## ERRATA TO "DISTRIBUTION IN COPRIME RESIDUE CLASSES OF POLYNOMIALLY-DEFINED MULTIPLICATIVE FUNCTIONS"

In the published version of this paper, §6 contains an incorrect argument for the absolute irreducibility of F(x)F(y) - w. A corrected proof follows. The results of the paper remain unaffected.

Suppose that F(x)F(y) - w = U(x,y)V(x,y) for some  $U(x,y),V(x,y) \in \overline{\mathbb{F}}_{\ell}[x,y]$ . Then for each root  $\theta \in \overline{\mathbb{F}}_{\ell}$  of F, we find that  $-w = U(\theta,y)V(\theta,y)$ , and so in particular  $U(\theta,y)$  is constant. Thus, if we write

$$U(x,y) = \sum_{k>0} a_k(x)y^k,$$

with each  $a_k(x) \in \overline{\mathbb{F}}_{\ell}[x]$ , then  $a_k(\theta) = 0$  for each k > 0. Since F has no multiple roots over  $\overline{\mathbb{F}}_{\ell}$ , each such  $a_k(x)$  is forced to be a multiple of F(x), hence  $U(x,y) \equiv a_0(x) \pmod{F(x)}$ . A symmetric argument shows that  $V(x,y) \equiv b_0(y) \pmod{F(y)}$  for some  $b_0(y) \in \overline{\mathbb{F}}_{\ell}[y]$ , so that  $V(x,\theta) = b_0(\theta)$ . Consequently, for any root  $\theta \in \overline{\mathbb{F}}_{\ell}$  of F,

$$-w \equiv F(x)F(\theta) - w \equiv U(x,\theta)V(x,\theta) \equiv a_0(x)b_0(\theta) \pmod{F(x)},$$

which shows that  $U(x,y) \equiv a_0(x) \equiv c \pmod{F(x)}$  for some constant  $c \in \overline{\mathbb{F}}_{\ell}$ . But this forces  $c = U(\theta,\theta)$ , showing that F(x) divides  $U(x,y) - U(\theta,\theta)$ . By symmetry, so does F(y), and we obtain  $U(x,y) = U(\theta,\theta) + F(x)F(y)Q(x,y)$  for some  $Q(x,y) \in \overline{\mathbb{F}}_{\ell}[x,y]$ . Degree considerations now imply that for U(x,y) to divide F(x)F(y) - w, either Q(x,y) is a nonzero constant, in which case V(x,y) is constant, or Q(x,y) = 0, in which case U(x,y) is constant.

The arXiv version already includes this corrected argument.

<sup>&</sup>lt;sup>1</sup>In the published version, it was argued (incorrectly) that F(x), F(y) divide U(x,y) - U(0,0).