

**[Turn over**

A coordinate plane with x and y axes ranging from 0 to 9. A grid is shown. Two triangles are plotted:  $\triangle ABC$  and  $\triangle A'B'C'$ . The vertices of  $\triangle ABC$  are  $A(1, 3)$ ,  $B(2, 5)$ , and  $C(4, 4)$ . The vertices of  $\triangle A'B'C'$  are  $A'(2, 1)$ ,  $B'(4, 3)$ , and  $C'(8, 2)$ . The triangles are similar, with  $\triangle A'B'C'$  being a dilation of  $\triangle ABC$  by a factor of 2.

State fully the two transformations.

[illegible]

- 2** The function  $f$  is defined for  $x \in \mathbb{R}$  by  $f(x) = x^2 - 6x + c$ , where  $c$  is a constant. It is given that  $f(x) > 2$  for all values of  $x$ .

Find the set of possible values of  $c$ .

[4]

This image shows a full page of primary-ruled paper. It features approximately 20 horizontal dashed lines spaced evenly down the page, providing a guide for handwriting practice. The background is white, and there are no margins or other markings present.

- 3 (a)** Give the complete expansion of  $\left(x + \frac{2}{x}\right)^5$ . [2]

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- (b)** In the expansion of  $(a + bx^2)\left(x + \frac{2}{x}\right)^5$ , the coefficient of  $x$  is zero and the coefficient of  $\frac{1}{x}$  is 80.

Find the values of the constants  $a$  and  $b$ . [4]

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- 4 (a) Show that the equation

$$3 \tan^2 x - 3 \sin^2 x - 4 = 0$$

may be expressed in the form  $a \cos^4 x + b \cos^2 x + c = 0$ , where  $a$ ,  $b$  and  $c$  are constants to be found. [3]

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- (b) Hence solve the equation  $3 \tan^2 x - 3 \sin^2 x - 4 = 0$  for  $0^\circ \leq x \leq 180^\circ$ . [4]

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- 5** A circle has equation  $(x - 1)^2 + (y + 4)^2 = 40$ . A line with equation  $y = x - 9$  intersects the circle at points  $A$  and  $B$ .

**(a)** Find the coordinates of the two points of intersection. [4]

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**(b)** Find an equation of the circle with diameter  $AB$ . [3]

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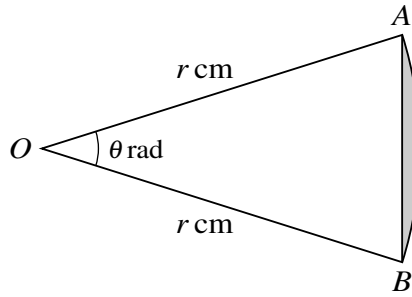
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The diagram shows a sector  $OAB$  of a circle with centre  $O$  and radius  $r$  cm. Angle  $AOB = \theta$  radians. It is given that the length of the arc  $AB$  is 9.6 cm and that the area of the sector  $OAB$  is  $76.8 \text{ cm}^2$ .

- (a) Find the area of the shaded region. [5]

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- (b) Find the perimeter of the shaded region. [2]

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- 7 The function  $f$  is defined by  $f(x) = 2 - \frac{5}{x+2}$  for  $x > -2$ .

(a) State the range of  $f$ .

[1]

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**(b)** Obtain an expression for  $f^{-1}(x)$  and state the domain of  $f^{-1}$ .

[4]

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



(c) Obtain an expression for  $fg(x)$  giving your answer in the form  $\frac{ax+b}{cx+d}$ , where  $a$ ,  $b$ ,  $c$  and  $d$  are integers. [3]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- 8** A progression has first term  $a$  and second term  $\frac{a^2}{a+2}$ , where  $a$  is a positive constant.
- (a)** For the case where the progression is geometric and the sum to infinity is 264, find the value of  $a$ . [5]

[illegible]

[illegible]

- 9 A curve which passes through  $(0, 3)$  has equation  $y = f(x)$ . It is given that  $f'(x) = 1 - \frac{2}{(x-1)^3}$ .

**(a)** Find the equation of the curve.

[4]

[illegible]

The tangent to the curve at  $(0, 3)$  intersects the curve again at one other point,  $P$ .

- (b) Show that the  $x$ -coordinate of  $P$  satisfies the equation  $(2x + 1)(x - 1)^2 - 1 = 0$ . [4]

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- (c) Verify that  $x = \frac{3}{2}$  satisfies this equation and hence find the  $y$ -coordinate of  $P$ . [2]

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The graph shows a Cartesian coordinate system with a curve defined by the equation  $y = 9x - (2x + 1)^{\frac{3}{2}}$ . A straight line segment (chord) connects two points on the curve, labeled A and B. Point A has coordinates  $(1\frac{1}{2}, 5\frac{1}{2})$  and point B has coordinates  $(7\frac{1}{2}, 3\frac{1}{2})$ . The region bounded by the curve and the chord AB is shaded in light gray.

(a) Find the coordinates of the maximum point of the curve. [4]

[illegible]

- (b) Verify that the line  $AB$  is the normal to the curve at  $A$ . [3]

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- (c) Find the area of the shaded region. [5]

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## Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

[illegible]

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