

Computer Vision HW1

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2021-02-06

Problem 1. A simple image formation model (10pts)

The goal of this first exercise is to take images with different settings of a camera to create pictures with perspective projection and with orthographic projection. Both pictures should cover the same piece of the scene. You can take pictures of real places (e.g., the street, a living room, ...) or you can also create your own simple world (e.g., you can print `simpleWorld.pdf` and create your own scenes. I recommend printing on mate paper). To create pictures with orthographic projection you can do two things:

- (1) use the zoom of the Digital camera
- (2) crop the central part of a picture

You will have to play with the distance between the camera and the scene, and with the zoom (or amount of cropping) so that both images look as similar as possible only differing in the type of projection (similar to figure 1.4, in the lecture 1 notes). Submit the two pictures and label out clearly which parts of the images reveal their projection types.

1.1 Perspective Projection



1.2 Orthographic Projection

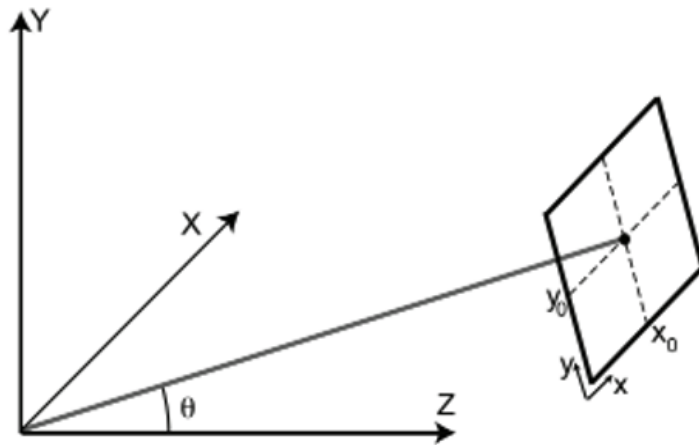


Problem 2. Orthographic projection (10pts)

Prove the projection equations (eq. 1.2 and 1.3 in chapter_01_simplesystem.pdf) that relate the coordinates of one point in 3D world and the image coordinates of the projection of the point in the camera plane. You can use drawings or sketches if necessary.

$$x = \alpha X + x_0 \quad (1.2)$$

$$y = \alpha(\cos(\theta)Y - \sin(\theta)Z) + y_0 \quad (1.3)$$



There are three hypotheses in this simple vision system.

1. The camera center (x_0, y_0) is inside the plane $X=0$
 2. The horizontal axis of camera (x) is parallel to the ground plane $(Y=0)$
 3. The camera is tilted so that the line connecting the origin of the world coordinates system and the image center is perpendicular to the image plane
- To prove equation **1.2**, we know that x is parallel to the ground plane, therefore x -axis in the camera plane is parallel to the X -axis in the 3D world. We can make any shift on the X -axis and the shift will be carried over to the x -axis with a resolution factor α which is a constant, but without any change in magnitude. However, since $(0, 0, 0)$ in the 3D world is mapped to (x_0, y_0) , we will need to add x_0 to any shift made on the X -axis to reflect the actual coordinates in the camera plane. Therefore, we have $x = \alpha X + x_0$.
 - To prove equation **1.3**, we need to be reminded that the Z -axis does not look like is pointing towards the observer. Instead, the Z -axis is identical to the Y -axis up to a sign change and a scaling. A point moving parallel to the Z -axis will be indistinguishable from a point moving down parallel to the Y -axis. Therefore, y is a linear combination of Y and Z . Using the same method as above, we first make a shift on Y and calculate the corresponding shift on the camera plane and then make a shift on Z and calculate the distance moved from (x_0, y_0) . Using trigonometry, we can easily know that the shift on Y

projecting onto the camera plane is equal to $\cos(\theta)Y$ and the shift on Z projecting onto the camera plane is equal to $\sin(\theta)Z$. Taking the difference between Y and Z, multiplying by the resolution factor and add y_0 because $(0, 0, 0)$ is mapped to (x_0, y_0) . Therefore, we have $y = \alpha(\cos(\theta)Y - \sin(\theta)Z) + Y_0$

Problem 3. Constraints (10pts)

In the Lecture slide, we have written all the derivative constraints for $Y(x,y)$. Write the constraints for $Z(x,y)$.

Problem 4. Approximation of derivatives (10pts)

Fill the missing kernels (lines 51 and 65 in Build Constraints) in the script *SimpleWorld.ipynb*. Please include your answers also in the report.

- The problem 4.1 (lines 51) is from Sobel operators.
 - $\partial Y/\partial t = -n_y * \partial Y/\partial x + n_x * \partial Y/\partial y$ (lecture 3 p.26)
- The problem 4.2 (lines 65) is from Laplacian operators.
 - $\partial^2 y/\partial y^2$

```

48     c += 1 # increment constraint counter
49     if horizontalsum > 0 and groundsum == 0 and verticalsum == 0: #(x,y belongs to horizontal edge)
50         # dY/dt = 0
51         # dy/dt = -ny*dy/dx + nx*dy/dy (lecture 3 p.26)
52         Aij[:,c] = -ny * np.array([[ -1, 0, 1], [ -2, 0, 2], [ -1, 0, 1]])/8 + nx * np.array([[ -1, -2, -1], [ 0, 0, 0], [ 1, 2, 1]])/8; # problem 4.1
53         # https://en.wikipedia.org/wiki/Sobel_operator
54         # https://aishack.in/tutorials/sobel-laplacian-edge-detectors/
55         ii[c] = i
56         jj[c] = j
57         b[c] = 0
58         c += 1 # increment constraint counter
59     if groundsum == 0:
60         # laplacian = 0
61         # 0.1 is a weight to reduce the strength of ths constraint
62         Aij[:,c] = 0.1*np.array([[ 0, 0, 0], [ -1, 2, -1], [ 0, 0, 0]]);
63         ii[c] = i
64         jj[c] = j
65         b[c] = 0
66         c += 1 # increment constraint counter
67         # laplacian operator
68         # d^2y/dy^2
69         Aij[:,c] = 0.1*np.array([[ 0, -1, 0], [ 0, 2, 0], [ 0, -1, 0]]); # problem 4.2
70         ii[c] = i;
71         jj[c] = j;
72         b[c] = 0;
73         c = c+1; # increment constraint counter
74
75         Aij[:,c] = 0.1*np.array([[ 0, -1, 1], [ 0, 1, -1], [ 0, 0, 0]]);
76         ii[c] = i;
77         jj[c] = j;
78         b[c] = 0;
79         c = c+1; # increment constraint counter
80

```

Problem 5. Run the code (10pts)

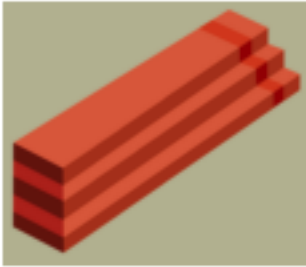
Select some of the images included with the code and show some new view points on them. You can also try with new images taken by you if you decide to create your own simple world.

5.1 I choose “steps.png” for the example

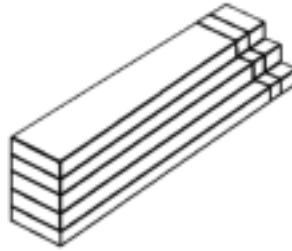
Classify in to 4 categories: - 3D orientation: vertical - 3D orientation: horizontal - Occlusion edges - Contact edges

```
<class 'numpy.ndarray'>
```

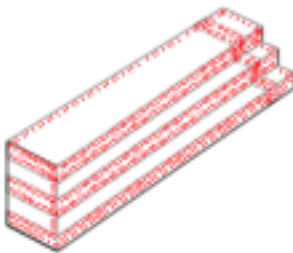
Input image



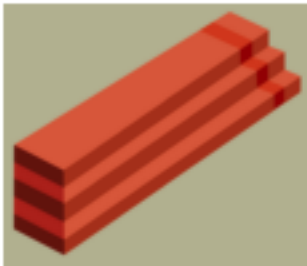
Edges



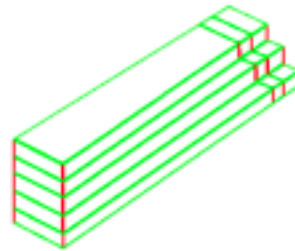
Normals



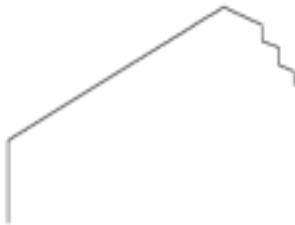
Input image



Edges



Occlusion boundaries

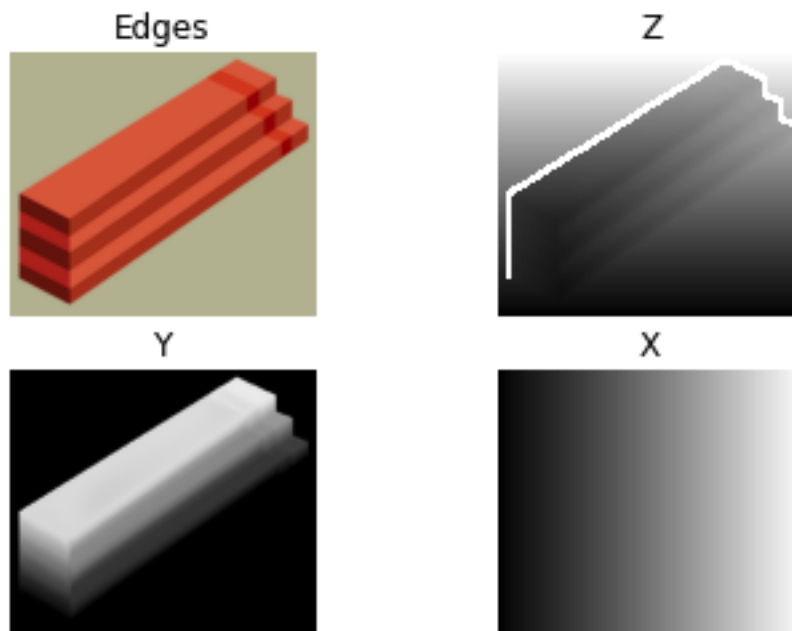


Contact boundaries



5.2 Render Image

```
Text(0.5, 1.0, 'X')
```



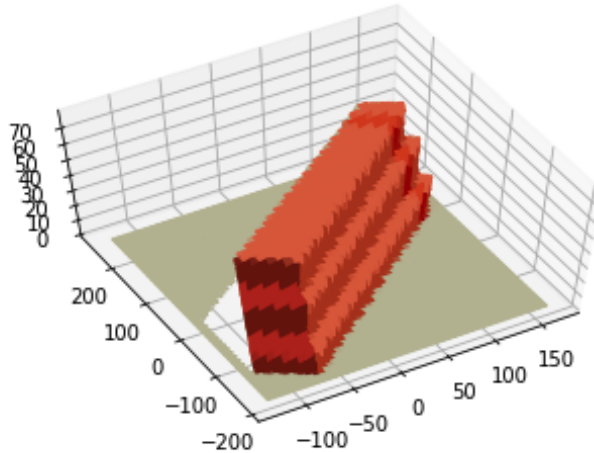
5.3 3D reconstruction

- I changed output angle to `ax.view_init(20, -120)`



```
1 import matplotlib.pyplot as plt
2 from mpl_toolkits.mplot3d import Axes3D
3 fig = plt.figure()
4 ax = fig.add_subplot(111, projection='3d')
5 # Specify here the angle you want to see
6 ax.view_init(60, -120)
7 ax.plot_surface(X,Z,Y, facecolors=img/255., shade=False)
```

<mpl_toolkits.mplot3d.art3d.Poly3DCollection at 0x7ff085658908>



Problem 6. Violating simple world assumptions (5pts)

Find one example from the four images provided with the problem set (img1.jpg, ..., img4.jpg). When the recovery of 3D information fails. Include the image and the reconstruction in your writeup, and explain why it fails. - I found **img3** is fail to 3D reconstruction.

Problem 7. The real world (Extra 5pts)

A research problem is a question for which we do not know the answer. In fact, there might not even be an answer. This question is optional and could be extended into a larger course project.

The goal of this problem is to test the 3D reconstruction code with real images. A number of the assumptions we have made will not work when the input are real images of more complex scene. For instance, the simple strategy of differentiating between foreground and background segmentation will not work with other scenes.

Try taking pictures of real-world scenes (not the cubes) and propose modifications to the scheme proposed in this lecture so that you can get some better 3D reconstructions. The goal is not to build a general system, but to be able to handle a few more situations.