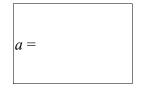
### **Event 1 (Individual)**

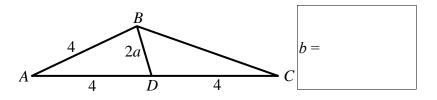
Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若  $a = \log_{\frac{1}{4}} \frac{1}{2}$  ,求 a 的值。

Find the value of a , if  $a = \log_{\frac{1}{4}} \frac{1}{2}$ .



(ii) 如圖示,AB = AD = DC = 4, BD = 2a。 若 BC 之長為 b,求 b 的值。 In the figure, AB = AD = DC = 4, BD = 2a. Find b, the length of BC.



(iii) 已知  $f(x) = px^3 + qx + 5$  且  $f(-7) = \sqrt{2}b + 1$ 。若 c = f(7),求 c 的值。 It is given that  $f(x) = px^3 + qx + 5$  and  $f(-7) = \sqrt{2}b + 1$ . Find the value of c, if c = f(7).

d =		
и		

FOR OFFICIAL USE

Score for accuracy

× Mult. factor for speed



Team No.

Ų			

+ Bonus score

Time



Total score

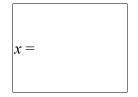
Min.

### **Event 2 (Individual)**

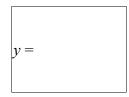
Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若  $\frac{x}{(x-1)(x-4)} = \frac{x}{(x-2)(x-3)}$ , 求 的 值。

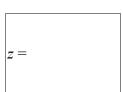
If  $\frac{x}{(x-1)(x-4)} = \frac{x}{(x-2)(x-3)}$ , find the value of x.



(ii) 若  $f(t) = 3 \times 52^t$  且 y = f(x)。求 y 的值。 If  $f(t) = 3 \times 52^t$  and y = f(x), find the value of y.



(iii) 甲可在 y 日完成某一項工程, 乙可在(y+3)日完成同一工程。
 假如甲乙二人合作,可在 z 日完成,求 z 的值。
 A can finish a job in y days, B can finish a job in (y+3) days.
 If they worked together, they can finish the job in z days, find the value of z.



(iv) 用 z 粒 骰子 擲得 7 點 的 概率 是 w , 求 w 的 值。

The probability of throwing z dice to score 7 is w, find the value of w.

|--|

FOR OFFICIAL USE

Score for	,
accuracy	•

× Mult. factor for speed



Team No.



+ score

**Bonus** 

Time



Total score

Min.

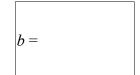
### **Event 3 (Individual)**

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若  $a = \sin 30^{\circ} + \sin 300^{\circ} + \sin 3000^{\circ}$ , 求 a 的值。 If  $a = \sin 30^{\circ} + \sin 300^{\circ} + \sin 3000^{\circ}$ , find the value of a.



(ii) 已知  $\frac{x+y}{2} = \frac{z+x}{3} = \frac{y+z}{4}$  且 x+y+z=36a。求 b 之值,若 b=x+y。



It is given that  $\frac{x+y}{2} = \frac{z+x}{3} = \frac{y+z}{4}$  and x+y+z = 36a.

Find the value of b, if b = x + y.

Find the value of d.

- (iii) 已知方程 x+6+8k=k(x+b)有正整數解。求 k 的最小值 c。
  It is given that the equation x+6+8k=k(x+b) has positive integral solution. Find c, the least value of k.
- (iv) 一輛汽車以平均時速 40c km/h 完成了旅程的 40%。為著使全程的平均速 度為 100 km/h, 車速被調至 d km/h 行畢全程。求 d 的值。

  A car has already travelled 40% of its journey at an average speed of 40c km/h. In order to make the average speed of the whole journey become 100 km/h, the speed of the car is adjusted to d km/h to complete the rest of the journey.

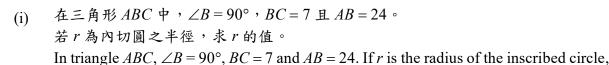
FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = Team No.

+ Bonus score Time Min. Sec.

#### **Event 4 (Individual)**

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

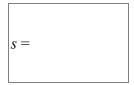




find the value of r.



(ii) 若  $x^2 + x - 1 = 0$  且  $s = x^3 + 2x^2 + r$ , 求 s 的 值。 If  $x^2 + x - 1 = 0$  and  $s = x^3 + 2x^2 + r$ , find the value of s.



(iii) 已知  $F_1 = F_2 = 1$  且  $F_n = F_{n-1} + F_{n-2}$ ,其中  $n \ge 3$ 。若  $F_t = s + 1$ ,求 t 的值。 It is given that  $F_1 = F_2 = 1$  and  $F_n = F_{n-1} + F_{n-2}$ , where  $n \ge 3$ . If  $F_t = s + 1$ , find the value of t.

$$t =$$

(iv) 若  $u = \sqrt{t(t+1)(t+2)(t+3)+1}$  , 求 u 的值。 If  $u = \sqrt{t(t+1)(t+2)(t+3)+1}$  , find the value of u .

u =		

FOR OFFICIAL USE

Score for accuracy

Mult. factor for speed



Team No.

score

Bonus

Time

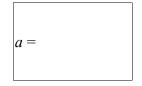
Total score

Min.

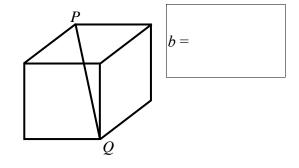
### **Event 5 (Individual)**

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

It is given that  $\log_7(\log_3(\log_2 x)) = 0$ . Find the value of a, if  $a = x^{\frac{1}{3}}$ . (i) 已知  $\log_7(\log_3(\log_2 x)) = 0 \circ \stackrel{1}{\text{$ :$}} a = x^{\frac{1}{3}}$  , 求 a 的值。



如圖示,PQ 是正方體的一條對角綫,且 $PQ = \frac{a}{2}$ 。 (ii) 若 b 為此正方體的總表面積, 求 b 的值。 In the figure, PQ is a diagonal of the cube and  $PQ = \frac{a}{2}$ . Find the value of b, if b is the total surface area of the cube.



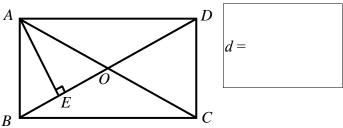
如圖示, $L_1$ 、 $L_2$ 為三個圓的切綫。如果最大圓的半徑是 18,最小圓半徑是 4b, (iii) 求 c,若 c 為圓 W 的半徑。 In the figure,  $L_1$  and  $L_2$  are tangents to the three circles. If the radius of the largest circle

is 18 and the radius of the smallest circle is 4b, find c, where c is the radius of the circle

 $L_1$ W  $L_2$ 

如圖,ABCD 為一長方形。 $AE \perp BD$ (iv) 且  $BE = EO = \frac{c}{6}$  。求長方形 ABCD 之面積 d 。 Refer to the figure, ABCD is a rectangle.  $AE \perp BD$ and  $BE = EO = \frac{c}{6}$ .

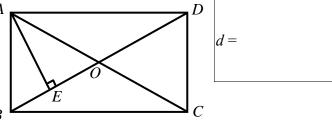
Find d, the area of the rectangle ABCD.



**FOR OFFICIAL USE** 

W.

Score for Mult. factor for = speed accuracy Bonus score Total score



Team No.

Time

Min.

### Event 6 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

- $2^{a.9b}$  為一四位數,其千位數是 2,百位數是 a,十位數是 9,個位數是 b, (i) 求a及b的值。
- $2^{a} \cdot 9^{b}$  is a four digit number and its thousands digit is 2, its hundreds digit is a, its tens digit is 9 and its units digit is b, find the values of a and b.
- (ii) b =
- 若  $c = \left(1 + \frac{1}{2} + \frac{1}{3}\right)\left(\frac{1}{2} + \frac{1}{3} + \frac{1}{4}\right) \left(1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4}\right)\left(\frac{1}{2} + \frac{1}{3}\right)$  , 求 c 的值。 c =Find the value of c, if  $c = \left(1 + \frac{1}{2} + \frac{1}{3}\right) \left(\frac{1}{2} + \frac{1}{3} + \frac{1}{4}\right) - \left(1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4}\right) \left(\frac{1}{2} + \frac{1}{3}\right)$ .
- (iv) 求 d 的值,若  $d = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) - \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) \left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \dots + \frac{1}{1994}\right) \circ dt = \left(1 + \frac{1}{2} + \dots + \frac$ Find the value of d, if  $d = \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right)\left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right) - \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1995}\right)\left(\frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{1994}\right).$

d =

### **FOR OFFICIAL USE**

Score for Mult. factor for Team No. = accuracy speed Bonus Time score

Total score

Sec.

Min.

### Event 7 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

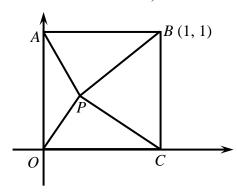
(i) 設  $p \cdot q \cdot r$  為三角形 PQR 的三邊。若  $p^4 + q^4 + r^4 = 2r^2(p^2 + q^2)$ ,且  $a = \cos^2 R$ ,其中 R 的對邊為 r,求 a 的值。

a =

- Let p, q, r be the three sides of triangle PQR. If  $p^4 + q^4 + r^4 = 2r^2(p^2 + q^2)$ , find the value of a, where  $a = \cos^2 R$  and R denotes the angle opposite r.
- (ii) 如圖,P 為正方形 OABC 內的任意點,且 b 為 PO+PA+PB+PC 之最小值,求 b 的值。

b = b

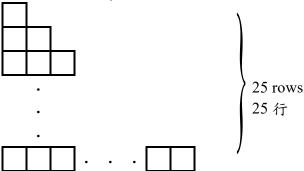
Refer to the diagram, P is any point inside the square OABC and b is the minimum value of PO + PA + PB + PC, find the value of b.



(iii) 長度同為 1 的火柴被排成下列圖案。若以 c 表示用去火柴枝的總長,求 c 的值。

*c* =

Identical matches of length 1 are used to arrange the following pattern, if c denotes the total length of matches used, find the value of c.



(iv) 求 d 的值, 若  $d = \sqrt{111111-222}$ 。

Find the value of d, where  $d = \sqrt{111111 - 222}$ .

d =		

### FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = Team No.

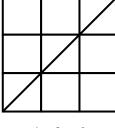
+ Bonus score Time Min.

#### **Event 8 (Group)**

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

在方格紙上繪畫尺寸為  $\ell \times b$  的長方形,其中  $\ell \setminus b$  為正整數並添上對角綫一條。以  $\ell \setminus \ell$  化表相交的端點總數(不包括首尾兩點在內)。 (如右圖示)

Rectangles of length  $\ell$  and breadth b where  $\ell$ , b are positive integers, are drawn on square grid paper. For each of these rectangles, a diagonal is drawn and the number of vertices V intersected (excluding the two end points) is counted (see the figure).



$$\ell = b = 3$$

$$V = 2$$

(i) 當  $\ell = 6$ , b = 4 時,求 V 的值。 Find the value of V, when  $\ell = 6$ , b = 4. V =

(ii) 當  $\ell = 5$  , b = 3 時 , 求 V 的值。 Find the value of V , when  $\ell = 5$  , b = 3 . V =

(iii) 當  $\ell = 12$  且 1 < b < 12 時,求使 V = 0 時,b 的不同個數 r。
When  $\ell = 12$  and 1 < b < 12, find r, the number of different values of b that makes V = 0?

r =

(iv) 當  $\ell = 108$ , b = 72 時,求 V 的值。 Find the value of V, when  $\ell = 108$ , b = 72.

V =

### FOR OFFICIAL USE

Score for accuracy

Mult. factor for speed



Team No.

score

Bonus

Time



Total score

Min.

### Event 9 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form.

除非特別聲明,答案須用數字表達,並化至最簡。

 $A \cdot B \cdot C \cdot D$  為自  $0 \le 9$  間的不同整數,且

 $求 A \cdot B \cdot C 及 D 之值。$ 

A, B, C, D are different integers ranging from 0 to 9 and

Find the values of A, B, C and D.

A =		
-----	--	--

$$B =$$

$$D =$$

FOR OFFICIAL USE

Score for accuracy

× Mult. factor for speed

=

Total score

Bonus

score

Team No.

Time

Min.

### Hong Kong Mathematics Olympiad (1994-95) Event 10 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

在直角坐標平面上,x-和 y-坐標同為整數的點稱為格點。P是起始時位於(0,0)的移動點,它每一步必須沿坐標綫的其中一過個方向走 1 個單位的距離。

Lattice points are points on a rectangular coordinate plane having both x- and y-coordinates being integers. A moving point P is initially located at (0, 0). It moves 1 unit along the coordinate lines (in either directions) in a single step.

(i) 若 P 走 1 步, 它可到達 a 個格點, 求 a 的值。

If P moves 1 step then P can reach a different lattice points, find the value of a.

a =

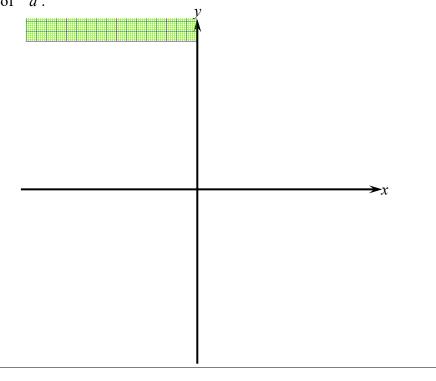
(ii) 若 P 可走不超過 2 步,它可到達 b 個格點,求 b 的值。
If P moves not more than 2 steps then P can reach b different lattice points, find the value of b.

*b* =

(iii) 若 P 走 3 步,它可到達 c 個格點,求 c 的值。 If P moves 3 steps then P can reach c different lattice points, find the value of c.

*c* =

(iv) 若 P 走 9 步,它停在直綫 x+y=9 上的概率是 d,求 d 的值。 If d is the probability that P lies on the straight line x+y=9 when P advances 9 steps, find the value of d.



### FOR OFFICIAL USE

Score for accuracy × Mult. factor for speed = Team No.

+ Bonus score Time Min. Sec.