#### 1991 HI2

某科學家發現某樣本中細菌的數量每小時增加一倍。

於下午四時,他發現細菌的數量為 $3.2 \times 10^8$ ,

若於同日正午該樣本中細菌的數量為 $N \times 10^7$ ,求N的值。

A scientist found that the population of a bacteria culture doubled every hour. At 4:00 pm, he found that the number of bacteria was 3.2×10<sup>8</sup>. If the number of bacteria in that culture at noon on the same day was  $N\times10^7$ , find the value of N.

### 1994 HI1

設 
$$\log_3 p = 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots$$
 至無窮項,求  $p$  的值。

Suppose  $\log_3 p = 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots$  to an infinite number of terms.

Find the value of p.

## 1997 FG1.3

若 
$$1 + 3 + 3^2 + \dots + 3^8 = \frac{3^c - 1}{2}$$
 , 求  $c$  的值。

If  $1 + 3 + 3^2 + \dots + 3^8 = \frac{3^c - 1}{2}$ , find the value of c.

### 1998 HI2

已知 8、a、b 形成一等差級數,且 a、b、36 形成一等比級數。 若a和b皆為正數,求a、b的和。

Given that 8, a, b form an A.P. and a, b, 36 form a G.P.

If a and b are both positive numbers, find the sum of a and b.

## 1998 FG4.3

圖形  $S_0$ ,  $S_1$ ,  $S_2$ , ... 用以下方法構成:把綫段[0,1]的中間三分之一取去, 得到  $S_0$ , 把  $S_0$  的兩條組成綫段, 每段的中間三分之一取去, 得到  $S_1$ , 把  $S_1$ 的四條組成綫段,每段的中間三分之一取去,得到 S2, S3、S4 ... 等用類似 方法獲得。求在構成 S5 的過程中取去的綫段的總長度 c(答案以分數表示)。

A sequence of figures  $S_0, S_1, S_2, \cdots$  are constructed as follows.  $S_0$  is obtained by removing the middle third of [0,1] interval;  $S_1$  by removing the middle third of each of the two intervals in S<sub>0</sub>; S<sub>2</sub> by removing the middle third of each of the four intervals in S<sub>1</sub>; S<sub>3</sub>, S<sub>4</sub>, 設  $F = 1 + 2 + 2^2 + 2^3 + \dots + 2^{120}$  及  $T = \sqrt{\frac{\log(1+F)}{\log 2}}$  ,求 T 的值。  $\dots$  are obtained similarly. Find the total length c of the intervals removed in the construction of S<sub>5</sub> (Give your answer in fraction).

# 2001 FI3.3

If  $\sin 30^{\circ} + \sin^2 30^{\circ} + \dots + \sin^7 30^{\circ} = 1 - \cos^R 45^{\circ}$ , find the value of R.

## 2002 FI2.2

已知 
$$99Q = \frac{99}{100} \times (1 + \frac{99}{100} + \frac{99^2}{100^2} + \frac{99^3}{100^3} + \cdots)$$
,求  $Q$  的值。

Given that  $99Q = \frac{99}{100} \times (1 + \frac{99}{100} + \frac{99^2}{100^2} + \frac{99^3}{100^3} + \cdots)$ , find the value of Q.

### 2005 FG2.4

設 
$$d = \frac{1}{2} + \frac{2}{4} + \frac{3}{8} + \frac{4}{16} + \dots + \frac{10}{2^{10}}$$
 , 求  $d$  的值。

Let  $d = \frac{1}{2} + \frac{2}{4} + \frac{3}{8} + \frac{4}{16} + \dots + \frac{10}{2^{10}}$ , find the value of d.

### 2006 HG3

已知 
$$0^{\circ} < \theta < 90^{\circ}$$
 及  $1 + \sin \theta + \sin^2 \theta + \dots = \frac{3}{2}$ 。若  $y = \tan \theta$ ,求  $y$  的值。

Given that  $0^{\circ} < \theta < 90^{\circ}$  and  $1 + \sin \theta + \sin^2 \theta + \dots = \frac{3}{2}$ .

If  $y = \tan \theta$ , find the value of y.

# 2007 FG2.1

若 
$$R = 1 \times 2 + 2 \times 2^2 + 3 \times 2^3 + \dots + 10 \times 2^{10}$$
 , 求  $R$  的 值 。

If  $R = 1 \times 2 + 2 \times 2^2 + 3 \times 2^3 + \dots + 10 \times 2^{10}$ , find the value of R.

# 2009 FI1.3

設 
$$F = 1 + 2 + 2^2 + 2^3 + \dots + 2^{120}$$
 及  $T = \sqrt{\frac{\log(1+F)}{\log 2}}$  ,求  $T$  的值。

Let 
$$F = 1 + 2 + 2^2 + 2^3 + \dots + 2^{120}$$
 and  $T = \sqrt{\frac{\log(1+F)}{\log 2}}$ , find the value of  $T$ .

Last updated: 2022-06-25

#### 2010 FG2.1

If  $p = 2 - 2^2 - 2^3 - 2^4 - \dots - 2^9 - 2^{10} + 2^{11}$ , find the value of p.

## 2012 HI5

已知  $\log_4 N = 1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \cdots$  , 求 N 的值。

Given that  $\log_4 N = 1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \cdots$ , find the value of N.

### 2015 FI1.4

若 n 為正整數及  $f(n) = 2^n + 2^{n-1} + 2^{n-2} + \dots + 2^2 + 2^1 + 1$ , 求 δ= f(10) 的值。

If n is a positive integer and  $f(n) = 2^n + 2^{n-1} + 2^{n-2} + \cdots + 2^2 + 2^1 + 1$ , determine the value of  $\delta = f(10)$ .

# 2017 FI3.4

若  $f(x) = 2^0 + 2^1 + 2^2 + \dots + 2^{x-2} + 2^{x-1}$  , 求 d = f(10) 的值。

If  $f(x) = 2^0 + 2^1 + 2^2 + \dots + 2^{x-2} + 2^{x-1}$ , determine the value of d = f(10).

### 2019 HI4

設 n 為正整數。若  $a_n = 1 + 2 + \dots + 2^n$  及  $b = a_{10} - a_5 + a_1$  , 求 b 的值。

Let *n* be a positive integer. If  $a_n = 1 + 2 + \dots + 2^n$  and  $b = a_{10} - a_5 + a_1$ , find the value of *b*.

# Answers

1991 HI2 2	1994 HI1 9	1997 FG1.4 9	1998 HI2 40	1998 FG4.3 <u>665</u> 729
2001 FI3.3 14	2002 FI2.2 1	2005 FG2.4 509 256	$\frac{2006 \text{ HG3}}{\sqrt{2}}$	2007 FG2.1 18434
2009 FI1.3	2010 FG2.1	2012 HI5	2015 FI1.4	2017 FI3.4
11	6	8	2047	1023
2019 HI4 1987				