

# Evaluating US Socioeconomic Factors of COVID Confirmed Cases

Keywords: Web Scrapping, Linear Regression, COVID-19

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## Install Packages

Install the required libraries

- `library(broom)` # convert analysis objects from R into tidy tibbles
- `library(tidyverse)` # tidy data
- `library(psych)` # EDA

- library(countrycode) # get the continents
- library(lubridate) # adjust the date variable
- library(usmap) # find out the US states
- library(readxl) # read MS excel file
- library(corrplot) #for visualization of correlation
- library(leaps) # regsubsets
- library(car) # ncvTest
- library(corrplot) # multicollinearity plot
- library(performance) # multicollinearity table

## Web Scraping COVID-19 Data

- The data source is from [Johns Hopkins University](https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_data). Here is the [link](https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_data)

```
url_in <- "https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_data"
```

## Data Scraping

```
+ time_series_covid19_confirmed_global.csv
+ time_series_covid19_deaths_global.csv
+ time_series_covid19_confirmed_US.csv
+ time_series_covid19_deaths_US.csv

df <- tibble(file_names = c("time_series_covid19_confirmed_global.csv",
                             "time_series_covid19_deaths_global.csv",
                             "time_series_covid19_confirmed_US.csv",
                             "time_series_covid19_deaths_US.csv")) -> df
```

## Data Mapping

### Using Regex for mapping

```
df %>%
  mutate(url = str_c(url_in, file_names, sep = "")) -> df

df %>%
  mutate(data = map(url, ~read_csv(., na = ""))) -> df
```

```
## Parsed with column specification:
## cols(
##   .default = col_double(),
##   `Province/State` = col_character(),
##   `Country/Region` = col_character()
## )

## See spec(...) for full column specifications.

## Parsed with column specification:
## cols(
##   .default = col_double(),
##   `Province/State` = col_character(),
##   `Country/Region` = col_character()
## )

## See spec(...) for full column specifications.
```

```
## Parsed with column specification:
## cols(
##   .default = col_double(),
##   iso2 = col_character(),
##   iso3 = col_character(),
##   Admin2 = col_character(),
##   Province_State = col_character(),
##   Country_Region = col_character(),
##   Combined_Key = col_character()
## )

## See spec(...) for full column specifications.

## Parsed with column specification:
## cols(
##   .default = col_double(),
##   iso2 = col_character(),
##   iso3 = col_character(),
##   Admin2 = col_character(),
##   Province_State = col_character(),
##   Country_Region = col_character(),
##   Combined_Key = col_character()
## )

## See spec(...) for full column specifications.

df %>%
  mutate(case_types = as.factor(str_extract(file_names, "[:alpha:]*_[gU][:alpha:]*"))) ->
  df
# alpha = Any letter, [A-Za-z]
# reference: https://www.petefreitag.com/cheatsheets/regex/character-classes/

df %>%
  dplyr::select(case_types, data) -> df
```

## Clean Data

```
df %>%
  mutate(vars = map(df$data, names)) -> df
# map(df$vars, ~unlist(.)[1:15]) for checking

fix_names <- function(df, pattern, rePattern){
  stopifnot(is.data.frame(df), is.character(pattern), is.character(rePattern))
  names(df) <- str_replace_all(names(df), pattern, rePattern)
  return(df)
}

df %>%
  mutate(data = map(data, ~fix_names(., "([ey])/", "\\1_")),
         data = map(data, ~fix_names(., "Admin2", "County")),
         data = map(data, ~fix_names(., "Long_", "Long")),
         data = map_if(data, str_detect(df$case_types, "US"),
                        ~dplyr::select(., -c("UID", "iso2", "iso3",
                                                "code3", "FIPS", "Combined_Key"))),
         data = map_if(data, str_detect(df$case_types, "global"),
```

```

      ~mutate(., County = "NA")),
data = map_if(data, !str_detect(df$case_types, "deaths_US"),
  ~mutate(., Population = 0)),
data = map(data, ~unite(., "Country_State",
  c("Country_Region", "Province_State"),
  remove = FALSE, na.rm = TRUE,
  sep = "_"))

) -> df

df %>%
  mutate(vars = map(df$data, names)) -> df # synchronize the vars correspondingly
# map(df$vars, ~unlist(.)) # for checking

df %>%
  mutate(data = map(data, ~pivot_longer(data = ., cols = contains("/"),
    names_to = "Date",
    values_to = "dailyValues",
    names_transform = list(Date = mdy)))

  ) -> df

# df$data <- map(df$data, names) # synchronize the vars correspondingly
# map(df$vars, ~unlist(.)) # for checking

# crate a function to fix in type of Date
mdyDate <- function(df, varsDate){
  # stopifnot(is.data.frame(df), is.character(varsDate))
  df[[varsDate]] <- ymd(df[[varsDate]])
  return(df)
}

df %>%
  mutate(data = map(data, ~mdyDate(., "Date"))) -> df_long

# str(df_long) # check the data set

```

## Add Continents and fix NAs

```

df_long %>%
  mutate(data = map(data, ~mutate(., Continent = countrycode(Country_Region,
    origin = "country.name",
    destination = "continent"))))

  ) -> df_long

df_long %>%
  mutate(data = map(data, ~mutate(., Continent = case_when(
    Country_Region == "Diamond Princess" ~ "Asia",
    Country_Region == "Kosovo" ~ "Americas",
    Country_Region == "MS Zaandam" ~ "Europe",
    TRUE ~ Continent)
  ))) -> df_long

map(df_long$data, ~unique(.$Continent))

## [[1]]
## [1] "Asia"      "Europe"    "Africa"    "Americas" "Oceania"  NA

```

```
##
## [[2]]
## [1] "Asia"      "Europe"    "Africa"    "Americas" "Oceania"  NA
##
## [[3]]
## [1] "Americas"
##
## [[4]]
## [1] "Americas"
```

## Unnest the Data Frames

```
# 1
df_long %>%
  unnest(cols = data) %>%
  ungroup() -> df_all

# 2
remove(df, df_long)

# 3
df_all %>%
  dplyr::select(-vars) -> df_all
```

## Get World Population Data

- source: [UN source](#)

```
# 1
df_pop <- read_csv("../data/WPP2019_TotalPopulation.csv")

## Parsed with column specification:
## cols(
##   LocID = col_double(),
##   Location = col_character(),
##   PopTotal = col_double(),
##   PopDensity = col_double()
## )

# summarize(df_pop, across(everything(), ~sum(is.na(.)))) # check NAs

# 2
semi_join(df_pop, df_all, by = c("Location" = "Country_Region")) -> df_pop

# 3
df_pop %>%
  mutate(rank_p = rank(-PopTotal, na.last = TRUE),
         rank_d = rank(-PopDensity, na.last = TRUE),
         PopTotal = (PopTotal*1000)) -> df_pop

df_all %>%
  inner_join(df_pop, by = c("Country_Region" = "Location")) -> df_all
```

## Tidy Data

- Because COVID-19 data is a time series data, we only focus on 2020/01/22 - 2021/01/22 for our experiment.

```
#df_all %>%
  #filter(case_types == "confirmed_US") %>%
  #select(Date, Province_State, County, dailyValues) %>%
  #tail()

# extract one year
df_all %>%
  filter(case_types == "confirmed_US" & as_date(Date) <= as_date("2021-01-22") | case_types == "deaths_US") %>%
  names(covid)

## [1] "case_types"      "Country_State"   "Province_State"  "Country_Region"
## [5] "Lat"            "Long"           "County"          "Population"
## [9] "Date"           "dailyValues"    "Continent"       "LocID"
## [13] "PopTotal"       "PopDensity"     "rank_p"          "rank_d"
```

Find out each US state using usmap

```
state_map <- us_map(regions = "states")
state_map %>%
  distinct(full) %>%
  rename("Province_State" = "full") -> USstates
```

Obtain the number of confirmed cases for each state

```
covid %>%
  filter(case_types == "confirmed_US" & as_date(Date) == as_date("2021-01-22")) %>%
  dplyr::select(Province_State, County, dailyValues) %>%
  group_by(Province_State) %>%
  tally(dailyValues) %>%
  right_join(USstates) %>%
  rename("confirmed" = "n") -> confirmed
```

## Joining, by = "Province\_State"

Obtain the number of death cases for each state

```
covid %>%
  filter(case_types == "deaths_US" & as_date(Date) == as_date("2021-01-22")) %>%
  dplyr::select(Province_State, County, dailyValues) %>%
  group_by(Province_State) %>%
  tally(dailyValues) %>%
  right_join(USstates) %>%
  rename("deaths" = "n") -> deaths
```

## Joining, by = "Province\_State"

```
full_join(confirmed, deaths) -> covid
```

## Joining, by = "Province\_State"

## Read 2019 American community survey estimate by race by state

- Source: <https://www.governing.com/now/State-Population-By-Race-Ethnicity-Data.html>

```
race <- read_csv("../data/2019_state_community_by_race.csv")
```

```
## Parsed with column specification:
```

```
## cols(
##   State = col_character(),
##   `American Indian and Alaska Native alone` = col_double(),
##   `Asian alone` = col_double(),
##   `Black or African American alone` = col_double(),
##   `Native Hawaiian and Other Pacific Islander alone` = col_double(),
##   `Some other race alone` = col_double(),
##   `Total Population` = col_double(),
##   `Two or more races` = col_double(),
##   `White alone` = col_double()
## )
```

```
race %>%
  rename(Province_State = State) -> race
```

```
covid %>%
```

```
left_join(race, by = "Province_State") %>%
  rename(American_Indian_and_Alaska_Native_alone = "American Indian and Alaska Native alone",
         Asian_alone = "Asian alone",
         Black_or_African_American_alone = "Black or African American alone",
         Native_Hawaiian_and_Other_Pacific_Islander_alone = "Native Hawaiian and Other Pacific Islander",
         Some_other_race_alone = "Some other race alone",
         Total_Population = "Total Population",
         Two_or_more_races = "Two or more races",
         White_alone = "White alone") -> covid
```

```
#race %>%
```

```
  #anti_join(covidForRegression, by = "Province_State") #-->Check if there are some diff value of state
```

```
# The 2020 American Community Survey (ACS) 1-year estimates will be released on September 23, 2021.
```

```
# Since the 2020 survey does not yet release, we use the 2019 survey here
```

## Read 2021 Household income

- This data is tided from [World Population Review](#), and the original, and source is from [US Census](#)

```
householdIncome2021 <- read_csv("../data/MedianHouseholdIncome2021.csv")
```

```
## Parsed with column specification:
```

```
## cols(
##   State = col_character(),
##   HouseholdIncome = col_double()
## )
```

```
householdIncome2021
```

```
## # A tibble: 51 x 2
```

```
##   State      HouseholdIncome
##   <chr>          <dbl>
## 1 Maryland      84805
```

```
## 2 New Jersey      82545
## 3 Hawaii          81275
## 4 Massachusetts   81215
## 5 Connecticut     78444
## 6 Alaska          77640
## 7 New Hampshire   76768
## 8 California      75235
## 9 Virginia        74222
## 10 Washington     73775
## # ... with 41 more rows
```

```
householdIncome2021 %>%
  rename(Province_State = State) -> householdIncome2021

covid %>%
  left_join(householdIncome2021, by = "Province_State") -> covid

# Recheck
#covid %>%
#  dplyr::select(Province_State, HouseholdIncome) %>%
#  dplyr::arrange(desc(HouseholdIncome))
```

## Exploratory Data Analysis

### Data Analysis and Visualization

```
str(covid)

## tibble [51 x 12] (S3: tbl_df/tbl/data.frame)
##  $ Province_State      : chr [1:51] "Alabama" "Alaska" "Arizona" "Arkansas" ...
##  $ confirmed           : num [1:51] 436087 52926 708041 281382 3147207 ...
##  $ deaths              : num [1:51] 6486 254 12001 4549 36615 ...
##  $ American_Indian_and_Alaska_Native_alone : num [1:51] 23265 115544 332273 17216 321112 ...
##  $ Asian_alone         : num [1:51] 66129 43678 241721 46078 5865435 ...
##  $ Black_or_African_American_alone         : num [1:51] 1319551 22551 343729 467468 2282144 ...
##  $ Native_Hawaiian_and_Other_Pacific_Islander_alone : num [1:51] 1892 9923 14168 12829 155871 ...
##  $ Some_other_race_alone : num [1:51] 74451 12602 364442 75590 5424558 ...
##  $ Total_Population      : num [1:51] 4903185 731545 7278717 3017804 39512 ...
##  $ Two_or_more_races     : num [1:51] 91522 57476 280574 83603 1978145 ...
##  $ White_alone          : num [1:51] 3326375 469771 5701810 2315020 23484 ...
##  $ HouseholdIncome       : num [1:51] 50536 77640 58945 47597 75235 ...

covid %>% head()

## # A tibble: 6 x 12
##   Province_State confirmed deaths American_Indian~ Asian_alone Black_or_Africa~
##   <chr>          <dbl> <dbl>          <dbl>          <dbl>          <dbl>
## 1 Alabama      436087   6486          23265          66129          1319551
## 2 Alaska       52926    254          115544         43678          22551
## 3 Arizona     708041  12001         332273         241721         343729
## 4 Arkansas    281382   4549          17216          46078          467468
## 5 California  3147207  36615         321112        5865435        2282144
## 6 Colorado    383008   5462          57578         188461         240538
## # ... with 6 more variables:
## #   Native_Hawaiian_and_Other_Pacific_Islander_alone <dbl>,
```



```
## #   Some_other_race_alone <dbl>, Total_Population <dbl>,
## #   Two_or_more_races <dbl>, White_alone <dbl>, HouseholdIncome <dbl>
```

### Top 5 Confirmed Covid-19 Cases (Jan. 22, 2020 to Jan. 22, 2021)

```
covid %>%
  dplyr::select(1, 2) %>%
  arrange(desc(confirmed)) %>%
  head(5)
```

```
## # A tibble: 5 x 2
##   Province_State confirmed
##   <chr>           <dbl>
## 1 California      3147207
## 2 Texas           2227789
## 3 Florida         1627603
## 4 New York        1309403
## 5 Illinois        1093375
```

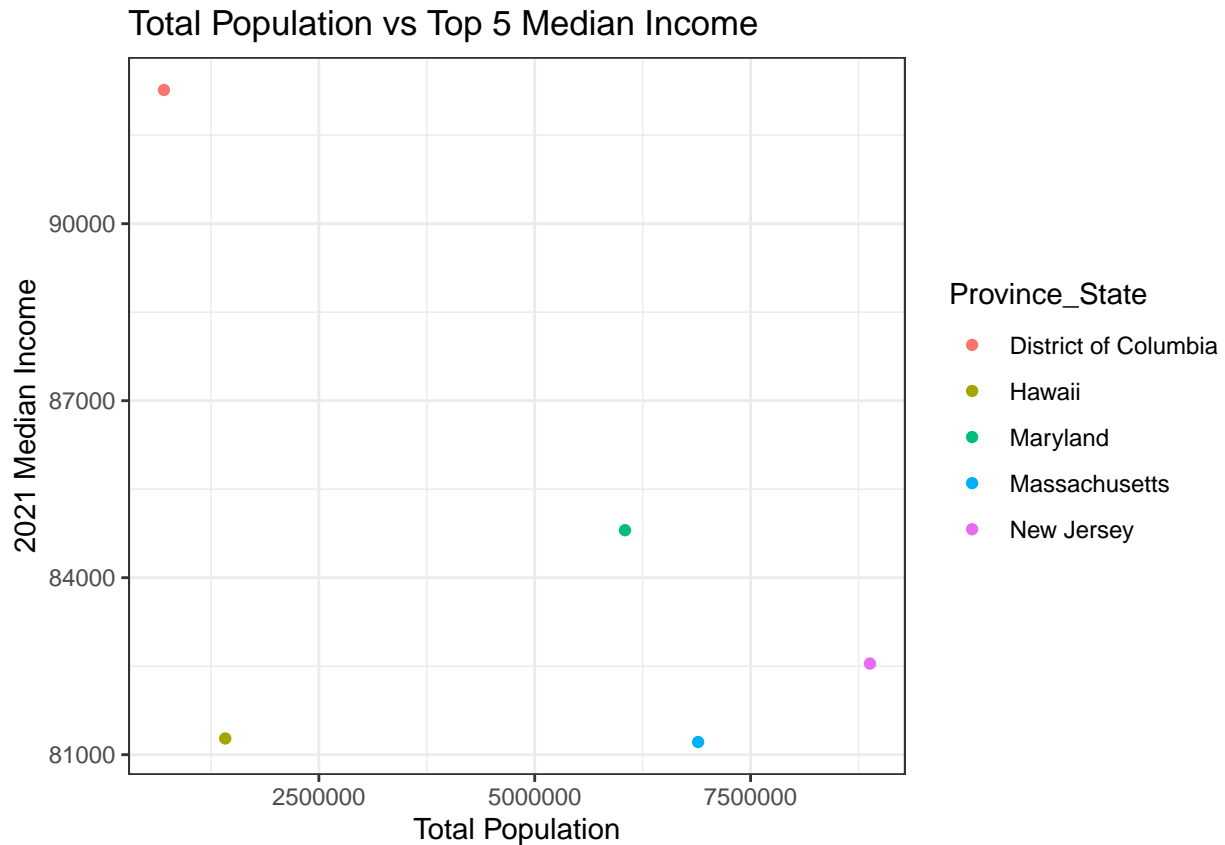
### Top 5 Death Cases (Jan. 22, 2020 to Jan. 22, 2021)

```
covid %>%
  dplyr::select(1, 3) %>%
  arrange(desc(deaths)) %>%
  head(5)
```

```
## # A tibble: 5 x 2
##   Province_State deaths
##   <chr>           <dbl>
## 1 New York        41974
## 2 California      36615
## 3 Texas           34381
## 4 Florida         25011
## 5 New Jersey      20875
```

### Total Population vs Top 5 Median Income

```
covid %>%
  dplyr::arrange(desc(HouseholdIncome)) %>%
  head(5) %>%
  ggplot(aes(x = Total_Population, y = HouseholdIncome, color = Province_State)) +
  geom_point() +
  theme_bw() +
  labs(x = "Total Population", y = "2021 Median Income",
       title = "Total Population vs Top 5 Median Income")
```



In order to run the linear regression model smoothly, we deleted the `Province State` variable from our covid data and saved it as `covidForRegression` dataframe. The reason of removing these two is :

- The `Province State` variable has 51 different categorical types, and each observation has its own type, making it difficult to run a regression model.
- We refer to the existing paper [1](#) & [2](#) and select some similar independent variables as predictors.

```
covid %>%
  dplyr::select(-Province_State) -> covidForRegression
names(covidForRegression)

## [1] "confirmed"
## [2] "deaths"
## [3] "American_Indian_and_Alaska_Native_alone"
## [4] "Asian_alone"
## [5] "Black_or_African_American_alone"
## [6] "Native_Hawaiian_and_Other_Pacific_Islander_alone"
## [7] "Some_other_race_alone"
## [8] "Total_Population"
## [9] "Two_or_more_races"
## [10] "White_alone"
## [11] "HouseholdIncome"
```

## Descriptive Statistics

```
describe(covidForRegression)

##               vars    n    mean    sd
```

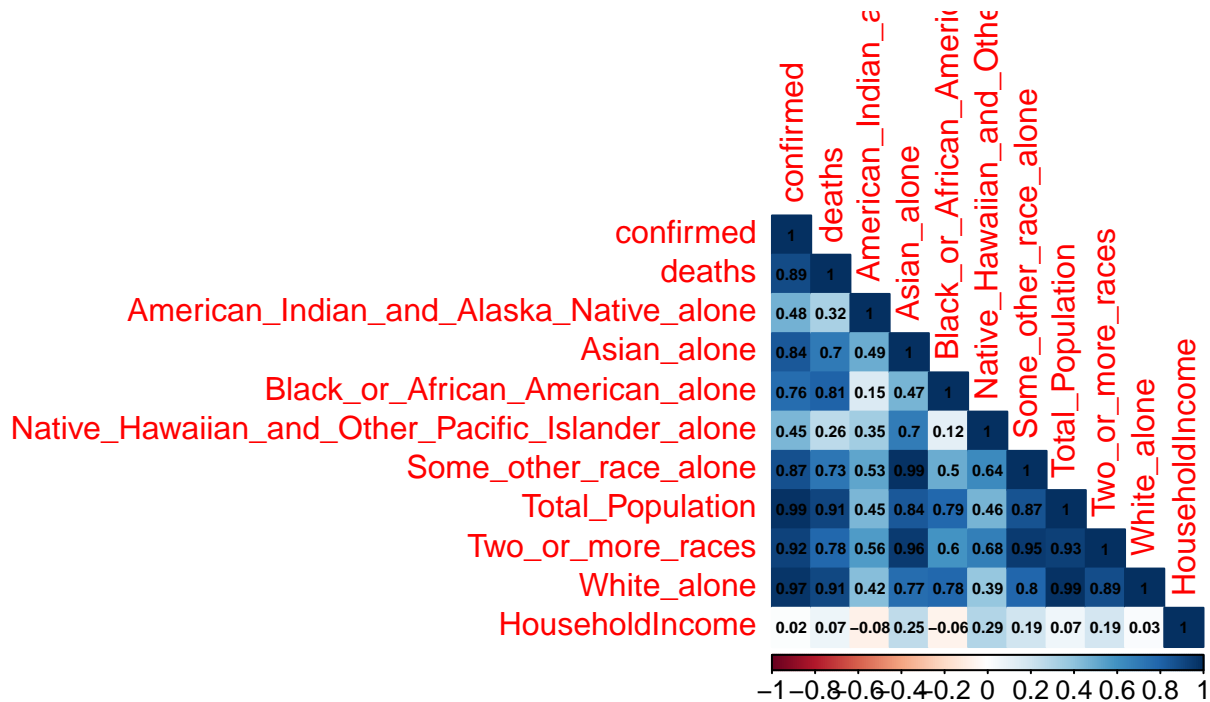
## confirmed	1	51	486333.45	569046.28
## deaths	2	51	8233.76	9596.98
## American_Indian_and_Alaska_Native_alone	3	51	55830.12	78344.82
## Asian_alone	4	51	365431.06	856969.06
## Black_or_African_American_alone	5	51	823326.88	992012.64
## Native_Hawaiian_and_Other_Pacific_Islander_alone	6	51	12327.12	30362.26
## Some_other_race_alone	7	51	320638.29	806711.25
## Total_Population	8	51	6436069.08	7360660.47
## Two_or_more_races	9	51	221743.04	305472.96
## White_alone	10	51	4636772.57	4879687.14
## HouseholdIncome	11	51	63212.49	10997.18
##			median	trimmed
## confirmed	336915		371693.90	341293.04
## deaths	5462		6321.95	5601.26
## American_Indian_and_Alaska_Native_alone	23860		37053.78	26287.98
## Asian_alone	125742		195764.44	163707.21
## Black_or_African_American_alone	363167		638520.95	505434.65
## Native_Hawaiian_and_Other_Pacific_Islander_alone	3254		5152.68	3767.29
## Some_other_race_alone	109373		148097.27	135321.35
## Total_Population	4467673		4941366.54	4167653.83
## Two_or_more_races	137034		162344.49	155352.76
## White_alone	3296909		3682867.05	3022032.51
## HouseholdIncome	61439		62515.10	10152.84
##			min	max
## confirmed	10759		3147207	3136448
## deaths	169		41974	41805
## American_Indian_and_Alaska_Native_alone	1727		332273	330546
## Asian_alone	4633		5865435	5860802
## Black_or_African_American_alone	7116		3553922	3546806
## Native_Hawaiian_and_Other_Pacific_Islander_alone	175		155871	155696
## Some_other_race_alone	2153		5424558	5422405
## Total_Population	578759		39512223	38933464
## Two_or_more_races	15367		1978145	1962778
## White_alone	300058		23484958	23184900
## HouseholdIncome	45081		92266	47185
##			kurtosis	se
## confirmed			8.62	79682.42
## deaths			3.05	1343.85
## American_Indian_and_Alaska_Native_alone			5.36	10970.47
## Asian_alone			30.44	119999.67
## Black_or_African_American_alone			0.88	138909.55
## Native_Hawaiian_and_Other_Pacific_Islander_alone			15.79	4251.57
## Some_other_race_alone			28.75	112962.17
## Total_Population			7.38	1030698.63
## Two_or_more_races			18.95	42774.77
## White_alone			4.90	683292.87
## HouseholdIncome			-0.46	1539.91

# Linear Model Assumptions

## Multicollinearity

### Plot

```
correlation <- cor(covidForRegression)
corrplot(correlation, method="color", addCoef.col = "black", number.cex = 0.5, type = "lower")
```



### Table

Check the inversely related values of Tolerance and VIF. **Tolerance** has to be  $> 0.10$  and **VIF**  $< 10$ . If these stipulated are not fulfilled, multicollinearity is at hand.

```
reg <- lm(confirmed ~ ., data = covidForRegression)
check_collinearity(reg)
```

```
## Warning: Model matrix is rank deficient. VIFs may not be sensible.
```

```
## # Check for Multicollinearity
```

```
##
```

```
## Low Correlation
```

```
##
```

	Term	VIF	Increased SE	Tolerance
##	American_Indian_and_Alaska_Native_alone	3.05	1.75	0.33
##	Native_Hawaiian_and_Other_Pacific_Islander_alone	4.43	2.11	0.23
##	HouseholdIncome	1.38	1.18	0.72

```
##
```

```
## Moderate Correlation
```

```
##
```

	Term	VIF	Increased SE	Tolerance
##	deaths	9.23	3.04	0.11
##	Black_or_African_American_alone	5.05	2.25	0.20

```
##
## High Correlation
##
##           Term      VIF Increased SE Tolerance
##      Asian_alone 136.39      11.68      0.01
## Some_other_race_alone 87.55      9.36      0.01
##      Total_Population 84.30      9.18      0.01
##      Two_or_more_races 133.56     11.56      0.01
```

## Remediation - Removing Highly Correlated Predictors

- Remove highly correlated predictors from the model. If you have two or more factors with a high VIF, remove one from the model.
- According to the result, we firstly remove the high correlation variables: `Some_other_race_alone`, `Total_Population`, and `Two_or_more_races`, and keep the majority of race variables.
- After we removed, now the independent variables have very low correlation with each other.

```
covidForRegression %>%
  dplyr::select(-Total_Population, -Two_or_more_races, -Some_other_race_alone) -> covidForRegression2
names(covidForRegression2)
```

```
## [1] "confirmed"
## [2] "deaths"
## [3] "American_Indian_and_Alaska_Native_alone"
## [4] "Asian_alone"
## [5] "Black_or_African_American_alone"
## [6] "Native_Hawaiian_and_Other_Pacific_Islander_alone"
## [7] "White_alone"
## [8] "HouseholdIncome"
```

```
reg <- lm(confirmed ~ ., data = covidForRegression2)
check_collinearity(reg)
```

```
## # Check for Multicollinearity
```

```
##
```

```
## Low Correlation
```

```
##
```

```
##           Term      VIF Increased SE Tolerance
## American_Indian_and_Alaska_Native_alone 1.50      1.22      0.67
##      Black_or_African_American_alone 3.64      1.91      0.27
## Native_Hawaiian_and_Other_Pacific_Islander_alone 2.50      1.58      0.40
##      HouseholdIncome 1.26      1.12      0.80
```

```
## Moderate Correlation
```

```
##
```

```
##           Term      VIF Increased SE Tolerance
##      deaths 7.88      2.81      0.13
## Asian_alone 5.55      2.36      0.18
## White_alone 8.88      2.98      0.11
```

## Independence

We would need to know more from the data providers to really assess this. We will assume it holds.

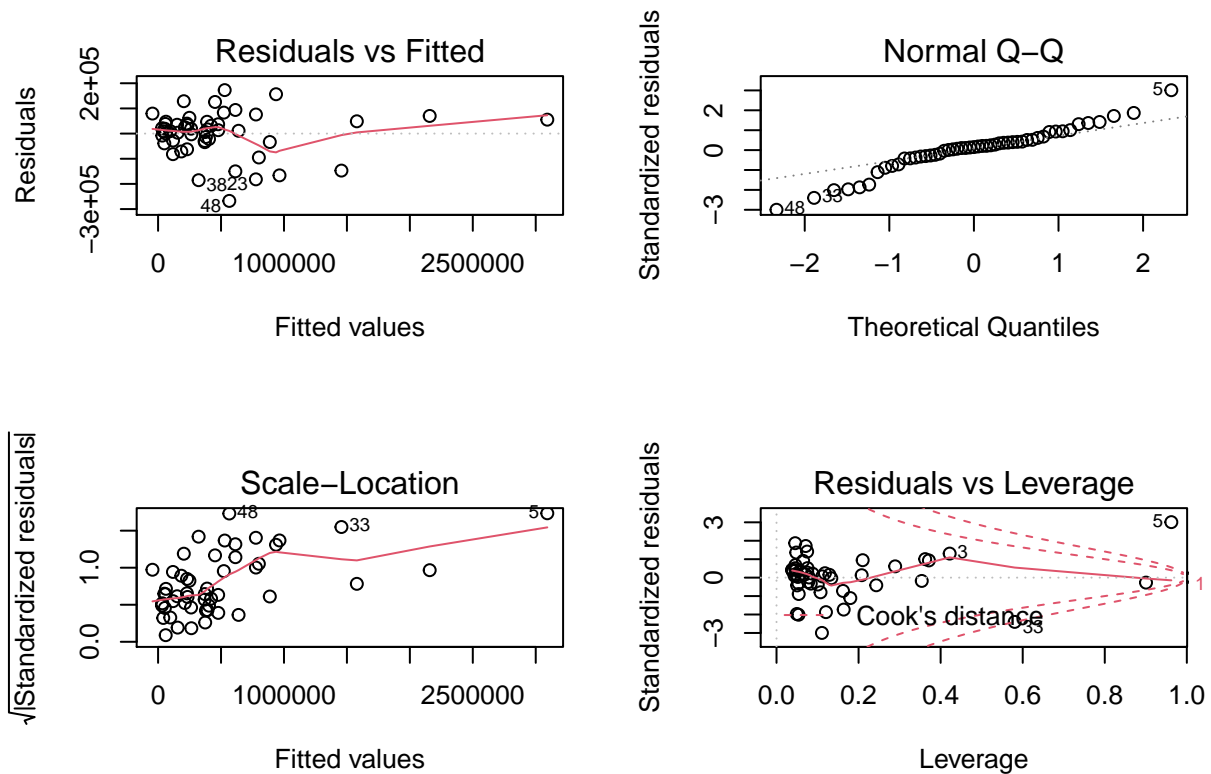
## Linearity

The lack of fit F test works only with **simple linear regression** so we see the residual plots. As for the residuals versus fitted plot below, there may be no pattern indicating non-linearity in the data, but we attempt to remove some potential outliers.

```
par(mfrow = c(2,2))
# summary(reg)
plot(reg)
```

```
## Warning in sqrt(crit * p * (1 - hh)/hh): NaNs produced
```

```
## Warning in sqrt(crit * p * (1 - hh)/hh): NaNs produced
```



## Remediation - Removing Influential Outliers

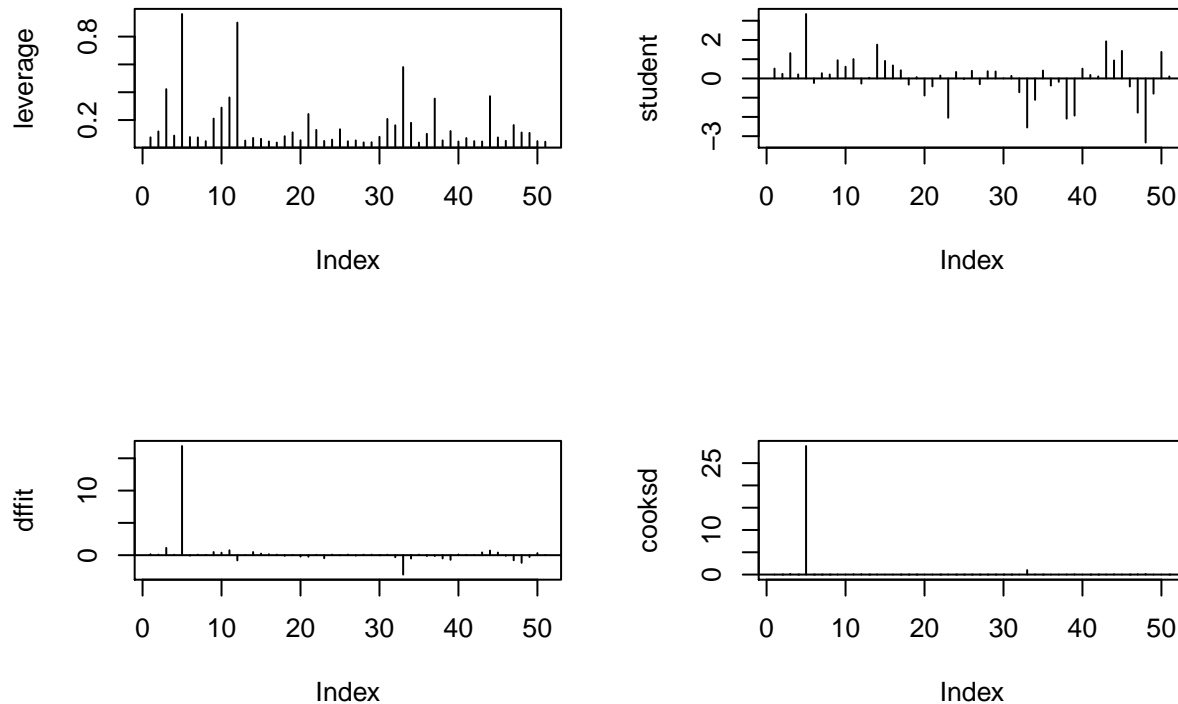
- Get other diagnostics measures

Take away the largest values of **cooks** and **leverage**. That is, observations 5 (California), is no longer present.

```
leverage <- hatvalues(reg)
student <- rstudent(reg)
dfs <- dffits(reg)
cooksd <- cooks.distance(reg)
data.frame(confirmed = covidForRegression2$confirmed, fitted = reg$fitted,
           residual = reg$residual, leverage, student, dffits = dfs, cooksd) -> diag

par(mfrow=c(2,2))
plot(leverage,type='h')
abline(h=0)
```

```
plot(student,type='h')
abline(h=0)
plot(dfs,type='h',ylab='dffit')
abline(h=0)
plot(cooksd,type='h')
abline(h=0)
```



```
diag %>%
  arrange(desc(leverage)) %>%
  head(3)
```

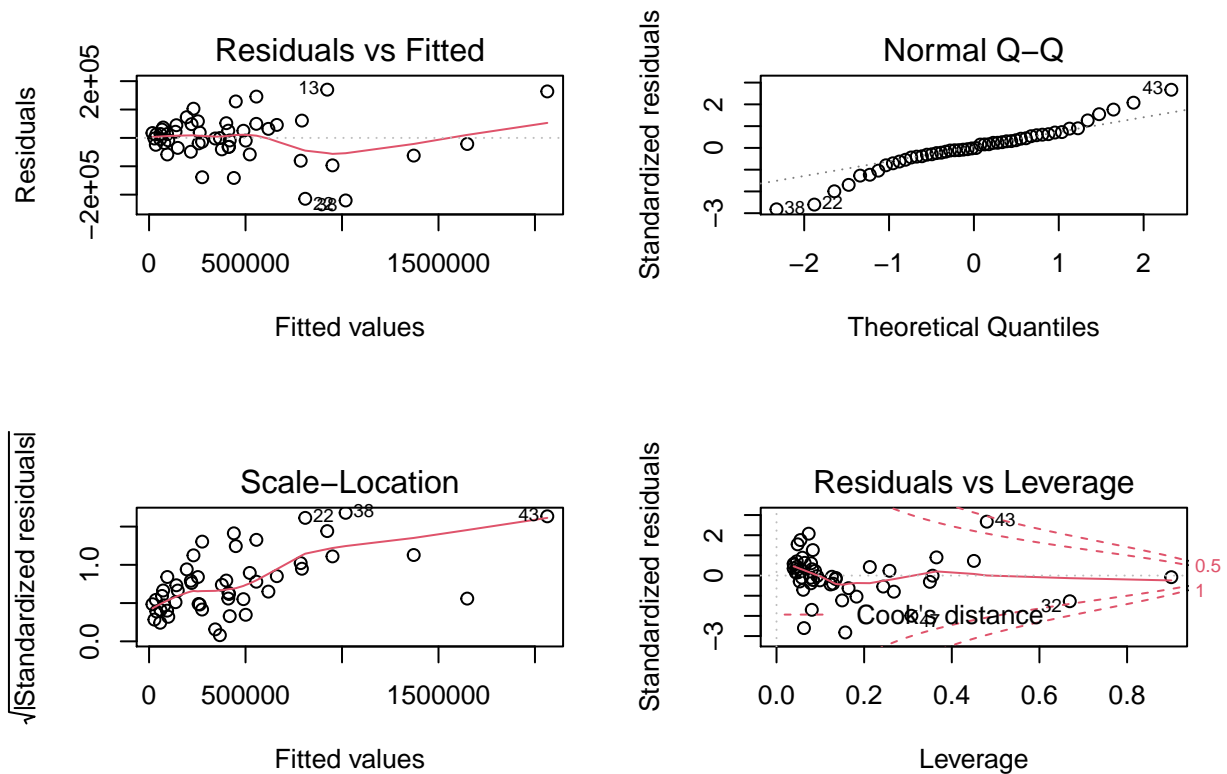
##	confirmed	fitted	residual	leverage	student	dffits	cooksd
## 5	3147207	3091857.30	55349.699	0.9622216	3.3473969	16.8936369	28.83180263
## 12	25658	33724.59	-8066.588	0.9005303	-0.2673471	-0.8044132	0.08267023
## 33	1309403	1456505.11	-147102.113	0.5805405	-2.5490024	-2.9987585	0.99665047

```
diag %>%
  arrange(desc(cooksd)) %>%
  head(3)
```

##	confirmed	fitted	residual	leverage	student	dffits	cooksd
## 5	3147207	3091857.3	55349.70	0.9622216	3.347397	16.893637	28.8318026
## 33	1309403	1456505.1	-147102.11	0.5805405	-2.549002	-2.998758	0.9966505
## 3	708041	614260.7	93780.28	0.4220373	1.314555	1.123322	0.1551054

- Look at the Residual vs Fitted plot; linearity has occurred.

```
reg1 <- lm(confirmed ~ ., data = covidForRegression2[5,])
par(mfrow=c(2,2))
plot(reg1)
```



## Homoscedasticity

With a small p-value, we have evidence that the variances are non-constant

```
# test homoscedasticity
ncvTest(reg1)

## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 18.38094, Df = 1, p = 1.8086e-05
```

## Remediation - Square Root of Y

With a high p-value of 0.84229, there is no evidence of non-constant variance.

```
covidForRegression2 %>%
  mutate(confirmed = sqrt(confirmed)) -> covidForRegressionSQRT

reg2 <- lm(confirmed ~ ., data = covidForRegressionSQRT[-5,])
ncvTest(reg2)

## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 0.03958722, Df = 1, p = 0.84229
```

## Normality

- The p-value of the Shapiro-Wilk Test 0.1822 is greater than  $\alpha$  0.05 so the data is follow a normal distribution.



```
# test normality
shapiro.test(rstudent(reg2))

##
##  Shapiro-Wilk normality test
##
## data:  rstudent(reg2)
## W = 0.96747, p-value = 0.1822
```

## Linear Model Selection

Our final mission is to select the **fewest** predictors and the determine by the **lowest** mean squared error in the linear model.

Adding all variables as full model first. We can see that only three variables in the linear model are significant at the beginning, which is `deaths`, `Black_or_African_American_alone`, and `White_alone`.

```
summary(reg2)

##
## Call:
## lm(formula = confirmed ~ ., data = covidForRegressionSQRT[-5,
##    ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -222.18  -76.64   10.25   68.97  164.51
##
## Coefficients:
##              Estimate Std. Error t value
## (Intercept)      3.624e+02  1.103e+02   3.285
## deaths           1.192e-02  5.486e-03   2.173
## American_Indian_and_Alaska_Native_alone  3.498e-04  2.184e-04   1.602
## Asian_alone      -1.807e-04  1.219e-04  -1.483
## Black_or_African_American_alone  5.840e-05  2.727e-05   2.142
## Native_Hawaiian_and_Other_Pacific_Islander_alone  1.095e-05  7.942e-04   0.014
## White_alone      4.288e-05  8.548e-06   5.017
## HouseholdIncome -1.027e-03  1.640e-03  -0.626
##
##              Pr(>|t|)
## (Intercept)    0.00206 **
## deaths         0.03547 *
## American_Indian_and_Alaska_Native_alone  0.11674
## Asian_alone    0.14562
## Black_or_African_American_alone  0.03807 *
## Native_Hawaiian_and_Other_Pacific_Islander_alone  0.98906
## White_alone    1.01e-05 ***
## HouseholdIncome  0.53469
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 98.64 on 42 degrees of freedom
## Multiple R-squared:  0.9041, Adjusted R-squared:  0.8882
## F-statistic: 56.58 on 7 and 42 DF,  p-value: < 2.2e-16
```

## Exhaustive Search

Using algorithm to select the best model exhaustively. Also, to use all X-variables available, change the `nvmax` option. Because I am too lazy to count variables, I entered a much larger number, such as my favorite number 69 to do it.

```
reg_fitExhaustive <- regsubsets(confirmed ~ ., data = covidForRegressionSQRT[-5,], nvmax = 69)
summary(reg_fitExhaustive)
```

```
## Subset selection object
## Call: regsubsets.formula(confirmed ~ ., data = covidForRegressionSQRT[-5,
##      ], nvmax = 69)
## 7 Variables (and intercept)
##
```

		Forced in	Forced out
## deaths		FALSE	FALSE
## American_Indian_and_Alaska_Native_alone		FALSE	FALSE
## Asian_alone		FALSE	FALSE
## Black_or_African_American_alone		FALSE	FALSE
## Native_Hawaiian_and_Other_Pacific_Islander_alone		FALSE	FALSE
## White_alone		FALSE	FALSE
## HouseholdIncome		FALSE	FALSE

```
## 1 subsets of each size up to 7
## Selection Algorithm: exhaustive
##      deaths American_Indian_and_Alaska_Native_alone Asian_alone
## 1 ( 1 ) " " " " " "
## 2 ( 1 ) " " " " " "
## 3 ( 1 ) "*" " " "*"
## 4 ( 1 ) "*" " " "*"
## 5 ( 1 ) "*" "*" "*"
## 6 ( 1 ) "*" "*" "*"
## 7 ( 1 ) "*" "*" "*"
##      Black_or_African_American_alone
## 1 ( 1 ) " "
## 2 ( 1 ) "*"
## 3 ( 1 ) " "
## 4 ( 1 ) "*"
## 5 ( 1 ) "*"
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"
##      Native_Hawaiian_and_Other_Pacific_Islander_alone White_alone
## 1 ( 1 ) " " "*"
## 2 ( 1 ) " " "*"
## 3 ( 1 ) " " "*"
## 4 ( 1 ) " " "*"
## 5 ( 1 ) " " "*"
## 6 ( 1 ) " " "*"
## 7 ( 1 ) "*" "*"
##      HouseholdIncome
## 1 ( 1 ) " "
## 2 ( 1 ) " "
## 3 ( 1 ) " "
## 4 ( 1 ) " "
## 5 ( 1 ) " "
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"
##
```

Select the variables and choose the optimal model

```
summary(reg_fitExhaustive)$adjr2

## [1] 0.8574573 0.8711181 0.8792470 0.8866123 0.8922247 0.8907509 0.8881502

summary(reg_fitExhaustive)$cp

## [1] 15.171783 10.157020 7.661584 5.618763 4.397164 6.000190 8.000000

summary(reg_fitExhaustive)$bic

## [1] -90.61260 -92.79050 -93.21127 -93.54488 -93.29474 -89.85308 -85.94128

which.max(summary(reg_fitExhaustive)$adjr2)

## [1] 5

which.min(summary(reg_fitExhaustive)$cp)

## [1] 5

which.min(summary(reg_fitExhaustive)$bic)

## [1] 4
```

## Sequential Search

We can also choose the best model by means of a stepwise procedure, starting with one model and ending with another

### Forward Method

Forward addition can be used to perform variable selection.

```
reg_fitForward <- regsubsets(confirmed ~ .,
                             data = covidForRegressionSqrt[-c(5),],
                             method = "forward")

summary(reg_fitForward)

## Subset selection object
## Call: regsubsets.formula(confirmed ~ ., data = covidForRegressionSqrt[-c(5),
## ], method = "forward")
## 7 Variables (and intercept)
##
##               Forced in Forced out
## deaths                FALSE      FALSE
## American_Indian_and_Alaska_Native_alone    FALSE      FALSE
## Asian_alone                FALSE      FALSE
## Black_or_African_American_alone            FALSE      FALSE
## Native_Hawaiian_and_Other_Pacific_Islander_alone    FALSE      FALSE
## White_alone                FALSE      FALSE
## HouseholdIncome            FALSE      FALSE
## 1 subsets of each size up to 7
## Selection Algorithm: forward
##           deaths American_Indian_and_Alaska_Native_alone Asian_alone
## 1  ( 1 ) " "      " "                                " "
## 2  ( 1 ) " "      " "                                " "
## 3  ( 1 ) " "      " "                                " "
## 4  ( 1 ) "*"      " "                                " "
## 5  ( 1 ) "*"      " "                                "*"
```

```
## 6 ( 1 ) "*"      "*"      "*"
## 7 ( 1 ) "*"      "*"      "*"
##      Black_or_African_American_alone
## 1 ( 1 ) " "
## 2 ( 1 ) "*"
## 3 ( 1 ) "*"
## 4 ( 1 ) "*"
## 5 ( 1 ) "*"
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"
##      Native_Hawaiian_and_Other_Pacific_Islander_alone White_alone
## 1 ( 1 ) " "      "*"
## 2 ( 1 ) " "      "*"
## 3 ( 1 ) " "      "*"
## 4 ( 1 ) " "      "*"
## 5 ( 1 ) " "      "*"
## 6 ( 1 ) " "      "*"
## 7 ( 1 ) "*"      "*"
##      HouseholdIncome
## 1 ( 1 ) " "
## 2 ( 1 ) " "
## 3 ( 1 ) "*"
## 4 ( 1 ) "*"
## 5 ( 1 ) "*"
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"

```

Select the variables and choose the optimal model

```
summary(reg_fitForward)$adjr2
```

```
## [1] 0.8574573 0.8711181 0.8780890 0.8831499 0.8867090 0.8907509 0.8881502
```

```
summary(reg_fitForward)$cp
```

```
## [1] 15.171783 10.157020 8.137825 7.011779 6.566962 6.000190 8.000000
```

```
summary(reg_fitForward)$bic
```

```
## [1] -90.61260 -92.79050 -92.73407 -92.04092 -90.79917 -89.85308 -85.94128
```

```
which.max(summary(reg_fitForward)$adjr2)
```

```
## [1] 6
```

```
which.min(summary(reg_fitForward)$cp)
```

```
## [1] 6
```

```
which.min(summary(reg_fitForward)$bic)
```

```
## [1] 2
```

## Backward Method

Backward elimination can be used to perform variable selection.

```
reg_fitBackward <- regsubsets(confirmed ~ .,
                             data = covidForRegressionSqrt[-c(5),], method = "backward")
summary(reg_fitBackward)
```

```
## Subset selection object
## Call: regsubsets.formula(confirmed ~ ., data = covidForRegressionSQRT[-c(5),
## ], method = "backward")
## 7 Variables (and intercept)
##
##                                Forced in Forced out
## deaths                        FALSE      FALSE
## American_Indian_and_Alaska_Native_alone  FALSE      FALSE
## Asian_alone                    FALSE      FALSE
## Black_or_African_American_alone  FALSE      FALSE
## Native_Hawaiian_and_Other_Pacific_Islander_alone  FALSE      FALSE
## White_alone                   FALSE      FALSE
## HouseholdIncome               FALSE      FALSE
## 1 subsets of each size up to 7
## Selection Algorithm: backward
##      deaths American_Indian_and_Alaska_Native_alone Asian_alone
## 1 ( 1 ) " " " " " "
## 2 ( 1 ) "*" " " " "
## 3 ( 1 ) "*" " " "*"
## 4 ( 1 ) "*" " " "*"
## 5 ( 1 ) "*" "*" "*"
## 6 ( 1 ) "*" "*" "*"
## 7 ( 1 ) "*" "*" "*"
##      Black_or_African_American_alone
## 1 ( 1 ) " "
## 2 ( 1 ) " "
## 3 ( 1 ) " "
## 4 ( 1 ) "*"
## 5 ( 1 ) "*"
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"
##      Native_Hawaiian_and_Other_Pacific_Islander_alone White_alone
## 1 ( 1 ) " " "*"
## 2 ( 1 ) " " "*"
## 3 ( 1 ) " " "*"
## 4 ( 1 ) " " "*"
## 5 ( 1 ) " " "*"
## 6 ( 1 ) " " "*"
## 7 ( 1 ) "*" "*"
##      HouseholdIncome
## 1 ( 1 ) " "
## 2 ( 1 ) " "
## 3 ( 1 ) " "
## 4 ( 1 ) " "
## 5 ( 1 ) " "
## 6 ( 1 ) "*"
## 7 ( 1 ) "*"

```

Select the variables and choose the optimal model

```
summary(reg_fitBackward)$adjr2
```

```
## [1] 0.8574573 0.8651883 0.8792470 0.8866123 0.8922247 0.8907509 0.8881502
```

```
summary(reg_fitBackward)$cp

## [1] 15.171783 12.648768 7.661584 5.618763 4.397164 6.000190 8.000000

summary(reg_fitBackward)$bic

## [1] -90.61260 -90.54137 -93.21127 -93.54488 -93.29474 -89.85308 -85.94128

which.max(summary(reg_fitBackward)$adjr2)

## [1] 5

which.min(summary(reg_fitBackward)$cp)

## [1] 5

which.min(summary(reg_fitBackward)$bic)

## [1] 4
```

## Stepwise Method

We use algorithm to considers either adding or removing variables at each step to final the best model. Lower AIC (Akaike information criterion) values indicate a better-fit model.

```
null = lm(confirmed ~ 1, data = covidForRegressionSQRT[-c(5),])
full = lm(confirmed ~ ., data = covidForRegressionSQRT[-c(5),])
step(null, scope = list(lower = null, upper = full), direction = "both")

## Start:  AIC=569.67
## confirmed ~ 1
##
##
##           Df Sum of Sq    RSS    AIC
## + White_alone      1   3667200  595170  473.23
## + deaths           1   3265900  996470  499.00
## + Black_or_African_American_alone  1   2944490 1317880  512.98
## + Asian_alone      1   2115961 2146409  537.36
## + American_Indian_and_Alaska_Native_alone  1    265309 3997061  568.45
## <none>                                4262370  569.67
## + HouseholdIncome      1    121852 4140518  570.22
## + Native_Hawaiian_and_Other_Pacific_Islander_alone  1     19189 4243181  571.44
##
## Step:  AIC=473.23
## confirmed ~ White_alone
##
##           Df Sum of Sq    RSS    AIC
## + Black_or_African_American_alone      1     68250  526920  469.14
## + HouseholdIncome                      1     46407  548764  471.17
## + deaths                              1     44007  551164  471.39
## + Native_Hawaiian_and_Other_Pacific_Islander_alone  1     35741  559429  472.13
## <none>                                595170  473.23
## + American_Indian_and_Alaska_Native_alone      1     12741  582429  474.15
## + Asian_alone                                1      6779  588392  474.66
## - White_alone                              1   3667200 4262370  569.67
##
## Step:  AIC=469.14
## confirmed ~ White_alone + Black_or_African_American_alone
```

```

##
##
## Df Sum of Sq RSS AIC
## + HouseholdIncome 1 39105 487816 467.28
## + American_Indian_and_Alaska_Native_alone 1 28034 498887 468.41
## + Native_Hawaiian_and_Other_Pacific_Islander_alone 1 26719 500201 468.54
## <none> 526920 469.14
## + deaths 1 17914 509006 469.41
## + Asian_alone 1 16544 510377 469.54
## - Black_or_African_American_alone 1 68250 595170 473.23
## - White_alone 1 790959 1317880 512.98
##
## Step: AIC=467.28
## confirmed ~ White_alone + Black_or_African_American_alone + HouseholdIncome
##
## Df Sum of Sq RSS AIC
## + deaths 1 30415 457401 466.06
## <none> 487816 467.28
## + American_Indian_and_Alaska_Native_alone 1 17844 469972 467.42
## + Native_Hawaiian_and_Other_Pacific_Islander_alone 1 13595 474221 467.87
## - HouseholdIncome 1 39105 526920 469.14
## + Asian_alone 1 482 487334 469.23
## - Black_or_African_American_alone 1 60948 548764 471.17
## - White_alone 1 796518 1284334 513.69
##
## Step: AIC=466.06
## confirmed ~ White_alone + Black_or_African_American_alone + HouseholdIncome +
## deaths
##
## Df Sum of Sq RSS AIC
## + Asian_alone 1 23787 433614 465.39
## <none> 457401 466.06
## + American_Indian_and_Alaska_Native_alone 1 17851 439550 466.07
## + Native_Hawaiian_and_Other_Pacific_Islander_alone 1 8137 449263 467.17
## - deaths 1 30415 487816 467.28
## - Black_or_African_American_alone 1 30531 487932 467.30
## - HouseholdIncome 1 51606 509006 469.41
## - White_alone 1 274482 731883 487.57
##
## Step: AIC=465.39
## confirmed ~ White_alone + Black_or_African_American_alone + HouseholdIncome +
## deaths + Asian_alone
##
## Df Sum of Sq RSS AIC
## + American_Indian_and_Alaska_Native_alone 1 24973 408640 464.43
## - HouseholdIncome 1 10233 443847 464.56
## <none> 433614 465.39
## - Asian_alone 1 23787 457401 466.06
## - Black_or_African_American_alone 1 33415 467029 467.11
## + Native_Hawaiian_and_Other_Pacific_Islander_alone 1 17 433596 467.39
## - deaths 1 53720 487334 469.23
## - White_alone 1 291418 725032 489.10
##
## Step: AIC=464.43
## confirmed ~ White_alone + Black_or_African_American_alone + HouseholdIncome +

```

```
##      deaths + Asian_alone + American_Indian_and_Alaska_Native_alone
##
##
##              Df Sum of Sq    RSS    AIC
## - HouseholdIncome      1      3862 412503 462.90
## <none>                      408640 464.43
## - American_Indian_and_Alaska_Native_alone      1      24973 433614 465.39
## - Asian_alone      1      30909 439550 466.07
## + Native_Hawaiian_and_Other_Pacific_Islander_alone      1         2 408639 466.43
## - Black_or_African_American_alone      1      44852 453493 467.64
## - deaths      1      59879 468520 469.27
## - White_alone      1     249276 657917 486.24
##
## Step:  AIC=462.9
## confirmed ~ White_alone + Black_or_African_American_alone + deaths +
##      Asian_alone + American_Indian_and_Alaska_Native_alone
##
##              Df Sum of Sq    RSS    AIC
## <none>                      412503 462.90
## + HouseholdIncome      1      3862 408640 464.43
## - American_Indian_and_Alaska_Native_alone      1      31345 443847 464.56
## + Native_Hawaiian_and_Other_Pacific_Islander_alone      1         51 412452 464.89
## - Black_or_African_American_alone      1      51235 463738 466.75
## - Asian_alone      1      66859 479361 468.41
## - deaths      1      70052 482555 468.74
## - White_alone      1     260642 673144 485.38
##
## Call:
## lm(formula = confirmed ~ White_alone + Black_or_African_American_alone +
##      deaths + Asian_alone + American_Indian_and_Alaska_Native_alone,
##      data = covidForRegressionSqrt[-c(5), ])
##
## Coefficients:
##              (Intercept)
##              2.954e+02
##              White_alone
##              4.354e-05
##      Black_or_African_American_alone
##              6.140e-05
##              deaths
##              1.254e-02
##              Asian_alone
##              -2.163e-04
## American_Indian_and_Alaska_Native_alone
##              3.813e-04
```

## Comparison

We will select the fewest variable for each set, compare their MSE, and finally select the one with the local minimum MSE.

1. From exhaustive search, the fewest predictors is 4 in smallest BIC (Bayesian Information Criterion).

```
regExhaustive <- lm(confirmed ~ deaths + Asian_alone + Black_or_African_American_alone + White_alone
, data = covidForRegressionSqrt[-c(5),])
```



```
summary(regExhaustive)
```

```
##
## Call:
## lm(formula = confirmed ~ deaths + Asian_alone + Black_or_African_American_alone +
##     White_alone, data = covidForRegressionSQRT[-c(5), ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -232.97  -70.40   13.42   69.35  159.52
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.085e+02  2.043e+01  15.100 < 2e-16 ***
## deaths         1.221e-02  4.703e-03   2.597  0.0127 *
## Asian_alone    -2.135e-04  8.305e-05  -2.570  0.0135 *
## Black_or_African_American_alone  5.296e-05  2.652e-05   1.997  0.0519 .
## White_alone     4.699e-05  8.247e-06   5.698 8.76e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 99.31 on 45 degrees of freedom
## Multiple R-squared:  0.8959, Adjusted R-squared:  0.8866
## F-statistic: 96.79 on 4 and 45 DF,  p-value: < 2.2e-16
```

2. For forward method in sequential search, the fewest predictors is 2 in smallest BIC (Bayesian Information Criterion).

```
regForward <- lm(confirmed ~ Black_or_African_American_alone + White_alone,
                 data = covidForRegressionSQRT[-c(5),])
summary(regForward)
```

```
##
## Call:
## lm(formula = confirmed ~ Black_or_African_American_alone + White_alone,
##     data = covidForRegressionSQRT[-c(5), ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -237.00  -63.71   10.56   80.07  204.06
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.087e+02  2.170e+01  14.228 < 2e-16 ***
## Black_or_African_American_alone  6.614e-05  2.681e-05   2.467  0.0173 *
## White_alone     5.366e-05  6.388e-06   8.400 6.5e-11 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 105.9 on 47 degrees of freedom
## Multiple R-squared:  0.8764, Adjusted R-squared:  0.8711
## F-statistic: 166.6 on 2 and 47 DF,  p-value: < 2.2e-16
```

3. For backward method in sequential search, the fewest predictors is 4 in smallest BIC (Bayesian Information Criterion).

```
regBackward <- lm(confirmed ~ deaths + Asian_alone + Black_or_African_American_alone + White_alone
, data = covidForRegressionSQRT[-c(5),])
summary(regBackward)
```

```
##
## Call:
## lm(formula = confirmed ~ deaths + Asian_alone + Black_or_African_American_alone +
##     White_alone, data = covidForRegressionSQRT[-c(5), ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -232.97  -70.40   13.42   69.35  159.52
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.085e+02  2.043e+01  15.100 < 2e-16 ***
## deaths         1.221e-02  4.703e-03   2.597  0.0127 *
## Asian_alone    -2.135e-04  8.305e-05  -2.570  0.0135 *
## Black_or_African_American_alone  5.296e-05  2.652e-05   1.997  0.0519 .
## White_alone     4.699e-05  8.247e-06   5.698 8.76e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 99.31 on 45 degrees of freedom
## Multiple R-squared:  0.8959, Adjusted R-squared:  0.8866
## F-statistic: 96.79 on 4 and 45 DF,  p-value: < 2.2e-16
```

4. For stepwise method, the lowest AIC value is **462.9**, reporting the best model with 5 variables is: `lm(formula = confirmed ~ White_alone + Black_or_African_American_alone + deaths + Asian_alone + American_Indian_and_Alaska_Native_alone, data = covidForRegressionSQRT[-c(5), ])`.

```
regStepwise <- lm(formula = confirmed ~ White_alone + Black_or_African_American_alone +
deaths + Asian_alone + American_Indian_and_Alaska_Native_alone,
data = covidForRegressionSQRT[-c(5), ])
summary(regStepwise)
```

```
##
## Call:
## lm(formula = confirmed ~ White_alone + Black_or_African_American_alone +
##     deaths + Asian_alone + American_Indian_and_Alaska_Native_alone,
##     data = covidForRegressionSQRT[-c(5), ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -219.089  -71.294    8.229   68.185  164.196
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.954e+02  2.116e+01  13.956 < 2e-16
## White_alone     4.354e-05  8.258e-06   5.273 3.9e-06
## Black_or_African_American_alone  6.140e-05  2.627e-05   2.338 0.02401
## deaths         1.254e-02  4.588e-03   2.734 0.00899
## Asian_alone    -2.163e-04  8.098e-05  -2.670 0.01057
## American_Indian_and_Alaska_Native_alone  3.813e-04  2.085e-04   1.828 0.07426
```

```
##
## (Intercept) ***
## White_alone ***
## Black_or_African_American_alone *
## deaths **
## Asian_alone *
## American_Indian_and_Alaska_Native_alone .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 96.82 on 44 degrees of freedom
## Multiple R-squared:  0.9032, Adjusted R-squared:  0.8922
## F-statistic: 82.13 on 5 and 44 DF,  p-value: < 2.2e-16
```

5. Let us start to find the minimum MSE

```
#calculate MSE
```

```
anova(regExhaustive) %>% tidy() # 9863.275
```

```
## # A tibble: 5 x 6
##   term                df      sumsq  meansq statistic    p.value
##   <chr>             <int>    <dbl>    <dbl>    <dbl>    <dbl>
## 1 deaths              1 3265900. 3265900.    331.  2.25e-22
## 2 Asian_alone          1  55370.   55370.     5.61  2.22e- 2
## 3 Black_or_African_American_alone  1 177072.  177072.    18.0  1.11e- 4
## 4 White_alone          1  320182.  320182.    32.5  8.76e- 7
## 5 Residuals          45 443847.   9863.     NA     NA
```

```
anova(regForward) %>% tidy() # 11211.07
```

```
## # A tibble: 3 x 6
##   term                df      sumsq  meansq statistic    p.value
##   <chr>             <int>    <dbl>    <dbl>    <dbl>    <dbl>
## 1 Black_or_African_American_alone  1 2944490. 2944490.    263.  7.19e-21
## 2 White_alone          1  790959.  790959.    70.6  6.50e-11
## 3 Residuals          47 526920.   11211.     NA     NA
```

```
anova(regBackward) %>% tidy() # 9863.275
```

```
## # A tibble: 5 x 6
##   term                df      sumsq  meansq statistic    p.value
##   <chr>             <int>    <dbl>    <dbl>    <dbl>    <dbl>
## 1 deaths              1 3265900. 3265900.    331.  2.25e-22
## 2 Asian_alone          1  55370.   55370.     5.61  2.22e- 2
## 3 Black_or_African_American_alone  1 177072.  177072.    18.0  1.11e- 4
## 4 White_alone          1  320182.  320182.    32.5  8.76e- 7
## 5 Residuals          45 443847.   9863.     NA     NA
```

```
anova(regStepwise) %>% tidy() # 9375.065
```

```
## # A tibble: 6 x 6
##   term                df      sumsq  meansq statistic    p.value
##   <chr>             <int>    <dbl>    <dbl>    <dbl>    <dbl>
## 1 White_alone          1 3667200.  3.67e6    391.  1.60e-23
## 2 Black_or_African_American_alone  1  68250.   6.83e4     7.28  9.85e- 3
## 3 deaths              1  17914.   1.79e4     1.91  1.74e- 1
## 4 Asian_alone          1  65159.   6.52e4     6.95  1.15e- 2
```

```
## 5 American_Indian_and_Alaska_Native_~      1   31345.   3.13e4      3.34   7.43e- 2
## 6 Residuals                                44  412503.   9.38e3      NA     NA
```

## Final Selection

regStepwise has the smallest MSE value (9375.065) so we select it as the best model. Therefore, our final predictors of square root of COVID confirmed cases by US States is deaths, White\_alone, Black\_or\_African\_American\_alone, Asian\_alone and American\_Indian\_and\_Alaska\_Native\_alone.

```
finalReg <- lm(formula = confirmed ~ White_alone + Black_or_African_American_alone +
  deaths + Asian_alone + American_Indian_and_Alaska_Native_alone,
  data = covidForRegressionSQRT[-c(5), ])
summary(finalReg)
```

```
##
## Call:
## lm(formula = confirmed ~ White_alone + Black_or_African_American_alone +
##     deaths + Asian_alone + American_Indian_and_Alaska_Native_alone,
##     data = covidForRegressionSQRT[-c(5), ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -219.089  -71.294    8.229   68.185  164.196
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.954e+02  2.116e+01  13.956 < 2e-16
## White_alone     4.354e-05  8.258e-06   5.273  3.9e-06
## Black_or_African_American_alone  6.140e-05  2.627e-05   2.338  0.02401
## deaths          1.254e-02  4.588e-03   2.734  0.00899
## Asian_alone     -2.163e-04  8.098e-05  -2.670  0.01057
## American_Indian_and_Alaska_Native_alone  3.813e-04  2.085e-04   1.828  0.07426
##
## (Intercept)          ***
## White_alone           ***
## Black_or_African_American_alone      *
## deaths                 **
## Asian_alone            *
## American_Indian_and_Alaska_Native_alone .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 96.82 on 44 degrees of freedom
## Multiple R-squared:  0.9032, Adjusted R-squared:  0.8922
## F-statistic: 82.13 on 5 and 44 DF,  p-value: < 2.2e-16
```

## Model Equation

### Interpretation

With the large p-value 0.07426 of  $b_5$ , the predictor American\_Indian\_and\_Alaska\_Native\_alone is not in the significant level. In other words, we fail to reject the null ( $H_0: \beta_5 = 0$  cannot be rejected) so we can conclude  $b_5$  is 0. Therefore,  $b_5$  can be dropped from the model.

## Linear Equation

Thus, the expected value of square root of confirmed cases is:

$$\sqrt{\hat{Confirmed}} = 295.4 + 0.00004354White + 0.0000614Black + 0.01254Deaths - 0.0002163Asian$$

## References

- (1) Sehra, S., Fundin, S., Lavery, C., & Baker, J. (2020). Differences in race and other state-level characteristics and associations with mortality from COVID-19 infection. *Journal of Medical Virology*, 92(11), 2406–2408. <https://doi.org/10.1002/jmv.26095>
- (2) Sa, Filipa G., Socioeconomic Determinants of Covid-19 Infections and Mortality: Evidence from England and Wales (May 2020). CEPR Discussion Paper No. DP14781, Available at SSRN: <https://ssrn.com/abstract=3612850>