#### 1993 FI5.4

當以二進制表示 257(x),則其中有 d 個'0'。求 d 的值。

When  $257_{(x)}$  is represented in binary scale, there are d '0's. Find the value of d.

# 2003 FI4.3

已知 R, x, y 及 Z 是整數且 R>x>y>z。若 R, x, y 及 Z 滿足方程

$$2^{R} + 2^{x} + 2^{y} + 2^{z} = \frac{495 \times \frac{2}{3}}{16}$$
 , 求 R 的值。

Given that R, x, y, z are integers and R > x > y > z.

If R, x, y, z satisfy the equation  $2^R + 2^x + 2^y + 2^z = \frac{495 \times \frac{2}{3}}{16}$ , find the value of R.

### 2008 FG4.3

若  $208208 = 8^5a + 8^4b + 8^3c + 8^2d + 8e + f$ , 其中  $a \cdot b \cdot c \cdot d \cdot e$  及 f 為整數且 在六進制中,若 A 為  $12345_6 \div 13_6$  的餘數, 求 A 的值。  $0 \le a, b, c, d, e, f \le 7$ ,  $x = a \times b \times c + d \times e \times f$  的值。

If  $208208 = 8^5a + 8^4b + 8^3c + 8^2d + 8e + f$ , where a, b, c, d, e, and f are integers **2018 FG1.4** and  $0 \le a, b, c, d, e, f \le 7$ , find the value of  $a \times b \times c + d \times e \times f$ .

# 2011 FI1.2

設  $20112011 = a(20)^5 + b(20)^4 + c(20)^3 + d(20)^2 + e(20) + f$ , 其中  $a \cdot b \cdot c \cdot d$ e 及 f 為整數及 0 < a, b, c, d, e, f < 20。若 O = a + b + c + d + e + f求O的值。

Let  $20112011 = a(20)^5 + b(20)^4 + c(20)^3 + d(20)^2 + e(20) + f$ , where a, b, c, d, e and f are integers and 0 < a, b, c, d, e, f < 20.

If Q = a + b + c + d + e + f, find the value of Q.

# 2016 HI8

某數的 16 進制位是 1140。而同一數字的 a 進制位是 240,求 a 的值。 A number in base 16 is 1140.

The same number in base a is 240, what is the value of a?

#### 2016 HG8

若某正整數的二進位表示有以下特質:

- (1) 有 11 個位,
- (2) 有六個位是1,有五個位是零,

則稱該數為「好數」·(例如:2016 是一個「好數」,因為 2016=111111000002·) 求所有「好數」的和。

If the binary representation of a positive integer has the following properties:

- (1) the number of digits = 11,
- (2) the number of 1's = 6 and the number of 0's = 5,

then the number is said to be a "good number".

(For example, 2016 is a "good number" as  $2016 = 11111100000_2$ .)

Find the sum of all "good numbers".

## 2017 FG2.1

In base-6 system, if  $12345_6 \div 13_6$  has remainder A, determine the value of A.

在五進制中,若v為 2342345÷2345 的餘數,求 v 的值。

In base 5 system, if v is the remainder of 2342345 ÷ 2345, determine the value of v.

# 2019 FI2.4

假設  $D \cdot x \cdot v$  和 z 均為整數,其中 D > x > v > z。

若 
$$D \cdot x \cdot y$$
 和  $z$  滿足等式  $3^D - 3^x + 3^y - 3^z = \frac{1000 \times \frac{11}{50} + 2}{9}$  ,求  $D$  的值。

Suppose that D, x, y and z are integers with D > x > y > z. If D, x, y

and z satisfy the equation 
$$3^{D} - 3^{x} + 3^{y} - 3^{z} = \frac{1000 \times \frac{11}{50} + 2}{9}$$
, determine the value of D.

# 2019 FI3.4

若  $V_{(u+5)}$  為  $1231234_{(u+5)} \div 123_{(u+5)}$  的餘數,求 v 的值。

If  $v_{(u+5)}$  is the remainder of  $1231234_{(u+5)} \div 123_{(u+5)}$ , determine the value of v.

# Answers

1993 FI5.4	2003 FI4.3	2008 FG4.3	2011 FI1.2	2016 HI8
7	4	72	36	46
2016 HG8	2017 FG2.1	2018 FG1.4	2019 FI2.4	2019 FI3.4
386946	2	0	3	4