

```

Sys := {
  L'[t] == 10 (mL[t] - L[t]),
  Cl'[t] == 10 (mC[t] - Cl[t]),
  T'[t] == 10 (mT[t] - T[t]),
  mL'[t] ==  $\frac{10}{Cl[t]^2 + 1}$  - mL[t],
  mC'[t] ==  $\frac{10}{T[t]^2 + 1}$  - mC[t],
  mT'[t] ==  $\frac{10}{L[t]^2 + 1}$  - mT[t],
  L[0] == 1, Cl[0] == 0, T[0] == 0, mL[0] == mC[0] == mT[0] == 0}

```

Sys

```

{L'[t] == 10 (-L[t] + mL[t]), Cl'[t] == 10 (-Cl[t] + mC[t]),
  T'[t] == 10 (mT[t] - T[t]), mL'[t] ==  $\frac{10}{1 + Cl[t]^2}$  - mL[t], mC'[t] == -mC[t] +  $\frac{10}{1 + T[t]^2}$ ,
  mT'[t] ==  $\frac{10}{1 + L[t]^2}$  - mT[t], L[0] == 1, Cl[0] == 0, T[0] == 0, mL[0] == mC[0] == mT[0] == 0}

```

```

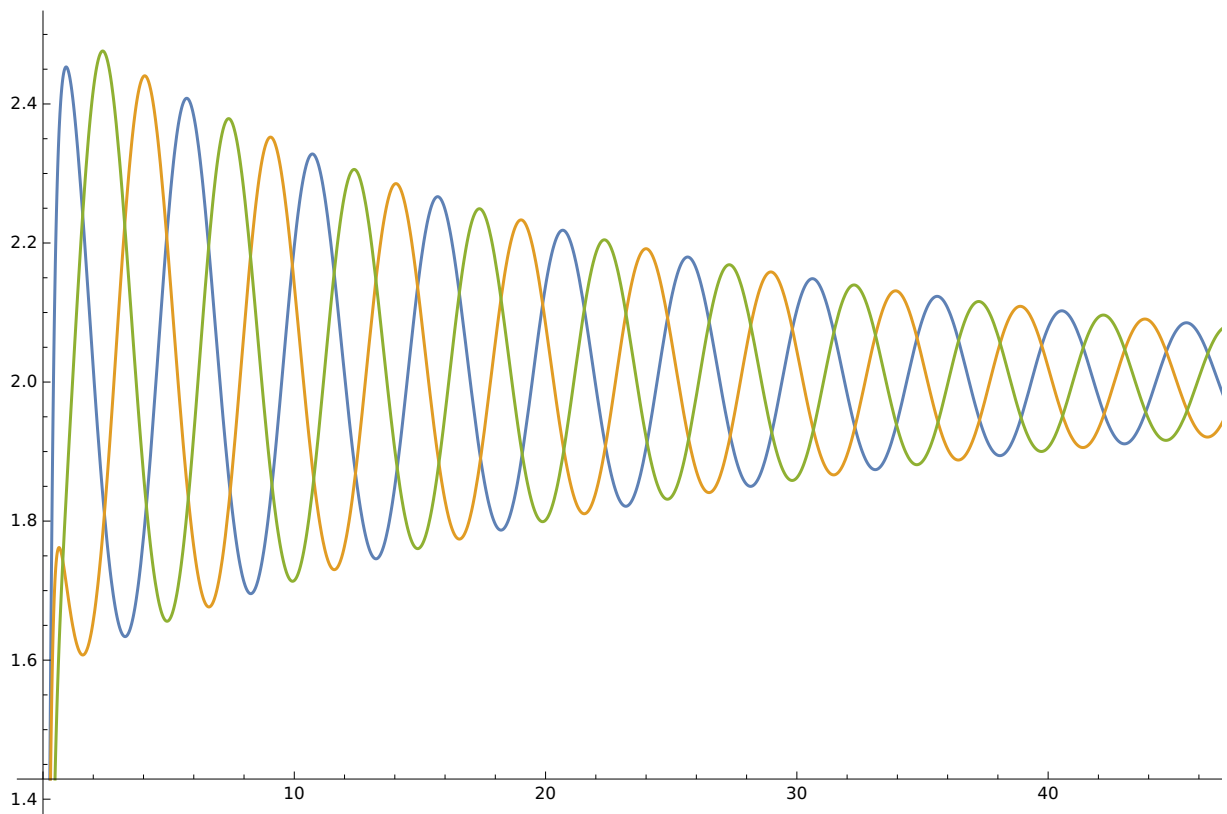
s := NDSolve[Sys,
  {Cl[t], L[t], mC[t], mL[t], mT[t], T[t], uC[t], uL[t], uT[t]}, {t, 0, 100, 0.0001}]

```

```

Plot[Evaluate[{Cl[t], L[t], T[t]} /. s], {t, 0, 50}]

```



```

Sys := {
  L'[t] == 10 (mL[t] - L[t]),
  Cl'[t] == 10 (mC[t] - Cl[t]),
  T'[t] == 10 (mT[t] - T[t]),
  mL'[t] == 10 uC[t] - mL[t],
  mC'[t] == 10 uT[t] - mC[t],
  mT'[t] == 10 uL[t] - mT[t],
  uL'[t] == -20 L[t] uL[t]^2 (mL[t] - L[t]),
  uC'[t] == -20 Cl[t] uC[t]^2 (mC[t] - Cl[t]),
  uT'[t] == -20 T[t] uT[t]^2 (mT[t] - T[t]),
  L[0] == 1,
  Cl[0] == 0,
  T[0] == 0,
  mL[0] == mC[0] == mT[0] == 0,
  uL[0] == 1/2,
  uC[0] == 1,
  uT[0] == 1
}

f[{L_, Cl_, T_, mL_, mC_, mT_, uL_, uC_, uT_}] := {
  10 (mL - L), 10 (mC - Cl), 10 (mT - T),
  10 uC - mL, 10 uT - mC, 10 uL - mT,
  -20 L * uL^2 * (mL - L), -20 Cl uC^2 (mC - Cl), -20 T uT^2 (mT - T)}

f[{L, Cl, T, mL, mC, mT, uL, uC, uT}]
{10 (-L + mL), 10 (-Cl + mC), 10 (mT - T), -mL + 10 uC, -mC + 10 uT,
 -mT + 10 uL, -20 L (-L + mL) uL^2, -20 Cl (-Cl + mC) uC^2, -20 (mT - T) T uT^2}

Sys := {y'[t] == f[y[t]], y[0] == {1, 0, 0, 0, 0, 0, 1/2, 1, 1}}
Sys
{y'[t] == f[y[t]], y[0] == {1, 0, 0, 0, 0, 0, 1/2, 1, 1}}

s := NDSolve[Sys, {y[t]}, {t, 0, 100, 0.0001}]
s

```

```

{{y[t] → InterpolatingFunction[

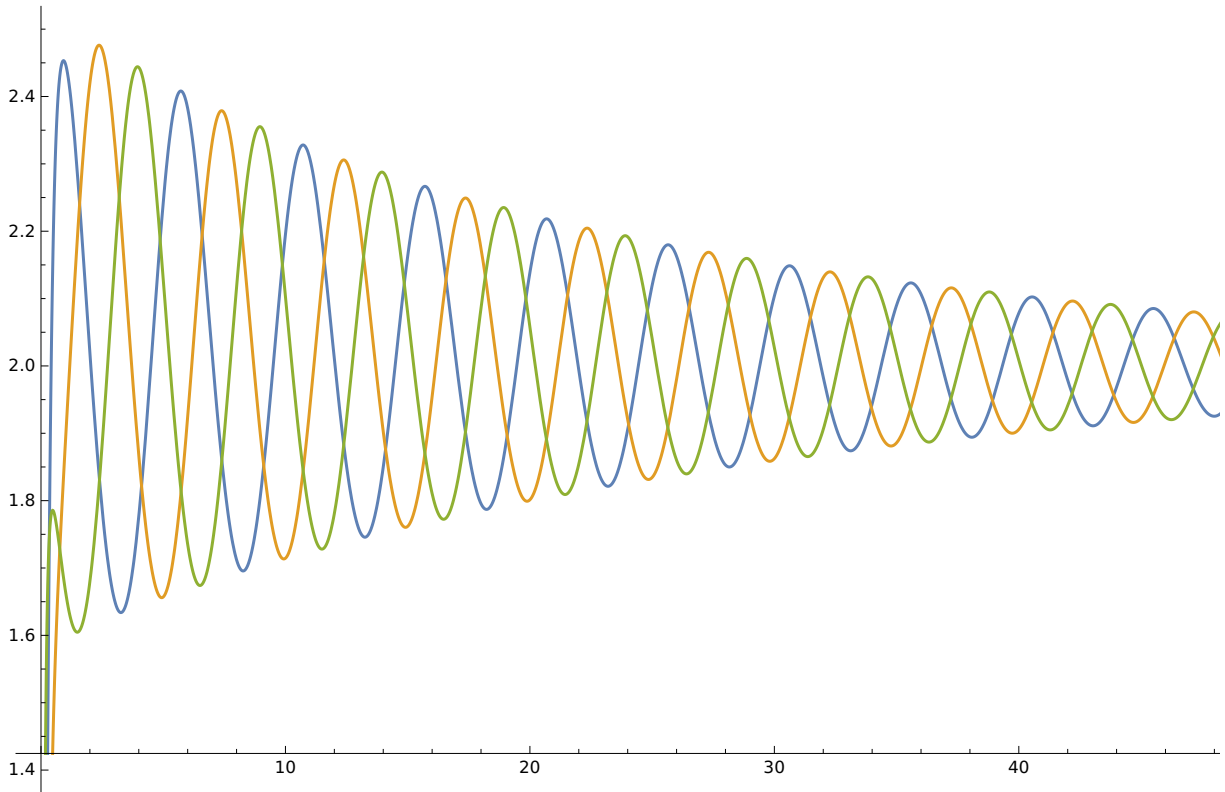
```



Domain: {{0., 100.}}
Output dimensions: {9}

```
][t]]}
```

```
Plot[Evaluate[Table[Indexd[y[t], i] /. s, {i, 2, 4}], {t, 0, 50}]]
```



```
Resolve[Exists[{x}, x^2 + b x + c == 0], Reals]
```

$$-b^2 + 4 c \leq 0$$

```
g[x_, y_, z_] := x^2 - 2 y + z^4
```

```
f[x_, y_, z_] := {2 x, 2 y, 3 z}
```

```
Lie[f_, g_, xs_] :=  $\nabla_{xs} g \cdot f$ 
```

```
Lie[f[x, y, z], g[x, y, z], {x, y, z}]
```

$$4 x^2 - 4 y + 12 z^4$$

```
xs := {L, Cl, T, mL, mC, mT, uL, uC, uT}
```

```
lin :=  $\alpha_1 L + \alpha_2 Cl + \alpha_3 T + \alpha_4 mL + \alpha_5 mC + \alpha_6 mT + \alpha_7 uL + \alpha_8 uC + \alpha_9 uT$ 
```

```
quad := ( $\alpha_1 L + \alpha_2 Cl + \alpha_3 T + \alpha_4 mL + \alpha_5 mC + \alpha_6 mT + \alpha_7 uL + \alpha_8 uC + \alpha_9 uT$ )  
( $\beta_1 L + \beta_2 Cl + \beta_3 T + \beta_4 mL + \beta_5 mC + \beta_6 mT + \beta_7 uL + \beta_8 uC + \beta_9 uT$ )
```

```
Resolve[ForAll[{L, Cl, T, mL, mC, mT, uL, uC, uT}, Lie[f[xs], lin, xs] == 0]]
```

$$\alpha_9 == 0 \ \&\& \ \alpha_8 == 0 \ \&\& \ \alpha_7 == 0 \ \&\& \ \alpha_6 == 0 \ \&\& \ \alpha_5 == 0 \ \&\& \ \alpha_4 == 0 \ \&\&$$

$$-10 \alpha_3 + \alpha_6 == 0 \ \&\& \ \alpha_3 == 0 \ \&\& \ -10 \alpha_2 + \alpha_5 == 0 \ \&\& \ \alpha_2 == 0 \ \&\& \ -10 \alpha_1 + \alpha_4 == 0 \ \&\& \ \alpha_1 == 0$$

```
Reduce[%22]
```

$$\alpha_9 == 0 \ \&\& \ \alpha_8 == 0 \ \&\& \ \alpha_7 == 0 \ \&\& \ \alpha_6 == 0 \ \&\& \ \alpha_3 == 0 \ \&\& \ \alpha_5 == 0 \ \&\& \ \alpha_2 == 0 \ \&\& \ \alpha_4 == 0 \ \&\& \ \alpha_1 == 0$$

```
Resolve[ForAll[{L, Cl, T, mL, mC, mT, uL, uC, uT}, Lie[f[xs], quad, xs] == 0]]
```

[illegible]

[illegible]

large output

[show less](#)[show more](#)[show all](#)

set size limit...

Reduce [%26]

... 1 ...

large output

show less

show more

show all

set size limit...

FindInstance[%26, { α , β }]

FindInstance: The methods available to FindInstance are insufficient to find the requested instances or prove they do not exist.

FindInstance[... 1 ..., { α , β }]

large output

show less

show more

show all

set size limit...