

**1989 HG3**

已知對所有正整數  $n$  ,  $1^2 + 2^2 + \cdots + n^2 = \frac{n(n+1)(2n+1)}{6}$  ,

求  $21^2 + 22^2 + \cdots + 30^2$  的值。

It is known that  $1^2 + 2^2 + \cdots + n^2 = \frac{n(n+1)(2n+1)}{6}$  for all positive integers  $n$  .

Find the value of  $21^2 + 22^2 + \cdots + 30^2$  .

**1991 HI16**

已知

It is known that

$$2^3 - 1^3 = 3 \times 1^2 + 3 \times 1 + 1$$

$$2^3 - 1^3 = 3 \times 1^2 + 3 \times 1 + 1$$

$$3^3 - 2^3 = 3 \times 2^2 + 3 \times 2 + 1$$

$$3^3 - 2^3 = 3 \times 2^2 + 3 \times 2 + 1$$

$$4^3 - 3^3 = 3 \times 3^2 + 3 \times 3 + 1$$

$$4^3 - 3^3 = 3 \times 3^2 + 3 \times 3 + 1$$

$$\vdots$$

$$\vdots$$

$$101^3 - 100^3 = 3 \times 100^2 + 3 \times 100 + 1$$

$$101^3 - 100^3 = 3 \times 100^2 + 3 \times 100 + 1$$

求  $1^2 + 2^2 + 3^2 + \cdots + 100^2$  的值。

Find the value of  $1^2 + 2^2 + 3^2 + \cdots + 100^2$ .

**1993 HI6**

已知對任何正整數  $n$  ,  $1^2 + 2^2 + \cdots + n^2 = \frac{n(n+1)(2n+1)}{6}$  。

求  $12^2 + 14^2 + 16^2 + \cdots + 40^2$  的值。

For any positive integer  $n$  , it is known that  $1^2 + 2^2 + \cdots + n^2 = \frac{n(n+1)(2n+1)}{6}$  .

Find the value of  $12^2 + 14^2 + 16^2 + \cdots + 40^2$  .

**1995 HG6**

已知  $1^2 + 2^2 + 3^2 + \cdots + n^2 = \frac{n}{6}(n+1)(2n+1)$  ,

求  $19 \times 21 + 18 \times 22 + 17 \times 23 + \cdots + 1 \times 39$  的值。

Given that  $1^2 + 2^2 + 3^2 + \cdots + n^2 = \frac{n}{6}(n+1)(2n+1)$  ,

find the value of  $19 \times 21 + 18 \times 22 + 17 \times 23 + \cdots + 1 \times 39$  .

**Answers**

1989 HG3 6585	1991 HI16 338350	1993 HI6 11260	1995 HG6 5130	
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