Mutually Exclusive Events

Let A, B be events, A and B are **mutually exclusive events** (互斥事件) if $A \cap B = \emptyset$.

i.e. The events A and B cannot happen on the same time.

e.g.1 In a rolling die:

A =the event that the number is odd = $\{1, 3, 5\}$

B =the event that the number is even = $\{2, 4, 6\}$

C = the event that the number is a multiple of 3 = {3, 6}

 $A \cap B = \emptyset$, : A and B are mutually exclusive events.

 $A \cap C = \{3\}, :: A \text{ and } C \text{ are } \underline{\text{not}} \text{ mutually exclusive events.}$

e.g.2 In tossing a coin 3 times:

 $A = \text{event that there are 2 heads and 1 tail} = \{\text{HHT}, \text{HTH}, \text{THH}\}$

 $B = \text{event that there are 3 heads} = \{\text{HHH}\}$

C = event that the first toss is a head = {HTT, HTH, HHT, HHH}

 $A \cap B = \emptyset$, :: A and B are mutually exclusive events.

 $A \cap C = \{HTH, HHT\}, :: A \text{ and } C \text{ are } \underline{\text{not}} \text{ mutually exclusive events.}$

By axiom 3 in Chapter 3, if A and B are mutually exclusive events, $A \cap B = \emptyset$,

 $P(A \cup B) = P(A) + P(B)$. This is called the **addition law**.(加法定理)

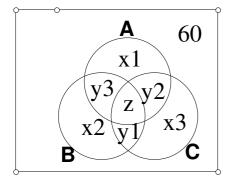
Example 3

60 students took part in a test of three questions *A*, *B* and *C*. 37 students answered *A* correctly, 30 answered *B* correctly and 25 answered *C* correctly, 20 students scored *A* and *B*, 17 scored *A* and *C*, 13 scored *B* and *C*, 5 got all *A*, *B* and *C*.

(a) How many students scored at least one question?

A student is selected at random, what is the probability of scoring none?

(b) What is the probability of scoring at most one question?



(a) Consider the above Venn diagram

$$x_1 + y_2 + y_3 + z = 37$$

 $x_2 + y_1 + y_3 + z = 30$
 $x_3 + y_1 + y_2 + z = 25$
 $y_3 + z = 20$; $y_2 + z = 17$; $y_1 + z = 13$
 $z = 5$

The remaining part is left as an exercise.

[Ans. (a) 47,
$$\frac{13}{60}$$
; (b) $\frac{1}{3}$]