Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

MATHEMATICS 9709/13

Paper 1 Pure Mathematics 1

October/November 2021

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages. Any blank pages are indicated.

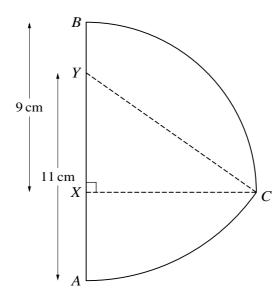
Describe fully,	in the correct orde	r, the two trans	sformations that	have been combined.	[4
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2	(a)	Find the first three terms, in ascending powers of x, in the expansion of $(1 + ax)^6$.	[1]
			••••
			••••
	(b)	Given that the coefficient of x^2 in the expansion of $(1-3x)(1+ax)^6$ is -3 , find the possible value of the constant a .	ues [4]
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a)	Express $5y^2 - 30y + 50$ in the form $5(y + a)^2 + b$, where a and b are constants.	[2]
		•••••
		•••••
)	The function f is defined by $f(x) = x^5 - 10x^3 + 50x$ for $x \in \mathbb{R}$.	
	Determine whether f is an increasing function, a decreasing function or neither.	[3]
		•••••
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a)	Find the smallest value of n for which the n th term is negative.	[2
	s given that the sum of the first $2k$ terms of this progression is equal to the sum of the first the value of k .	

(a)

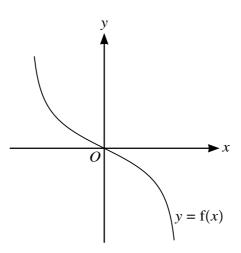


In the diagram, X and Y are points on the line AB such that BX = 9 cm and AY = 11 cm. Arc BC is part of a circle with centre X and radius 9 cm, where CX is perpendicular to AB. Arc AC is part of a circle with centre Y and radius Y and Y cm.

Show that angle $XYC = 0.9582$ radians, correct to 4 significant figures.	[1]
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b)	Find the perimeter of <i>ABC</i> .	[6]

(b)



The diagram shows the graph of y = f(x).

(a) On this diagram sketch the graph of $y = f^{-1}(x)$. [1]

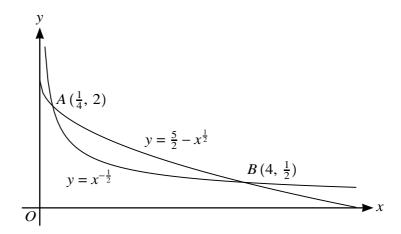
It is now given that $f(x) = -\frac{x}{\sqrt{4 - x^2}}$ where -2 < x < 2.

Find an expression for $f^{-1}(x)$.	[4]

The	function g is defined by $g(x) = 2x$ for $-a < x < a$, where a is a constant.	
(c)	State the maximum possible value of <i>a</i> for which fg can be formed.	[1]
		••••••
(4)	A comming that for each be forward for day deignalify an expression for fo(a)	[2]
(a)	Assuming that fg can be formed, find and simplify an expression for $fg(x)$.	[2]
		••••••

7	(a)	Show that the equation	$\frac{\tan x + \cos x}{\tan x - \cos x} = k$, where k is a constant, can be expressed as	
			$(k+1)\sin^2 x + (k-1)\sin x - (k+1) = 0.$	4]
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(b)	Hence solve the equation	$\frac{\tan x + \cos x}{\tan x - \cos x} = 4 \text{ for } 0^{\circ} \leqslant x \leqslant 360^{\circ}.$	[4]
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The diagram shows the curves with equations $y = x^{-\frac{1}{2}}$ and $y = \frac{5}{2} - x^{\frac{1}{2}}$. The curves intersect at the points $A\left(\frac{1}{4}, 2\right)$ and $B\left(4, \frac{1}{2}\right)$.

Find the area of the region between the two curves.	[6]

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1)	Find the coordinates of A and B in surd form and hence find the exact length of the chord AB

A straight line through the point (10, 0) with gradient m is a tangent to the circle.

F	Find the two possible values of m .	[5]
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10 A curve has equation y = f(x) and it is given that

$$f'(x) = (\frac{1}{2}x + k)^{-2} - (1 + k)^{-2},$$

where k is a constant. The curve has a minimum point at x = 2.

	ms of k and x , and hence find the set of possible values	of k .
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s now given that k	= -3 and the minimum point is at $(2, 3\frac{1}{2})$.	
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s now given that k Find $f(x)$.	= -3 and the minimum point is at $(2, 3\frac{1}{2})$.	
Find $f(x)$.	$= -3$ and the minimum point is at $(2, 3\frac{1}{2})$.	
Find $f(x)$.		

(c) Find the coordinates of the other stationary point and determine its nature.	••••
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Additional Page

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