

Univariate Regression

Confidence Intervals

$$Var[y_i] = \hat{\sigma}^2 \left[1 + \frac{1}{n} + \frac{(X_i - \bar{X})^2}{S_{xx}} \right]$$

$$Var[\hat{y}_i] = \hat{\sigma}^2 \left[\frac{1}{n} + \frac{(X_i - \bar{X})^2}{S_{xx}} \right]$$

Hypothesis Testing

$$b_1 \sim t_{n-2}(\beta_1, \hat{\sigma}^2)$$

Properties of Estimators

$$s_{y \cdot x}^2 \sim \frac{\sum_{i=1}^n e_i^2}{n-2}$$

$$b_1 \sim N(\beta_1, \sigma^2 / S_{xx})$$

Parameter Estimates

$$b_1 = \frac{S_{xy}}{S_{xx}}$$

$$S_{xx} = \sum_{i=1}^n (x_i - \bar{x})^2$$

$$S_{xy} = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$b_0 = \bar{y} - b_1 * \bar{x}$$

Model Specification

$$Y_i = \beta_0 + \beta_1 \cdot X_i + \varepsilon_i$$

$$E[Y_i | X_i] = \beta_0 + \beta_1 \cdot X_i$$

$$\varepsilon_i \sim N(0, \sigma^2)$$

Anova

$$\frac{\overline{SS_{reg}}}{\overline{SS_{res}}} \sim F_{1, n-2}$$

$$r^2 = \frac{SS_{reg}}{SS_{total}}$$

$$SS_{reg} = b_1^2 \cdot S_{xx}$$

$$r \approx \text{Corr Coef.}$$