Hong Kong Mathematics Olympiad (1986 – 1987) Sample Event (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

 a =

(ii) 若 $\sin a^\circ = \cos b^\circ$,其中 270 < b < 360,求 b 的值。 If $\sin a^\circ = \cos b^\circ$, where 270 < b < 360, find the value of b.

b =

(iii) X以\$b 出售一貨品與Y 而虧蝕 30%。若X 購入該貨品之成本為\$c,求c 的值。 X sold an article to Y for \$b at a loss of 30%.

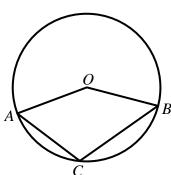
c =

If the cost price of the article for X is c, find the value of c.

d =

(iv) 附圖中,O 為圓心。若 $\angle ACB = \frac{3c^{\circ}}{10}$ 及 $\angle AOB = d^{\circ}$,求d的值。 In the figure, O is the centre of the circle.

If $\angle ACB = \frac{3c^{\circ}}{10}$ and $\angle AOB = d^{\circ}$, find the value of d.



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Score for accuracy

Mult. factor for speed

+ Bonus score

Total score

Team No.

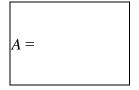
Time

Min.

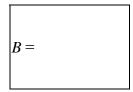
Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 1 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

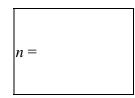
若 A = 11 + 12 + 13 + ... + 29, 求 A 的值。 (i) If A = 11 + 12 + 13 + ... + 29, find the value of A.



(ii) 若 $\sin A^{\circ} = \cos B^{\circ}$,其中 0 < B < 90,求 B 的值。 If $\sin A^{\circ} = \cos B^{\circ}$, where 0 < B < 90, find the value of B.



(iii) 附圖中, $\angle POR = B^{\circ}$, $\angle PRO = 50^{\circ}$ 。若 $\angle OSR = n^{\circ}$,求n的值。 In the given figure, $\angle PQR = B^{\circ}$, $\angle PRQ = 50^{\circ}$. If $\angle QSR = n^{\circ}$, find the value of n.



- (iv) 由 $1 \le n$ 號卡片中隨意抽出一張。若得到 5 之倍數之概率為 $\frac{1}{m}$,求 m 的值。 n cards are marked from 1 to n and one is drawn at random. If the chance of it being a m = nmultiple of 5 is $\frac{1}{m}$, find the value of m.

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Mult. factor for Score for = accuracy speed Bonus score

Time

Team No.

Total score

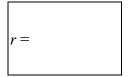
Min.

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 2 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 某球體之半徑為r,體積為 36π ,求r的值。

The volume of a sphere with radius r is 36π , find the value of r.



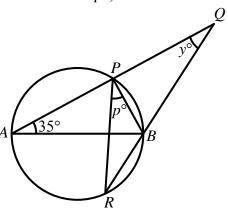
(ii) 若 $r^x + r^{1-x} = 4$,且 x > 0,求 x 的值。 If $r^x + r^{1-x} = 4$ and x > 0, find the value of x.

x =		

(iii) 若 a:b=5:4,b:c=3:x 且 a:c=y:4,求 y 的值。 In a:b=5:4,b:c=3:x and a:c=y:4, find the value of y.

(iv) 附圖中,AB 為該圓之直徑。APQ 及 RBQ 為直綫。若 $\angle PAB=35^\circ$, $\angle PQB=y^\circ$ 及 $\angle RPB=p^\circ$,求 p 的值。

In the figure, AB is a diameter of the circle. APQ and RBQ are straight lines. If $\angle PAB = 35^{\circ}$, $\angle PQB = y^{\circ}$ and $\angle RPB = p^{\circ}$, find the value of p.



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Score for accuracy

Mult. factor for speed

+ Bonus score

Total score

Team No.

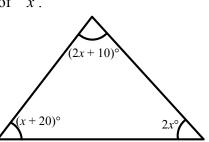
Time

Min. Sec.

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 3 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 如圖所示,求 x 的值。 In the figure, find the value of x.



x =

P, Q 之坐標依次為(a, 2)及(x, -6)。若 PQ 的中點之坐標為(18, b),求 a 的值。 (ii) The coordinates of the points P and Q are (a, 2) and (x, -6) respectively. If the coordinates of the mid-point of PQ is (18, b), find the value of a.

a =

(iii) 某人以均匀速度 a km/h 由 X 往 Y, 並以均匀速度 2a km/h 由 Y 返 X。 若其平均速度為c km/h,求c的值。

- A man travels from X to Y at a uniform speed of a km/h and returns at a uniform speed of 2a km/h. If his average speed is c km/h, find the value of c.
- (iv) 若 $f(y) = 2y^2 + cy 1$, 求 f(4) 的值。 If $f(y) = 2y^2 + cy - 1$, find the value of f(4).

f(4) =

FOR OFFICIAL USE

Mult. factor for Score for = accuracy speed **Bonus** score Total score

Team No.

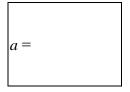
Time

Min. Sec.

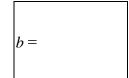
Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 4 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

若曲線 $y = 2x^2 - 8x + a$ 與 x-軸相切,求 a 的值。 If the curve $y = 2x^2 - 8x + a$ touches the x-axis, find the value of a.



(ii) 附圖中,AB 為該圓之直徑。若AC=15,BC=a 及AB=b,求b 的值。 In the figure, AB is a diameter of the circle. If AC = 15, BC = a and AB = b, find the value of b.



- \boldsymbol{A}
- (iii) 直綫 5x + by + 2 = d 過點(40, 5)。求 d 的值。 The line 5x + by + 2 = d passes through (40, 5). Find the value of d.

d =

(iv) X以\$d 出售一貨品與Y,得利潤2.5%。若X購入該貨品之成本為\$K,求K的值。 X sold an article to Y for \$d\$ at a profit of 2.5%. If the cost price of the article for X is $|_{K}$ = \$K, find the value of K.

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Score for Mult. factor for = speed accuracy **Bonus** score Total score

Team No.

Time

Min. Sec.

Final Events (Individual)

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 5 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 設 $x = 19.\dot{8}\dot{7}$ 。若 $19.\dot{8}\dot{7} = \frac{a}{99}$,求 a 的值。

(提示: 99x = 100 x - x)

Let $x = 19.\dot{8}\dot{7}$. If $19.\dot{8}\dot{7} = \frac{a}{99}$, find the value of a.

(Hint: 99x = 100 x - x)



(ii) 若 $f(y) = 4 \sin y^\circ$,且 f(a-18) = b,求 b 的值。 If $f(y) = 4 \sin y^\circ$ and f(a-18) = b, find the value of b.

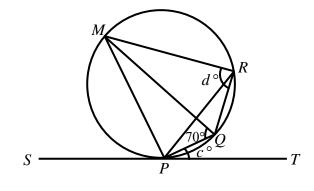
b =

(iii) 若 $\frac{\sqrt{3}}{b\sqrt{7}-\sqrt{3}}=\frac{2\sqrt{21}+3}{c}$,求c的值。
If $\frac{\sqrt{3}}{b\sqrt{7}-\sqrt{3}}=\frac{2\sqrt{21}+3}{c}$, find the value of c.

c =

(iv) 附圖中,ST與圓相切於 $P \circ 若 \angle MQP = 70^\circ$, $\angle QPT = c^\circ \mathcal{R} \angle MRQ = d^\circ$,求 d 的值。 In the figure, ST is a tangent to the circle at P. If $\angle MQP = 70^\circ$, $\angle QPT = c^\circ$ and $\angle MRQ = d^\circ$, find the value of d.

d =



FOR OFFICIAL USE

Score for accuracy

Mult. factor for speed

Team No.

+ Bonus score

Time

Min.

Sec.

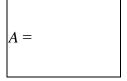
Total score

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Hong Kong Mathematics Olympiad (1986 – 1987) Sample Event (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

若 $100A = 35^2 - 15^2$, 求 A 的值。 If $100A = 35^2 - 15^2$, find the value of A.



(ii) 若 $(A-1)^6 = 27^B$, 求 B 的值。 If $(A-1)^6 = 27^B$, find the value of B.



(iii) 附圖所示三角之和是 C° 。求C的值。

In the given diagram, the sum of the three marked angles is C° . Find the value of C.



- (iv) 若直綫 x + 2y + 1 = 0 及 9x + Dy + 1 = 0 互相平行,求 D 的值。 If the lines x + 2y + 1 = 0 and 9x + Dy + 1 = 0 are parallel, find D.

D =		
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Score for Mult. factor for Team No. = speed accuracy **Bonus** Time score Total score Min.

Final Events (Group Sample)

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 6 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若 α、β 為 $x^2 - 10x + 20 = 0$ 之根,且 $p = \alpha^2 + \beta^2$,求 p 的值。 If α , β are the roots of $x^2 - 10x + 20 = 0$, and $p = \alpha^2 + \beta^2$, find the value of p.

p =

(ii) 一正三角形之周界為p。若其面積為 $k\sqrt{3}$,求k的值。 The perimeter of an equilateral triangle is p. If its area is $k\sqrt{3}$, find the value of k.

k =

(iii) 一正 N 邊形之每一內角為 140°。求 N 的值。 Each interior angle of an N-sided regular polygon is 140°. Find the value of N. N =

(iv) 若 $M = (10^2 + 10 \times 1 + 1^2)(10^2 - 1^2)(10^2 - 10 \times 1 + 1^2)$,求 M 的值。 If $M = (10^2 + 10 \times 1 + 1^2)(10^2 - 1^2)(10^2 - 10 \times 1 + 1^2)$, find the value of M.

M =

FOR OFFICIAL USE

Score for accuracy

Mult. factor for speed

+ Bonus score

Total score

Team No.

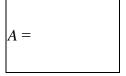
Time

Min.

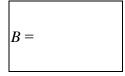
Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 7 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 在下午三點三十分時,時鐘兩針所構成之銳角為 A° 。求A 的值。 The acute angle formed by the hands of a clock at 3:30 p.m. is A° . Find the value of A.



(ii) 若 $\tan(3A+15)^\circ = \sqrt{B}$,求 B 的值。 If $\tan(3A+15)^\circ = \sqrt{B}$, find the value of B.



(iii) 若 $\log_{10}AB = C \log_{10}15$,求 C 的值。 If $\log_{10}AB = C \log_{10}15$, find the value of C.

<i>C</i> =		
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(iv) 點 $(1,3) \cdot (4,9)$ 及 (2,D) 共线。求D 的值。 The points (1,3), (4,9) and (2,D) are collinear. Find the value of D.

D =	

FOR OFFICIAL USE

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 8 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

A =

If $x + \frac{1}{x} = 2A$, and $x^3 + \frac{1}{x^3} = B$, find the value of B. B =

(iii) 共有 N 個 α 值可满足方程 $\cos^3 \alpha - \cos \alpha = 0$, 其中 $0^\circ \le \alpha \le 360^\circ$ 。 求 N 的值。 There are exactly N values of α satisfying the equation $\cos^3 \alpha - \cos \alpha = 0$, where $0^{\circ} \le \alpha \le 360^{\circ}$. Find the value of N.

N =

(iv) 若某年五月第N日為星期四,且同年五月第K日為星期一,其中10 < K < 20, 求 K的值。

K =

If the N^{th} day of May in a year is Thursday and the K^{th} day of May in the same year is Monday, where 10 < K < 20, find the value of K.

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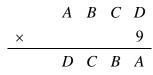
Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 9 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form.

除非特別聲明,答案須用數字表達,並化至最簡。

在所示乘法中,不同字母代表由0至9之不同整數。

In the given multiplication, different letters represent different integers ranging from 0 to 9.



求A的值。 (i)

Find the value of A.



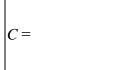
(ii)求B的值。

Find the value of B.



(iii) 求 C 的值。

Find the value of C.



(iv) 求*D*的值。

Find the value of D.

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Score for Mult. factor for Team No. = speed accuracy **Bonus** Time score Total score Min.

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Final Events (Group)

Hong Kong Mathematics Olympiad (1986 – 1987) Final Event 10 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) $p \cdot q \cdot r \otimes s$ 之平均數為 $5 \cdot s$ $p \cdot q \cdot r \cdot s \otimes s$ A 之平均數為 $8 \cdot s \cdot s$ A 的值。 The average of p,q,r and $s \cdot s \cdot s$ $S \cdot s$

A =

The average of p, q, r, s and A is 8. Find the value of A.

- (ii) 若直綫 3x-2y+1=0 及 Ax+By+1=0 互相垂直,求 B 的值。 If the lines 3x-2y+1=0 and Ax+By+1=0 are perpendicular, find the value of B. B=
- (iii) 若 $Cx^3 3x^2 + x 1$ 除以 x + 1 得之餘數為 $-7 \circ 求 C$ 的值。 When $Cx^3 - 3x^2 + x - 1$ is divided by x + 1, the remainder is -7. Find the value of C.
- (iv) 若 $P \cdot Q$ 為正整數使 P + Q + PQ = 90,且 D = P + Q,求 D 的值。 (提示:因式分解 1 + P + Q + PQ)

 If P,Q are positive integers such that P + Q + PQ = 90 and D = P + Q, find the value of D. (Hint: Factorise 1 + P + Q + PQ)

D=		
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