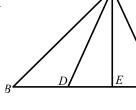
Area same height different bases (HKMO Classified Questions by topics)

1985 FI4.3

在圖中,BD=5,DE=4,EC=3。若 $\Delta AEC$ 之面積 為 24  $B \Delta ABC$ 之面積為 C,求 C 的值。

In the figure, BD = 5, DE = 4, EC = 3.

If the area of  $\triangle AEC$  is 24 and the area of  $\triangle ABC$  is c, find the value of c.

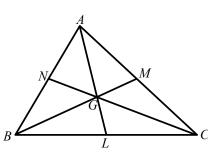


1986 FG10.2

 $\Delta ABC$  之中綫  $AL \cdot BM \cdot CN$  相交於  $G \circ$  若  $\Delta ABC$  之面積為  $54 \text{ cm}^2$ ,

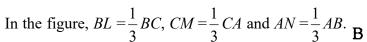
 $\Delta ANG$  之面積為 x cm<sup>2</sup>, 求 x 的值。

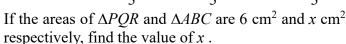
The medians AL, BM, CN of  $\triangle ABC$  meet at G. If the area of  $\triangle ABC$  is 54 cm<sup>2</sup> and the area of  $\triangle ANG$  is x cm<sup>2</sup>. Find the value of x.



1992 HG7

在圖中,
$$BL = \frac{1}{3}BC$$
、 $CM = \frac{1}{3}CA$ 及 $AN = \frac{1}{3}AB$ 。





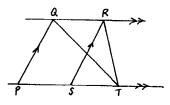


在圖中,PQRS之面積為  $80 \text{ cm}^2$ 。

若  $\Delta QRT$  之面積為 A cm<sup>2</sup> , 求 A 的值。

In the figure, the area of PQRS is 80 cm<sup>2</sup>.

If the area of  $\triangle QRT$  is  $A \text{ cm}^2$ , find the value of A.



# 1993 HI10

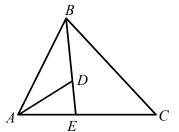
在圖中,BDE 及 AEC 為直綫、AB=2、BC=3、 $\angle ABC=60$ °、

$$AE:EC=1:2$$
。若  $BD:DE=9:1$  及三角形 $\Delta DBA$  的面積  $=\frac{a\sqrt{3}}{20}$  ,

求a的值。

Created by Mr. Francis Hung

In the figure, BDE and AEC are straight lines, AB = 2, BC = 3,  $\angle ABC = 60^{\circ}$ , AE : EC = 1 : 2. If BD : DE = 9 : 1 and area of  $\triangle DBA = \frac{a\sqrt{3}}{20}$ , find the value of a.



1993 FG9.1-2

點  $X \cdot Y \cdot Z$  依次將  $BC \cdot CA \cdot AB$  分成  $1:2 \circ$  設  $\Delta AZY$  的面積:  $\Delta ABC$  的面積 =2:a 及  $\Delta AZY$  的面積:  $\Delta XYZ$  的面積  $=2:b \circ$  求 a 及 b 的值。

BC, CA, AB are divided respectively by the points X, Y, Z in the ratio 1 : 2. Let

area of  $\triangle AZY$ : area of  $\triangle ABC = 2$ : a and area of  $\triangle AZY$ : area of  $\triangle XYZ = 2$ : b.

Find the value of a and b.



E 是平行四邊形 ABCD 其中一條邊 CD 的中點。若三角形 ADE 與平行四邊 形 ABCD 面積的比等於 1:a ,求 a 的值。

ABCD is a parallelogram and E is the midpoint of CD. If the ratio of the area of the triangle ADE to the area of the parallelogram ABCD is 1:a, find the value of a.

1998 FI1.3

在圖中,BD = 2 cm,DC = c cm,

且ΔABD 的面積= $\frac{1}{3}$ ×ΔABC 的面積,

求c的數值。

In the figure, BD = 2 cm, DC = c cm

and area of  $\triangle ABD = \frac{1}{3} \times \text{area of } \triangle ABC$ ,

find the value of c.

M

Area same height different bases (HKMO Classified Questions by topics)

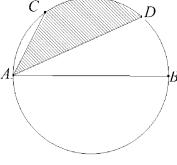
### 2000 FI4.2

在下圖中,AB 為圓的直徑。C 和 D 把弧 AB 分 為三等份。斜綫面積為 2。

若圓的面積為Q,求Q的值。

In the following figure, AB is a diameter of the circle. C and D divide the arc AB into three equal parts. The shaded area is 2.

If the area of the circle is Q, find the value of Q.



# 2000 FI5.3

已知 $\Delta ABC$  的面積為 3; D、E 和 F 分別為

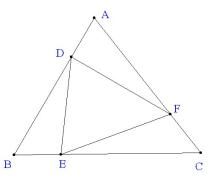
$$AB \cdot BC$$
 和  $CA$  上的點使得  $AD = \frac{1}{3}AB \cdot BE =$ 

$$\frac{1}{3}BC \cdot CF = \frac{1}{3}CA \circ$$

如果  $\Delta DEF$  的面積為 R , 求 R 的值。

Given that the area of the  $\triangle ABC$  is 3; D, E and F are the points on AB, BC and CA B

respectively such that  $AD = \frac{1}{3}AB$ ,  $BE = \frac{1}{3}BC$ ,

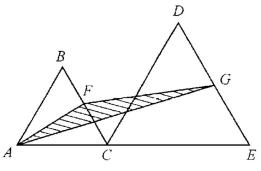


 $CF = \frac{1}{3}CA$ . If the area of  $\triangle DEF$  is R, find the value of R.

# 2004 HI9

在圖中,C在 AE 上, $\Delta ABC$  和  $\Delta CDE$  是等邊三角形,且 F、G 分別是 BC 和 DE 的中點。  $若\Delta ABC$  的面積是  $24\text{cm}^2$ ,  $\Delta CDE$  的面積是  $60\text{ cm}^2$ ,  $\Delta AFG$  的面積是 Q cm<sup>2</sup>,求 Q 的值。

In the figure, C lies on AE,  $\triangle ABC$  and  $\triangle CDE$  are equilateral triangles, F and G are the mid-points of BC and DE respectively. If the area of  $\triangle ABC$  is  $24 \text{ cm}^2$ , the area of  $\triangle CDE$  is  $60 \text{ cm}^2$ , and the area of  $\triangle AFG$  is  $Q \text{ cm}^2$ , find the value of Q.



### 2005 HG7

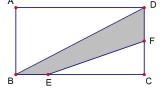
如圖,ABCD 和 CEFG 是兩個正方形, $FG = 4 \text{ cm} \circ \angle AEG$  的面積是  $g \text{ cm}^2$ ,求 g 的值。

In the figure, ABCD and CEFG are two squares and FG = 4 cm. If the area of  $\Delta AEG$  is equal to  $g \text{ cm}^2$ , find the value of g.

### 2006FG3.4

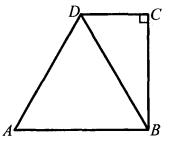
如圖, ABCD 是一長方形, F 是 CD 的中點及 BE:EC=1:3。若長方形 ABCD 的面積是  $12~\rm cm^2$  及陰影部份 BEFD 的面積是  $R~\rm cm^2$ ,求 R 的值。

In the figure, ABCD is a rectangle, F is the midpoint of CD and BE : EC = 1 : 3. If the area of the rectangle ABCD is  $12 \text{ cm}^2$  and the area of BEFD is  $R \text{ cm}^2$ , find the value of R.



### 2011 HI10

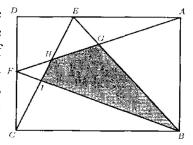
如圖,ABCD 為個梯形,其中  $\angle C = 90^{\circ}$ 。若等邊三角形 ABD 的面積為 $16\sqrt{3}$ ,求 梯形 ABCD 的面積。 In the figure, ABCD is a trapezium with  $\angle C = 90^{\circ}$ . If the area of the equilateral triangle ABD is  $16\sqrt{3}$ , find the area of trapezium ABCD.



# 2011 FG4.4

在圖中,ABCD 為一長方形,及 E 及 F 分別為綫段 AD 及 DC 上的點。點 G 為綫段 AF 及 BE 的交點,點 H 為綫段 AF 及 CE 的交點,點 I 為綫段 BF 及 CE 的交點。若 AGE,DEHF 及 CIF 的面積分別為  $2 \times 3$  及 1,求灰色部份 BGHI 的面積。

In the figure, ABCD is a rectangle, and E and F are points on AD and DC, respectively. Also, G is the intersection of AF and BE, H is the intersection of AF and CE, and I is the intersection of BF and CE. If the areas of AGE, DEHF and CIF are 2, 3 and 1, respectively, find the area of the grey region BGHI.

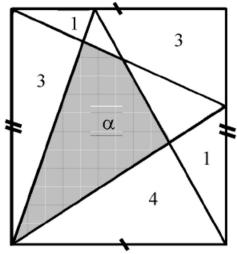


Area same height different bases (HKMO Classified Questions by topics)

### 2014 FI1.1

求下圖中陰影部分的面積 α。

Determine the area of the shaded region,  $\alpha$ , in the figure.

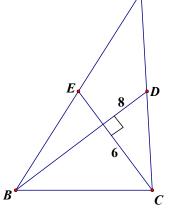


### 2016 HI10

如圖,在  $\triangle ABC$  中,BD 和 CE 分別是 AC 和 AB 兩邊上的中綫,且  $BD \perp CE$ 。已知 BD=8,CE=6,求  $\triangle ABC$  的面積。

As shown in the figure, BD and CE are the medians of the sides AC and AB of  $\Delta ABC$  respectively, and  $BD \perp CE$ .

Given that BD = 8, CE = 6, find the area of  $\triangle ABC$ .



# 2016 HG7

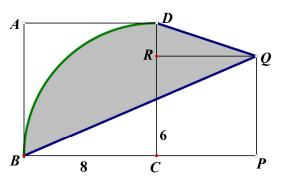
設三角形三條中綫的長度為9、12及15。求該三角形的面積。

The lengths of the three medians of a triangle are 9, 12 and 15. Find the area of the triangle.

### 2018 HI12

如圖所示,ABCD 及 PQRC 為 兩個連接的正方形。以 C 為圓心 及 CB 為半徑繪畫出弧 BD 。已 知 BC=8 及 RC=6 。 求弧 BD 及綫段 DQ 與 BQ 所圍成的區域的面積。

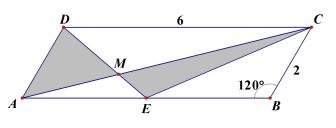
As shown in the figure, two squares ABCD and PQRC are joined together. An arc BD is drawn with centre C and radius CB.



Given that BC = 8 and RC = 6. Find the area of the region bounded by the arc BD, line segments DQ and BQ.

### 2018 FG3.1

AC 是平行四邊形 ABCD 的對角綫,CD=6,BC=2 及  $\angle ABC=120^\circ$ 。若 E 是 AB 的中點,AC 與 DE 相 交於 M 及陰影部分的總面 積是 $\alpha$ ,求  $\alpha$  的值。

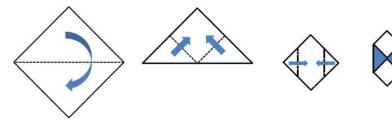


ABCD is a parallelogram with diagonal AC, CD = 6, BC = 2, and  $\angle ABC = 120^{\circ}$ . If E is the midpoint of AB, AC and DE intersect at M, and the total area of the shaded regions in  $\alpha$ , determine the value of  $\alpha$ .

### 2019 FI3.1

一張正方形紙的面積為  $100 \text{ cm}^2$ ,按照圖中的虛幾和箭咀的方向對摺。若圖中的陰影部份為  $s \text{ cm}^2$ ,求 s 的值。

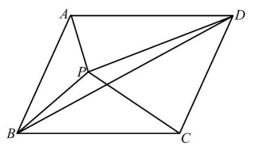
A piece of square paper of area  $100 \text{ cm}^2$ , is folded in half along the dotted line as shown below. If the area of the shaded region in the last figure is  $s \text{ cm}^2$ , determine the value of s.



### 2019 FG3.2

下圖中,P 點在平行四邊形 ABCD 內。若  $\Delta ABP$ 、 $\Delta BPC$  和  $\Delta BPD$  的面積分別為  $73~\rm cm^2$ 、 $100~\rm cm^2$  和  $e~\rm cm^2$ ,求  $e~\rm bid$ 。

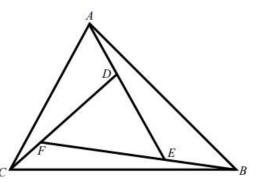
In the diagram below, point P is inside parallelogram ABCD. If areas of  $\triangle ABP$ ,  $\triangle BPC$  and  $\triangle BPD$  are 73 cm<sup>2</sup>, 100 cm<sup>2</sup> and e cm<sup>2</sup> respectively, determine the value of e.



### 2021 P1Q10

在圖三中,BEF、ADE 及 CFD 是直線,使得 BE:EF=1:2,AD:DE=1:3 及 CF:FD=1:4。若  $\Delta DEF$  的面積是 24 平方單位,求  $\Delta ABC$  的面積。

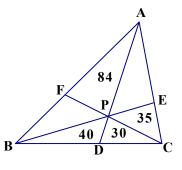
In Figure 3, BEF, ADE and CFD are straight lines such that BE: EF = 1: 2, AD: DE = 1: 3 and CF: FD = 1: 4. If the area of  $\Delta DEF$  is 24 square unit, find the area of  $\Delta ABC$ .



## 2023 HI10

在圖中,D、E 及 F 分別為 BC、AC 及 AB 上的 點。AD、BE 及 CF 相交於 P 使得  $\Delta APF$  的面積 = 84、 $\Delta BPD$  的面積 = 40、 $\Delta CPD$  的面積 = 30 及  $\Delta CPE$  的面積 = 35。求 $\Delta ABC$  的面積。

In the figure, D, E and F are points lying on BC, AB and AB respectively. AD, BE and CF intersect at P such that such that area of  $\Delta APF = 84$ , area of  $\Delta BPD = 40$ , area of  $\Delta CPD = 30$  and area of  $\Delta CPE = 35$ . Find the area of  $\Delta ABC$ .



# Answer

1985 FI4.3	1986 FG10.2	1992 HG7	1992 FI4.1	1993 HI10
96	9	42	40	9
1993 FG9.1-2	1997 FGS.1	1998 FI1.3	2000 FI4.2	2000 FI5.3
a = 9, b = 3	4	4	12	1
2004 HI9 12	2005 HG7 8	2006FG3.4 15 4	$2011 \text{ HI}10$ $24\sqrt{3}$	2011 FG4.4 6
2014 FI1.1	2016 HI10	2016 HG7	2018 HI12	2018 FG3.1
5	32	72	16π	$2\sqrt{3}$
2019 FI3.1 25 4	2019 FG3.2 27	2021 P1Q10 59	2023 HI10 315	