$\sqrt{a+b-2\sqrt{ab}}$ (HKMO Classified Questions by topics)

1993 FI1.4

If
$$\sqrt{3-2\sqrt{2}} = \sqrt{2} - \sqrt{d}$$
, find the value of d.

1999 HG3

求
$$\log(\sqrt{3+\sqrt{5}}+\sqrt{3-\sqrt{5}})$$
 的值。

Find the value of $\log(\sqrt{3+\sqrt{5}} + \sqrt{3-\sqrt{5}})$.

2001 FG2.1

已知
$$x = \sqrt{7-4\sqrt{3}}$$
 及 $\frac{x^2-4x+5}{x^2-4x+3} = a$, 求 a 的值。

Given that $x = \sqrt{7 - 4\sqrt{3}}$ and $\frac{x^2 - 4x + 5}{x^2 - 4x + 3} = a$, find the value of a.

2004 HI5

設
$$E = \sqrt{12 + 6\sqrt{3}} + \sqrt{12 - 6\sqrt{3}}$$
 , 求 E 的值。

Let $E = \sqrt{12 + 6\sqrt{3}} + \sqrt{12 - 6\sqrt{3}}$, find the value of E.

2005 HI3

若 x 是實數且滿足
$$\left(\sqrt{5+2\sqrt{6}}\right)^x + \left(\sqrt{5-2\sqrt{6}}\right)^x = 10$$
,求 x 的最小可能的值。 求實數 $c = \frac{\left(4+\sqrt{15}\right)^{\frac{3}{2}} + \left(4-\sqrt{15}\right)^{\frac{3}{2}}}{\left(6+\sqrt{35}\right)^{\frac{3}{2}} - \left(6-\sqrt{35}\right)^{\frac{3}{2}}}$ 的值。

If x is a real number satisfying the equation $\left(\sqrt{5+2\sqrt{6}}\right)^{3} + \left(\sqrt{5-2\sqrt{6}}\right)^{3} = 10$,

find the smallest possible value of x.

2006 HI1

設
$$\sqrt{20 + \sqrt{300}} = \sqrt{x} + \sqrt{y}$$
 及 $w = x^2 + y^2$,求 w 的值。

Let $\sqrt{20+\sqrt{300}} = \sqrt{x} + \sqrt{y}$, where x and y are rational numbers and $w = x^2 + y^2$, find the value of w.

2009 HG5

設
$$x \cdot y$$
 及 z 為正整數且滿足 $\sqrt{z-\sqrt{28}} = \sqrt{x} - \sqrt{y}$ 。 求 $x+y+z$ 的值。

Let x, y and z be positive integers and satisfy $\sqrt{z} - \sqrt{28} = \sqrt{x} - \sqrt{y}$.

Find the value of x + y + z.

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2011 HI7

求
$$\sqrt{7-\sqrt{12}-\sqrt{13-2\sqrt{12}}}$$
 的值。

Find the value of $\sqrt{7-\sqrt{12}-\sqrt{13-2\sqrt{12}}}$

2013 HI1

化簡
$$\sqrt{94-2\sqrt{2013}}$$
 。

Simplify $\sqrt{94-2\sqrt{2013}}$.

2013 FI3.1, 2015 FI4.2

求 β =
$$\frac{(7+4\sqrt{3})^{\frac{1}{2}}-(7-4\sqrt{3})^{\frac{1}{2}}}{\sqrt{3}}$$
 的值。

Determine the value of $\beta = \frac{(7 + 4\sqrt{3})^{\frac{1}{2}} - (7 - 4\sqrt{3})^{\frac{1}{2}}}{\sqrt{2}}$.

2015 FG3.1

化簡
$$\sqrt{3+\sqrt{5}} + \sqrt{3-\sqrt{5}}$$
 。

Simplify $\sqrt{3+\sqrt{5}} + \sqrt{3-\sqrt{5}}$

2016 FG4.3

求實數
$$c = \frac{\left(4 + \sqrt{15}\right)^{\frac{3}{2}} + \left(4 - \sqrt{15}\right)^{\frac{3}{2}}}{\left(6 + \sqrt{35}\right)^{\frac{3}{2}} - \left(6 - \sqrt{35}\right)^{\frac{3}{2}}}$$
的值

Determine the value of real number $c = \frac{\left(4 + \sqrt{15}\right)^{\frac{3}{2}} + \left(4 - \sqrt{15}\right)^{\frac{3}{2}}}{\left(6 + \sqrt{35}\right)^{\frac{3}{2}} - \left(6 - \sqrt{35}\right)^{\frac{3}{2}}}$

2017 FI3.2

求
$$b = \frac{\sqrt{6 + 2\sqrt{8}} + \sqrt{6 - 2\sqrt{8}}}{2}$$
 的值。

Determine the value of $b = \frac{\sqrt{6 + 2\sqrt{8} + \sqrt{6 - 2\sqrt{8}}}}{2}$.

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Answers

1993 FI1.4 1	1999 HG3 1/2	2001 FG2.1 2	2004 HI5 6	2005 HI3 -2
2006 HI1 250	2009 HG5 16	2011 HI7 $\sqrt{6} - \sqrt{2}$	$2013 \text{ HI1} $ $\sqrt{61} - \sqrt{33}$	2013 FI3.1, 2015 FI4.2 2
2015 FG3.1 $\sqrt{10}$	$ \begin{array}{c} 2016 \text{ FG4.3} \\ \hline 7 \\ \hline 13 \end{array} $	2017 FI3.2 2		

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