *Control.Monad* module in base and has the following signature:

Context stores everything we need to reconstruct the hole, and up does exactly that:

```
up :: Zipper a \rightarrow Maybe (Zipper a)

up (Zipper _ Top) = Nothing

up (Zipper l (Left cxt r)) = Just $ Zipper (Fork l r) cxt

up (Zipper r (Right l cxt)) = Just $ Zipper (Fork l r) cxt
```

Implementations of left, right, and enter are very similar to the list zipper case and are left as an exercise for the reader. leave differs slightly in that we now move all the way up rather than left:

```
leave :: Zipper a \rightarrow Tree a
leave z = case up z of
  Just z' \rightarrow leave z'
  Nothing \rightarrow _hole z
```

Generic Zipper The list and binary tree zippers we have considered so far are homogeneous zippers: the type of the focus does not change upon zipper movement. Such a zipper can be a very useful abstraction. For example, a well-known window manager XMonad[17] uses a rose tree zipper to track the window under focus. For other tasks, however, one might need to traverse heterogeneous structures. A zipper that can accommodate such needs is usually called a generic zipper as it relies only on the generic structure of Algebraic Data Types (ADTs). One can view an ADT as an Abstract Syntax Tree (AST) where each node is a Haskell constructor rather than a syntax construct.

The generic zipper we will use is very similar to the one presented in[1]. The most common technique in Haskell for supporting heterogeneous types is Existential Quantification. However, not every type can act as a hole. To support moving down the tree, we need the hole to be dissectible, i.e. we would like to be able to dissect the value into the constructor and its arguments. Even though Data.Data.gfoldl allows us to achieve this, we define out own typeclass which additionally allows us to propagate down arbitrary constraints:

For example, here is how we can make Tree an instance of Dissectible

```
instance c (Tree a) => Dissectible c (Tree a) where
  dissect (Fork 1 r) = LOne Fork 'LCons' 1 'LCons' r
  dissect x = LOne x
```

We can unpack a *Fork* and the zipper will thus be able to go down. *Leafs*, however, are left untouched and trying to go down from a *Leaf* will return *Nothing*.

To allow the zipper to move left and right, we need a means to encode arguments to the right of the hole. Following Adams et al, we define a GADT representing constructor arguments to the right of the hole:

```
data Right c provides r where
    RNil :: Right c r r
    RCons :: (c b, Dissectible c b)
           => b 	o Right c provides r 	o Right c (b 	o provides) r
For example, for a tuple (Int, Int, Int, Int, Int, Int), we can have
  lefts = LOne (,,,,,) 'LCons' 1 'LCons' 2 'LCons' 3
  hole = 4
  rights = 5 'RCons' 6 'RCons' RNil
generalising this a little, we arrive at:
  data LocalContext c hole rights parent =
    LocalContext !(Left c (hole \rightarrow rights)) !(Right c rights parent)
  data \mathit{Context} :: (\mathit{Type} \rightarrow \mathit{Constraint}) \rightarrow \mathit{Type} \rightarrow \mathit{Type} \rightarrow \mathit{Type} where
    RootContext :: ∀ c root. Context c root root
    (:>) :: ∀ c parent root hole rights. (c parent, Dissectible c parent)
          => !(Context c parent root)
          → !(LocalContext c hole rights parent)

ightarrow Context c hole root
And just like before the Zipper is a product of the hole and context:
  data Zipper (c :: Type \rightarrow Constraint) (root :: Type) =
    ∀ hole. (c hole, Dissectible c hole) =>
       Zipper { _zHole :: !hole
               , _zCxt :: !(Context c hole root)
}
```

Implementation of movements is quite straightforward and is left out. Please, refer to (**TODO**: *github repo*) for complete code. We now consider a rather interesting application of generic zipper: embedding of attribute grammars.

3 Attribute Grammars

Attribute grammars (AGs) are an extension of context-free grammars that allow to specify context-sensitive syntax as well as the semantics. AGs achieve it by associating a set of attributes with each grammar symbol. These attributes are defined using evaluation rules assiciated with production rules of the context-free grammar.

Attributes are then usually divided into two disjoint sets: synthesized attributes and the inherited attributes. Such distinction is required for the construction of a dependency graph. It is then used for specification of the evaluation order and detection of circularity. In the zipper-based embedding of attribute grammars we make no use of a dependency graph and thus do not divide attributes into classes.

Let us consider the repmin problem as an example of a problem that requires multiple traversals:

Given a tree of integers, replace every integer with the minimum integer in the tree, in one pass.

The classical solution is the following circular program:

Although quite elegant, the code lacks modularity and is very difficult to reason about. Attribute Grammars provide a more modular approach. Viera et al[22] identified three steps for solving repmin: computing the minimal value, passing it down from the root to the leaves, and constructing the resulting tree. We can associate each step with an attribute[19]:

- A synthesized attribute localMin :: Int represents the minimum value of a subtree. Computing the minimal value thus corresponds to evaluation of the localMin attribute for the root tree.
- An inherited attribute globalMin :: Int is used to pass down the minimal value.
- Finally, a synthesized attribute updated :: Tree Int is the subtree with leaf
 values replaced by values of their globalMin attributes. The solution is thus
 the value of updated attribute for the root tree.

The obtained AG is presented in figure 1. **TODO:** Do we actually need to explain the algorithms here? It seems a little bit childish to explain how to compute the minimum of a binary tree... If we absolutely have to explain stuff, maybe just put it in the caption.

We now move on to embed this attribute grammar into Haskell. Semantic rules simply become functions, which, given a zipper, return values of the attributes. For example,

```
{	t localMin}:: {	t Zipper} ({	t WhereAmI Position}) (Tree Int) 	o Int
```

Fig. 1: Attribute grammar for repmin. The syntax is closely mirrors the one used in [19]. SYN and INH introduce synthesized and inherited attributes respectively. SEM is used for defining semantic rules. A new data type *Root* is introduced as it is common in the AG setting to "connect" localMin with globalMin.

```
localMin z@(Zipper \text{ hole } \_) = \mathbf{case} whereami hole of C_{Leaf} \rightarrow \mathbf{let} \ Leaf \ x = \mathbf{hole} \ \mathbf{in} \ x
C_{Fork} \rightarrow \mathbf{let} \ Just \ 1 = \mathbf{child} \ 0 \ z; \ Just \ r = \mathbf{child} \ 1 \ z
\mathbf{in} \ \mathbf{min} \ (\mathbf{localMin} \ 1) \ (\mathbf{localMin} \ r)
```

Apart from the type signature, the code is pretty straightforward and closely mirrors the AG we defined earlier. whereami function allows us to "look around" and returns the position of the zipper. Thus the case corresponds to the pattern matches on the left of the vertical bars on figure 1.

Position of the zipper is encoded using the following GADT which can be generated automatically using Template Haskell:

```
data Position :: Type 
ightarrow Type where C_{Leaf} :: Position (Tree Int) C_{Fork} :: Position (Tree Int)
```

Parametrization on the type of the hole allows the code like $let\ Leaf\ x = hole\ in\ x$ to typecheck, even though the generic zipper itself knows close to nothing about the type of the hole. It might seem trivial at first, because the binary tree zipper is in fact homogeneous. The "position trick" however extends also to heterogeneous zippers which we will encounter in more advanced examples.

```
\texttt{child} \; :: \; \textit{Int} \; \rightarrow \; \textit{Zipper} \; \texttt{cxt} \; \texttt{root} \; \rightarrow \; \textit{Maybe} \; (\textit{Zipper} \; \texttt{cxt} \; \texttt{root})
```

child n moves the zipper to the n'th child, if there is one.

4 Related Work

5 Conclusion

Acknowledgements

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