

[Turn over

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- 1 (a)** Expand $(1 + 3x)^6$ in ascending powers of x up to, and including, the term in x^2 . [2]

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- (b)** Hence find the coefficient of x^2 in the expansion of $(1 - 7x + x^2)(1 + 3x)^6$. [2]

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- Showing all necessary working, determine which of the following statements is correct.

- C** The line and curve do not intersect for any values of c .

[4]

This image shows a single page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

A 3D diagram of a rectangular prism. The front-left vertical edge is labeled x . The bottom-left horizontal edge is labeled x . The bottom-right receding edge is labeled x .

[3]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, leaving ample room for writing practice. There is no text or other markings on the page.

- 4** The transformation R denotes a reflection in the x -axis and the transformation T denotes a translation of $\begin{pmatrix} 3 \\ -1 \end{pmatrix}$.

- (a)** Find the equation, $y = g(x)$, of the curve with equation $y = x^2$ after it has been transformed by the sequence of transformations R followed by T. [2]

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- (b)** Find the equation, $y = h(x)$, of the curve with equation $y = x^2$ after it has been transformed by the sequence of transformations T followed by R. [2]

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- (c)** State fully the transformation that maps the curve $y = g(x)$ onto the curve $y = h(x)$. [2]

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- 5 (a) Show that the equation

$$4 \sin x + \frac{5}{\tan x} + \frac{2}{\sin x} = 0$$

may be expressed in the form $a \cos^2 x + b \cos x + c = 0$, where a , b and c are integers to be found. [3]

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- (b) Hence solve the equation $4 \sin x + \frac{5}{\tan x} + \frac{2}{\sin x} = 0$ for $0^\circ \leq x \leq 360^\circ$. [3]

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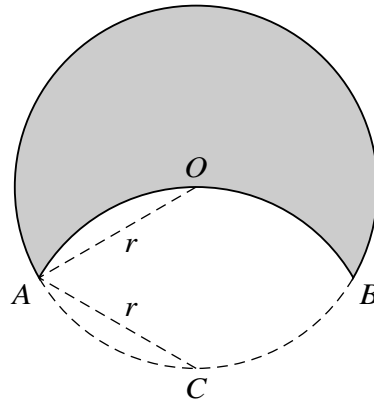
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The diagram shows a motif formed by the major arc AB of a circle with radius r and centre O , and the minor arc AOB of a circle, also with radius r but with centre C . The point C lies on the circle with centre O .

- (a) Given that angle $ACB = k\pi$ radians, state the value of the fraction k . [1]

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- (b) State the perimeter of the shaded motif in terms of π and r . [1]

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This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

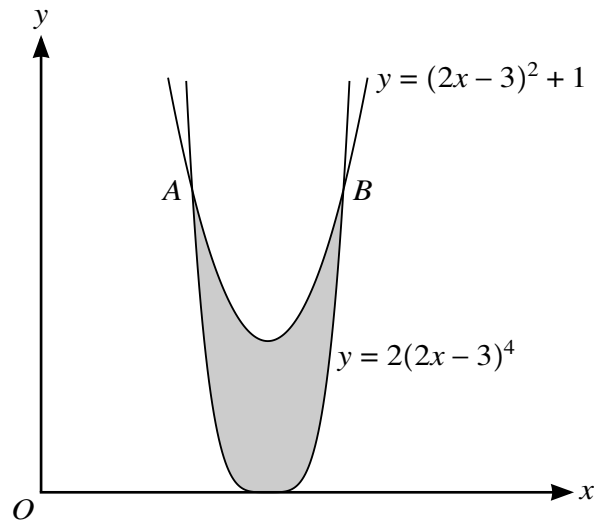
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- 7 The sum of the first two terms of a geometric progression is 15 and the sum to infinity is $\frac{125}{7}$. The common ratio of the progression is negative.

Find the third term of the progression.

[7]

This image shows a full page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page, typical of notebook or legal stationery. There are no margins, text, or other markings on the page.



The diagram shows the curves with equations $y = 2(2x - 3)^4$ and $y = (2x - 3)^2 + 1$ meeting at points A and B.

- (a) By using the substitution $u = 2x - 3$ find, by calculation, the coordinates of A and B. [4]

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(b) Find the exact area of the shaded region.

[5]

[illegible]

- 9 (a) Express $4x^2 - 12x + 13$ in the form $(2x + a)^2 + b$, where a and b are constants. [2]

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The function f is defined by $f(x) = 4x^2 - 12x + 13$ for $p < x < q$, where p and q are constants. The function g is defined by $g(x) = 3x + 1$ for $x < 8$.

- (b) Given that it is possible to form the composite function gf , find the least possible value of p and the greatest possible value of q . [3]

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(c) Find an expression for $gf(x)$.

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The function h is defined by $h(x) = 4x^2 - 12x + 13$ for $x < 0$.

(d) Find an expression for $h^{-1}(x)$.

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- 10** A curve has a stationary point at $(2, -10)$ and is such that $\frac{d^2y}{dx^2} = 6x$.

(a) Find $\frac{dy}{dx}$. [3]

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(b) Find the equation of the curve. [3]

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- (c) Find the coordinates of the other stationary point and determine its nature. [3]

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- (d) Find the equation of the tangent to the curve at the point where the curve crosses the y-axis. [2]

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(a) Find the equation of the line AB , giving the answer in the form $y = mx + c$. [3]

[illegible]

(b) Find the coordinates of A , giving each coordinate in surd form.

[4]

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(c) Find the equation of the tangent at A , giving the answer in the form $y = mx + c$, where c is in surd form.

[2]

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This image shows a full page of a worksheet designed for handwriting practice. It consists of multiple horizontal rows, each defined by two parallel dashed lines. The lines are evenly spaced and extend across the entire width of the page, providing a guide for letter height and placement. There is no text or other markings on the page.

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