## 1982 FI.3.2

求 
$$b$$
 的值,若  $\frac{\sin(4b)^{\circ}}{\cos(4b)^{\circ}} = \sqrt{\sqrt{9}} \ (0 < 4b < 90)$ 。

Find the value of b if  $\frac{\sin(4b)^\circ}{\cos(4b)^\circ} = \sqrt{\sqrt{9}}$  (0 < 4b < 90).

#### 1983 FI4.2

已知  $\sqrt{12} = -b \tan \frac{\pi}{3}$  。求 b 的值。Given  $\sqrt{12} = -b \tan \frac{\pi}{3}$ . Find the value of b. If  $\tan(3 \times 75 + 15)^\circ = \sqrt{B}$ , find the value of B.

# 1983 FG9.1

If  $\sin \theta = \frac{3}{5}$ ,  $a = \sqrt{\tan^2 \theta + 1}$ , find the value of a.

## 1984 FI4.2

$$\theta$$
為銳角, $\cos \theta = \frac{15}{17}$ 。若  $\tan \theta = \frac{b}{15}$ ,求  $b$  的值。

 $\theta$  is an acute angle such that  $\cos \theta = \frac{15}{17}$ . If  $\tan \theta = \frac{b}{15}$ , find the value of b.

#### 1985 FG6.3

若  $\sin(55-y)^\circ = \frac{d}{s}$ , 求 d 的值。 If  $\sin 30^\circ = \frac{d}{s}$ , find the value of d.

# 1986 FI2.4

If  $\sin A = \frac{3}{5}$  and  $\frac{\cos A}{\tan A} = \frac{q}{15}$ , find the value of q.

# 1986 FI3.2

若  $8 \sin^2 2910^\circ + 12 \cos^2 2925^\circ = x$ ,求 x 的值。

If  $8 \sin^2 2910^\circ + 12 \cos^2 2925^\circ = x$ , find the value of x.

# 1986 FG6.3

若 
$$\tan \theta = \frac{-7}{24}$$
,90° <  $\theta$  < 180° 及 100  $\cos \theta = r$ ,求  $r$  的值。

If  $\tan \theta = \frac{-7}{24}$ ,  $90^{\circ} < \theta < 180^{\circ}$  and  $100 \cos \theta = r$ , find the value of r.

#### 1986 FG10.3

If  $k = \frac{3\sin\theta + 5\cos\theta}{2\sin\theta + \cos\theta}$  and  $\tan\theta = 3$ , find the value of k.

#### 1987 FG7.2

若 
$$tan(3\times75+15)^{\circ}=\sqrt{B}$$
 , 求 B 的值。

#### 1987 FG8.1

若 
$$A = \frac{5\sin\theta + 4\cos\theta}{3\sin\theta + \cos\theta}$$
 ,且  $\tan\theta = 2$  ,求  $A$  的值。

If  $A = \frac{5\sin\theta + 4\cos\theta}{3\sin\theta + \cos\theta}$  and  $\tan\theta = 2$ , find the value of A.

#### 1988 FI5.2

若  $\tan^2 495^\circ + 1 = b$ , 求 b 的值。If  $\tan^2 495^\circ + 1 = b$ , find the value of b.

設 
$$\frac{1}{B} = \frac{\sin 37^{\circ} \sin 45^{\circ} \cos 60^{\circ} \sin 60^{\circ}}{\cos 30^{\circ} \cos 45^{\circ} \cos 53^{\circ}}$$
 , 求  $B$  的值。

If  $\frac{1}{B} = \frac{\sin 37^{\circ} \sin 45^{\circ} \cos 60^{\circ} \sin 60^{\circ}}{\cos 30^{\circ} \cos 45^{\circ} \cos 53^{\circ}}$ , find the value of B.

# 1989 FI3.2

已知 
$$\tan \theta = \frac{-\alpha}{15}$$
,90°<  $\theta$ < 180°,且  $\sin \theta = \frac{b}{34}$ ,求  $b$  的值。

If  $\tan \theta = \frac{-8}{15}$ ,  $90^{\circ} < \theta < 180^{\circ}$  and  $\sin \theta = \frac{b}{34}$ , find the value of b.

# 1989 FSG.4

已知 
$$k = \frac{4\sin\theta + 3\cos\theta}{2\sin\theta - \cos\theta}$$
 ,且  $\tan\theta = 3$  ,求  $k$  的值。

If  $k = \frac{4\sin\theta + 3\cos\theta}{2\sin\theta - \cos\theta}$  and  $\tan\theta = 3$ , find the value of k.

# 1989 FG10.3

已知 
$$k = \frac{6\cos^2\theta + 2\sin\theta\cos\theta + \sin^2\theta}{\cos^2\theta + \sin\theta\cos\theta + \sin^2\theta}$$
,且  $\tan\theta = 2$ ,求  $k$  的值。

If 
$$k = \frac{6\cos^2\theta + 2\sin\theta\cos\theta + \sin^2\theta}{\cos^2\theta + \sin\theta\cos\theta + \sin^2\theta}$$
 and  $\tan\theta = 2$ , find the value of  $k$ .

#### Trigonometric Expression (HKMO Classified Questions by topics)

#### 1990 HI14

若 
$$\frac{1}{A} = \frac{\cos 45^{\circ} \sin 70^{\circ} \cos 60^{\circ} \tan 40^{\circ}}{\cos 340^{\circ} \sin 135^{\circ} \tan 220^{\circ}}$$
, 求  $A$  的值。

If 
$$\frac{1}{A} = \frac{\cos 45^{\circ} \sin 70^{\circ} \cos 60^{\circ} \tan 40^{\circ}}{\cos 340^{\circ} \sin 135^{\circ} \tan 220^{\circ}}$$
, find the value of  $A$ .

#### 1990 FI4.3

If 
$$\sin \theta = \frac{-12}{15}$$
, where  $180^{\circ} < \theta < 270^{\circ}$ , and  $\tan \theta = \frac{c}{3}$ , find the value of  $c$ .

#### 1990 FG7.2

If 
$$K = \frac{6\cos\theta + 5\sin\theta}{2\cos\theta + 3\sin\theta}$$
 and  $\tan\theta = 2$ , find the value of  $K$ .

#### 1991 FI4.3

若 
$$\cos \theta = \frac{40}{41}$$
, 其中 θ 為銳角,且  $c = \frac{1}{\sin \theta} + \frac{1}{\tan \theta}$ ,求 c 的值。

If 
$$\cos \theta = \frac{40}{41}$$
, where  $\theta$  is an acute angle, and  $c = \frac{1}{\sin \theta} + \frac{1}{\tan \theta}$ ,

find the value of c.

# 1991 FI5.4

若 
$$K = \frac{\sin 65^{\circ} \tan^2 60^{\circ}}{\tan 30^{\circ} \cos 30^{\circ} \cos 25^{\circ}}$$
 ,求  $K$  的值。

If 
$$K = \frac{\sin 65^{\circ} \tan^2 60^{\circ}}{\tan 30^{\circ} \cos 30^{\circ} \cos 25^{\circ}}$$
, find the value of  $K$ .

# 1992 FI3.1

若 
$$a = \frac{\sin 15^{\circ}}{\cos 75^{\circ}} + \frac{1}{\sin^2 75^{\circ}} - \tan^2 15^{\circ}$$
,求  $a$  的值。

If 
$$a = \frac{\sin 15^{\circ}}{\cos 75^{\circ}} + \frac{1}{\sin^2 75^{\circ}} - \tan^2 15^{\circ}$$
, find the value of a.

# 1995 FI3.1

若 
$$a = \sin 30^{\circ} + \sin 300^{\circ} + \sin 3000^{\circ}$$
, 求  $a$  的值。

If 
$$a = \sin 30^\circ + \sin 300^\circ + \sin 3000^\circ$$
, find the value of a.

#### 2000 HI9

求 
$$\frac{12\sin^2 48^\circ + 12\sin^2 42^\circ}{\sin 330^\circ \tan 135^\circ - \sin^2 48^\circ \sin^2 42^\circ \tan 180^\circ}$$
 的值。

Find the value of 
$$\frac{12\sin^2 48^\circ + 12\sin^2 42^\circ}{\sin 330^\circ \tan 135^\circ - \sin^2 48^\circ \sin^2 42^\circ \tan 180^\circ}$$
.

#### 2003 FG3.2

已知 
$$f(n) = \sin \frac{n\pi}{4}$$
 , 其中  $n$  是整數。若  $c = f(1) + f(2) + \cdots + f(2003)$  , 求  $c$  的值。

Given that  $f(n) = \sin \frac{n\pi}{4}$ , where *n* is an integer.

If  $c = f(1) + f(2) + \cdots + f(2003)$ , find the value of c.

#### 2004 HI8

若 
$$t = \sin^4 \frac{\pi}{6} - \cos^2 \frac{2\pi}{6}$$
 ,求  $t$  的值。If  $t = \sin^4 \frac{\pi}{6} - \cos^2 \frac{2\pi}{6}$ , find the value of  $t$ .

#### 2005 HI4

設 
$$t$$
 為實數且滿足  $(1+\sin t)(1+\cos t)=\frac{5}{4}$ 。若  $N=\sin t+\cos t$ ,求  $N$  的值。

Let t be a real number satisfying  $(1 + \sin t)(1 + \cos t) = \frac{5}{4}$ .

If  $N = \sin t + \cos t$ , find the value of N.

# 2005 FG1.3

已知 
$$\tan \alpha = -\frac{1}{2}$$
。若  $c = \frac{2\cos\alpha - \sin\alpha}{\sin\alpha + \cos\alpha}$ ,求  $c$  的值。

Given that  $\tan \alpha = -\frac{1}{2}$ . If  $c = \frac{2\cos \alpha - \sin \alpha}{\sin \alpha + \cos \alpha}$ , find the value of c.

# 2007 HG7

設 
$$k = \sin 30^{\circ} + \cos 60^{\circ} + \sin 90^{\circ} + \cos 120^{\circ} + \dots + \sin 1890^{\circ} + \cos 1920^{\circ}$$
,求  $k$  的值。

Let 
$$k = \sin 30^{\circ} + \cos 60^{\circ} + \sin 90^{\circ} + \cos 120^{\circ} + \dots + \sin 1890^{\circ} + \cos 1920^{\circ}$$
,

find the value of k.

# 2007 FI3.1

設 
$$a = \cos^4 \theta - \sin^4 \theta - 2 \cos^2 \theta$$
, 求  $a$  的值。

Suppose that  $a = \cos^4 \theta - \sin^4 \theta - 2 \cos^2 \theta$ , find the value of a.

# 2008 FI1.

設 
$$A = 15 \times \tan 44^{\circ} \times \tan 45^{\circ} \times \tan 46^{\circ}$$
, 求  $A$  的值。

Let 
$$A = 15 \times \tan 44^{\circ} \times \tan 45^{\circ} \times \tan 46^{\circ}$$
, find the value of  $A$ .

#### 2008 FGS.3

已知 
$$\cos \alpha = -\frac{99}{101}$$
 及  $180^{\circ} < \alpha < 270^{\circ}$ 。求  $\cot \alpha$  的值。

Given that  $\cos \alpha = -\frac{99}{101}$  and  $180^{\circ} < \alpha < 270^{\circ}$ . Find the value of  $\cot \alpha$ .

# 2009 FG2.1

已知 
$$\tan \theta = \frac{5}{12}$$
,其中  $180^{\circ} \le \theta \le 270^{\circ}$ 。若  $A = \cos \theta + \sin \theta$ ,求  $A$  的值。

Given  $\tan \theta = \frac{5}{12}$ , where  $180^{\circ} \le \theta \le 270^{\circ}$ . If  $A = \cos \theta + \sin \theta$ , find the value of A.

#### 2010 FG1.1

Find the value of  $\sin^2 1^\circ + \sin^2 2^\circ + \dots + \sin^2 89^\circ$ .

## 2012 HG9

求 
$$\sin^2 1^\circ + \sin^2 2^\circ + \sin^2 3^\circ + \dots + \sin^2 359^\circ + \sin^2 360^\circ$$
 的值。

Evaluate 
$$\sin^2 1^\circ + \sin^2 2^\circ + \sin^2 3^\circ + \dots + \sin^2 359^\circ + \sin^2 360^\circ$$
.

#### 2012 FG2.1

Find the value of  $2 \times \tan 1^{\circ} \times \tan 2^{\circ} \times \tan 87^{\circ} \times \tan 88^{\circ} \times \tan 89^{\circ}$ .

# 2019 FI1.4

在 
$$\Delta XYZ$$
 中,已知  $XY \perp YZ$ , $\angle XZY = \theta$ ,綫段  $YZ$  和  $XZ$  的長度分別為 12 和  $20$ 。若  $D = (\sin \theta + \tan \theta)^2$ ,求  $D$  的值。

In  $\triangle XYZ$ ,  $XY \perp YZ$ ,  $\angle XZY = \theta$ , and the length of YZ and XZ are 12 and 20 respectively. If  $D = (\sin \theta + \tan \theta)^2$ , determine the value of D.

# Answers

Allowels				
1982 FI3.2 15	1983 FI4.2 -2	1983 FG9.1 5/4	1984 FI4.2 8	1985 FG6.3 4
1986 FI2.4	1986 FI3.2	1986 FG6.3	1986 FG10.3	1987 FG7.2
16	8	-96	2	3
1987 FG8.1	1988 FI5.2	1989 HI14	1989 FI3.2	1989 FSG.4
2	2	2	16	3
1989 FG10.3	1990 HI14	1990 FI4.3	1990 FG7.2	1991 FI4.3
2	2	4	2	9
1991 FI5.4 6	1992 FI3.1 2	1995 FI3.1 $\frac{1}{2}$	2000 HI9 24	2003 FG3.2 $1 + \sqrt{2}$
2004 HI8 -\frac{3}{16}	$ \begin{array}{r} 2005 \text{ HI4} \\ -2 + \sqrt{10} \\ 2 \end{array} $	2005 FG1.3 5	$\frac{2007 \text{ HG7}}{\frac{3}{2}}$	2007 FI3.1 -1
2008 FI1.1 15	$2008 \text{ FGS.3} $ $\frac{99}{20} = 4.95$	$ \begin{array}{r} 2009 \text{ FG2.1} \\ -\frac{17}{13} \end{array} $	2010 FG1.1 44.5	2012 HG9 180
2012 FG2.1 2	2019 FI1.4 1024 225			