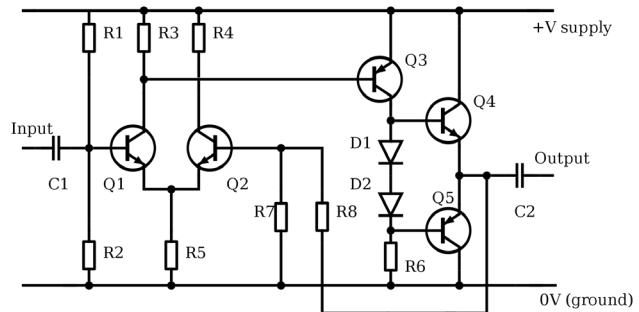


Lecture 4 – Machine elements

Andrés Faíña (anfv@itu.dk)



From parts to machines

What you have learnt:

Part modelling

3D printing

Laser cutting

How do you build a machine?

Forces and Moments (Physics 101)

Mechanisms

Bearings and guides

Power transmission

Fasteners

Forces and Moments

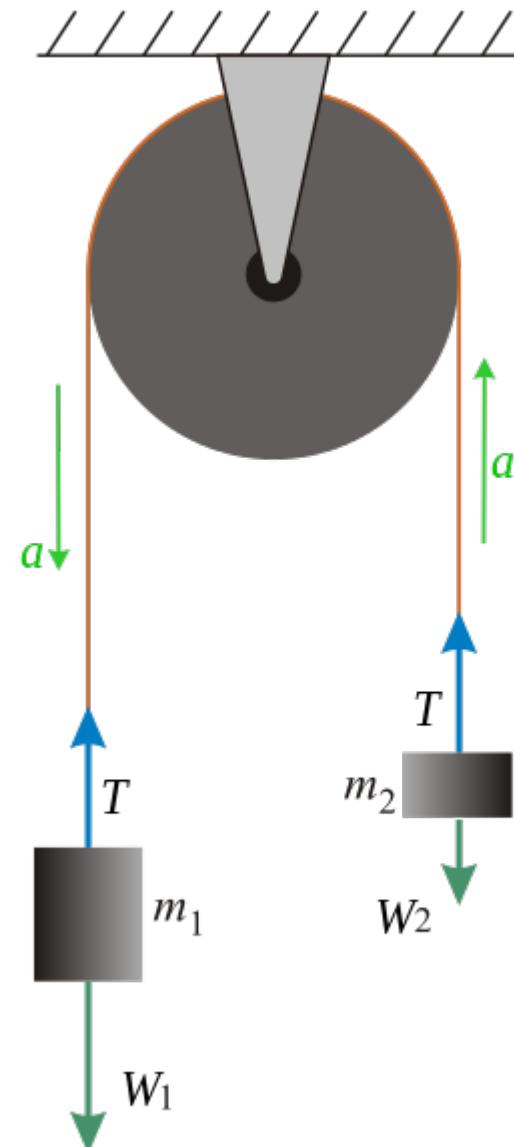
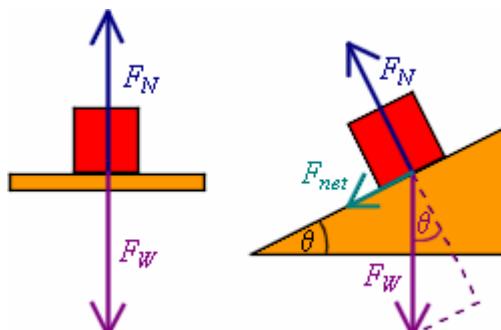
Forces

A quantitative description of an interaction that causes a change in an object's motion

$$\sum \mathbf{F} = m \cdot \mathbf{a}$$

Force and acc are vectors:

Magnitude
Direction

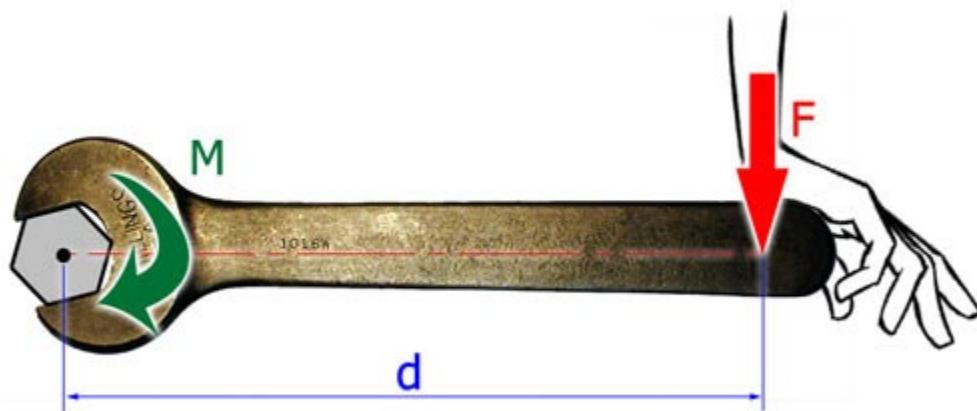
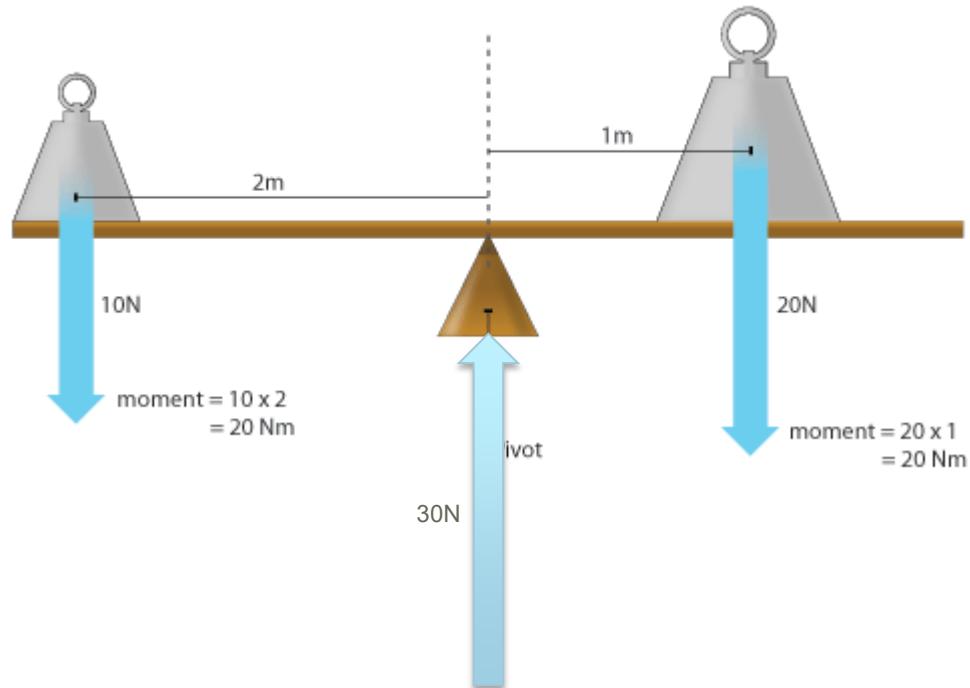


Moments or torque

Turning effect of a force

$$M = F \cdot d$$

$$\sum M = I \cdot \alpha$$



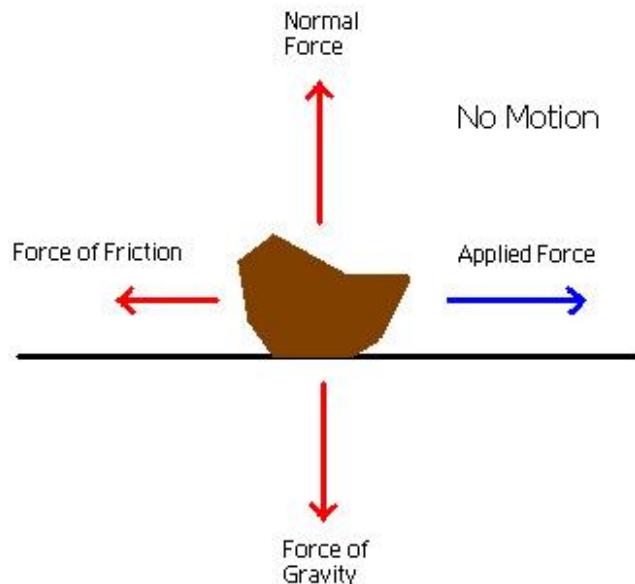
Static equilibrium

$$\begin{aligned}\sum \mathbf{F} &= m \mathbf{a} \\ \mathbf{a} &= \mathbf{0}\end{aligned}$$

$$\begin{aligned}\sum \mathbf{M} &= I \boldsymbol{\alpha} \\ \boldsymbol{\alpha} &= \mathbf{0}\end{aligned}$$

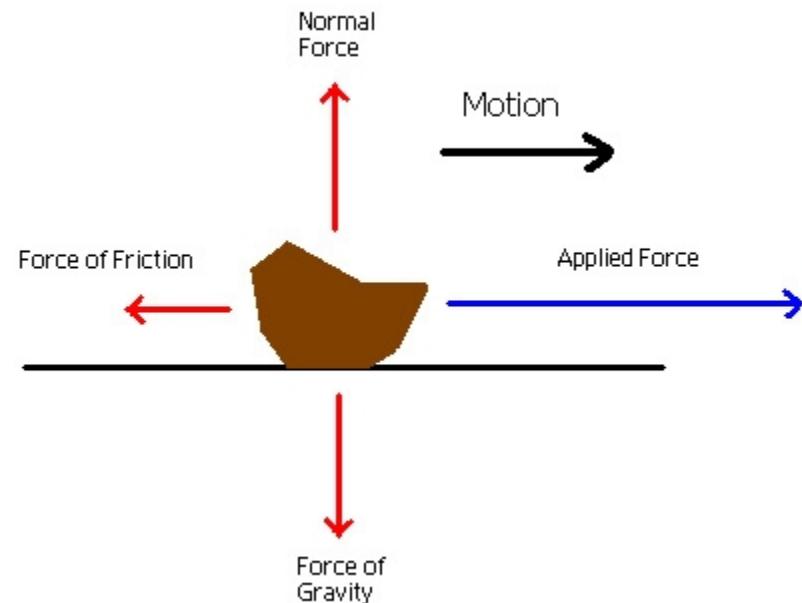
Therefore...

$$\sum \mathbf{F} = \mathbf{0}$$

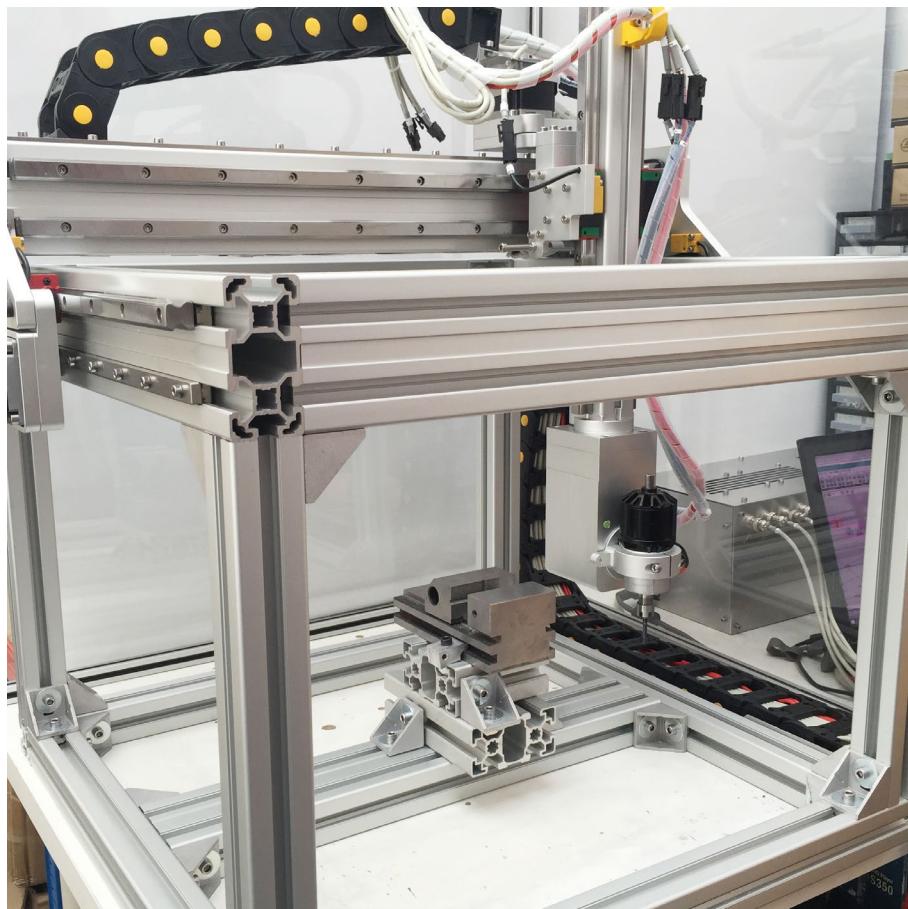


Therefore...

$$\sum \mathbf{M} = \mathbf{0}$$



Structural elements



Mechanisms

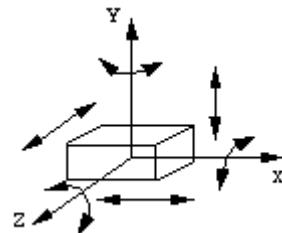
Degrees of freedom

number of independent parameters that define its configuration

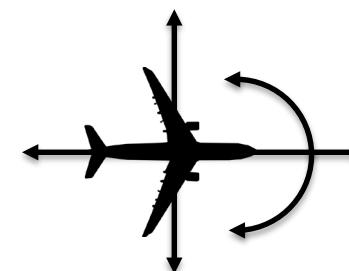
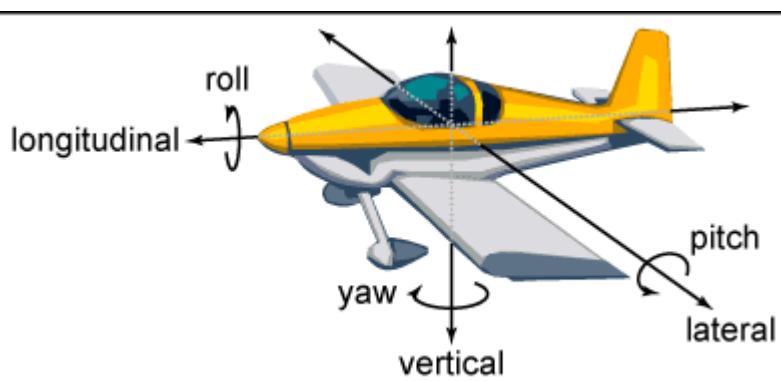
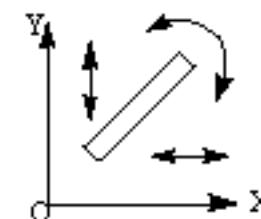
In a machine:

dof = motors or actuators

A rigid object in space
has 6 *dof*

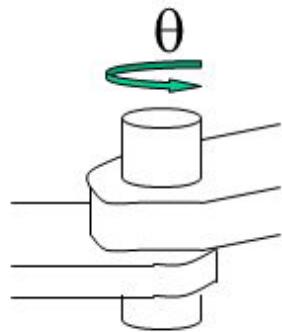


A rigid object in a plane
has 3 *dof*

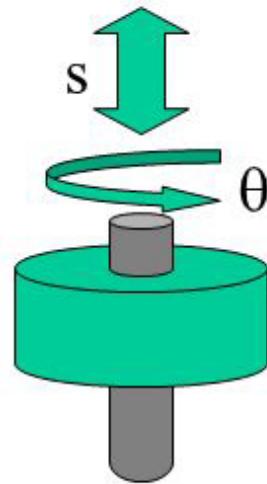


Kinematic pairs

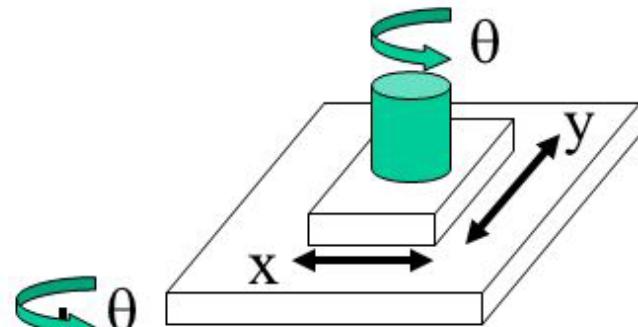
connection between two bodies that imposes constraints on their relative movement



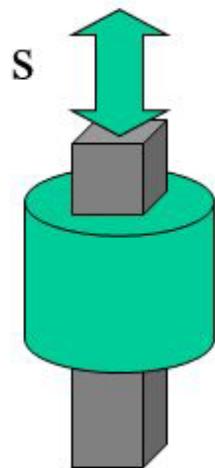
Revolute/pin joint



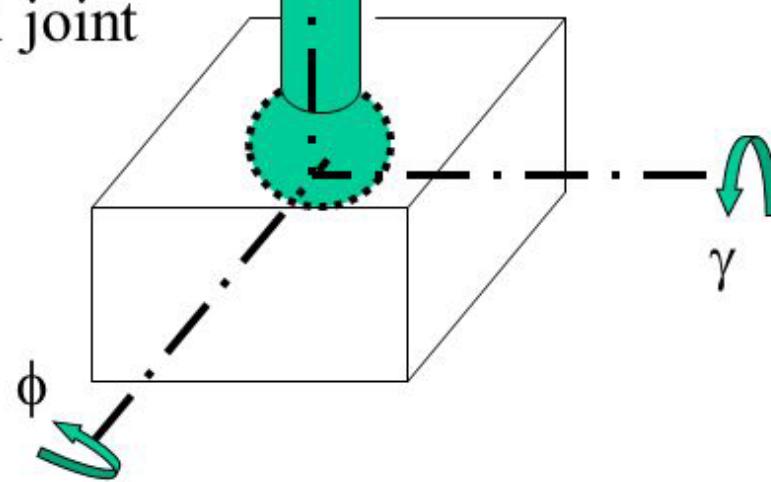
Cylindrical joint



Planar joint



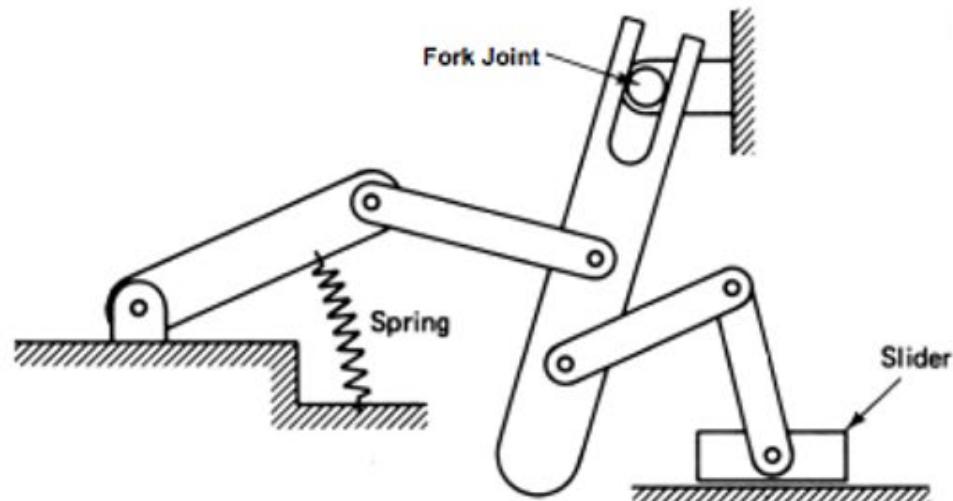
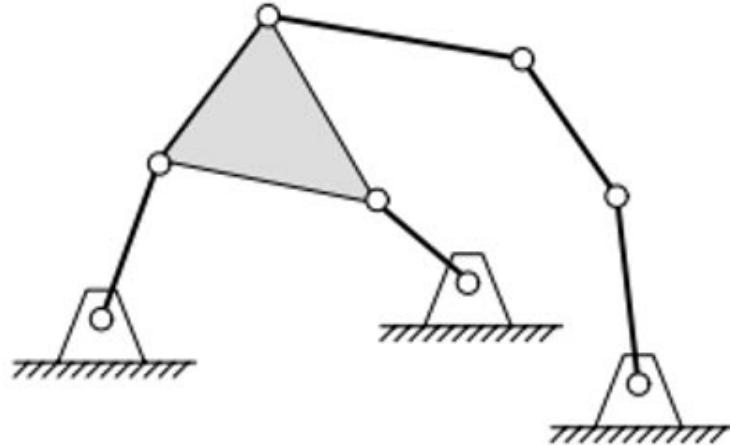
Prismatic joint



Spherical joint

dof can be difficult to calculate...

Determine the degree of freedom of the following mechanisms

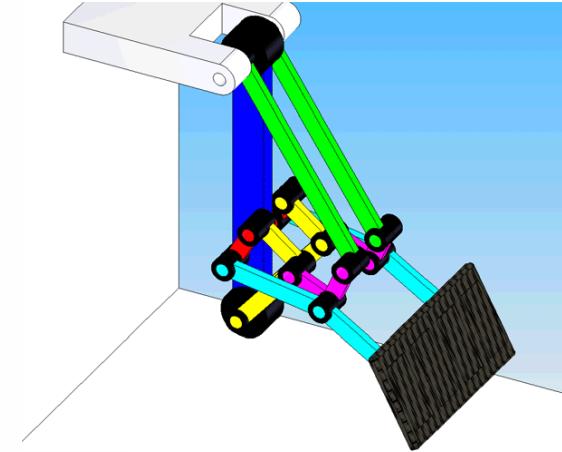
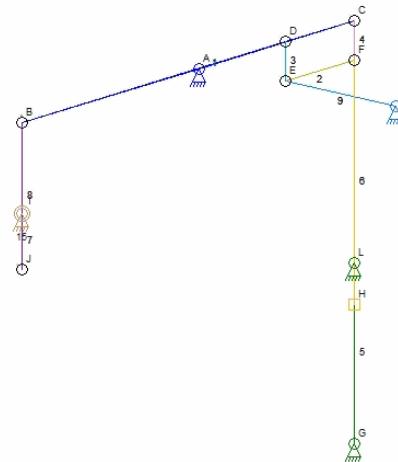
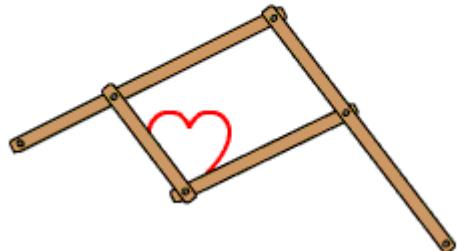


Gruebler's Equation:

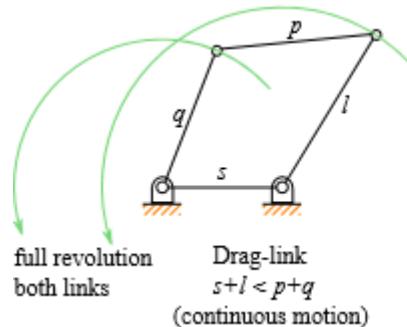
$$M = \text{degrees of freedom} = 3(n - 1) - 2j_p - j_h$$

4 bar linkage

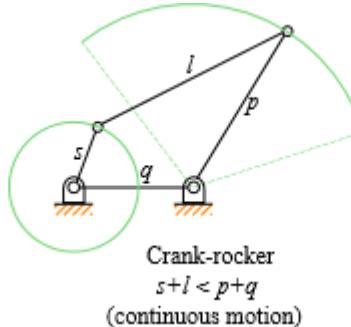
A **mechanical linkage** is an assembly of bodies connected to manage forces and movement.



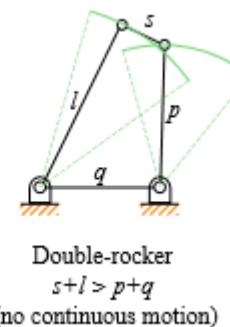
A 4 bar linkage is the simplest movable closed chain linkage



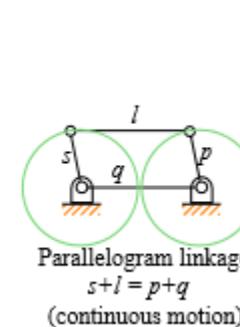
full revolution
both links
Drag-link
 $s+l < p+q$
(continuous motion)



Crank-rocker
 $s+l < p+q$
(continuous motion)

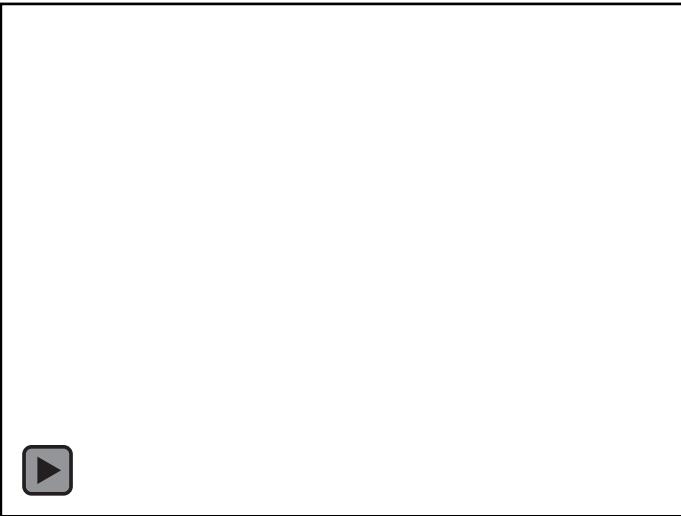


Double-rocker
 $s+l > p+q$
(no continuous motion)

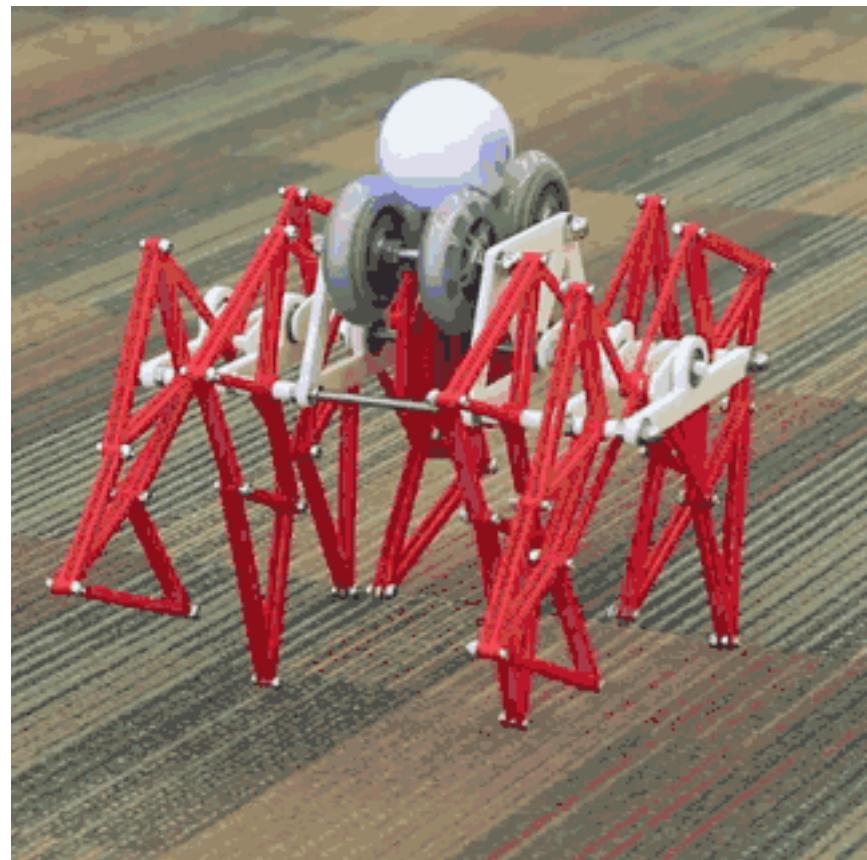
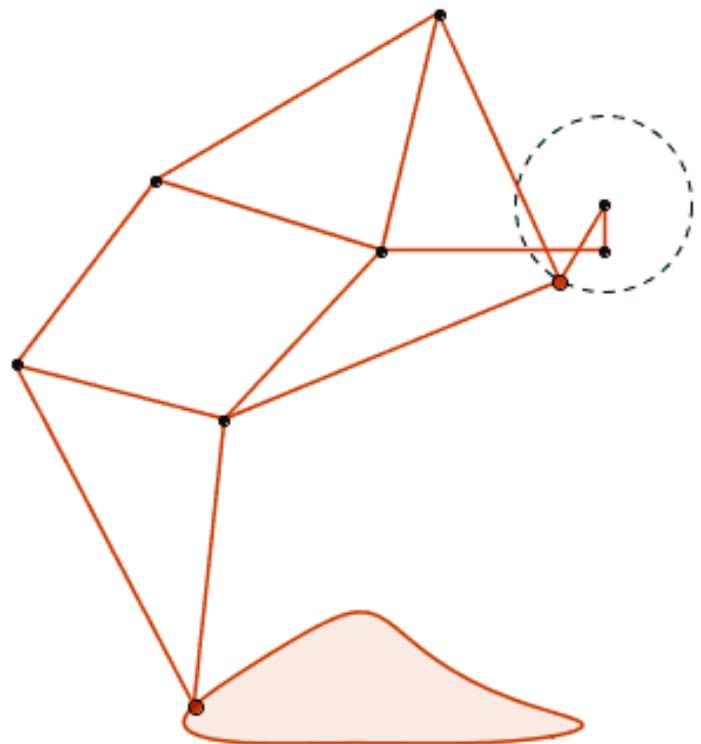


Parallelogram linkage
 $s+l = p+q$
(continuous motion)

Some 4 bar linkages



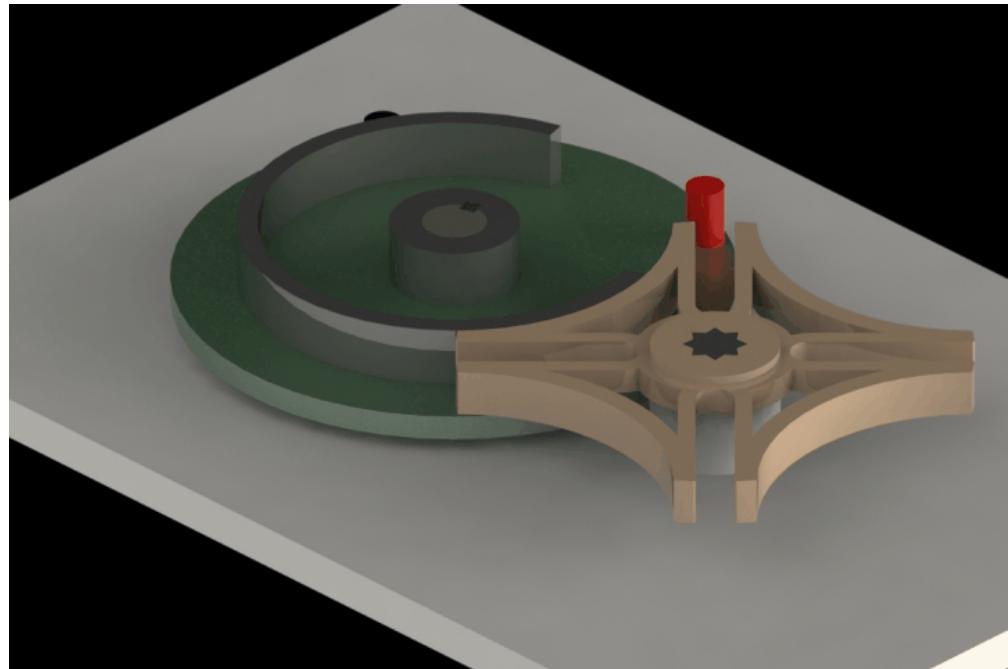
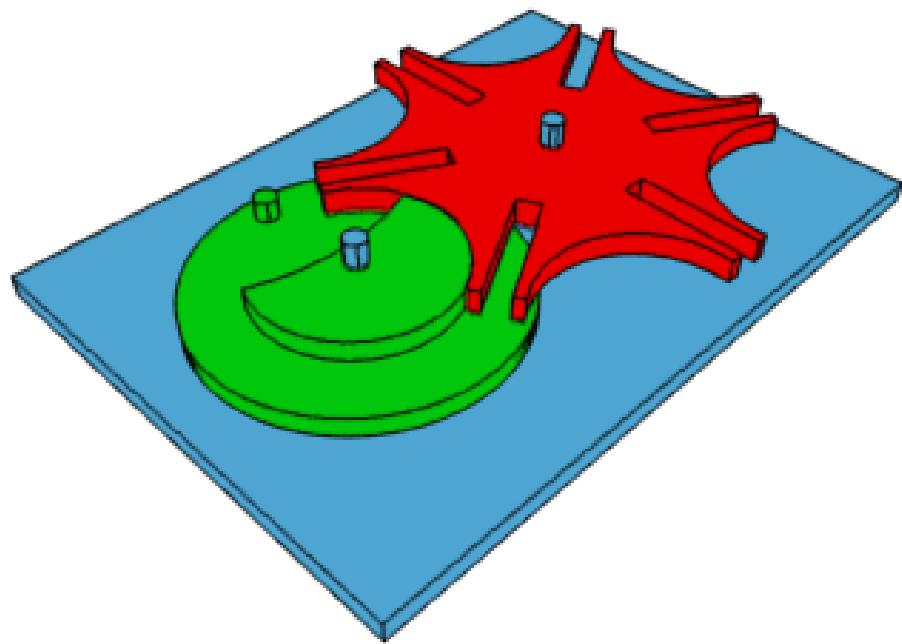
Theo Jansen Linkage



Theo Jansen Linkage made at ITU



Geneva drive



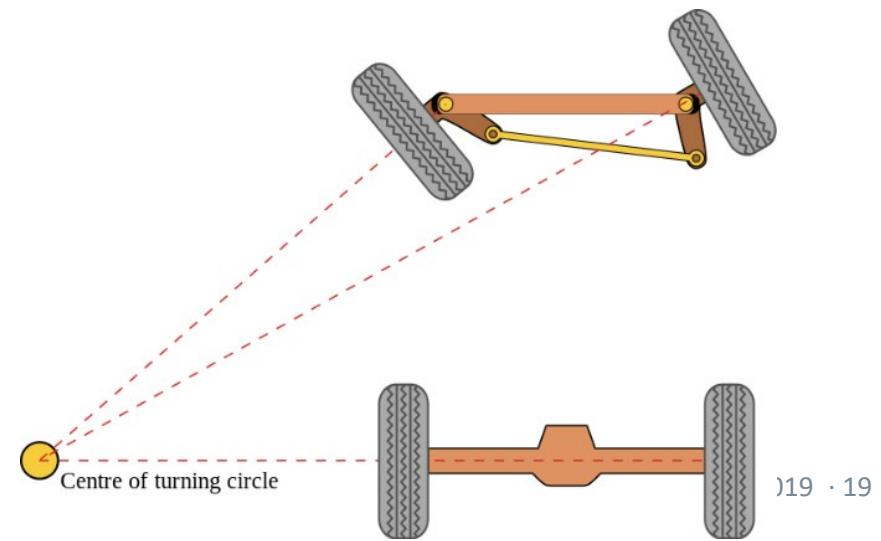
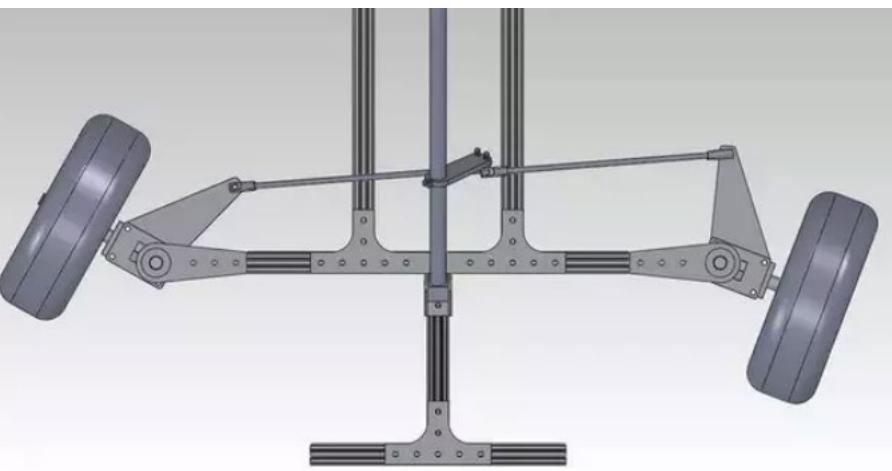
And many more...



EEZYbotARM
MK2



daGHIzmo
2k16



19 · 19

Task I: Test some linkages

Option 1:

Build some 4 bar linkages with Lego parts

Option2:

Check the behaviour of a 4 bar linkage

<http://dynref.engr.illinois.edu/aml.html#aml-sj>

Option 3:

Check Theo Jansen linkage

<http://www.mekanizmalar.com/theo-jansen.html>

Option 4:

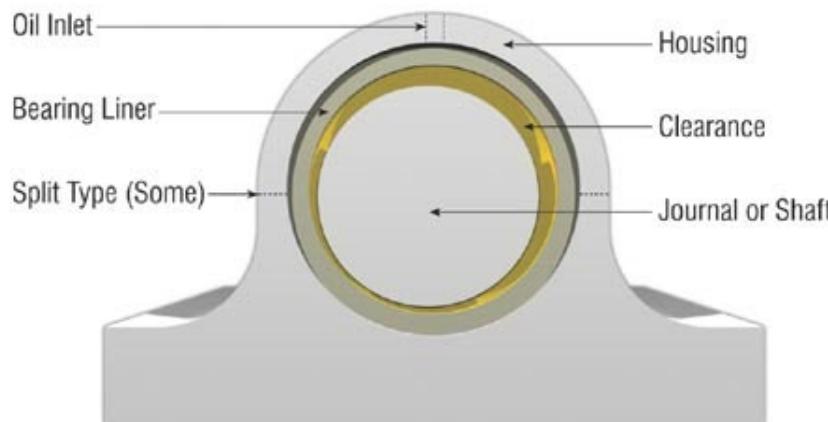
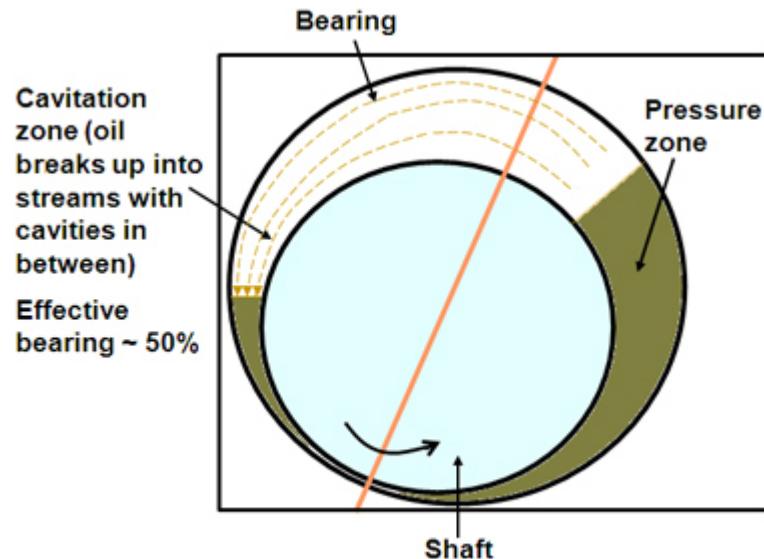
Look “linkage” up in Thingiverse

Bearings and guides

Plain bearings

Simplest bearing
No rolling elements
Low friction
Plastic
Bronze

Compact
Lightweight
Support high loads
Cheap

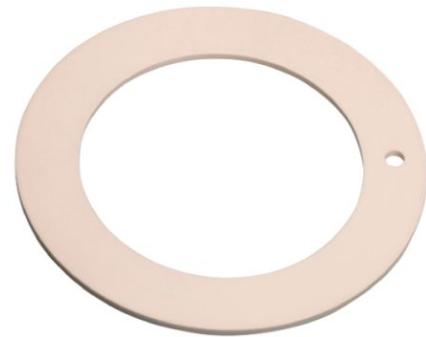
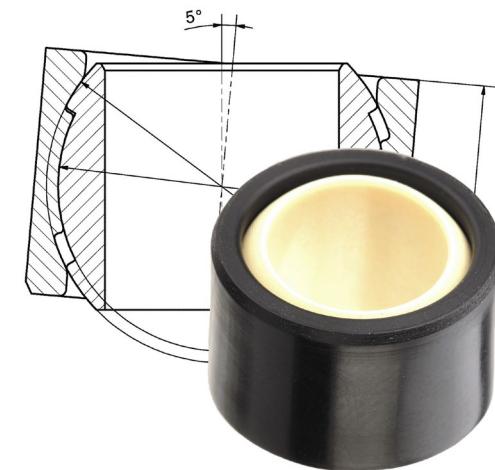


Common Journal Bearing Components

- Housing
- Bearing liner
- Segment (split type)
- Oil inlet
- Drain
- Journal

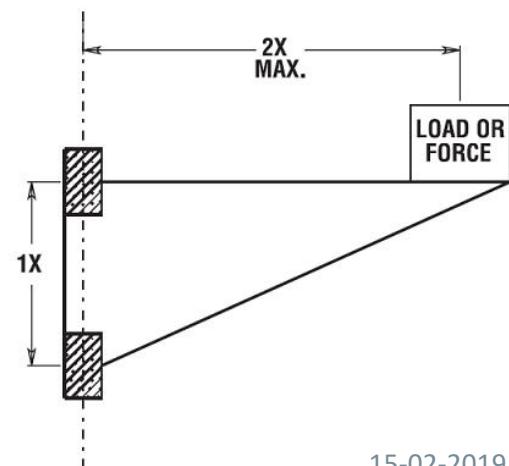
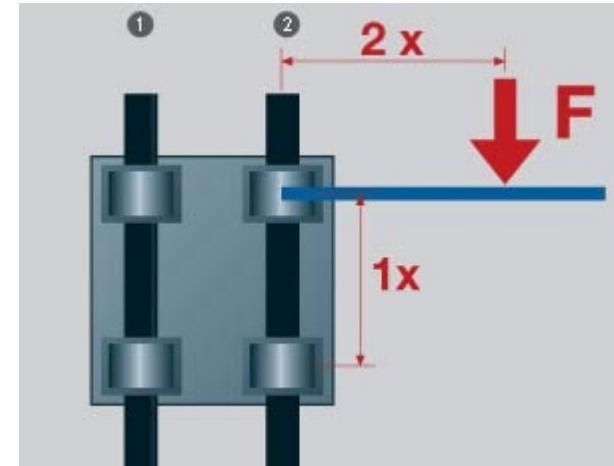
Figure 2. Plain Bearings (Journal Bearings)

Plain bearings



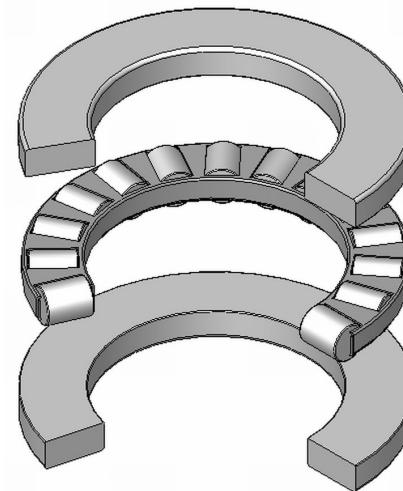
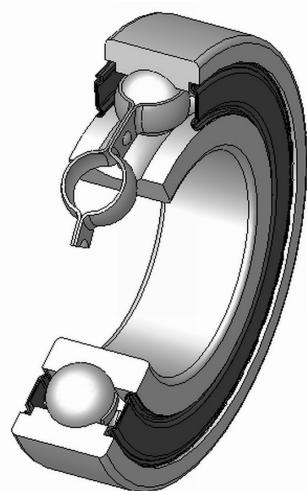
Plain bearings- Rule 1:2

if either the drive force or applied load force are a greater distance than twice the bearing length, then a binding or chattering of the system can occur.



Rolling bearings

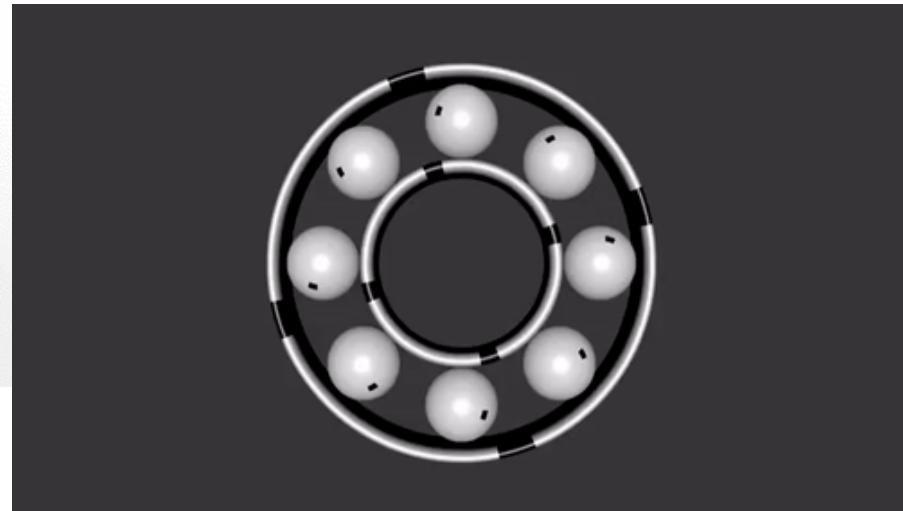
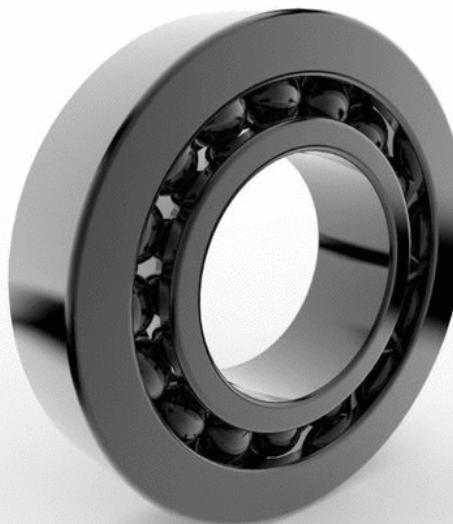
Almost no friction
High loads
Require lubrication
More expensive



Radial
bearing

Thrust
bearing

Linear
bearing

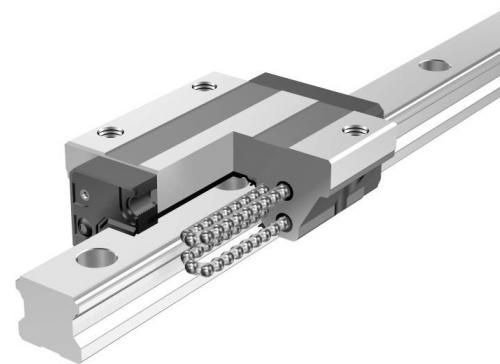


Linear guides

Using plain bearings:



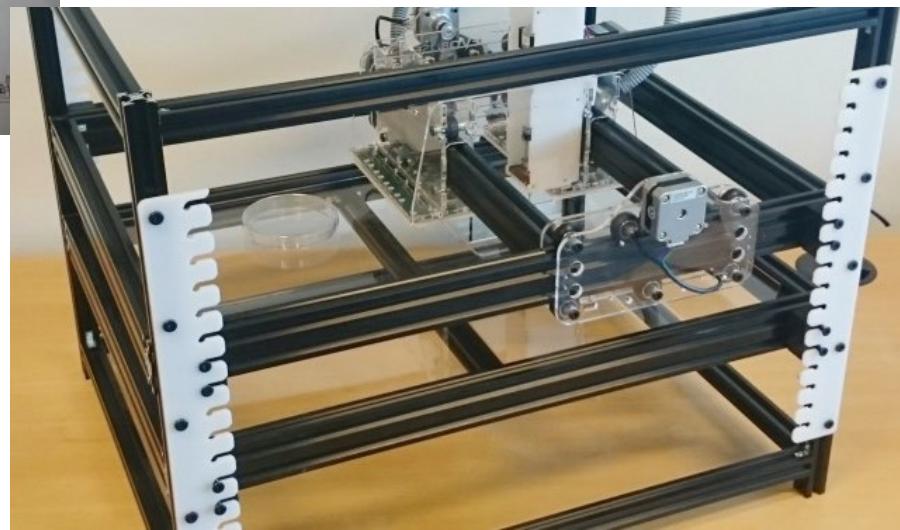
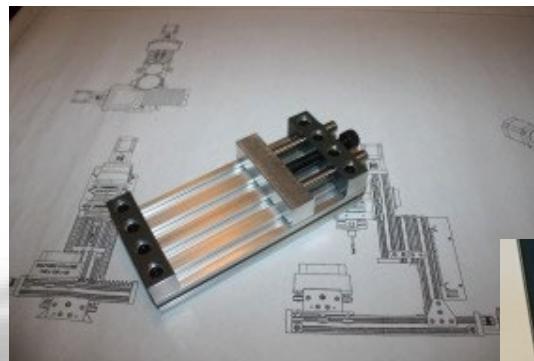
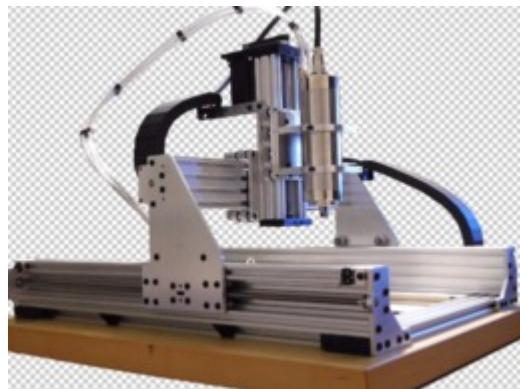
Using rolling bearings:



Linear guides: V-slot



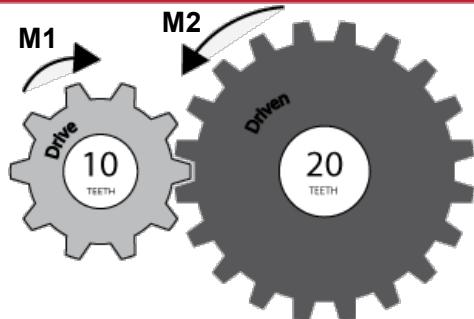
Linear guides: V- slot



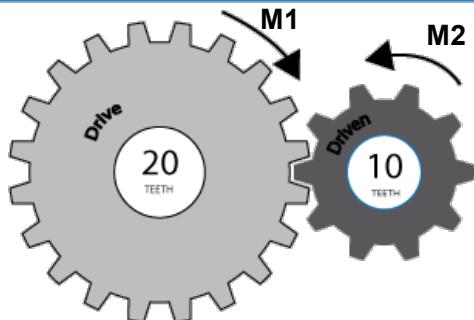
Power Transmission (forces)

Gears

Gear reduction occurs when the drive gear is smaller or has fewer teeth than the driven gear.



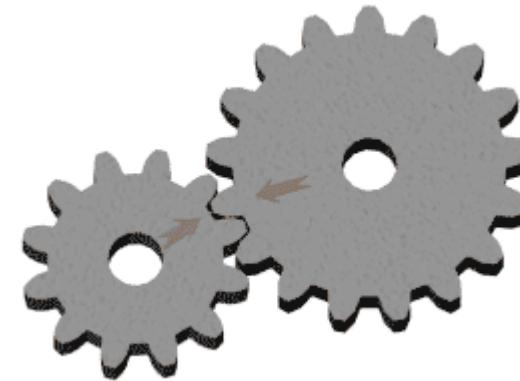
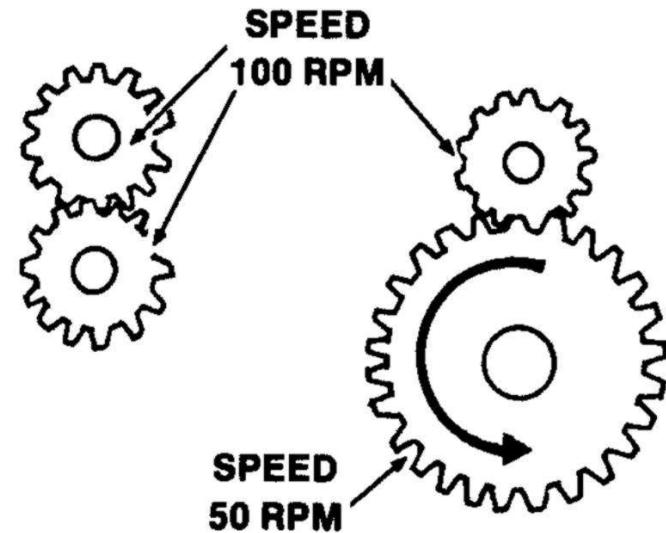
Overdrive occurs when the drive gear is larger or has more teeth than the driven gear.



$$\text{Gear ratio} = \frac{\text{Teeth output gear}}{\text{Teeth input gear}}$$

RATIO 1 TO 1

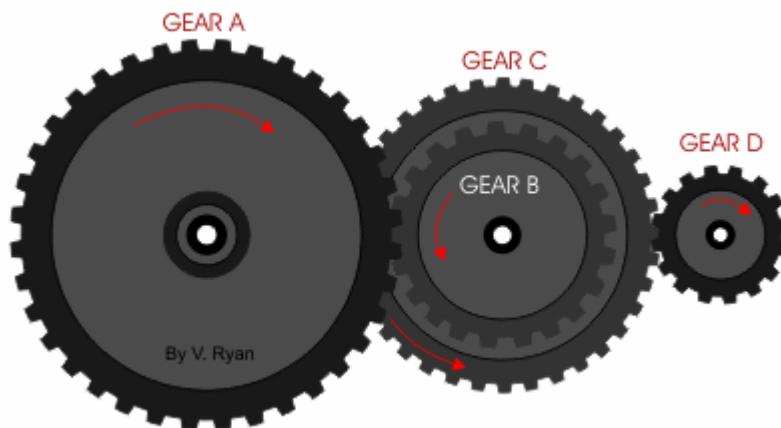
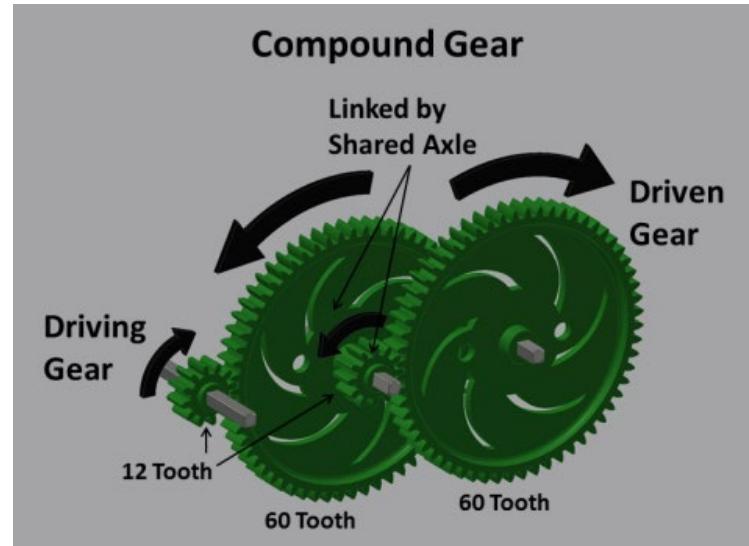
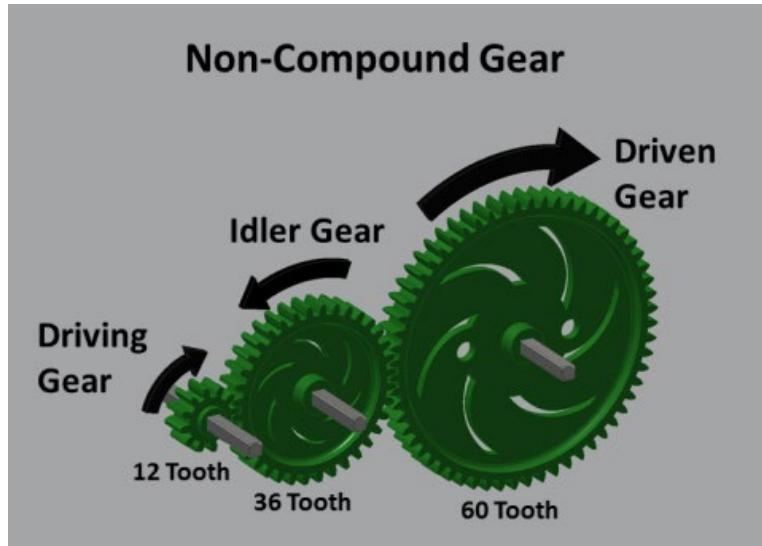
RATIO 2 TO 1



$$M2 = \text{Gear ratio} * M1$$

$$\text{Speed2} = \frac{1}{\text{Gear ratio}} * \text{Speed1}$$

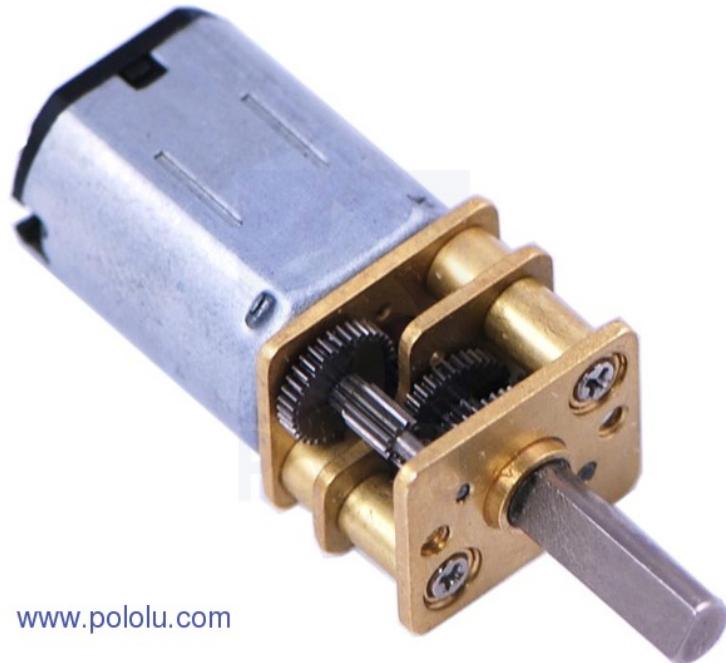
Compound Gears



Compound Gear Ratio = Reduction 1 x Reduction 2

$$\text{Compound Gear Ratio} = (60 / 12) \times (60 / 12) = (5/1) \times (5/1) = 25/1$$

DC motor + reduction



www.pololu.com

Motor Type	Stall Current @ 6 V	No-Load Speed @ 6 V	Approximate Stall Torque @ 6 V	Single-Shaft (Gearbox Only)
high-power, carbon brushes (HPCB)	1600 mA	3000 RPM	4 oz-in	10:1 HPCB
		1000 RPM	9 oz-in	30:1 HPCB
		625 RPM	15 oz-in	50:1 HPCB
		400 RPM	22 oz-in	75:1 HPCB
		320 RPM	30 oz-in	100:1 HPCB
		200 RPM	40 oz-in	150:1 HPCB
		140 RPM	50 oz-in	210:1 HPCB
		120 RPM	60 oz-in	250:1 HPCB
		100 RPM	70 oz-in	298:1 HPCB
		32 RPM	125 oz-in	1000:1 HPCB



Pololu

Types of Gears



Spur Gear



Helical Gear



Double Helical Gear
(Herringbone Gear)



Spiral Bevel Gear



Miter Gear



Straight Bevel Gear



Internal Gear

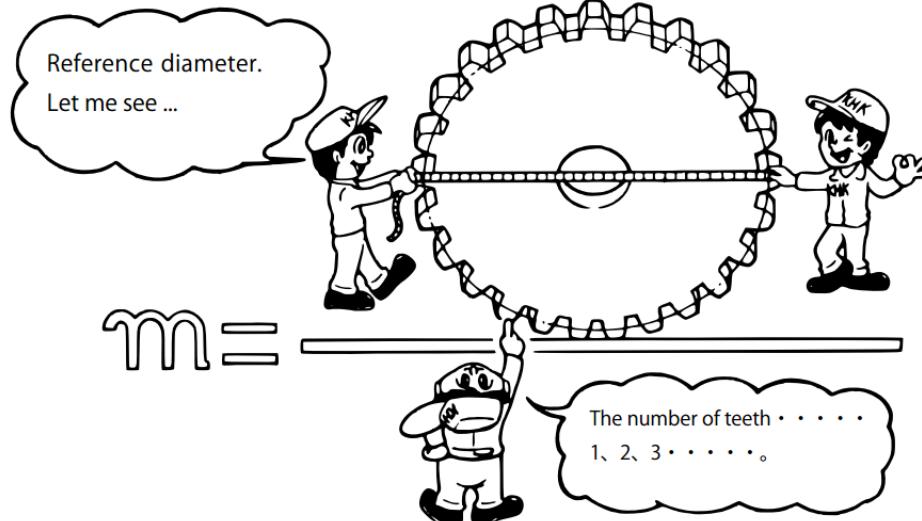


Worm Gear



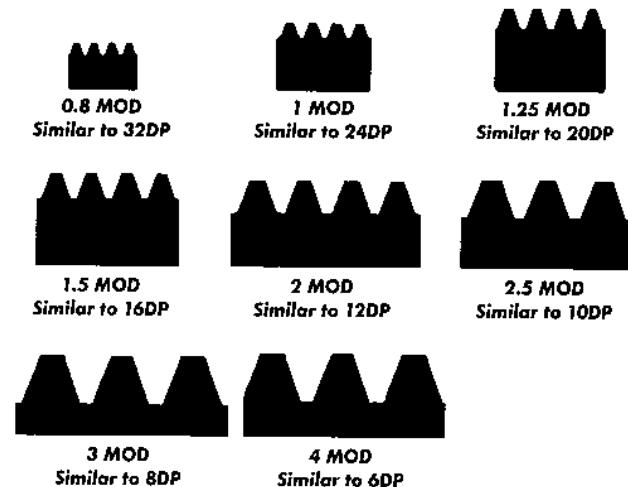
Rack and Pinion

The Module of a Gear



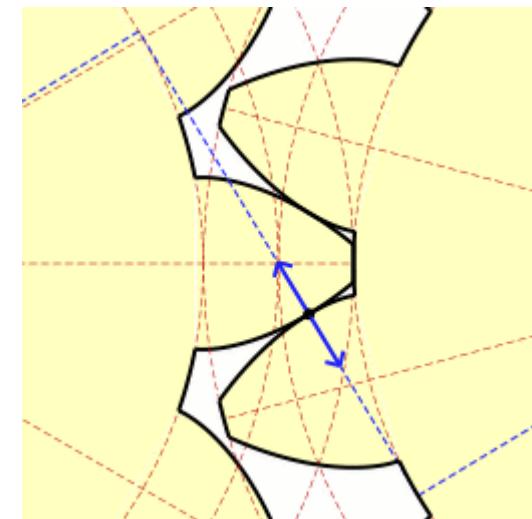
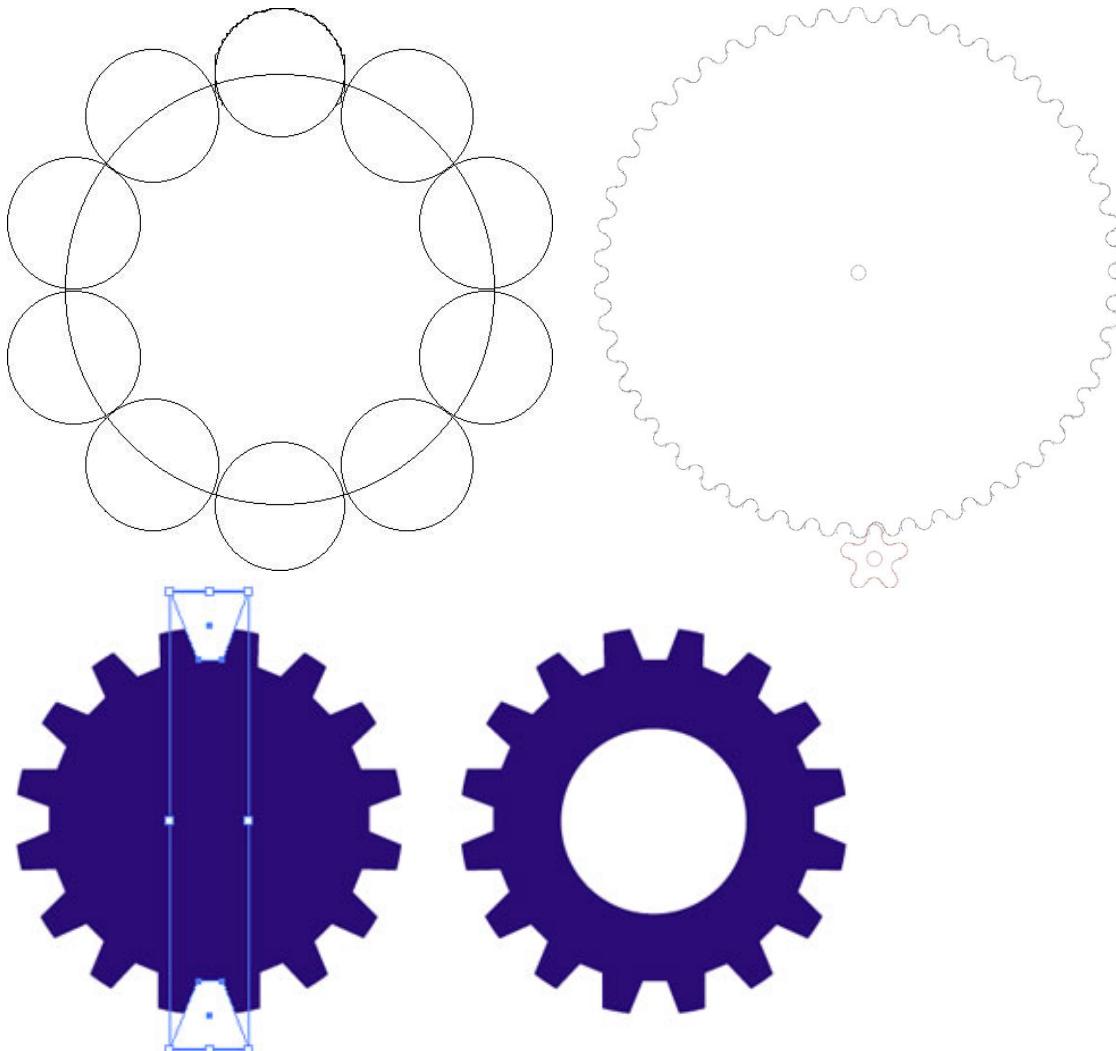
Gears only work with gears of
the same module!

Gear of module < 1 are difficult to laser cut / 3d print!



Gears – Tooth profile

There is a plugin to create gears in Fusion 360!

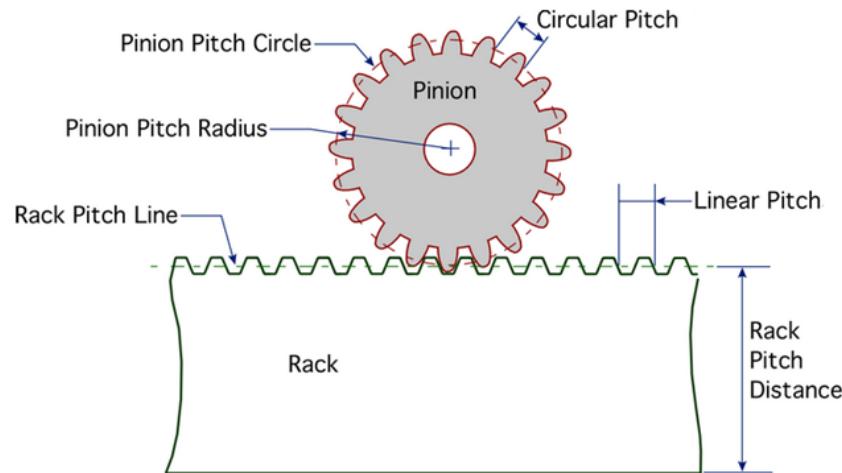
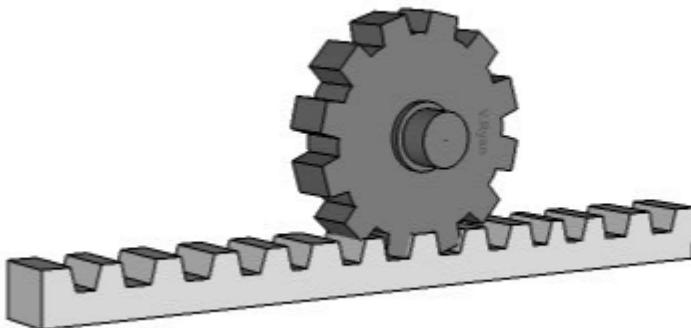


“Real” gears

Pinion and Racks



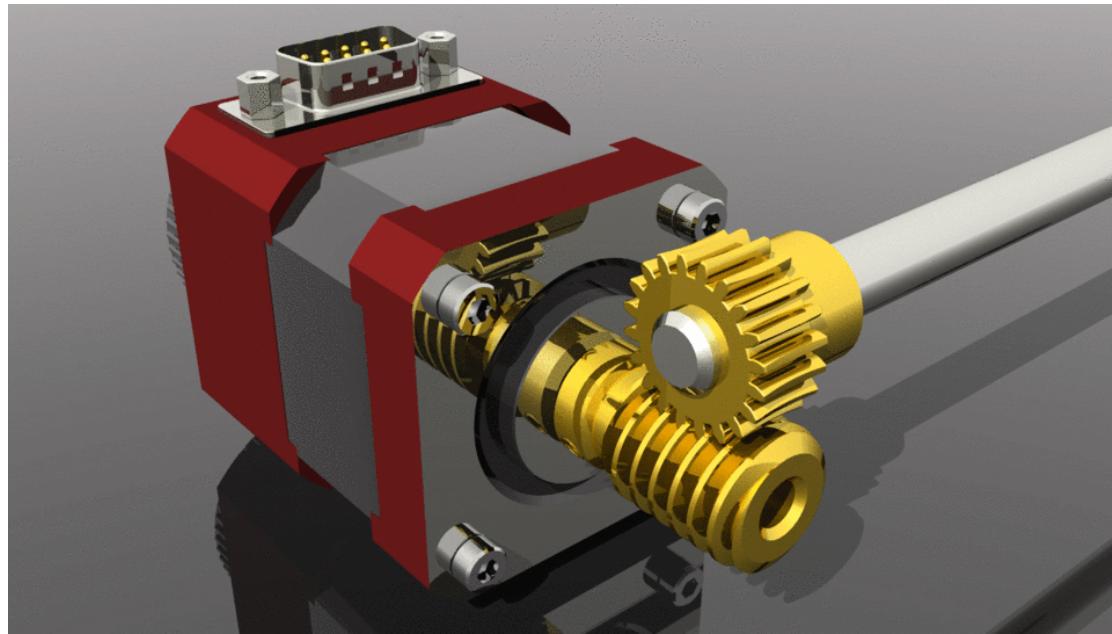
Translate
turning motion into linear motion
linear motion into rotational motion



Endless gear or Worm gear

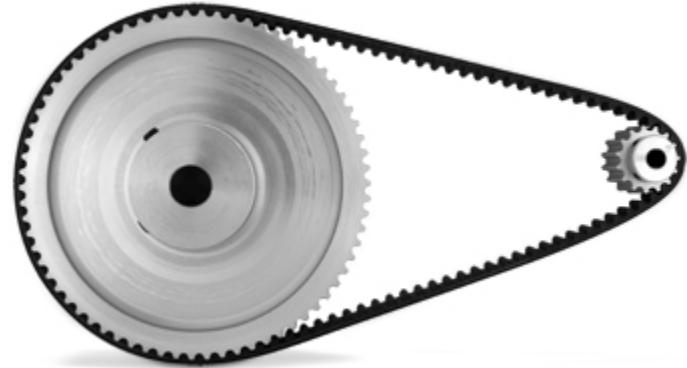
Translate turning motion
into linear motion

Precise and accurate
linear motion
High reduction (slow)
Self-locking
Not very efficient



Power transmission – Belts

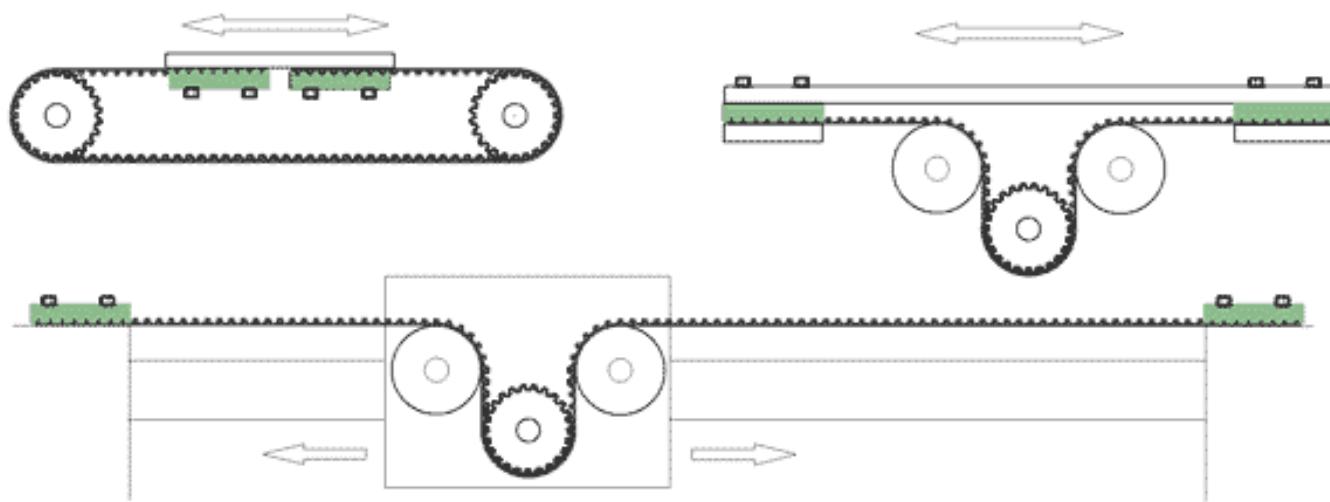
Loop of flexible material
Links 2 or more pulleys



Rotational movement

Lightweight
Cheap
Easy

Linear movement



Power transmission – Lead screw

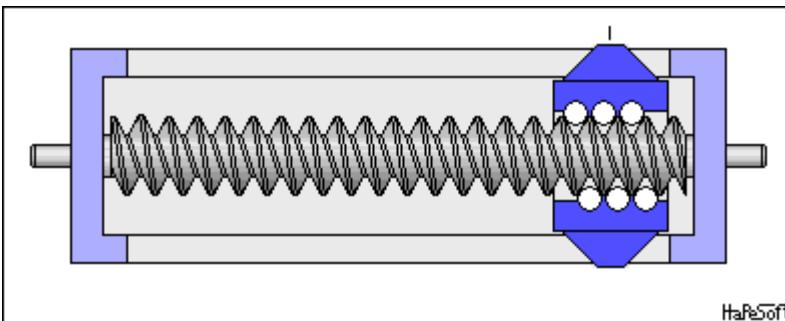
Translate turning motion into linear motion

Same principle as screws and nut (but larger pitch)

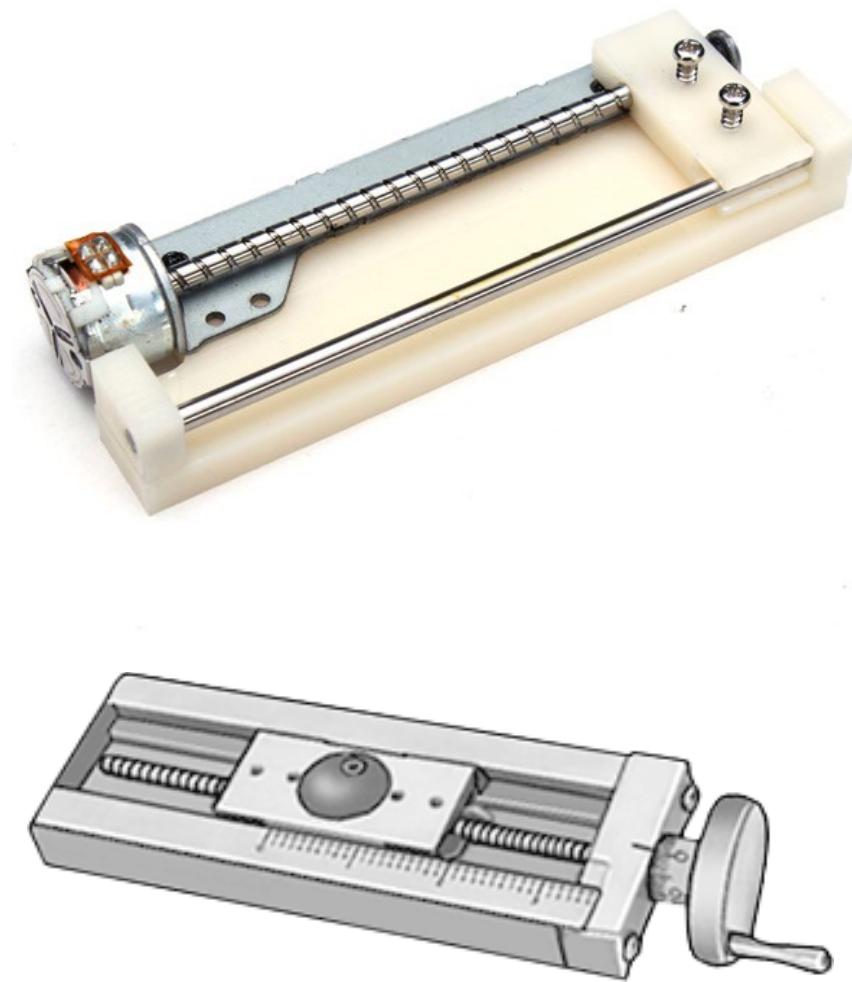
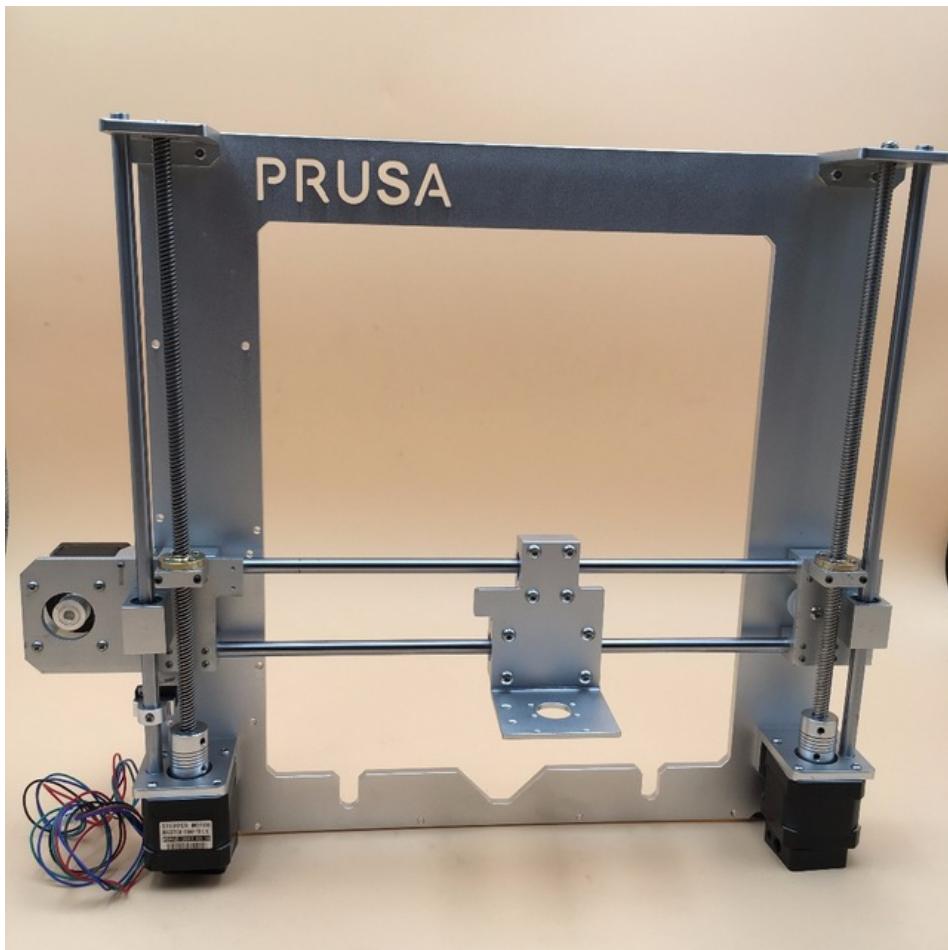
Precise and accurate linear motion

Self-locking

Not very efficient



Lead screw – Applications



Some mechanisms in action



Some mechanisms in action II



Task 2:

Test some power transmission devices with Lego:

Gears

Endless screw + gear

Pinion and rack

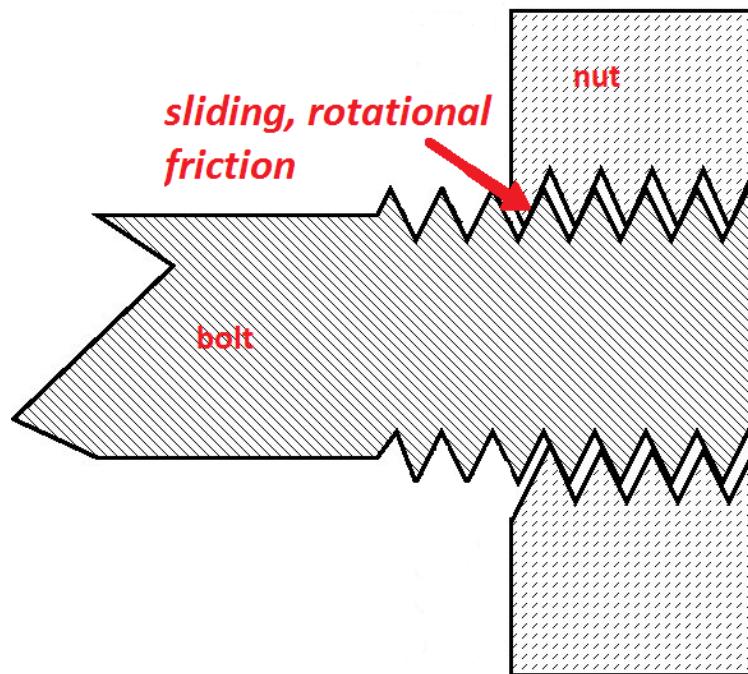
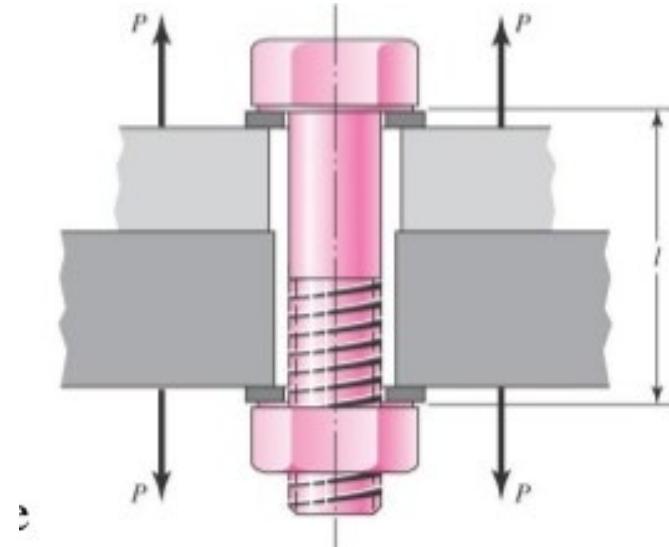


<https://www.youtube.com/watch?v=BZIkTLrnLKw>

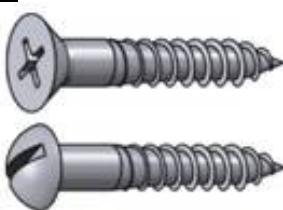
Fasteners

Screws

a solid profile wrapped around a rod or nail



Types of screws



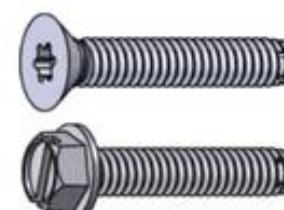
Wood Screws

Screws with a smooth shank and tapered point for use in wood. Abbreviated WS.



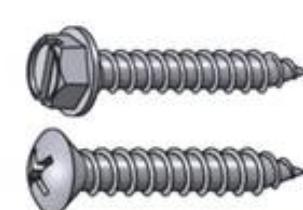
Machine Screws

Screws with threads for use with a nut or tapped hole. Abbreviated MS.



Thread Cutting Machine Screws

Machine screws with a thread cutting (self tapping) point.



Sheet Metal Screws

Fully threaded screws with a point for use in sheet metal. Abbreviated SMS.



Self Drilling SMS

A sheet metal screw with a self drilling point.



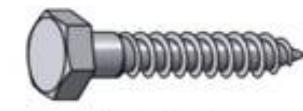
Hex Bolts

Bolts with a hexagonal head with threads for use with a nut or tapped hole. Abbreviated HHMB or HXBT.



Carriage Bolts

Bolts with a smooth rounded head that has a small square section underneath.



Lag Bolts

Bolts with a wood thread and pointed tip. Abbreviated Lag.



Socket Screws

Socket screws, also known as Allen Head, are fastened with a hex Allen wrench.



Set Screws

Machine screws with no head for screwing all the way into threaded holes.



Eye Bolts

A bolt with a circular ring on the head end. Used for attaching a rope or chain.



Eye Lags

Similar to an eye bolt but with wood threads instead of machine thread.



J-Bolts

J shaped bolts are used for tie-downs or as an open eye bolt.



U-Bolts

Bolts in U shape for attaching to pipe or other round surfaces. Also available with a square bend.



Shoulder Bolts

Shoulder bolts (also known as stripper bolts) are used to create a pivot point.

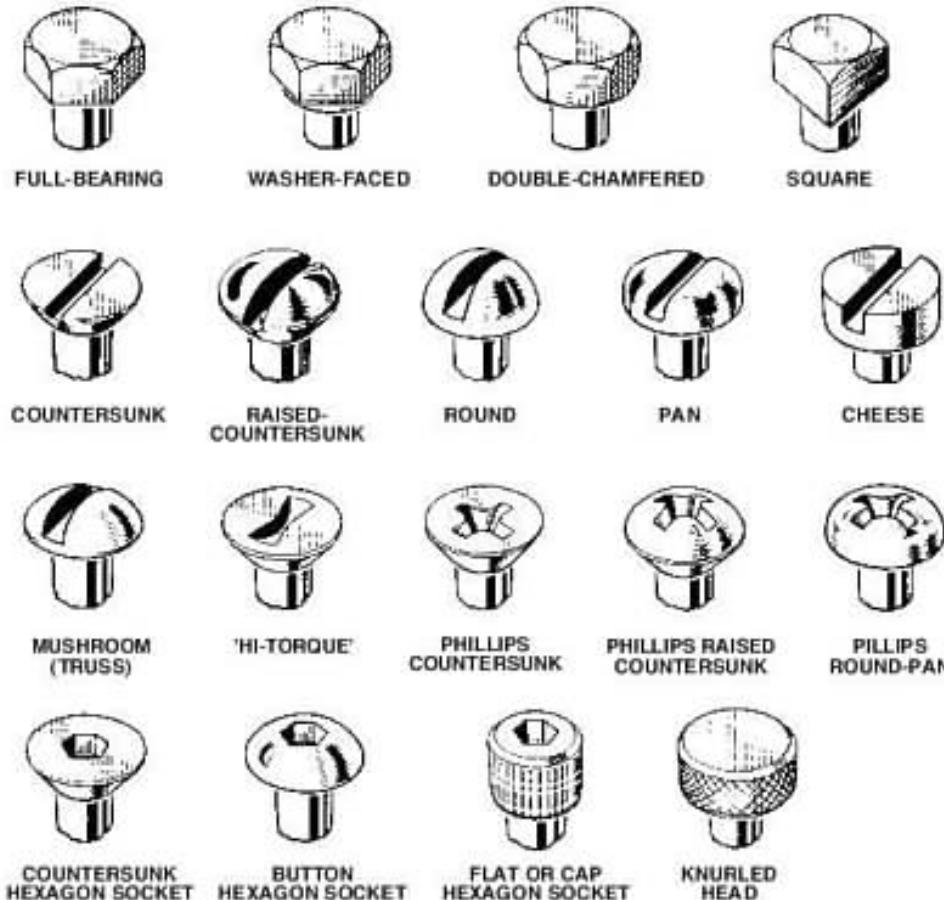


Elevator Bolts

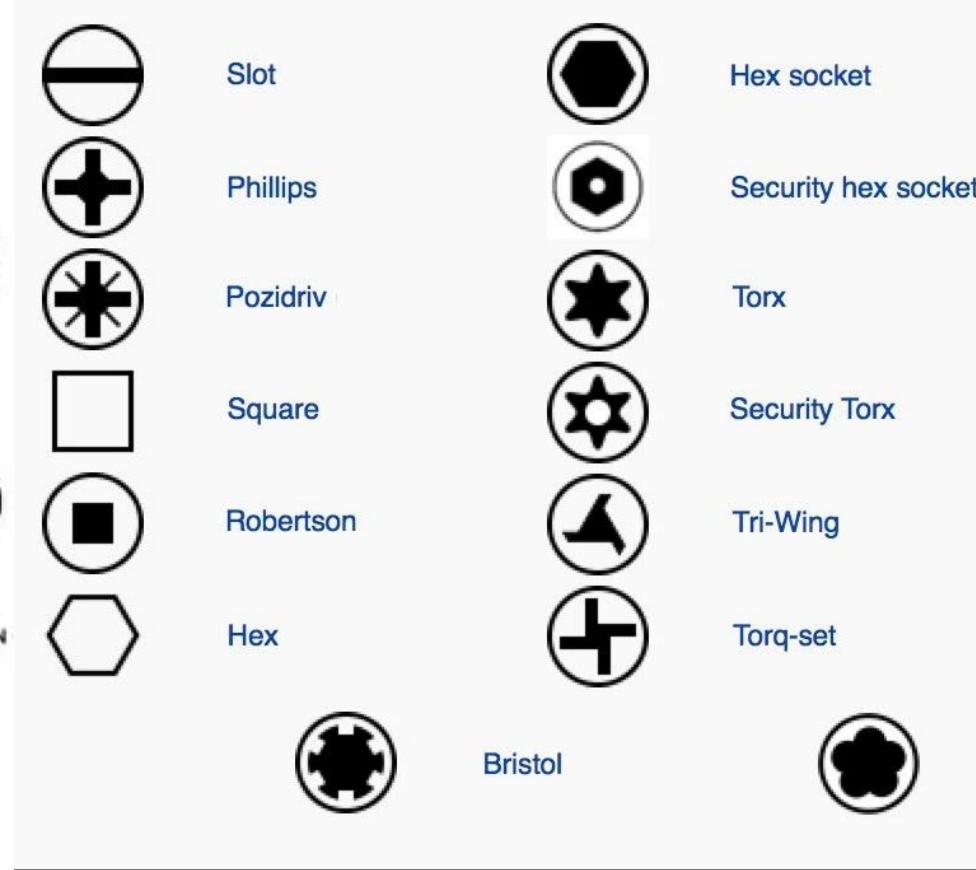
Elevator bolts are often used in conveyor systems. They have a large, flat head.

Screws- Heads and Screw drives

Heads

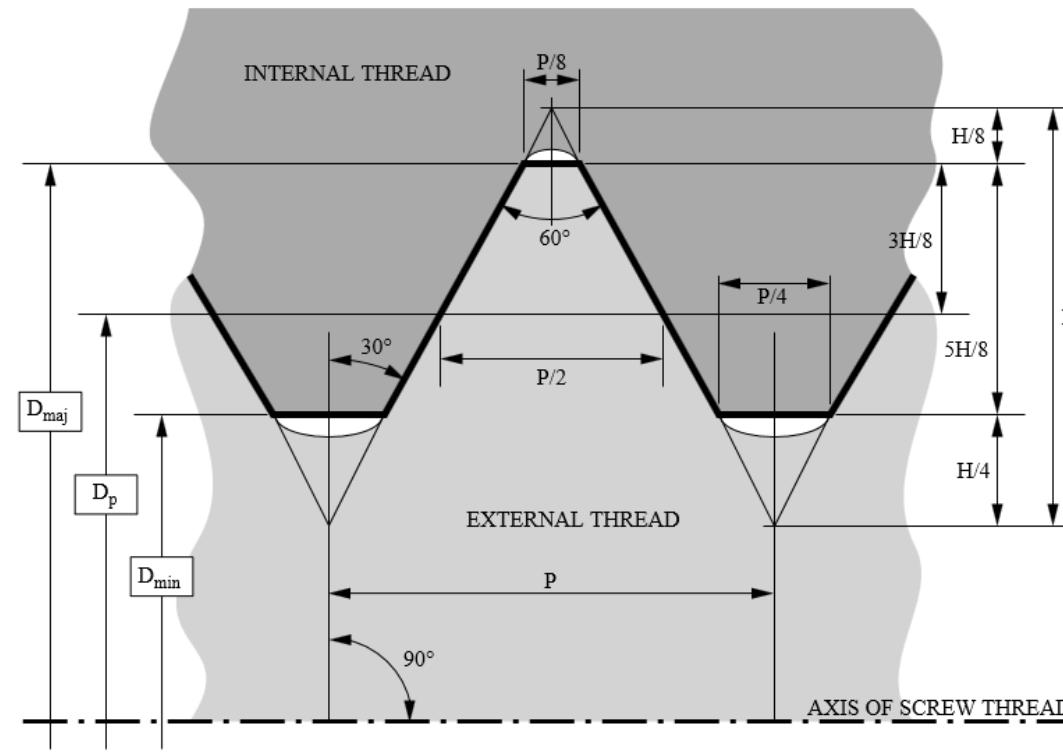


Screw drives



Machine Screws

Standards: Metric UNC (Imperial)

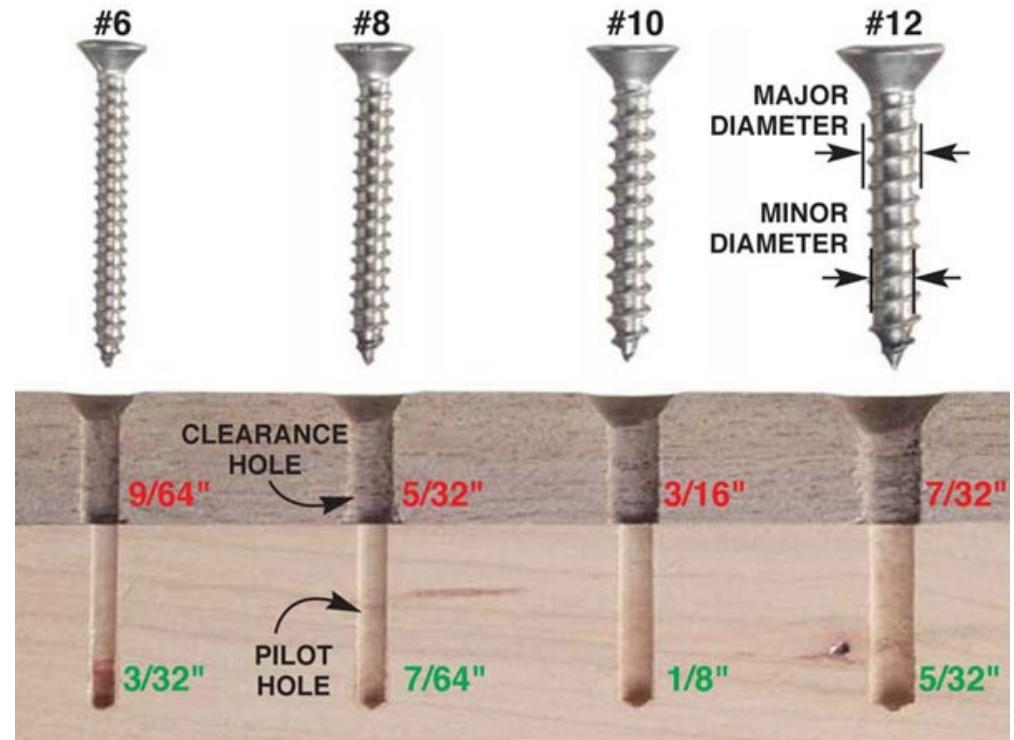
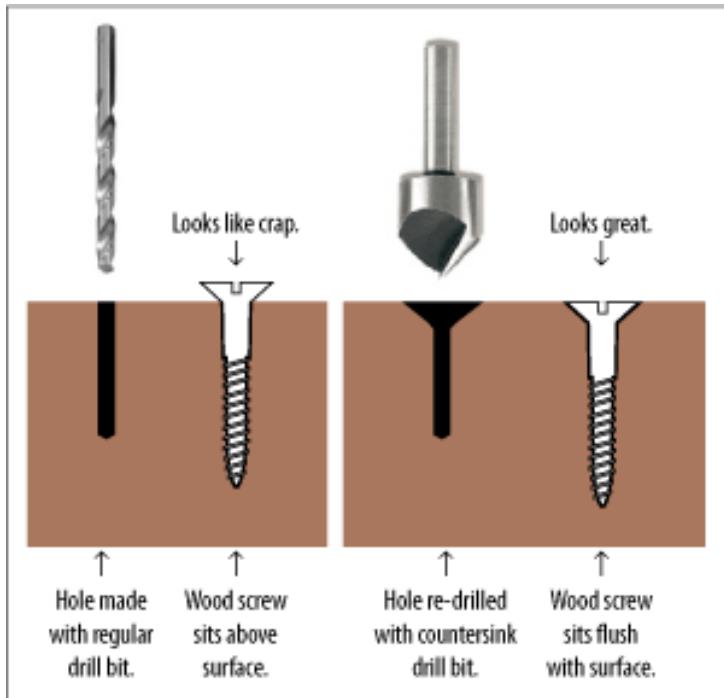


ISO 262 selected sizes for screws, bolts and nuts

Nominal diameter <i>D</i> (mm)		Pitch <i>P</i> (mm)		Nominal diameter <i>D</i> (mm)		Pitch <i>P</i> (mm)	
1st choice	2nd choice	Coarse	Fine	1st choice	2nd choice	Coarse	Fine
1		0.25	0.2	16		2	1.5
1.2		0.25	0.2		18	2.5	2 or 1.5
	1.4	0.3	0.2	20		2.5	2 or 1.5
1.6		0.35	0.2		22	2.5	2 or 1.5
	1.8	0.35	0.2	24		3	2
2		0.4	0.25		27	3	2
2.5		0.45	0.35	30		3.5	2
3		0.5	0.35		33	3.5	2
	3.5	0.6	0.35	36		4	3
4		0.7	0.5		39	4	3
5		0.8	0.5	42		4.5	3
6		1	0.75		45	4.5	3
	7	1	0.75	48		5	3
8		1.25	1 or 0.75		52	5	4
10		1.5	1.25 or 1	56		5.5	4
12		1.75	1.5 or 1.25		60	5.5	4
	14	2	1.5	64		6	4

Wood Screws

Self-tapping
Bigger pitch than Metric screws



Defining Screws

Minimum: Type of thread and length

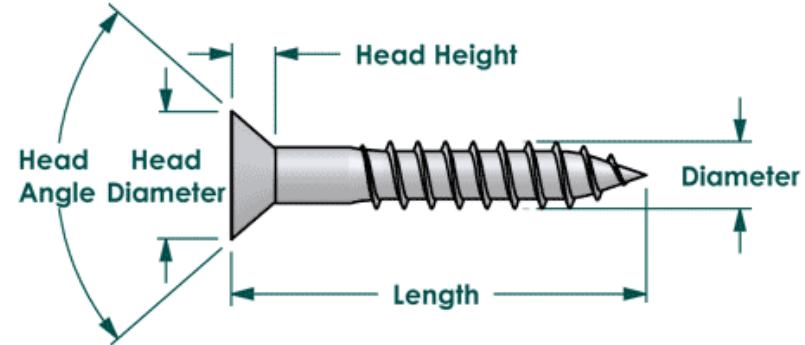
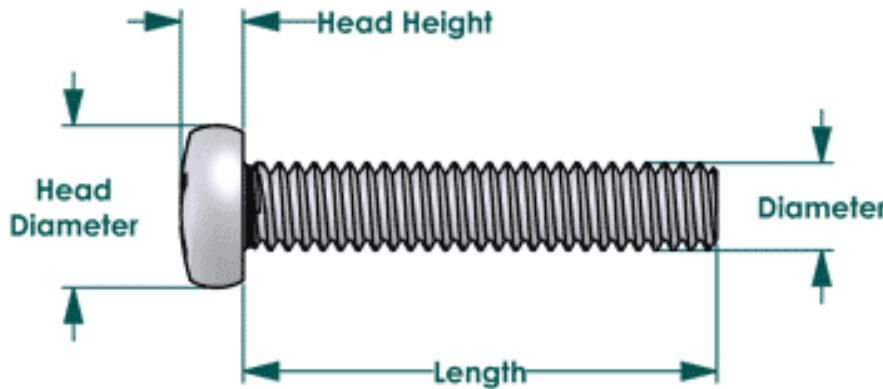
Examples:

M5x30

M3x20

#8-32x1^{``} (Imperial screw, avoid them)

Optional: Type of head, screw drive



Thread rods

“Infinite” screws

Cut them to appropriate lengths

Can be used as a cheap lead screw

Very small pitch (slow but
accurate movements)

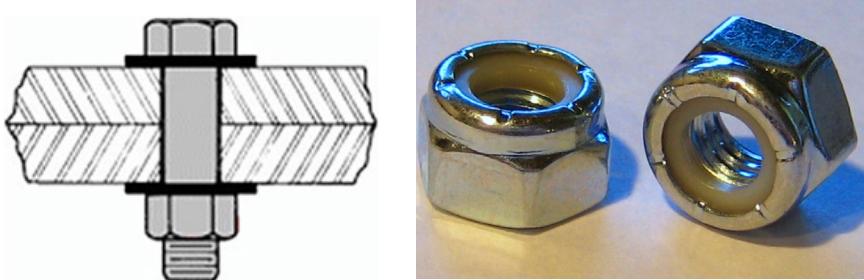


Nuts, inserts and tapping

Nyloc

Nuts

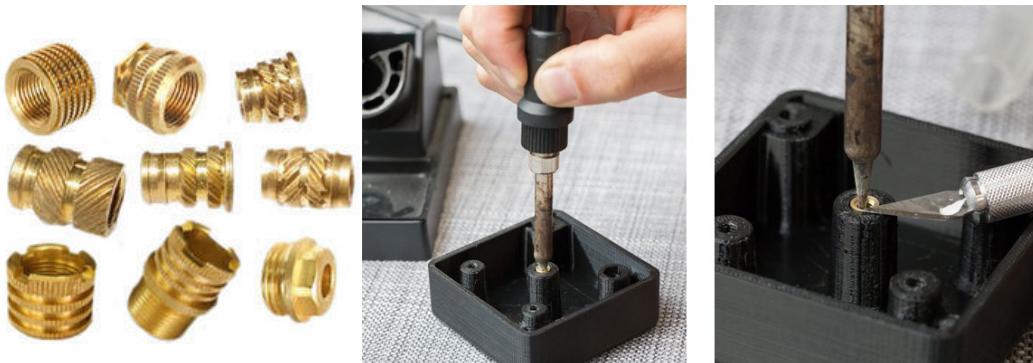
Nyloc nuts to avoid loosening



Inserts

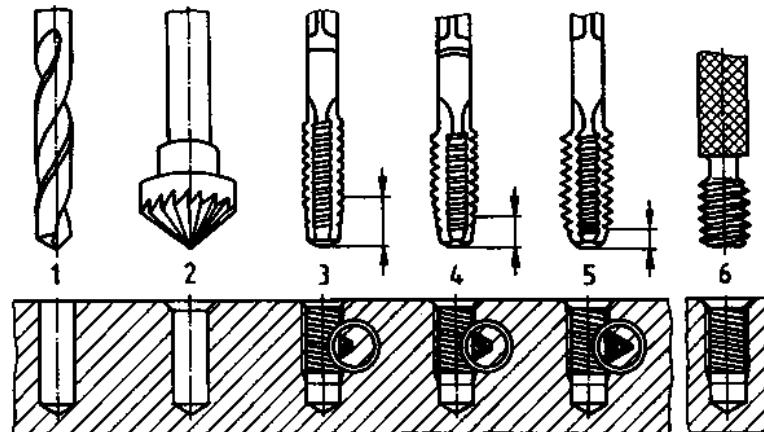
Premade thread

Attached them to a part



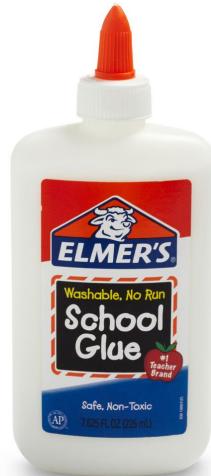
Tapping

Create a thread on a hole



Fasteners – Adhesives

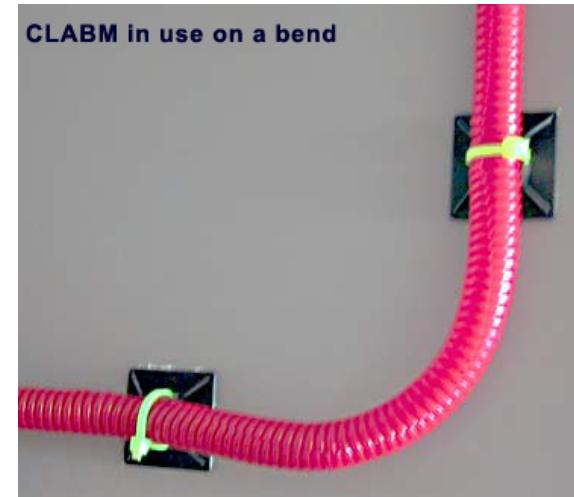
Hot glue
Glue
Glue stick
Tape
Double sided tape



Fasteners – Cable ties



CLABM in use on a bend



Mandatory activity

Finish the two proposed tasks:

Check different linkages

Test power transmission with LEGO

Design a mechanism in Fusion 360:

Add joints to simulate the movement

Add contact sets if needed

Groups of 3 members:

3D print/laser cut it (gripper for robot)

Ideas:

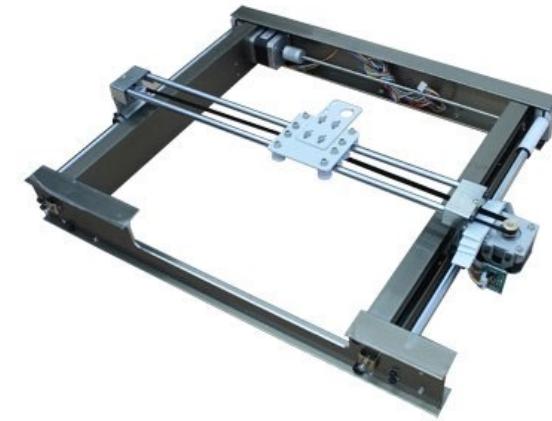
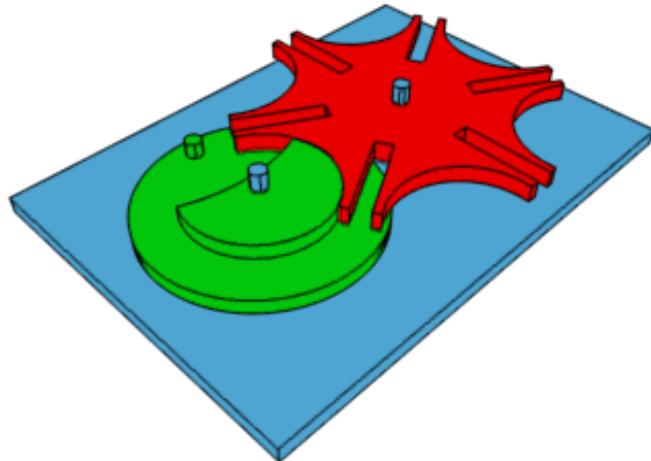
Gripper in front of the robot

Theo Jansen mechanism

Gear reduction

Geneva drive

XY platform



What do we have in stock?

V-slot system (aluminium profiles, wheels, etc.)

8 and 3mm rods

3mm plain bearings

5 and 8mm rolling bearings

Pulleys and belts (GT2)

Thread rod (3, 4, 5, 8)

8mm lead screw

And gears, racks?

A few, but try to laser cut/3D print them

Other elements:

If cheap, we can buy them. Ask first!

Resources - Design

Designing gears:

<http://www.learningfusion360.com/lesson-4-modelling-a-gear/>

<https://www.desktopmakes.com/single-post/2017/05/04/The-Easy-Way-to-Design-Gears-in-Fusion-360>

<http://www.instructables.com/id/How-To-3D-Printable-Bevel-Gears-Fusion-360/>

<http://www.instructables.com/id/How-to-make-gears-easily/>

V-Slot:

<http://openbuilds.org/>

Models of parts:

<https://www.tracepartsonline.net>

Resources – Shops (with 3d models too)

RS (Distributor):

<http://uk.rs-online.com/web/>

TME (Distributor): :

www.tme.eu/

V-Slot (V-Slot system and mechanics):

<http://openbuildspartstore.com/>

Igus (Bearings and guides):

www.igus.com

SKF (Bearings and guides): :

www.skf.com

Ebay (cheap parts):

www.ebay.com

Ready?

Let's design!

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