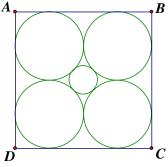
#### 1993 HI3

在圖中,ABCD 是一邊長為  $8(\sqrt{2}+1)$  的正方形。

求正方形中央小圓的半徑。

In the figure, *ABCD* is a square of side  $8(\sqrt{2}+1)$ . Find the radius of the small circle at the centre of the square.

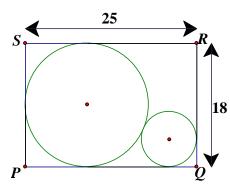


### 1993 FI4.3

PQRS 為一長方形,

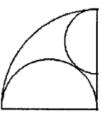
若細圓的半徑為 c, 求 c 的值。

PQRS is a rectangle. If c is the radius of the smaller circle, find the value of c.



### 1995 HG10

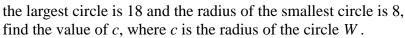
在圖中,象限的半徑和大半圓的直徑是 2, 求小半圓的半徑。 In the figure, the radius of the quadrant and the diameter of the large semi-circle is 2. Find the radius of the small semi-circle.



## 1995 FI5.3

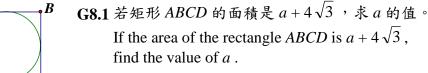
如圖示, $L_1$ 、 $L_2$ 為三個圓的切綫。如果最大圓的半徑是 18,最小圓半徑是 8,

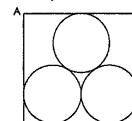
求 c 的值,若 c 為圓 W 的半徑。 In the figure,  $L_1$  and  $L_2$  are tangents to the three circles. If the radius of



1996 FG8 在本題內,所有不命名的圓皆是單位圓。

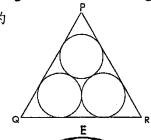
In this question, all unnamed circles are unit circles.





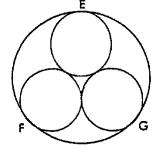
G8.2 若等邊三角形 PQR 的面積是  $6+b\sqrt{3}$  ,求 b 的 值。

If the area of the equilateral triangle PQR is  $6 + b\sqrt{3}$ , find the value of b.

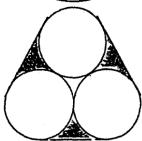


**G8.3** 若圓 *EFG* 的面積是  $\frac{(c+4\sqrt{3})\pi}{3}$  , 求 c 的值。

If the area of the circle *EFG* is  $\frac{(c+4\sqrt{3})\pi}{3}$ , find the value of c.



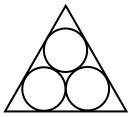
**G8.4** 若下圖所有直綫皆是兩個圓的公切綫,且陰影部份的面積是  $6+d\pi$ , 求 d 的值。 If all the straight lines in the diagram below are common tangents to the two circles, and the area of the shaded part is  $6+d\pi$ , find the value of d.



## 1997 HG9

圖中三個半徑為r cm 之全等圓被一三角形緊緊圍著。 若三角形之周界為(180+180√3) cm,求r 的值。

In the figure, three identical circles with radius r cm are tightly enclosed in a triangle. If the perimeter of the triangle is  $(180+180\sqrt{3})$  cm, find the value of r.

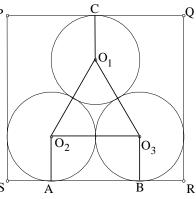


**Tangent** ⊥ **radius** (HKMO Classified Questions by topics)

#### 2000 HG7

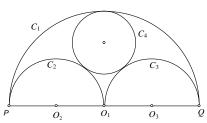
如圖二,已知三等圓互相外切,且內切於矩 P 形 PQRS, 求  $\frac{QR}{SR}$  的值。

(取  $\sqrt{3} = 1.7$  及答案須準確至二個小數位) In Figure 2, three equal circles are tangent to each other, and inscribed in rectangle PQRS, find the value of  $\frac{QR}{SR}$ . (Use  $\sqrt{3} = 1.7$  and give the answer correct to 2 decimal places)



#### 2002 HG8

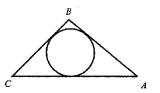
如圖,  $PQ \cdot PO_1 \cdot O_1Q$  分別是以 $O_1 \cdot O_2 \cdot$  $O_3$  為圓心的半圓  $C_1 \cdot C_2 \cdot C_3$  的直徑,圓  $C_4$ 內切於半圓  $C_1$  及外切於半圓  $C_2 \cdot C_3 \circ$ 若 PQ = 24, 求圓  $C_4$ 的面積 (取  $\pi = 3$ )。



In figure 2, PO, PO<sub>1</sub>, O<sub>1</sub>O are diameters of semi-circles C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub> with centres at 入一等邊三角形內。若圓的半徑為1單  $O_1$ ,  $O_2$ ,  $O_3$  respectively, and the circle  $C_4$  touches  $C_1$ ,  $C_2$ , and  $C_3$ . If PQ = 24, find the area of circle  $C_4$ . (Take  $\pi = 3$ ).

#### 2007 FG4.4

如圖一, $\triangle ABC$ 是一等腰三角形,AB=BC=20 cm 及 $\tan \angle BAC = \frac{4}{3} \circ \angle BAC$ 的內切圓的半徑為r cm, 求r的值。

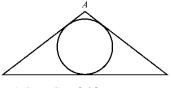


In Figure 1,  $\triangle ABC$  is an isosceles triangle, AB = BC = 20 cm and  $\tan \angle BAC = \frac{\pi}{3}$ .

If the length of radius of the inscribed circle of  $\triangle ABC$  is r cm, find the value of r.

## 2013 HG8

圖中, $\triangle ABC$  為一等腰三角形,其中AB=AC, BC = 240。已知  $\triangle ABC$  的內接圓的半徑是 24, 求 AB 的長度。

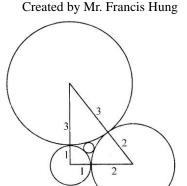


In the figure,  $\triangle ABC$  is an isosceles triangle with AB = AC, BC = 240. The radius of the inscribed circle of  $\triangle ABC$  is 24. Find the length of AB.

#### 2015 HG7

四個半徑分別為1單位、2單位、3單位及 r 單 位的圓互相相切如圖所示。求r的值。

Four circles with radii 1 unit, 2 units, 3 units and r units are touching one another as shown in the figure. Find the value of r.



### 2015 FG1.4

三個半徑分別為 2、3 及 10 單位的圓同時放於另一大圓內,使得四個圓剛 好彼此接觸。求大圓的半徑的值。

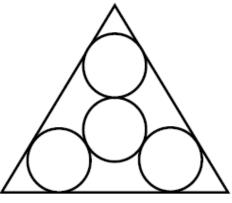
Three circles of radii 2, 3 and 10 units are placed inside another big circle in such a way that all circles are touching one another.

Determine the value of the radius of the big circle.

#### 2015 FG2.4

在下圖中,四個大小相同的圓形剛好放 位,求三角形的面積的值。

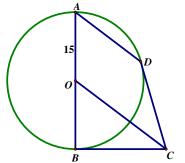
In the figure below, there are 4 identical circles placed inside an equilateral triangle. If the radii of the circles are 1 unit, what is the value of the area of the triangle?



# 2017 HI13

如圖,O 是圓 ADB 的圓心。BC 及 CD 分別是 圓形在點 B 及 D 的切幾。OC//AD,OA = 15。 若 AD + OC = 43, 求 CD 的長。

As shown in the figure, O is the centre of the circle ADB. BC and CD are tangents to the circle at points B and D respectively. OC //AD, OA = 15. If AD + OC = 43, find the length of CD.



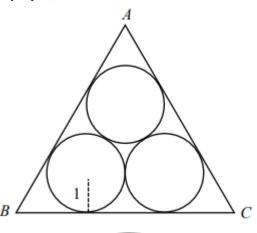
## 2021 P1Q5

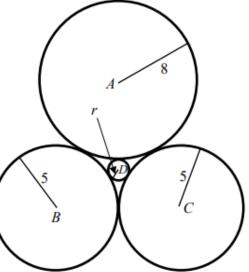
在圖一中,三個單位圓位於一等邊三 角形 ABC 內,使得每個圓均與另外 兩圓及三角形的兩邊相切。 求  $\Delta ABC$  的面積。

In Figure 1, three unit circles are placed inside an equilateral triangle ABC such that any circle is tangential to two sides of the triangle and to the other two circles. Find the area of  $\Delta ABC$ .

## 2021 P2Q3

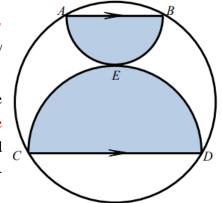
在圖中,四個半徑分別為 8.5.5 及 r 的圓互相外切。求r 的值。 In the figure, four circles of radii 8,5,5 and r are touching each other externally. Find the value of r.





## 2021 P2Q5

ABCD 是圓形而 ABE 及 CED 為半圓形互切 於 E 在圓內。已知圓面積為  $1~{\rm cm}^2$  及 AB // CD,求半圓形 ABE 及 CED 的面積之和。 ABCD is a circle while ABE and CED are semi-circles touching each other at E inside the circle. Given the area of circle is  $1~{\rm cm}^2$  and AB // CD, find the sum of the area of the semi-circles ABE and CED.



### 2022 P1Q15

PQR 是一個等腰三角形,其中 PQ = PR = 17 and QR = 16。將 I 及 H 分別 記為 PQR 的内心及垂心。求 IH 長度的值。

PQR is an isosceles triangle with PQ = PR = 17 and QR = 16. Denote the incentre and the orthocentre of PQR by I and H respectively. Find the length of HI.

# Answers

Allsweis				
1993 HI3	1993 FI4.3	1995 HG10 $\frac{2}{3}$	1995 FI5.3	1996 FG8.1
2	4		12	8
1996 FG8.2, 2021 P1Q5	1996 FG8.3	1996 FG8.4 $-\frac{3}{2}$	1997 HG9	2000 HG7
4	7		30	0.93
2002 HG8	2007 FG4.4	2013 HG8	$\frac{6}{23}$	2015 FG1.4
48	6	130		15
2015 FG2.4 $12\sqrt{3}$	2017 HI13 20 or $3\sqrt{11}$	$2021 \text{ P1Q5}$ $6 + 4\sqrt{3}$	2021 P2Q3 $\frac{8}{9}$	2021 P2Q5 1/2
$ \begin{array}{c} 2022 \text{ P1Q15} \\                                    $				