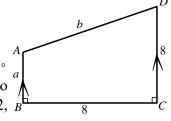
# Pythagoras' theorem (HKMO Classified Questions by topics)

#### 1985 FI4.2

在圖中,ABCD 為一梯形,AB 與 DC 平行 且 $\angle ABC = \angle DCB = 90^{\circ}$ 。

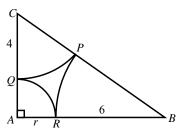
若 AB = a = 2 , BC = CD = 8 及 AD = b , 求 b 的值  $\circ$  a In the figure, ABCD is a trapezium with AB parallel to DC and  $\angle ABC = \angle DCB = 90^{\circ}$ . If AB = a = 2, BBC = CD = 8 and AD = b, find the value of b.



#### 1986 FG7.1

如圖所示,依次以 $A \times B \times C$  為圓心之弧  $QR \times RP \times PQ$  相切於  $R \times P \times Q \circ$  若  $AR = r \times RB = 6 \times QC = 4 \times QA = 90^\circ$ ,求 r 的值。

In the figure, QR, RP, PQ are 3 arcs, centres at A, B, C respectively, touching one another at R, P, Q. If AR = r, RB = 6, QC = 4,  $\angle A = 90^{\circ}$ , find the value of r.

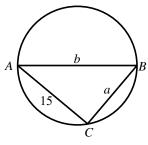


#### 1987 FI4.2

附圖中,AB為該圓之直徑。

In the figure, AB is a diameter of the circle.

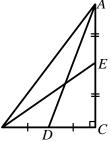
If AC = 15, BC = 8 and AB = b, find the value of b.



### 1990 HI17

在  $\Delta ABC$  中, $\angle C=90^\circ$  及 D、E 分別為 BC 及 CA 的中點。若 AD=7 及 BE=4,求 AB 的長度。

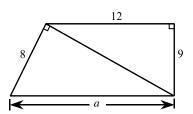
In  $\triangle ABC$ ,  $\angle C = 90^{\circ}$  and D, E are the mid-points of BC and CA respectively. If AD = 7 and BE = 4, find the length of AB.



### 1990 FI5.1

如圖所示,求a的值。

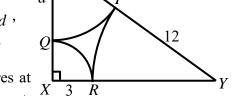
In the figure, find the value of a.



#### 1990 FG9.4

如圖所示,依次以X,Y,Z為圓心之三弧QR、

 $\stackrel{\frown}{RP}$ 、 $\stackrel{\frown}{PQ}$  互相切於 P、Q、R.。若 ZQ=d, XR=3,YP=12, $\angle X=90^\circ$ ,求 d 的值。

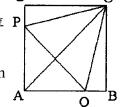


In the figure,  $\widehat{QR}$ ,  $\widehat{RP}$ ,  $\widehat{PQ}$  are 3 arcs, centres at X, Y and Z respectively, touching one another at

P, Q and R. If ZQ = d, XR = 3, YP = 12,  $\angle X = 90^{\circ}$ , find the value of d

### 1995 HG7 2008 FI4.4

在圖中, ABCD 為一正方形,且 AB=1 及 CPQ 為一等 P 邊三角形。求  $\Delta CPQ$  的面積。



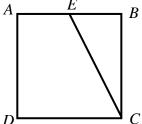
In the figure, ABCD is a square where AB = 1 and CPQ is an equilateral triangle. Find the area of  $\Delta CPQ$ .

### 1998 HI4

在圖中,ABCD 為一正方形。E 為 AB 上的一點,使 A 得 BE=1 及 CE=2。求正方形 ABCD 的面積。

In the figure, *ABCD* is a square.

E is a point on AB such that BE = 1 and CE = 2. Find the area of the square ABCD.



# 2001 FG2.2

E 是長方形 ABCD 內一點。已知  $EA \times EB \times EC$  和 ED 的長度分別為  $2 \times \sqrt{11} \times 4$  和 b,求 b 的值。

*E* is an interior point of the rectangle *ABCD*. Given that the lengths of *EA*, *EB*, *EC* and *ED* are 2,  $\sqrt{11}$ , 4 and *b* respectively, find the value of *b*.

# 2003 FI3.4

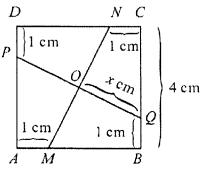
四邊形 ABCD 雨對角綫 AC 和 BD 互相垂直。AB=5,BC=4,CD=3。 若 DA=S,求 S 的值。

The diagonals AC and BD of a quadrilateral ABCD are perpendicular to each other. Given that AB = 5, BC = 4, CD = 3. If DA = S, find the value of S.

#### 2006 HI10

如圖二,ABCD 是一正方形,其邊長為 4 cm。綫段 PQ 和 MN 相交於點 O。 若 PD 、 NC 、 BQ 和 AM 的長度是 1 cm, OQ 的長度是 x cm,求 x 的值。

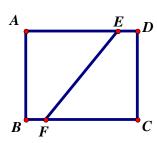
In Figure 2, ABCD is a square with side length equal to 4 cm. The line segments PQ and MN intersect at the point O. If the lengths of PD, NC, BQ and AM are 1 cm and the length of OQ is x cm, find the value of x.



### 2008 HG10

如圖,ABCD 是長方形紙張並有 AB=4 cm 及 BC=5 cm。將該紙張對摺,使 C 點與 A 點重合,得摺痕 EF。若 EF=r cm,求 r 的值。

In the figure, ABCD is rectangular piece of paper with AB = 4 cm and BC = 5 cm. Fold the paper by putting point C onto A to create a crease EF.

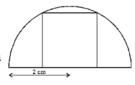


If EF = r cm, find the value of r.

## 2009 FG3.3

如圖,邊長為 Q cm 的正方形內接於半徑為 2 cm 的半 圓中,求 Q 的值。

In the figure, a square of side length Q cm is inscribed in a semi-circle of radius 2 cm. Find the value of Q.



### 2014 FG1.1

若一個等腰三角形對應底邊(不是兩條等腰邊)的高是 8, 且周長是 32, 求該三角形的面積。

If an isosceles triangle has height 8 from the base, not the legs, and perimeters 32, determine the area of the triangle.

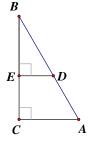
# 2015 FI3.4

在下圖中,BE = AC, $BD = \frac{1}{2}$  及 DE + BC = 1。

若  $\delta$  是 ED 的長度的 15 倍, 求  $\delta$  的值。

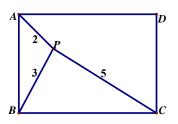
In the figure below, BE = AC,  $BD = \frac{1}{2}$  and DE + BC = 1.

If  $\delta$  is 15 times the length of  $\mbox{\it ED},$  determine the value of  $\delta$  .



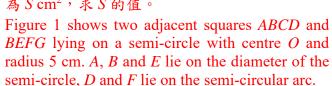
#### 2018 HI7

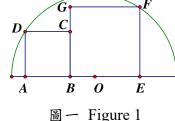
如圖所示,P 為長方形 ABCD 內的一點, 使得 PA=2,PB=3 及 PC=5。求 PD 的長度。 As shown in the figure, P is a point inside a rectangle ABCD such that PA=2, PB=3 and PC=5. Find the length of PD.



#### 2019 HG2

圖一所示,ABCD 和 BEFG 是兩個緊點的正方形,躺臥在一個以 O 為圓心,半徑為 5 cm 的半圓上。其中 A 、 B 和 E 在半圓的直徑,D 和 F 在半圓的弧上。設 ABCD 與 BEFG 的面積之和為 S cm²,求 S 的值。





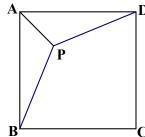
Let the sum of areas of ABCD and BEFG be  $S \text{ cm}^2$ , find the value of S.

### 2023 HI9

在圖中,P 為正方形 ABCD 內的一點使得 $\Delta ABP \cong A$   $\Delta ADP$ ,  $AP = 5\sqrt{2}$  及 BP = 13。

求正方形 ABCD 的面積。

In the figure, P is a point inside the square ABCD such that  $\triangle ABP \cong \triangle ADP$ .  $AP = 5\sqrt{2}$  and BP = 13. Find the area of square ABCD.



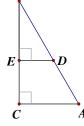
# 2023 FI4.1

在三角形ABC中, $\angle C = 90^{\circ}$ , $DE \perp BC$ ,BE = AC, $BD = \frac{1}{2}$  及 B

DE + BC = 1。如果  $\alpha = 4ED$ ,求  $\alpha$  的值。

In triangle ABC,  $\angle C = 90^{\circ}$ ,  $DE \perp BC$ , BE = AC,  $BD = \frac{1}{2}$  and  $E = \frac{1}{2}$ 

DE + BC = 1. If  $\alpha = 4ED$ , find the value of  $\alpha$ .



# 2024 HI5

在一直角三角形中,從銳角頂點所作的中線長度為7及9。求三角形斜邊的長。

In a right-angled triangle, the lengths of the medians from the vertices of the acute angles are 7 and 9. Find the length of the hypotenuse of the triangle.

# **Answers**

1985 FI4.2 10	1986 FG7.1 2	1987 FI4.2 17	1990 HI17 $2\sqrt{13}$	1990 FI5.1 17
1990 FG9.4 5	1995 HG7 2008 FI4.4 $2\sqrt{3} - 3$	1998 HI4 3	2001 FG2.2 3	2003 FG3.4 $3\sqrt{2}$
2006 HI10 √5	$   \begin{array}{r}     2008 \text{ HG10} \\     \hline     4\sqrt{41} \\     5   \end{array} $	$2009 \text{ FG3.3}$ $\frac{4\sqrt{5}}{5}$	2014 FG1.1 48	2015 FI3.4 15 4
$2018 \text{ HI7}$ $2\sqrt{5}$	2019 HG2 25	2023 HI9 289	2023 FI4.1 1	2024 HI5 $2\sqrt{26}$