**Difference of two squares factor** (HKMO Classified Questions by topics)

### 1982 FG10.2

(248-1) 可被兩個介乎於 60 至 70 之間的整數整除,求該兩數。

If  $(2^{48} - 1)$  is divisible by two whole numbers between 60 and 70, find them.

#### 1993 HI7

若 x 和 y 為質數,且滿足  $x^2 - y^2 = 117$ ,求 x 的值。

If x and y are prime numbers such that  $x^2 - y^2 = 117$ , find the value of x.

## 1993 FI5.3

已知  $2^{16}-1$  共有四質因子,求其中最大的一個,以 c 表它。

It is known that  $2^{16} - 1$  has four distinct prime factors, determine the largest one, denoted by c.

## 1995 HG4

若 x 及 y 為正整數,且 $x^2 = y^2 + 2000$ ,求x 的最小值。

Suppose x and y are positive integers such that  $x^2 = y^2 + 2000$ , find the least value of x.

## 1997 HI1

設 n 為一正整數。若  $n^2 = 29p + 1$ ,其中 p 為質數,試求 n 之值。

Let n be a positive integer.

If  $n^2 = 29p + 1$ , where p is a prime number, find the value of n.

## 1999 FG2.3

設c為質數,若11c+1是一正整數之平方,求c之值。

Let c be a prime number.

If 11c + 1 is the square of a positive integer, find the value of c.

## 2010 FGS.1

已知n為一正整數。若 $n^2 + 5n + 13$ 為一完全平方數,求n的值。

Given that n is a positive integer.

If  $n^2 + 5n + 13$  is a perfect square, find the value of n.

## 2011 HI5

整數 x 減去 12 後是一個整數的平方。將 x 加上 19 後則是另一個整數的平方。求 x 的值。

An integer x minus 12 is the square of an integer. x plus 19 is the square of another integer. Find the value of x.

## 2011 HG4

已知 n 為一正整數,且  $n^4 - 18n^2 + 49$  為一質數。求 n 的值。

Given that n is a positive integer and  $n^4 - 18n^2 + 49$  is a prime number, find the value of n.

#### 2013 FG3.1

若 m 和 n 是正整數且  $m^2 - n^2 = 43$  , 求  $m^3 - n^3$  的值。

If m and n are positive integers with  $m^2 - n^2 = 43$ , find the value of  $m^3 - n^3$ .

## 2016 FG4.1

若 a 及 b 為整數,且  $a^2$  與  $b^2$  相差 144,求 d=a+b 的最大值。

Let a and b are two integers and the difference between  $a^2$  and  $b^2$  is 144, determine the largest possible value of d = a + b.

#### 2018 FI1.1

已知  $x^2 = y^2 - 4y$ ,其中 x 及 y 為整數。求 A = x + y 的最大值。

Given that  $x^2 = y^2 - 4y$ , where x and y are integers.

Determine the largest value of A = x + y.

#### 2018 FI1.3

設 C 為正整數。已知  $144+2^{C}$  為平方數,求 C 的值。

Let C be a positive integer.

Given that  $144 + 2^C$  is a perfect square, determine the value of C.

## 2022 P1Q13

已知  $a^{2x}-b^{2y}=1672$ ,其中  $a \cdot b \cdot x$  及 y 為正整數。求 ax+by 的最小值。

Given that  $a^{2x} - b^{2y} = 1672$ , where a, b, x and y are positive integers.

Find the minimum value of ax + by.

# **Answers**

1982 FG10.2	1993 HI7	1993 FI5.3	1995 HG4	1997 HI1
63, 65	11	257	45	30
1999 FG2.3	2010 FGS.1	2011 HI5	2011 HG4	2013 FG3.1
13	4	237	4	1387
2016 FG4.1	2018 FI1.1	2018 FI1.3	2022 P1Q13	
72	4	8	23	