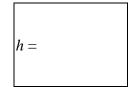
# Hong Kong Mathematics Olympiad (1989 – 1990) **Sample Event (Individual)**

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

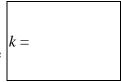
若方程  $3x^2 - 4x + \frac{h}{3} = 0$  有等根,求 h 的值。 (i)

If the equation  $3x^2 - 4x + \frac{h}{3} = 0$  has equal roots, find the value of h.



(ii) 若一圓柱體之高增加一倍,且新半徑為原來之h倍,則新體積為原來之k倍, 求 k 的值。

If the height of a cylinder is doubled and the new radius is h times the original, then the new volume is *k* times the original. Find the value of



若  $\log_{10} 210 + \log_{10} k - \log_{10} 56 + \log_{10} 40 - \log_{10} 120 + \log_{10} 25 = p$ , 求 p 的值。 If  $\log_{10} 210 + \log_{10} k - \log_{10} 56 + \log_{10} 40 - \log_{10} 120 + \log_{10} 25 = p$ , find the value of p.

p =

(iv) 若  $\sin A = \frac{p}{5}$  且  $\frac{\cos A}{\tan A} = \frac{q}{15}$  , 求 q 的值。 If  $\sin A = \frac{p}{5}$  and  $\frac{\cos A}{\tan A} = \frac{q}{15}$ , find the value of q. q =

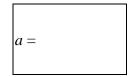
#### **FOR OFFICIAL USE**

Mult. factor for Score for speed accuracy **Bonus** score Total score

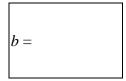
Team No.

Time

#### Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 1 (Individual)



(ii) 對  $K \ge 0$ ,  $\sqrt{K}$  表 K 的 非 負 平 方 根 。 若 b 是 方程  $\sqrt{a-x} = x-3$  的 根 , 求 b 的 值 。  $\sqrt{K}$  denotes the nonnegative square root of K, where  $K \ge 0$ . If b is the root of the equation  $\sqrt{a-x} = x-3$ , find the value of b.



(iii) 若 c 是  $\frac{20}{4+2\cos\theta}$  的最大值,求 c 的值。 If c is the greatest value of  $\frac{20}{4+2\cos\theta}$ , find the value of c.

c =

 $4+2\cos\theta$  (iv) 某人以 3c km/h 的速率行車 3 小時,再以 4c km/h 的速率行車 2 小時。

d =

若全程的平均速率是 d km/h,求 d 的值。 A man drives a car at 3c km/h for 3 hours and then 4c km/h for 2 hours. If his average speed for the whole journey is d km/h, find the value of d.

FOR OFFICIA	L USE	_	
Score for			Mult. fa
accuracy		×	spe

t. factor for speed = Bonus + Bonus score Total score

Team No.

Time

#### Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 2 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

 $\stackrel{\cdot}{=}$   $0^{\circ} \le \theta < 360^{\circ}$  , $\theta$  的方程  $3\cos\theta + \frac{1}{\cos\theta} = 4$  有 p 個根 ,求 p 的值 。 (i)

p =

If  $0^{\circ} \le \theta < 360^{\circ}$ , the equation in  $\theta$ :  $3\cos\theta + \frac{1}{\cos\theta} = 4$  has p roots.

Find the value of p.

If  $x - \frac{1}{x} = p$  and  $x^3 - \frac{1}{x^3} = q$ , find the value of q. q =

(iii) 一圓內接於一周界長 q cm 的正三角形。若圓的面積是  $k\pi$  cm<sup>2</sup>, 求 k 的值。 A circle is inscribed in an equilateral triangle of perimeter q cm. If the area of the circle is  $k\pi$  cm<sup>2</sup>, find the value of k.

k =

(iv) 正 k 邊形的每一內角為  $m^{\circ}$ 。求 m 的值。 Each interior angle of a regular polygon of k sides is  $m^{\circ}$ . Find the value of m.

m =

**FOR OFFICIAL USE** 

Score for Mult. factor for speed accuracy **Bonus** score Total score

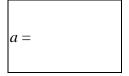
Team No.

Time

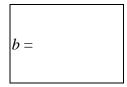
#### Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 3 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若  $998a + 1 = 999^2$ , 求 a 的值。 If  $998a + 1 = 999^2$ , find the value of a.



(ii) 若  $\log_{10}a = \log_2 b$  ,求 b 的值。 If  $\log_{10}a = \log_2 b$ , find the value of b.



(iii) 以 x 軸,y 軸及直綫 2x + y = b 所圍成的三角形的面積是 c 平方單位,求 c 的值。 The area of the triangle formed by the x-axis, the y-axis and the line 2x + y = b is c sq units. Find the value of c.

0	
q.	<i>c</i> =

(iv) 若  $64t^2 + ct + d$  是完全平方,求 d 的值。 If  $64t^2 + ct + d$  is a perfect square, find the value of d.

d =			
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#### FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = Bonus score

Total score

Team No.

Time

## Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 4 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 解下列 a 的方程  $2^{a+1} + 2^a + 2^{a-1} = 112$ 。

Solve for *a* in the equation  $2^{a+1} + 2^a + 2^{a-1} = 112$ .

a =

(ii) 若 a 是方程  $x^2 - bx + 35 = 0$  的一個根,求 b 的值。 If a is one root of the equation  $x^2 - bx + 35 = 0$ , find the value of b.

*b* =

(iii) 若  $\sin\theta = \frac{-b}{15}$  ,其中  $180^\circ < \theta < 270^\circ$  ,且  $\tan\theta = \frac{c}{3}$  ,求 c 的值 。

c =

- If  $\sin \theta = \frac{-b}{15}$ , where  $180^{\circ} < \theta < 270^{\circ}$ , and  $\tan \theta = \frac{c}{3}$ , find the value of c.
- (iv) 兩骰同擲,所得點數之和為c的概率是 $\frac{1}{d}$ 。求d的值。

d =

The probability of getting a sum of c in throwing two dice is  $\frac{1}{d}$ . Find the value of d.

# FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = 
+ Bonus score

Team No.

Time

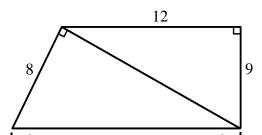
Total score

#### Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 5 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。



In the figure, find the value of a.





(ii) 若直綫 ax + by = 1 及 10x - 34y = 3 互相垂直,求 b 的值。 If the lines ax + by = 1 and 10x - 34y = 3 are perpendicular to each other, find the value of b.

b =

(iii) 某年五月第b日為星期五,而同年五月第c日為星期二,且 16 < c < 24,求 c 的值。

c =

If the  $b^{th}$  day of May in a year is Friday and the  $c^{th}$  day of May in the same year is Tuesday, where 16 < c < 24, find the value of c.

(iv) c 是第 d 個質數。求 d 的值。 c is the d<sup>th</sup> prime number. Find the value of d.

d =

#### FOR OFFICIAL USE

Score for accuracy 

Mult. factor for speed 

+ Bonus score

Team No.

Time

Total score

# Hong Kong Mathematics Olympiad (1989 – 1990) Sample Event (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 某兩數之和為 50, 其積為 25。若該兩數倒數之和為 a, 求 a 的值。 The sum of two numbers is 50, and their product is 25. If the sum of their reciprocals is a, find the value of a.



(ii) 若直綫 ax + 2y + 1 = 0 及 3x + by + 5 = 0 互相垂直,求 b 的值。 If the lines ax + 2y + 1 = 0 and 3x + by + 5 = 0 are perpendicular, find the value of b.

<i>b</i> =		

(iii) 一正三角形之面積為  $100\sqrt{3}\,\mathrm{cm}^2$ 。若其周界為  $p\,\mathrm{cm}$ ,求 p 的值。 The area of an equilateral triangle is  $100\sqrt{3}\,\mathrm{cm}^2$ . If its perimeter is  $p\,\mathrm{cm}$ , find the value of p.

(iv) 若  $x^3 - 2x^2 + px + q$  可被 x + 2 整除,求 q 的值。 If  $x^3 - 2x^2 + px + q$  is divisible by x + 2, find the value of q.

q =			

# FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = 

+ Bonus score

Total score

Team No.

Time

Min. Sec.

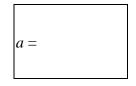
Final Events (Group Sample)

#### **Hong Kong Mathematics Olympiad (1989 – 1990)** Final Event 6 (Group)

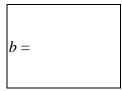
Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

差  $a = \frac{\left(68^3 - 65^3\right) \cdot \left(32^3 + 18^3\right)}{\left(32^2 - 32 \times 18 + 18^2\right) \cdot \left(68^2 + 68 \times 65 + 65^2\right)}$ , 求 a 的值。

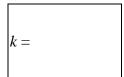
If  $a = \frac{\left(68^3 - 65^3\right) \cdot \left(32^3 + 18^3\right)}{\left(32^2 - 32 \times 18 + 18^2\right) \cdot \left(68^2 + 68 \times 65 + 65^2\right)}$ , find the value of a. (i)



若三點(a, b), (10, -4)及(20, -3)共綫, 求b的值。 (ii) If the 3 points (a, b), (10, -4) and (20, -3) are collinear, find the value of b.

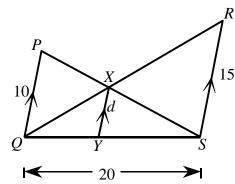


若在四時十五分,時鐘兩針之間的銳角是 k°,求 k 的值。 If the acute angle formed by the hands of a clock at 4:15 is  $k^{\circ}$ , find the value of k.



(iv) 在圖中, PQ = 10, RS = 15, QS = 20。若 XY = d, 求 d 的值。 In the figure, PQ = 10, RS = 15, QS = 20. If XY = d, find the value of d.





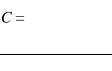
# **FOR OFFICIAL USE**

Mult. factor for Score for Team No. speed accuracy **Bonus** Time score Total score Min. Sec.

# **Hong Kong Mathematics Olympiad (1989 – 1990)** Final Event 7 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

- (i) 2個蘋果和3個橙共值6元。
  - 4個蘋果和7個橙共值13元。
  - 16 apples and 23 oranges cost *C* dollars. Find the value of *C* .



若  $K = \frac{6\cos\theta + 5\sin\theta}{2\cos\theta + 3\sin\theta}$ ,且  $\tan\theta = 2$ ,求 K 的值。 (ii) If  $K = \frac{6\cos\theta + 5\sin\theta}{2\cos\theta + 3\sin\theta}$  and  $\tan\theta = 2$ , find the value of K. K =

A、B均為小於10的正整數,且21A104×11=2B8016×9。

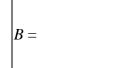
- A, B are positive integers less than 10 such that  $21A104 \times 11 = 2B8016 \times 9$ .
- (iii) 求A的值。

Find the value of A.

A =

(iv) 求 B 的值。

Find the value of B.



#### **FOR OFFICIAL USE**

Score for Mult. factor for speed accuracy **Bonus** score Total score

Team No.

Time

#### Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 8 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

在所示乘法中,字母 $A \setminus B \setminus C \setminus B \setminus K$ (其中A < B)代表由1至9的不同整數。

In the multiplication shown, the letters A, B, C and K (A < B) represent different integers from 1 to 9.

 $\begin{array}{c|cccc}
A & C \\
\hline
\times) & B & C \\
\hline
K & K & K
\end{array}$ 

(i) 求 A 的值。

Find the value of A.

A =

(ii) 求 B 的值。

Find the value of B.

B =

(iii) 求 C 的值。

Find the value of C.

*C* =

(iv) 求 *K* 的值。

Find the value of K.

K =

(提示: *KKK* = *K*×111。) (Hint: *KKK* = *K*×111.)

#### FOR OFFICIAL USE

Score for accuracy

Mult. factor for speed

=

Team No.

Time

Total score

Bonus

score

Min.

Sec.

## Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 9 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若 S = ab - 1 + a - b,且 a = 101,b = 9,求 S 的值。 If S = ab - 1 + a - b and a = 101, b = 9, find the value of S. S =

(ii) 若  $x = 1.9\dot{8}\dot{9}$ ,且  $x - 1 = \frac{K}{99}$ ,求 K 的值。 If  $x = 1.9\dot{8}\dot{9}$  and  $x - 1 = \frac{K}{99}$ , find the value of K.

K =

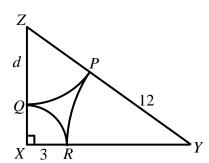
(iii)  $p \cdot q$  及 r 的平均值是  $18 \circ p + 1 \cdot q - 2 \cdot r + 3$  及 t 的平均值是  $19 \circ$  求 t 的值。 The average of p, q and r is 18.

t =

- The average of p + 1, q 2, r + 3 and t is 19. Find the value of t.
- (iv) 如圖所示,依次以 X , Y , Z 為圓心之三弧  $\stackrel{\frown}{QR}$  、  $\stackrel{\frown}{RP}$  、  $\stackrel{\frown}{PQ}$  互相切於 P 、 Q 、 R . 。 若 ZQ=d , XR=3 , YP=12 ,  $\angle X=90^\circ$  , 求 d 的值 。

d =

In the figure,  $\widehat{QR}$ ,  $\widehat{RP}$ ,  $\widehat{PQ}$  are 3 arcs, centres at X, Y and Z respectively, touching one another at P, Q and R. If ZQ = d, XR = 3, YP = 12,  $\angle X = 90^\circ$ , find the value of d.



# FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = 

+ Bonus score

Total score

Team No.

Time

## Hong Kong Mathematics Olympiad (1989 – 1990) Final Event 10 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

A =

(ii) 若  $\log_{10}(k-1) - \log_{10}(k^2 - 5k + 4) + 1 = 0$ ,求 k 的值。 If  $\log_{10}(k-1) - \log_{10}(k^2 - 5k + 4) + 1 = 0$ , find the value of k.



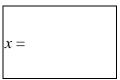
一凸 n 邊形其中一內角為 x°,而其餘內角之和為 2180°。

One interior angle of a convex n-sided polygon is  $x^{\circ}$ .

The sum of the remaining interior angles is 2180°.

(iii) 求*x* 的值。

Find the value of *x*.



(iv) 求 n 的值。

Find the value of n.

n =		

#### **FOR OFFICIAL USE**

Score for accuracy 

Mult. factor for speed 

+ Bonus score

Total score

Team No.

Time

Min.

Final Events (Group)

Sec.