Difference of two squares (HKMO Classified Questions by topics)

1983 FG10.1

1700 1 310.1	
$1^2 - 1 = 0 \times 2$	$1^2 - 1 = 0 \times 2$
$2^2 - 1 = 1 \times 3$	$2^2 - 1 = 1 \times 3$
$3^2 - 1 = 2 \times 4$	$3^2 - 1 = 2 \times 4$
$4^2 - 1 = 3 \times 5$	$4^2 - 1 = 3 \times 5$

$$A^2 - 1 = 3577 \times 3579$$

 $\stackrel{?}{=} A > 0$, $\stackrel{?}{=} A$ 的值。

$$A^2 - 1 = 3577 \times 3579$$

If $A > 0$, find the value of A.

若
$$A > 0$$
, 求 A 的值。

1984 FI1.1 1987 FSG.1

若
$$100a = 35^2 - 15^2$$
 , 求 a 的值。

If $100a = 35^2 - 15^2$, find the value of a.

1984 FSG.2

$$1^2 - 1 = 0 \times 2$$
, $2^2 - 1 = 1 \times 3$, $3^2 - 1 = 2 \times 4$, ..., $b^2 - 1 = 135 \times 137$

若
$$b>0$$
,求 b 的值。

$$1^2 - 1 = 0 \times 2$$
, $2^2 - 1 = 1 \times 3$, $3^2 - 1 = 2 \times 4$, ..., $b^2 - 1 = 135 \times 137$.

If b > 0, find the value of b.

1986 FG10.4 2014 FG3.1

若
$$S = \left(1 - \frac{1}{2^2}\right)\left(1 - \frac{1}{3^2}\right)\left(1 - \frac{1}{4^2}\right)\cdots\left(1 - \frac{1}{10^2}\right)$$
,求 S 的值。

If
$$S = \left(1 - \frac{1}{2^2}\right)\left(1 - \frac{1}{3^2}\right)\left(1 - \frac{1}{4^2}\right)\cdots\left(1 - \frac{1}{10^2}\right)$$
, find the value of S .

1988 FI2.2

If $50m = 54^2 - 4^2$, find the value of m.

1989 FI2.1

已知 $1000a = 85^2 - 15^2$, 求 a 的值。

If $1000a = 85^2 - 15^2$, find the value of a.

1990 FI3.1

若 998a + 1 = 999 2 , 求 a 的值。

If $998a + 1 = 999^2$, find the value of a.

1991 FI2.1

If $a^2 - 1 = 123 \times 125$ and a > 0, find the value of a.

1992 FI2.4

若 $d = 12^4 - 142^2$, 求 d 的值。

If $d = 12^4 - 142^2$, find the value of d.

1993 FI2.2

If $b = 126^2 - 136^2$, find the value of b.

1996 FIS.4

已知 $d^2-1=257\times259$ 。求 d 的正值。

It is known that $d^2 - 1 = 257 \times 259$. Find the positive value of d.

1997 FG4.1

已知 $a = 103 \times 97 \times 10009$, 求 a 的值。

It is given that $a = 103 \times 97 \times 10009$, find the value of a.

1999 FIS.4

若
$$\frac{d}{114} = \left(1 - \frac{1}{2^2}\right)\left(1 - \frac{1}{3^2}\right)\cdots\left(1 - \frac{1}{57^2}\right)$$
,求 d 之值。

If
$$\frac{d}{114} = \left(1 - \frac{1}{2^2}\right)\left(1 - \frac{1}{3^2}\right) \cdots \left(1 - \frac{1}{57^2}\right)$$
, find the value of d.

2000 FG2.1

如果 191 為兩個連續平方數之差,而 a 為其中最小的平方數,求 a 的值。

If 191 is the difference of two consecutive perfect squares,

find the value of the smallest square number, a.

2008 FGS.1

計算 $(\sqrt{2008} + \sqrt{2007})^{2007} \times (\sqrt{2007} - \sqrt{2008})^{2007}$ 的值。

Calculate the value of $(\sqrt{2008} + \sqrt{2007})^{2007} \times (\sqrt{2007} - \sqrt{2008})^{2007}$.

2017 FI2.3

若c為1000000 與一個平方數之最小的相差,其中此平方數為64的倍數, 求c的值。

If c is the smallest difference between 1 000 000 and a square, where the square is a multiple of 64, determine the value of c.

2018 FI2.1

 $7778^{2} - 2223^{2}$ 之值的所有數字之和是 a , 求 a 的值。

Determine the value of a, where a is the sum of all digits of $7778^2 - 2223^2$.

2023 FI3.2

如果
$$B = \sqrt{(401)^2 - 100 \times 16}$$
 , 求 B 的值。

If $B = \sqrt{(401)^2 - 100 \times 16}$, find the value of B.

Answers

1983 FG10.1 3578	1984FI1.1 1987FSG.1	1984 FSG.2 136	$\frac{1986 \text{ FG}10.4 \text{ 2014 FG}3.1}{100000000000000000000000000000000000$	1988 FI2.2 58
1989 FI2.1	1990 FI3.1	1991 FI2.1	1992 FI2.4	1993 FI2.2
7	1000	124	572	-2620
1996 FIS.4	1997 FG4.1	1999 FIS.4	2000 FG2.1	2008 FGS.1
258	99999919	58	9025	-1
2017 FI2.3	2018 FI2.1	2023 FI3.2		·
15936	40	399		