Factor (HKMO Classified Questions by topics)

1985 FG7.2

N之最小值。

When the positive integer N is divided by 6, 5, 4, 3 and 2,

the remainders are 5, 4, 3, 2 and 1 respectively. Find the least value of N.

1985 FG8.1-2

M、N均為小於10之正整數,且258024M8×9=2111110N×11。 求M及N的值。

M, N are positive integers less than 10 and $258024M8 \times 9 = 2111110N \times 11$. Find the value of M and N.

1988 FG7.1-2

 $M \cdot N$ 是小於 10 的正整數,且 $8M420852 \times 9 = N9889788 \times 11$ 。 求M及N的值。

M, N are positive integers less than 10 and $8M420852 \times 9 = N9889788 \times 11$. Find the value of M and N.

1990 HI13 2013FG4.3

正整數 N 被 10、9、8、7、6、5、4、3 及 2 除所得的餘數依次是 <math>9、8、 7、6、5、4、3、2及1, 求 N 的最小值。

A positive integer N, when divided by 10, 9, 8, 7, 6, 5, 4, 3 and 2, leaves 如果 a 是一個三位數, 駁在 504 之後, 新組成的六位數可被 7、9、11 整除, remainders 9, 8, 7, 6, 5, 4, 3, 2 and 1 respectively. Find the least value of N.

1990 FG7.3-4

 $A \cdot B$ 均為小於 10 的正整數,且 $21A104 \times 11 = 2B8016 \times 9$ 。求 $A \in B$ 的 值。

A, B are positive integers less than 10 such that $21A104 \times 11 = 2B8016 \times 9$. Find the value of A and B.

1995 FG6.1-2

 $2^{a} \cdot 9^{b}$ 為一四位數,其千位數是 2,百位數是 a,十位數是 9,個位數是 b, 求a及b的值。

 $2^{a} \cdot 9^{b}$ is a four digit number and its thousands digit is 2, its hundreds digit is a, its tens digit is 9 and its units digit is b, find the value of a and b.

1996 FG6.4

若 r, s, t, u 是正整數及 $r^5 = s^4, t^3 = u^2, t - r = 19$ 及 d = u - s, 求 d 的值。 If r, s, t, u are positive integers and $r^5 = s^4$, $t^3 = u^2$, t - r = 19 and d = u - s, find the value of d.

1998 HG4

正整數 N 分別被 6、5、4、3 及 2 除時,其餘數依次為 5、4、3、2 及 1。求 給出整數 a、b、c,使得 $a^2 = b^3 = c$ 。若 c > 1,求 c 的最小值。

Let a, b, c be integers such that $a^2 = b^3 = c$. If c > 1, find the smallest value of c.

1999 FI4.1

李先生今年a歲,a<100。若把李先生的出生月份與a相乘,其結果是 253。 求a的值。

Mr. Lee is a years old, a < 100.

If the product of a and his month of birth is 253, find the value of a.

1999 FIS.3

W和F為兩大於20的整數。

若 W 與 F 之積為 770, W 與 F 之和為 c, 求 c 之值。

W and F are two integers which are greater than 20. If the product of W and F is 770 and the sum of W and F is c, find the value of c.

1999 FG3.1

設小於 100 的正整數,同時又是完全平方及完全立方的數目共有 a 個, 求a之值。

Let a be the number of positive integers less than 100 such that they are both square and cubic numbers, find the value of a.

2000 FG4.1

求a的值。

Let a be a 3-digit number. If the 6-digit number formed by putting a at the end of the number 504 is divisible by 7, 9, and 11, find the value of a.

2000 FG5.1

如果 a 是可被 810 整除的最小立方數, 求 a 的值。

If a is the smallest cubic number divisible by 810, find the value of a.

2001 FI2.3

某班學生的人數少於 56 人。在一次數學測驗中有 $\frac{1}{3}$ 學生得甲等, $\frac{1}{7}$ 學 生得乙等,一半學生得丙等,餘下的學生都不及格。已知不及格的學生人數 是 R, 求 R 的值。

There are less than 56 students in a class. In a mathematics test, $\frac{1}{3}$ of the students got grade A, $\frac{1}{7}$ of the students got grade B, half of the students got grade C, and the rest failed. Given that R students failed in the mathematics test, find the value of R.

Factor (HKMO Classified Questions by topics)

2002 HI2

已知 $a^3 = 150b$,且 a 和 b 都是正整數。求 b 的最小值。

Given $a^3 = 150b$ and a, b are positive integers, find the least value of b.

2002 HG2

已知 $a \cdot b \cdot c$ 為三個連續奇數且 $b^3 = 3375$, 求 ac 的數值。

Given that a, b, c are three consecutive odd numbers and $b^3 = 3375$, find the value of ac.

2003 HI9

已知六位數 $N=\overline{x1527y}$ 是 4 的倍數,且 N 被 11 除餘 5。求 x+y 的值。

It is given that the 6-digit number $N = x\overline{1527 y}$ is a multiple of 4, and the remainder is 5 when N is divided by 11. Find the value of x + y.

2004 FI1.1

已知有 a 個少於 200 的正整數,它們每個都只有三個正因數,求 a 的值。

Given that there are a positive integers less than 200 and each of them has exactly three positive factors, find the value of a.

2005 FG1.1

若在1至200內能同時被3和7整除的數有a個,求a的值。

Suppose there are a numbers between 1 and 200 that can be divisible by 3 and 7, find the value of a.

2006 HI7

已知在數列
$$1001$$
, 1001001 , 1001001001 ,…, $1\underbrace{001001}_{2}\underbrace{001}_{2}$ … $1\underbrace{001}_{2}$,… 中有 R 個質數,

求 R 的值。

Given that the number of prime numbers in the sequence 1001, 1001001, 1001001001, \cdots , $1\underline{00}1\underline{00}1\cdots1\underline{00}1$, \cdots is R, find the value of R.

2007 HG1

若由 $1 \, \Xi \, 50$ 內與 50 互質的整數有 N 個,求 N 的值。

If there are N integers from 1 to 50 that are relatively prime to 50, find the value of N.

2007 FI3.3

若有 c 個正整數 n 使得 $\frac{n+17}{n-7}$ 也是正整數,求 c 的值。

If there is (are) c positive integer(s) n such that $\frac{n+17}{n-7}$ is also a positive integer,

find the value of c.

2008 HG2

有一批糖共x 粒,x 為正整數,這批糖能分別為 851 人及 943 人所均分。 求x 的最小可能值。

A total number of x candies, x is a positive integer, can be evenly distributed to 851 people as well as 943 people. Find the least possible value of x.

2008 HG4

已知 x 為正整數及 x < 60。若 x 恰有 10 個正因子,求 x 的值。

Given that x is a positive integer and x < 60. If x has exactly 10 positive factors, find the value of x.

2008 FIS.1

若 28 的所有正因子是 d_1, d_2, \ldots, d_n 及 $a = \frac{1}{d_1} + \frac{1}{d_2} + \cdots + \frac{1}{d_n}$, 求 a 的值。

If all the positive factors of 28 are d_1, d_2, \ldots, d_n and $a = \frac{1}{d_1} + \frac{1}{d_2} + \cdots + \frac{1}{d_n}$,

find the value of a.

2010 HG1

已知六位數 503xyz 可以被 7,9,11 整除。求三位數 xyz 的最小值。 Given that the six-digit number 503xyz is divisible by 7,9,11.

Find the minimum value of the three-digit number xyz.

2010 FI3.1

若 a 為 15147 的相異質因數的數目。求 a 的值。

If a is the number of distinct prime factors of 15147, find the value of a.

2011 HG1

 $若(1000-a)(1000-b)(1000-c)(1000-d)(1000-e) = 24^2$,其中 $a \cdot b \cdot c \cdot d$ 及 e 為偶數,且 a > b > c > d > e,求 $a \cdot b \cdot c \cdot d$ 及 e 的值。

If $(1000 - a)(1000 - b)(1000 - c)(1000 - d)(1000 - e) = 24^2$, where a, b, c, d and e are even numbers and a > b > c > d > e, find the values of a, b, c, d and e.

2011 FG3.1

若a為一正整數及 $a^2 + 100a$ 為一質數,求a的最大值。

If a is a positive integer and $a^2 + 100a$ is a prime number, find the maximum value of a.

2011 FG3.4

把數字 1, 2, ..., 10 分成兩組並設 P_1 及 P_2 分別為該兩組的乘積。

$$\overrightarrow{A} P_1 \stackrel{\wedge}{A} P_2$$
 的倍數,求 $\frac{P_1}{P_2}$ 的最小值。

Spilt the numbers 1, 2, ..., 10 into two groups and let P_1 be the product of the first group and P_2 the product of the second group.

If P_1 is a multiple of P_2 , find the minimum value of $\frac{P_1}{P_2}$.

2013 HI2

一個平行四邊形可被分成 178 個邊長為 1 單位的等邊三角形,若該平行 四邊形的周界為 P 單位, 求 P 的最大值。

A parallelogram is cut into 178 pieces of equilateral triangles with sides 1 unit. If the perimeter of the parallelogram is P units, find the maximum value of P.

2013 FG2.1

若 $4^3 + 4^r + 4^4$ 是一平方數,其中 r 是正整數,求 r 的最小值。 If $4^3 + 4^r + 4^4$ is a perfect square and r is a positive integer,

find the minimum value of r.

2014 HI6

設 n 為正整數,且 n < 1000。若 $(n-1)^2$ 整除 $(n^{2014}-1)$,求 n 的最大值。 Let n be a positive integer and n < 1000.

If $(n^{2014} - 1)$ is divisible by $(n - 1)^2$, find the maximum value of n.

2014 HI8

設 xy = 10x + y。若 xy + yx 為一個平方數,這樣的數有多少個? Let xy = 10x + y.

If $\overline{xy} + \overline{yx}$ is a square number, how many numbers of this kind exist?

2015 HI3

設正 n 邊形的內角為 x° ,其中 x 為整數。問 n 有多少個可能值? Let x° be the measure of an interior angle of an *n*-sided regular polygon, where x is an integer, how many possible values of n are there?

2016 HI13

設 $A \cdot B$ 和 C 為三個數字。利用這三 Let A, B and C be three digits. The 個數字組成的三位數有以下性質:

- (a) ACB 可以被 3 整除;
- (b) BAC 可以被 4 整除;
- (c) BCA 可以被 5 整除; 及
- (d) CBA 的因數數目為單數。 求三位數 ABC。

number formed by these three digits has the following properties:

- ACB is divisible by 3;
- (b) BAC is divisible by 4;
- BCA is divisible by 5; (c)
- CBA has an odd number of factors.

Find the 3-digit number *ABC*.

2017 HI7

設 N 為完全立方數,已知 N=161x+23y,其中 x 和 y 均為正整數。 $\bar{x} x + y$ 的最小值。

Let N be a perfect cube number. Given that N = 161x + 23y, where x and y are positive integers. Find the minimum value of x + y.

2018 HI15

設 $N^2 = \overline{abcdefabc}$ 為一個 9 位整數,其中 N 是 4 個相異質數的積及 a、 $b \cdot c \cdot d \cdot e \cdot f$ 均為非零數字且滿足 $\overline{def} = 2 \times \overline{abc}$ 。求 N^2 的最小值。

Let $N^2 = \overline{abcdefabc}$ be a nine-digit positive integer, where N is the product of four distinct primes and a, b, c, d, e, f are non-zero digits that satisfy $\overline{def} = 2 \times \overline{abc}$. Find the least value of N^2 .

2018 FI2.4

求整數 d,使得對於任何實數 x, $x^{13}+x+90$ 可被 x^2-x+d 整除。 Determine the integral value of d, so that $x^{13} + x + 90$ is divisible by $x^2 - x + d$ for

any real number x.

2018 FI4.2

若 $x \cdot y$ 為正整數及 b 為 $x \cdot y$ 組合的數量使得它們的乘積 $x \times y = 100$, 求b的值。

If x, y are positive integers numbers and b is the number of groups of x, y such that the product $x \times y = 100$, determine the value of b.

2019 HI13

已知正整數 $a \cdot b$ 及c 满足下列條件:

- (i) a > b > c,
- (ii) (a-b)(b-c)(a-c) = 84,
- (iii) abc < 100 °

設 M 為 a 的最大值。求 M 的值。

Given that a, b and c are positive integers satisfying the following conditions:

- (i) a > b > c.
- (ii) (a-b)(b-c)(a-c) = 84,
- (iii) abc < 100.

Let M be the maximum value of a. Find the value of M.

2021 P2Q4

已知 $a \cdot b \cdot c \cdot d$ 及e是連續正整數,其中a < b < c < d < e。若a + b + c + c < d < ed+e 是一個立方數及 b+c+d 是一個平方數, 求 c 的最小可能值。

Given that a, b, c, d and e are consecutive positive integers, where a < b < c <d < e. If a+b+c+d+e is a perfect cube and b+c+d is a perfect square, find the smallest possible value of c.

2022 P1Q5

設 N = 24x + 216y,其中x及y均為正整數。

若N為完全立方數,求 x+y 的最小值。

Let N = 24x + 216y, where both x and y are positive integers.

If N is a cube number, find the minimum value of x + y.

2023 HI11

已知 n 是一個少於 2023 正整數。

Given that n is a positive integer less than 2023.

If n has only 3 distinct factors, find the number of possible values of n.

2024 HG3

設 $a \cdot b$ 及c 為正整數。若ab+c=2023 及a+bc=2024,求a+b+c 的值。

Let a, b and c be positive integers.

If ab + c = 2023 and a + bc = 2024, find the value of a + b + c.

Answers

Allsweis				
1985 FG7.2	1985 FG8.1-2	1988 FG7.1-2	1990HI13 2013FG4.3	1990 FG7.3-4
59	M = 5, N = 2	M = 5, N = 6	2519	A = 1, B = 5
1995 FG6.1-2	1996 FG6.4	1998 HG4	1999 FI4.1	1999 FIS.3
a = 5, b = 2	757	64	23	57
1999 FG3.1	2000 FG4.1	2000 FG5.1	2001 FI2.3	2002 HI2
2	504	729000	1	180
2002 HG2	2003 HI9	2004 FI1.1	2005 FG1.1	2006 HI7
221	9	6	9	0
2007 HG1	2007 FI3.3	2008 HG2	2008 HG4	2008 FIS.1
20	8	34891	48	2
2010 HG1	2010 FI3.1	2011 HG1	2011 FG3.1	2011 FG3.4
118	3	a = 1006, b = 1002, c = 998, d = 996, e = 994	1	7
2013 HI2	2013 FG2.1	2014 HI6	2014 HI8	2015 HI3
180	1	107	8	22
2016 HI13	2017 HI7	2018 HI15	2018 FI2.4	2018 FI4.2
522	79	289578289	2	9
2019 HI13	2021 P2Q4	2022 P1Q5	2023 HI11	2024 HG3
9	75	16	14	1371