

Protocol description

- Client is Prover
- Server is Verifier

We have a group $\langle g \rangle$ whose order is n . Secrets are x_1 and x_2 , and public keys are $h_1 = g^{x_1}$ and $h_2 = g^{x_2}$.

Prover knowing x_1	Prover knowing x_2	Message	Verifier
$c_2, r_2, u_1 \in_R \mathbb{Z}_n$	$c_1, r_1, u_2 \in_R \mathbb{Z}_n$		
$a_1 = g^{u_1}$	$a_1 = g^{r_1} h^{-c_1}$		
$a_2 = g^{r_2} h_2^{-c_2}$	$a_2 = g^{u_2}$	$\xrightarrow{a_1, a_2}$	$c \in_R \mathbb{Z}_n$
		\xleftarrow{c}	
$c_1 = c - c_2 \pmod n$	$c_2 = c - c_1 \pmod n$		
$r_1 = u_1 + c_1 x_1 \pmod n$	$r_2 = u_2 + c_2 x_2 \pmod n$	$\xrightarrow{c_1, c_2, r_1, r_2}$	
			$\stackrel{?}{=} g^{r_1}$
			$a_1 h_1^{c_1}$
			$\stackrel{?}{=} g^{r_2}$
			$a_2 h_2^{c_2}$

When implemented properly, this results in the client proving to the server that it knows either x_1 or x_2 . Specifically, the client only needs to know a single one, and the server doesn't know which one.

It this passes, the server will then send the flag to the client.