Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/11

Paper 1 Pure Mathematics 1

October/November 2022

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

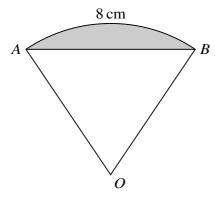
This document has 20 pages.

Solve the equation $3x + 2 = \frac{2}{x - 1}$.	[3

(a)	Find the equation of the tangent to the curve at P .	[2]
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(b)	Find the equation of the curve.	[4]
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Find the y-coordinate	of P.		[5]

ind the possible values of the constant p .	[6]



The diagram shows a sector OAB of a circle with centre O. The length of the arc AB is 8 cm. It is given that the perimeter of the sector is 20 cm.

)	Find the perimeter of the shaded segment.	[4]
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(b)	Find the area of the shaded segment.	[2]
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6	(a)	Show	that	the	equation

$\frac{1}{\sin\theta + \cos\theta} + \frac{1}{\sin\theta - \cos\theta} = 1$
may be expressed in the form $a \sin^2 \theta + b \sin \theta + c = 0$, where a , b and c are constants to be found.

) H	Hence solve the equati	$ \frac{1}{\sin\theta + \cos\theta} $	$+\frac{1}{\sin\theta-\cos\theta}=$	= 1 for $0^{\circ} \le \theta \le 360^{\circ}$.	[3
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A tool for putting fence posts into the ground is called a 'post-rammer'. The distances in millimetres

1)	Verify that the 9th impact is the first in which the post sinks less than 10 mm into the ground

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8	The function f is defined by $f(x) = 2$	$-\frac{3}{4x-p}$	for $x >$	$\frac{p}{4}$, where p is	a constant.
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neither.										
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	Express $f^{-1}(x)$ in the form $\frac{p}{a} - \frac{b}{cx - d}$, where a, b, c and d are integers.
•	
	Hence state the value of p for which $f^{-1}(x) \equiv f(x)$.

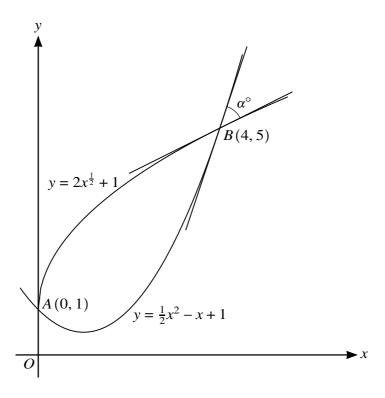
9	Functions	f and g	are both	defined t	for $x \in \mathbb{R}$	and are	given	by

$$f(x) = x^{2} - 4x + 9,$$

$$g(x) = 2x^{2} + 4x + 12.$$

(a)	Express $f(x)$ in the form $(x - a)^2 + b$.	[1]
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		•••••
(b)	Express $g(x)$ in the form $2[(x+c)^2+d]$.	[2]
		•••••

	Express $g(x)$ in the form $kf(x + h)$, where k and h are integers.	[1]
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,		•••••
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1	Describe fully the two transformations that have been combined to transform the graph of	of $y = f(x)$
	Describe fully the two transformations that have been combined to transform the graph to the graph of $y = g(x)$.	of $y = f(x)$
		[4]
	to the graph of $y = g(x)$.	[4]
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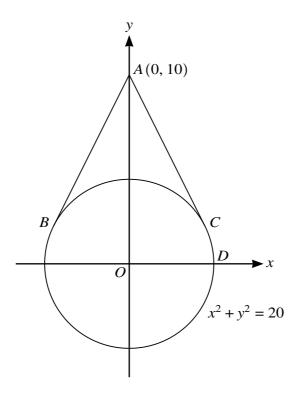


Curves with equations $y = 2x^{\frac{1}{2}} + 1$ and $y = \frac{1}{2}x^2 - x + 1$ intersect at A(0, 1) and B(4, 5), as shown in the diagram.

(a)	Find the area of the region between the two curves.	[5]
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The acute angle between the two tangents at B is denoted by α° , and the scales on the axes are the same.

Find α .	
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The diagram shows the circle with equation $x^2 + y^2 = 20$. Tangents touching the circle at points *B* and *C* pass through the point *A* (0, 10).

By letting the equation of a tangent be $y = mx + 10$, find the two possible values of m. [4]

Find the coordinates of B and C .	[3
	•••••
	•••••
point D is where the circle crosses the positive x -axis.	ra
point D is where the circle crosses the positive x -axis. Find angle BDC in degrees.	[3
	[3
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	[3
Find angle BDC in degrees.	

Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

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