

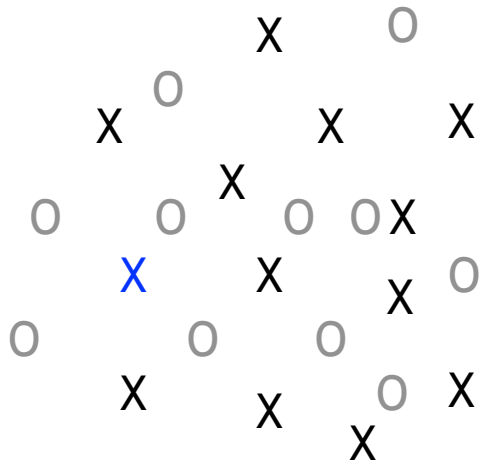
Data Visualization

The

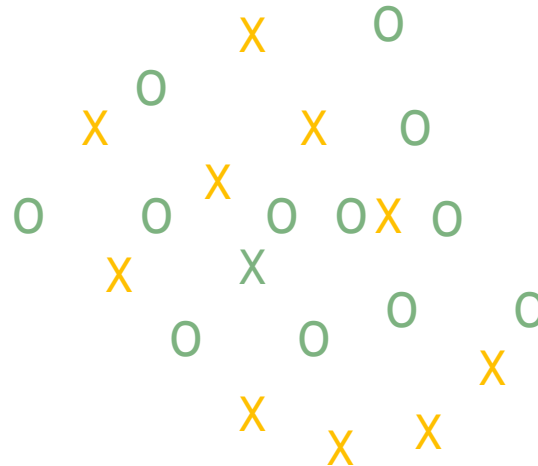
Foundations

The Modes of Perception

Find the outlier



Fast

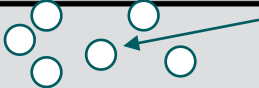









Slow

The Modes of Perception

- Pre-attentive
 - fast
 - parallel processing
 - effortless
- Pattern recognition
 - semi-fast
 - governed by laws of Gestalt
- Attentive
 - slow
 - sequential
 - high effort (attention is a very limited resource)

Main Properties of Graphics

Category	Example
<i>Position</i>	
<i>Shape</i>	
<i>Size</i>	
<i>Color</i>	
<i>Orientation (Line)</i>	
<i>Length (Line)</i>	
<i>Type and Size (Line)</i>	
<i>Brightness</i>	

Main Properties of Graphics Humans

Category	Amount of pre-attentive information
<i>Position</i>	<i>very high</i>
<i>Shape</i>	<i>----</i>
<i>Size</i>	<i>approx. 4</i>
<i>Color</i>	<i>approx. 8</i>
<i>Orientation (Line)</i>	<i>approx. 4</i>
<i>Length (Line)</i>	<i>----</i>
<i>Type and Size (Line)</i>	<i>----</i>
<i>Brightness</i>	<i>approx. 8</i>

Pre-attentive Perception

- Position
 - fast
 - effective
 - high number of different positions
- Color
 - use with care
- Shape
- Orientation

*Pre-attentive perception is effortless.
Exploit this as much as you can.*

Pattern Detection

„It is interesting to note that our brain [...] subconsciously always prefers meaningful situations and objects.“

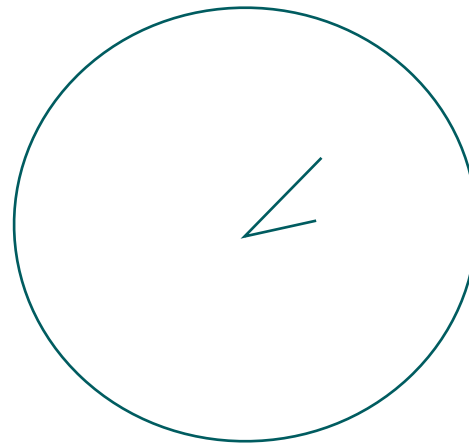
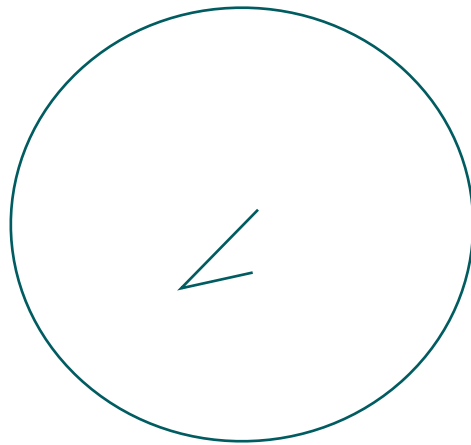
- Emergence
- Reification
- Multi-stability
- Invariance

*Pattern detection can be trained.
Exploit this for frequent visualizations.*

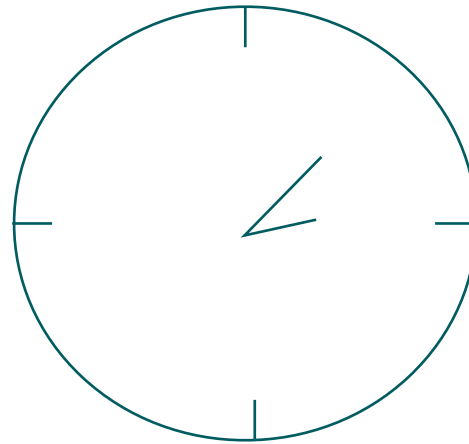
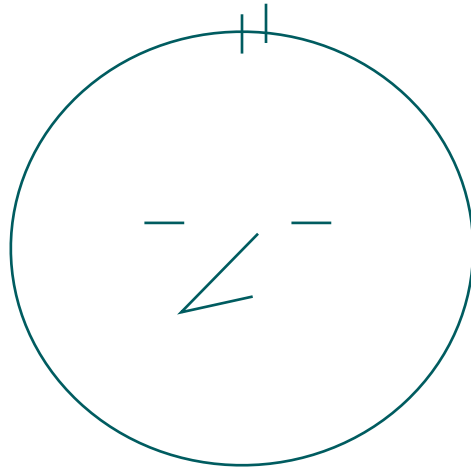
What is this?



What is this?

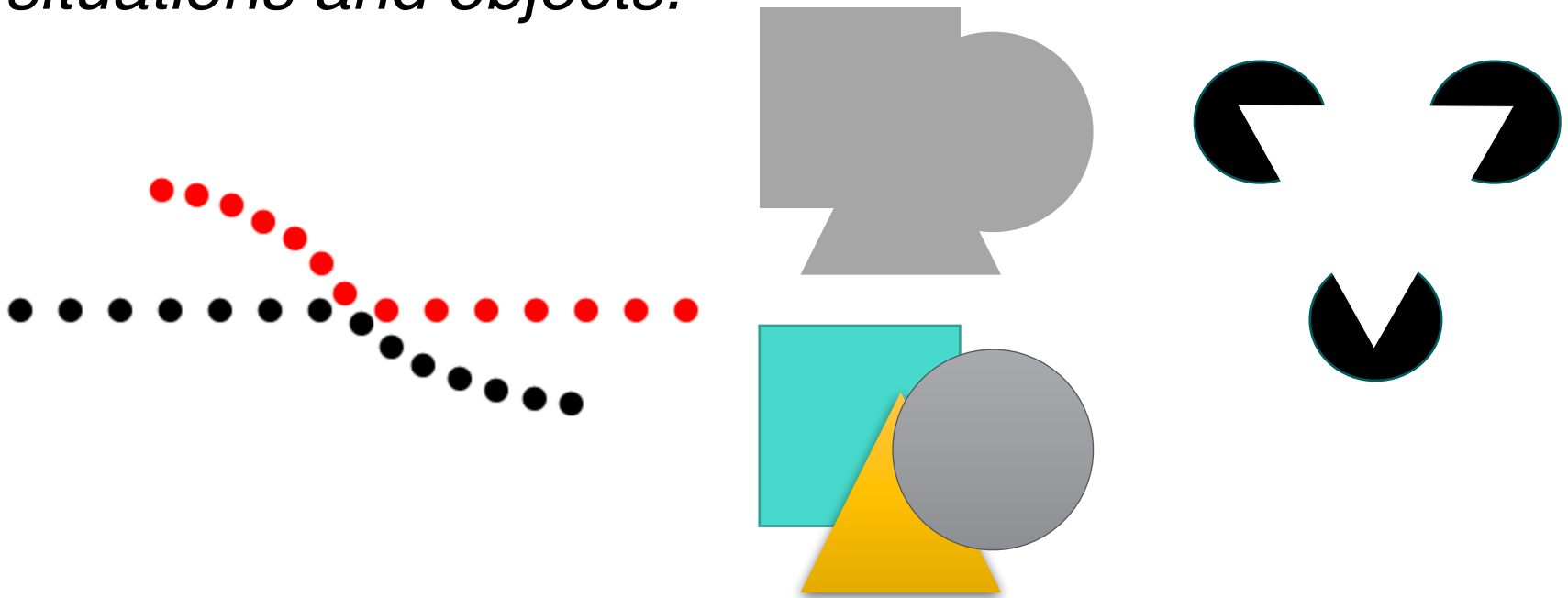


What is this?



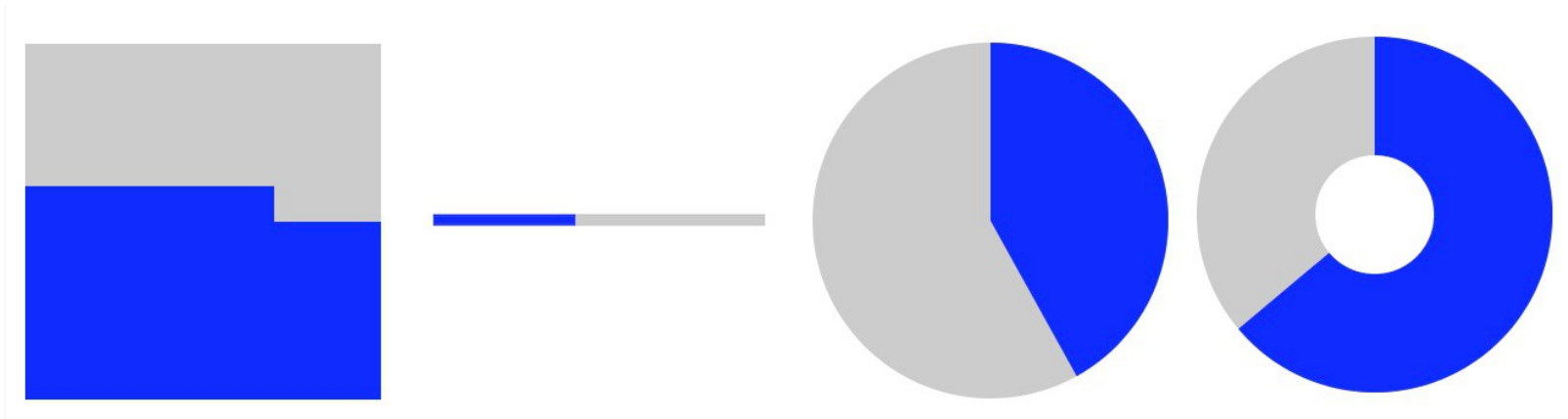
Laws of Gestalt

*„It is interesting to note that our brain,
in accordance with the laws of Gestalt,
subconsciously always prefers meaningful
situations and objects.“*



Accuracy of Graphics

Square Pie vs Stacked Bar vs Pie vs Donut



What do you think?

Why do we visualize data?

- Explore
 - use different techniques
 - avoid „construction“ bias
 - be careful with „aesthetics“
 - challenge findings -> use attentive mode
- Explain
 - focus on message or „story“
 - use pre-attentive mode

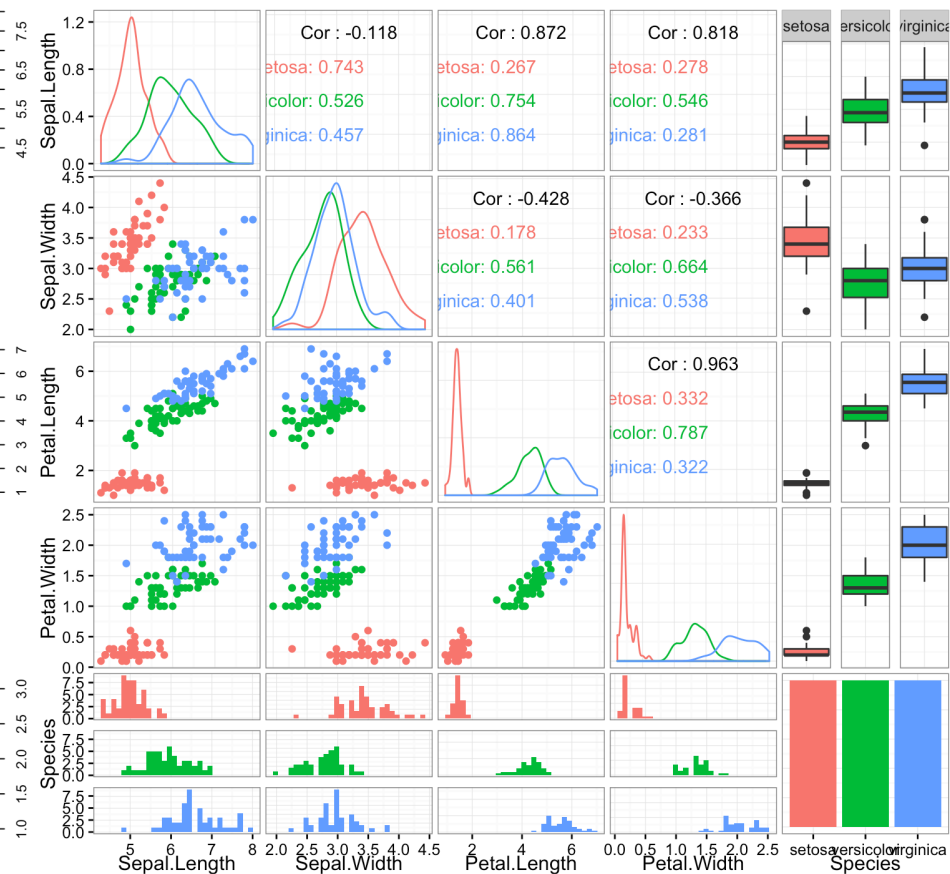
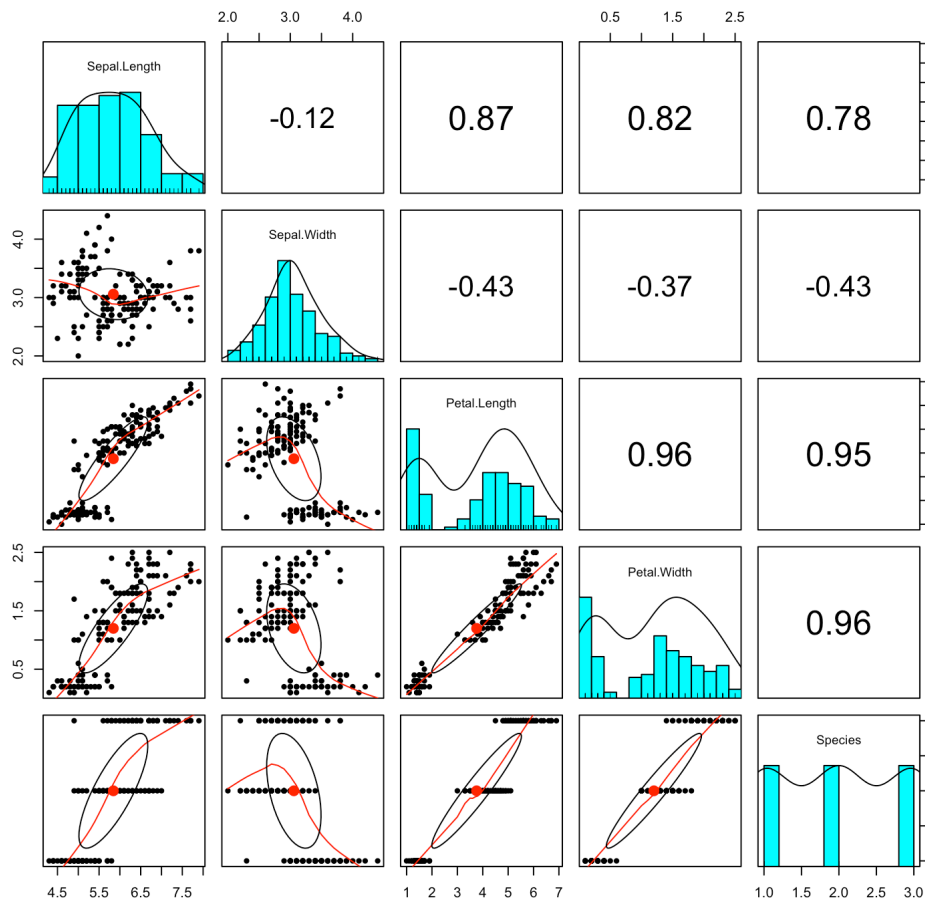
Don't trust your perception ;-)

Data Visualization

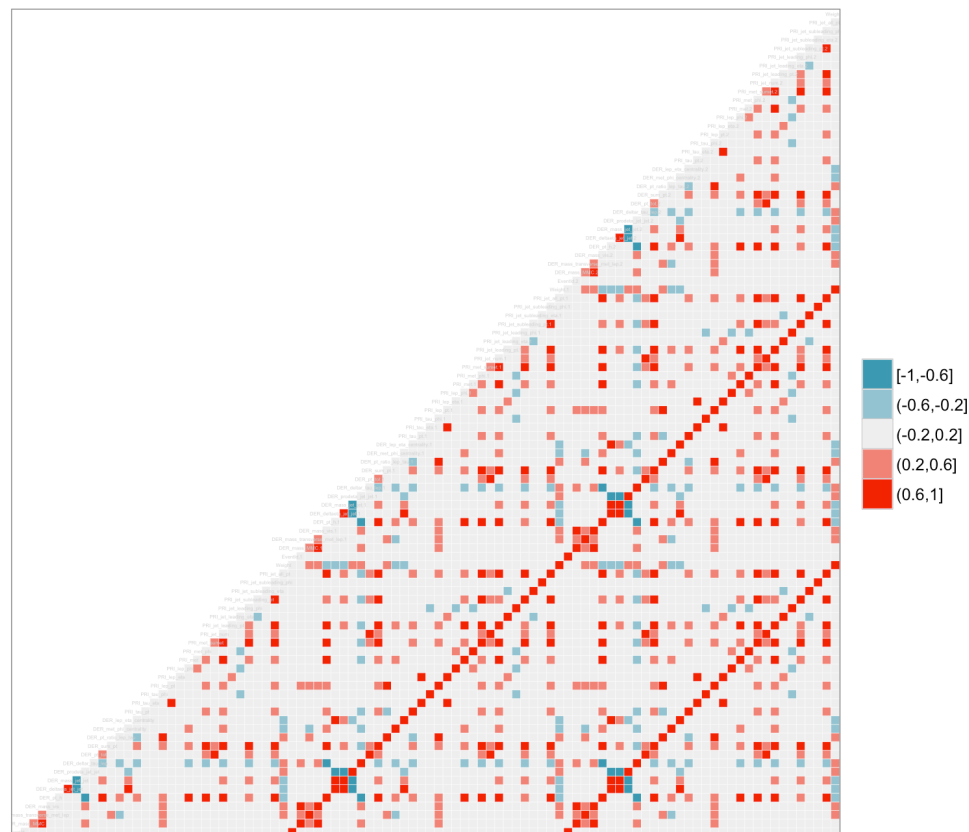
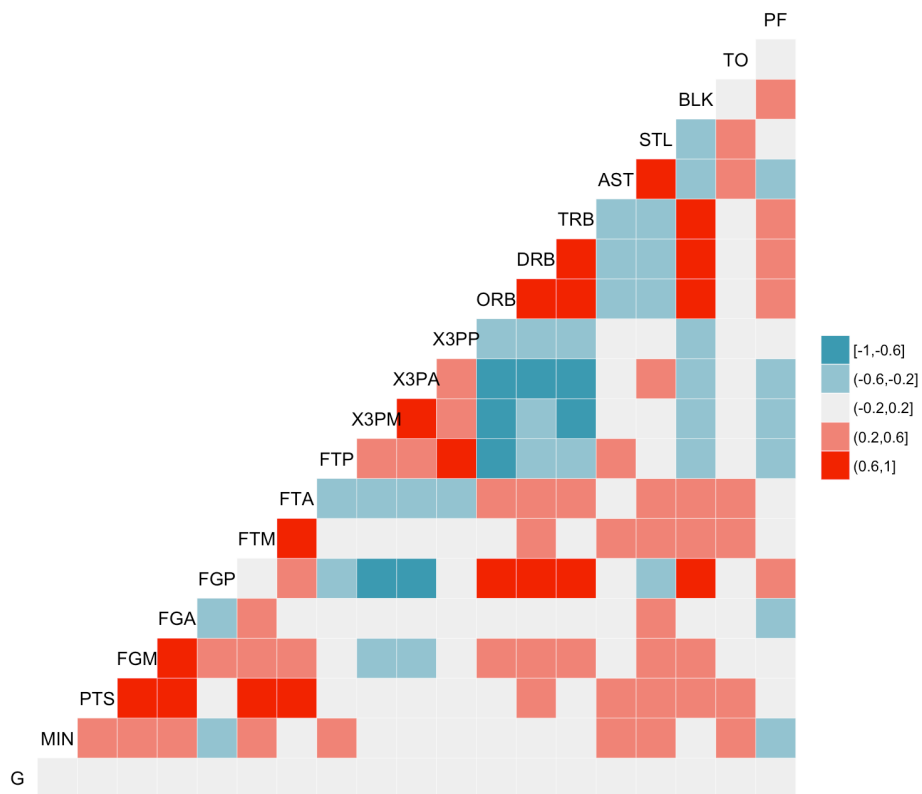
In

Higher Dimensions

Pair Plots



Correlation Plots



Fundamental Problems

- No accurate method in higher dimensions
 - Approximation methods
 - „Simulated“ dimensions (color, size, shape)
 - Animations?
- No notion of quality or accuracy for visualizations
 - Information Theory?
 - „Stability“?

All visualizations are wrong, but some are useful.

Approximation Methods

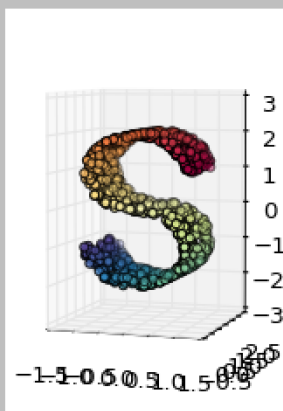
- Pair Plots
 - Axis-aligned projections
 - Interpretable in terms of original variables
- Singular Value Decomposition
 - Optimal with respect to 2-norm (Euclidean norm) and supremum norm
 - Comes with an error estimate
- Other methods
 - Stochastic Neighbor Embedding ((t-)SNE)
 - „Manifold Learning“

Manifold Learning Methods

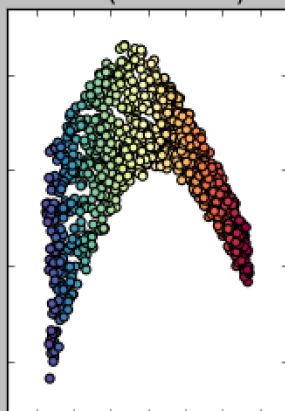
- Locally Linear Embedding
 - Neighborhood-preserving embedding
- Isomap
 - quasi-isometric
- Multi-Dimensional Scaling
 - quasi-isometric
- Spectral Embedding
 - Spectral clustering based on similarity
- Stochastic Neighbor Embedding (SNE, t-SNE)
 - preserves conditional probabilities for similarity
- Local Tangent Space Alignment (LTSA)

Manifold Learning

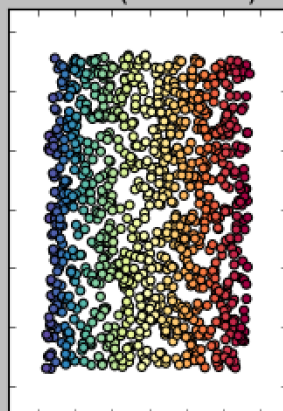
Manifold Learning with 1000 points, 10 neighbors



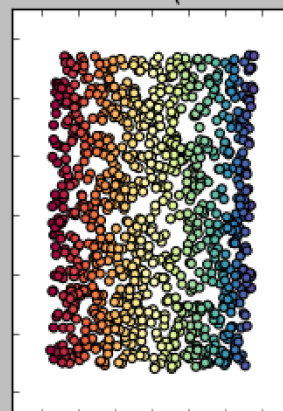
LLE (0.23 sec)



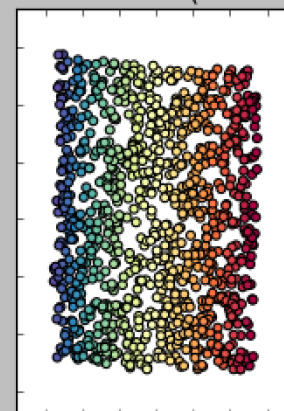
LTSA (0.27 sec)



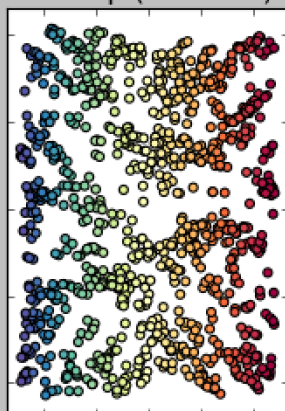
Hessian LLE (0.39 sec)



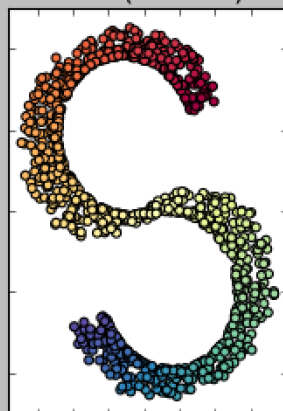
Modified LLE (0.3 sec)



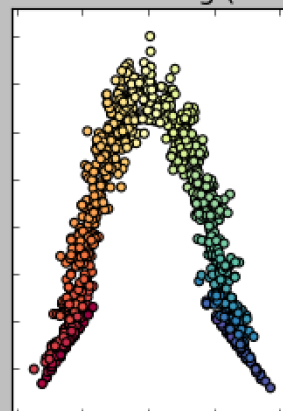
Isomap (0.44 sec)



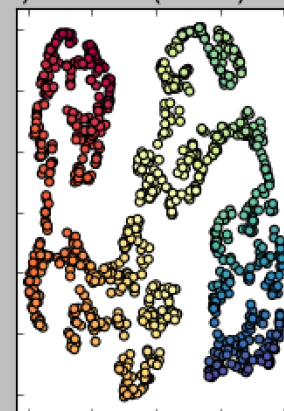
MDS (2.2 sec)



SpectralEmbedding (0.17 sec)

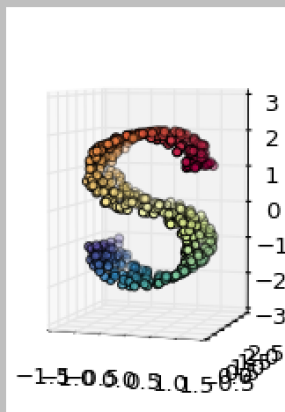


t-SNE (4 sec)

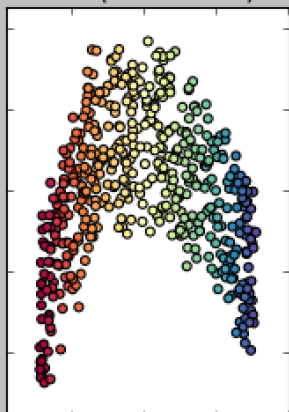


Manifold Learning

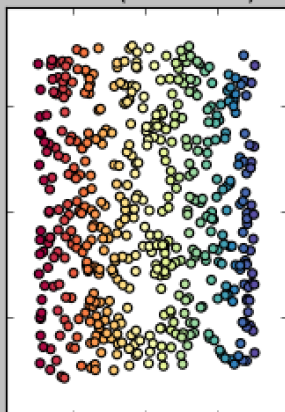
Manifold Learning with 500 points, 10 neighbors



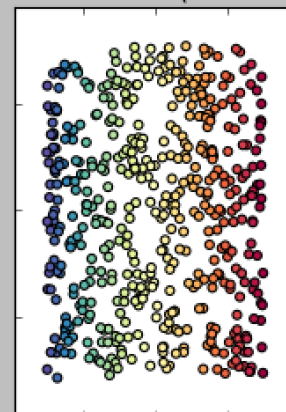
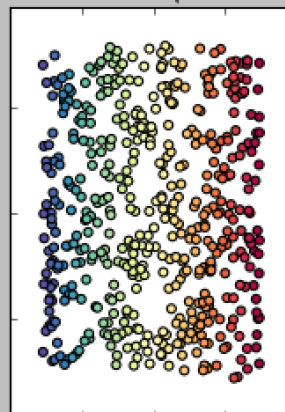
LLE (0.087 sec)



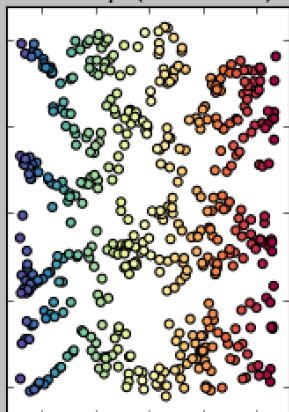
LTSA (0.11 sec)



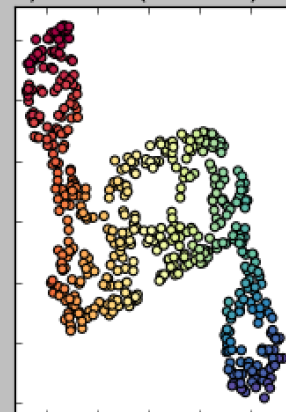
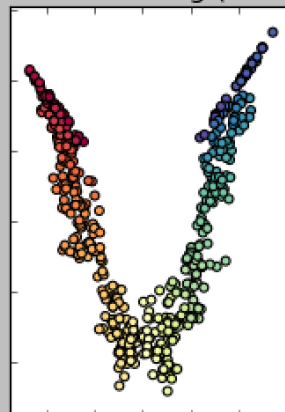
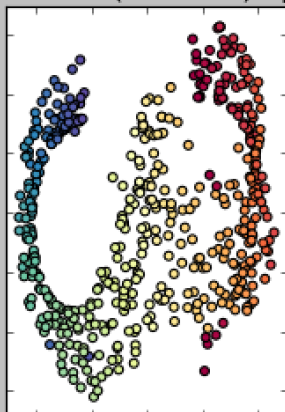
Hessian LLE (0.19 sec) Modified LLE (0.13 sec)



Isomap (0.11 sec)

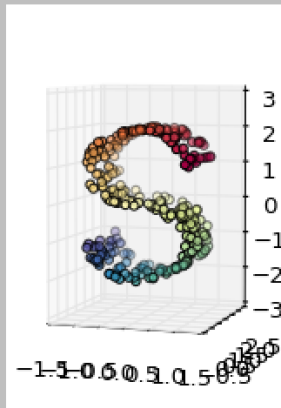


MDS (0.53 sec) SpectralEmbedding (0.066 sec) t-SNE (2.3 sec)

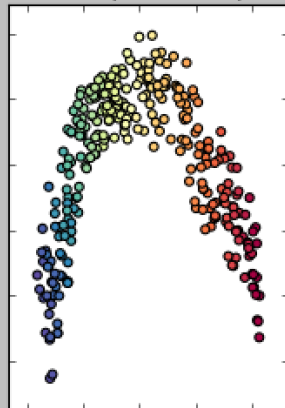


Manifold Learning

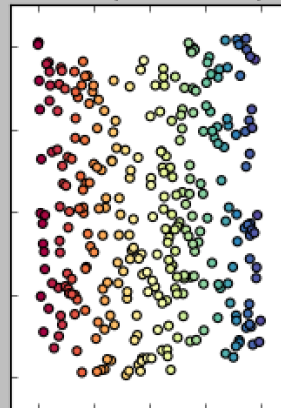
Manifold Learning with 300 points, 10 neighbors



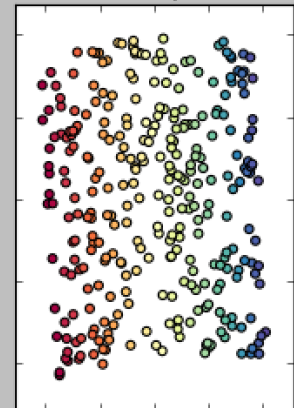
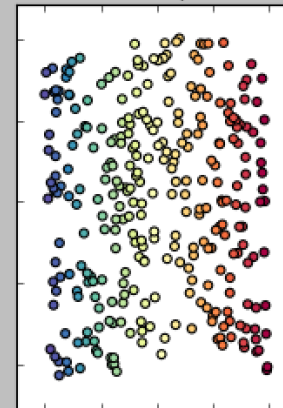
LLE (0.08 sec)



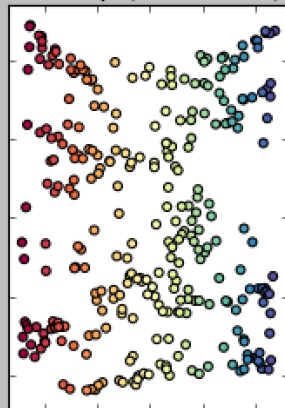
LTSA (0.066 sec)



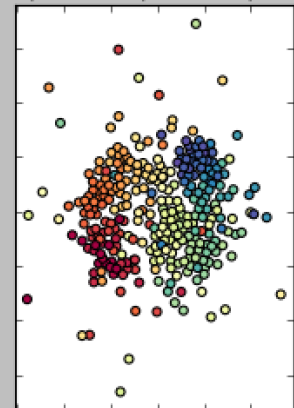
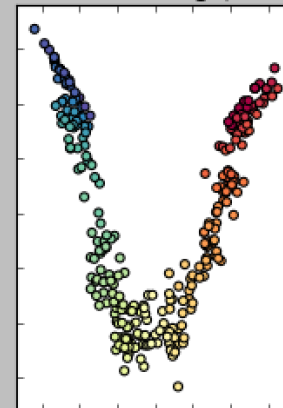
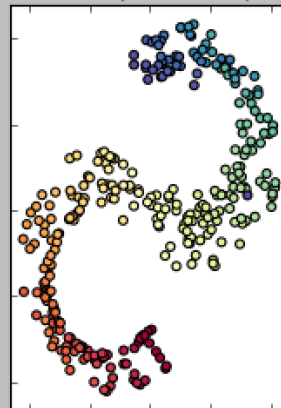
Hessian LLE (0.11 sec) Modified LLE (0.079 sec)



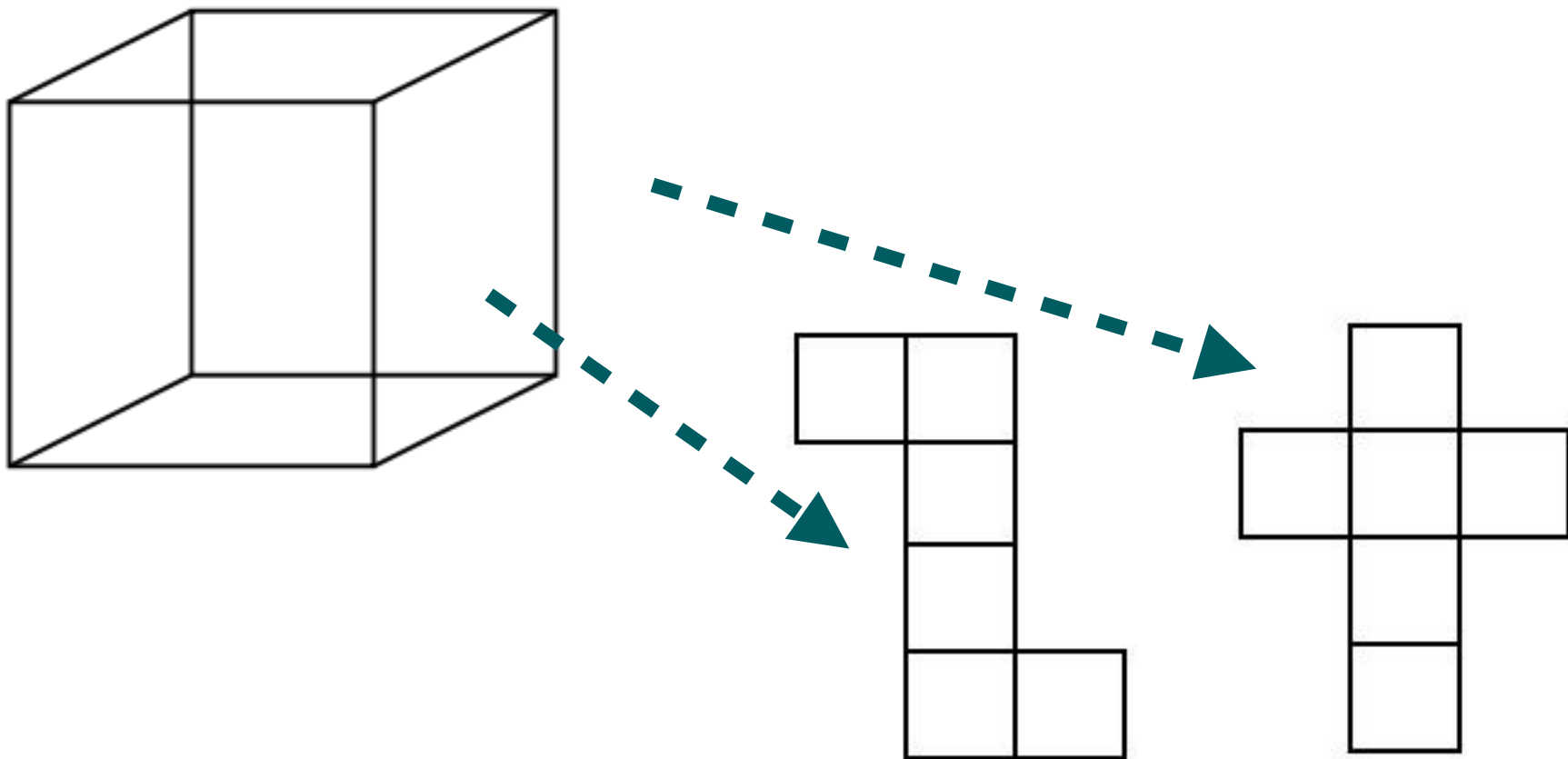
Isomap (0.037 sec)



MDS (0.19 sec) SpectralEmbedding (0.029 sec) t-SNE (1.4 sec)



Local Tangent Space Alignment



Principal Components and Curves

- **Principal Component Analysis**
 - orthogonal decomposition based on SVD
 - linear in all variables
 - tries to preserve variance
- **Principal Curves**
 - minimize the Sum of Squared Errors with respect to all variables (as PCA, preserve variance)
 - nonlinear
 - smooth

Principal Components and Curves

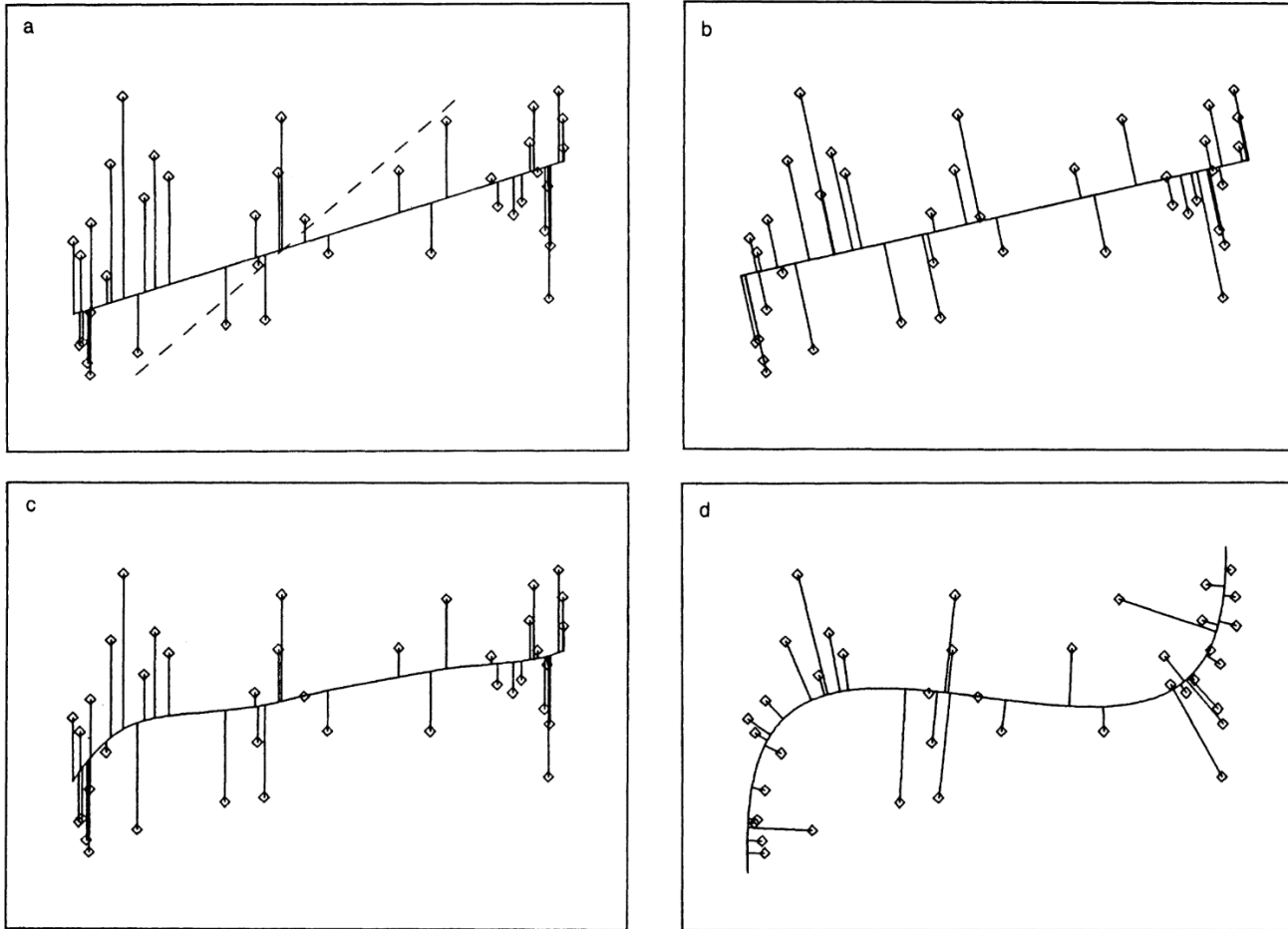
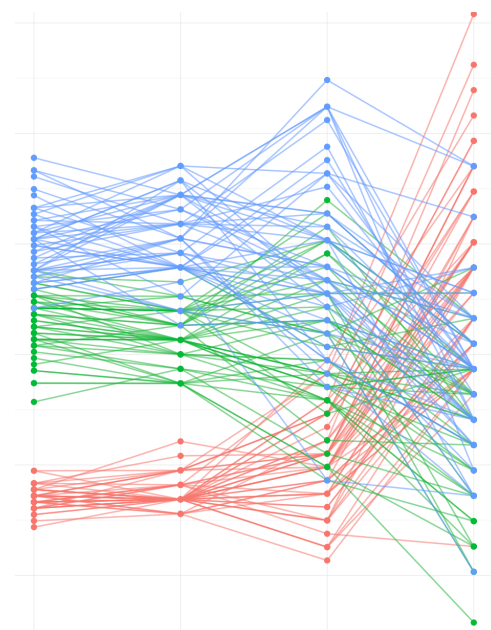
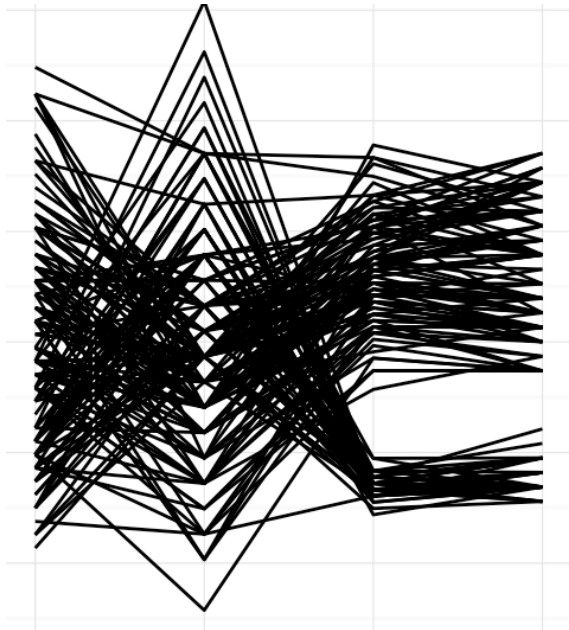


Figure 1. (a) The linear regression line minimizes the sum of squared deviations in the response variable. (b) The principal-component line minimizes the sum of squared deviations in all of the variables. (c) The smooth regression curve minimizes the sum of squared deviations in the response variable, subject to smoothness constraints. (d) The principal curve minimizes the sum of squared deviations in all of the variables, subject to smoothness constraints.

Parallel Coordinates

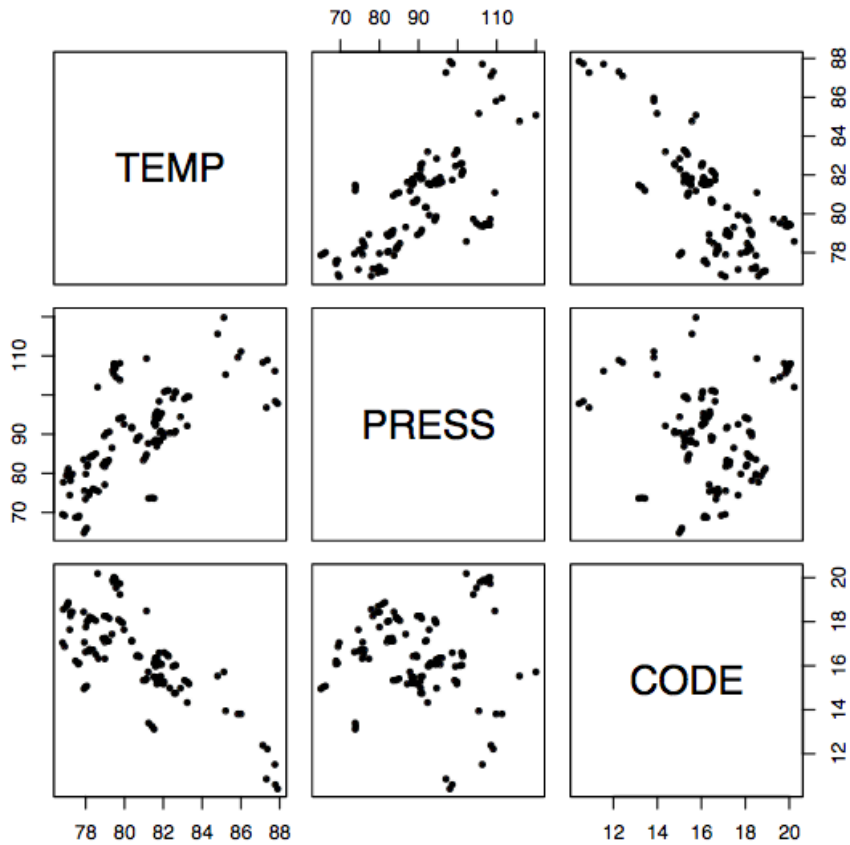
- Parallel Coordinates
 - especially useful for high-dimensional data
 - depends on ordering and scaling



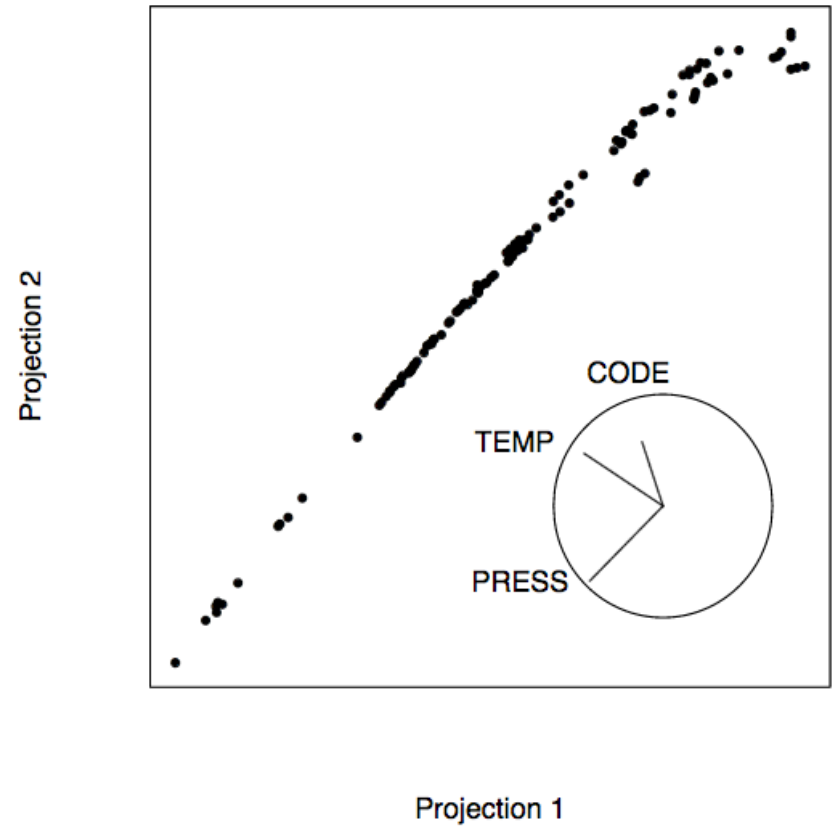
The Grand Tour

- **Animated sequence of 2-D projections**
 - [https://en.wikipedia.org/wiki/Grand_Tour_\(data_visualisation\)](https://en.wikipedia.org/wiki/Grand_Tour_(data_visualisation))
 - Asimov (1985): The grand tour: a tool for viewing multidimensional data.
- **Underlying idea**
 - Randomly generate 2-D projections (random walk)
 - Over time generate a dense subset of all possible 2-D projections
 - Optional: Follow a given path / guided tour

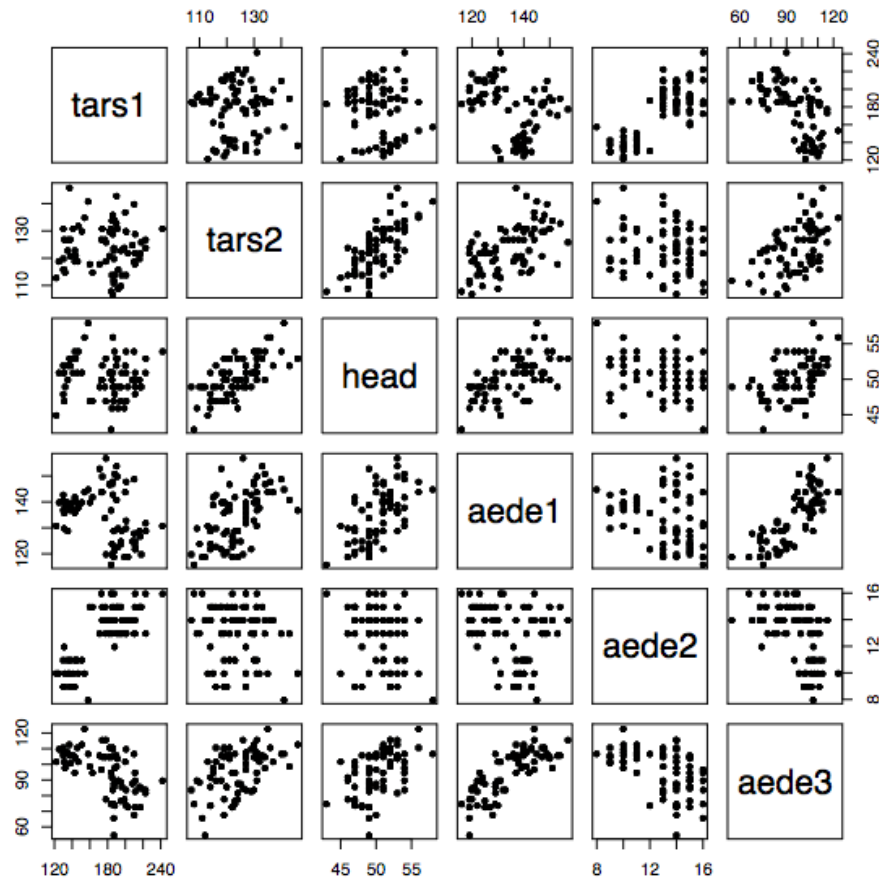
The Grand Tour



(Non-)linear association

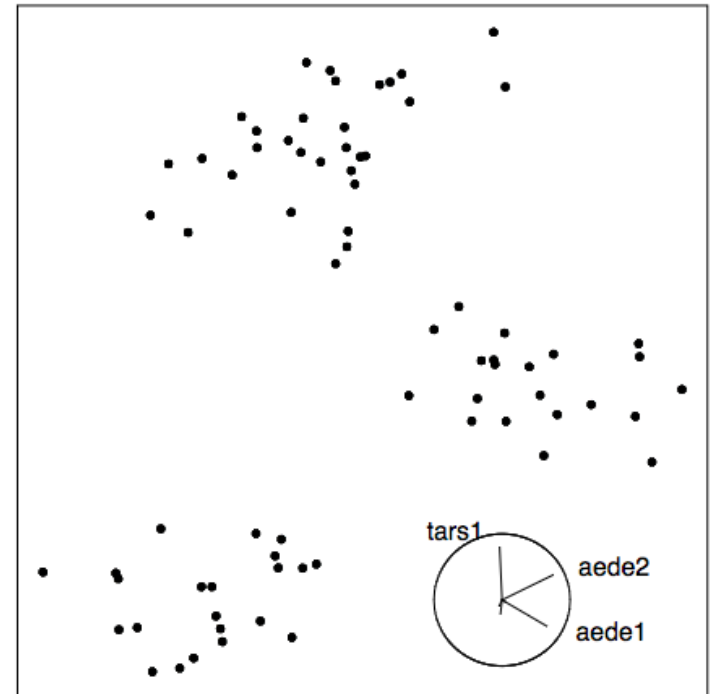


The Grand Tour



Projection 2

Clustering



Projection 1