MATH 3200 – Learning objectives to meet for Exam #1

The exam will cover Chapters 1 and 2 of the book, discussing mathematical statements and proof methods, respectively. While you *are* responsible for reading the book, the exam will not ask about definitions or concepts not covered in class or on homework.

What to be able to state

Basic definitions

Be able to give concise, complete, and precise definitions of each of the following terms.

- statement

- compound statement

- logically equivalent (compound) statements

- implication

- converse, inverse, contrapositive (of an implication)

- direct proof

- proof by contrapositive

- proof by contradiction

- even and odd integers, parity

- "a divides b", where a and b are integers

To give you some idea of what "complete" means here: If you are asked for the definition of **even**, it is *not* sufficient for you to write "$2k$" or "$n = 2k$." A satisfactory answer would be "An integer n is called *even* when $n = 2k$ for some integer k."

What to be able to do

You may be called on to perform any or all of the following tasks.

- Recognize examples and non-examples of mathematical statements

- Determine whether compound statements are true or false, given the truth values of the component statements

- Write out truth tables for compound mathematical statements

- Use truth tables for two compound statements to demonstrate that they are (or are not) logically equivalent

- Be able to negate mathematical statements, including compound statements involving quantifiers and connectives. Here the kind of negation you are expected to provide is one moving the "not" as far into the sentence as possible. You should be able to do this whether the initial statement is described in words or in symbols.

- Determine whether simple mathematical statements are true or false (e.g., $\forall x \in \mathbb{R}, \forall y \in \mathbb{R}, \ x - y < x + y$).

- Formulate proofs of statements involving parity, divisibility, and/or inequalities. (For inequality proofs, you will be provided with the list of rules.) Note that you may be required to determine yourself which proof method is appropriate. Your proofs should be logically correct and written in complete sentences; you can expect me to assess both aspects when assigning your grades.

What to expect on the exam

You can expect 5 (possibly multi-part) questions on the exam. These will include:

- at least one problem asking you to prove two mathematical statements are logically equivalent, by truth tables

- at least one problem asking you to prove a statement about even and odd numbers

- at least one problem assessing your negation skills