Assignment 1

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Download all python codes from

https://github.com/tyagio/AI1103/tree/main/assignment1/codes

and latex-tikz codes from

https://github.com/tyagio/AI1103/tree/main/assignment1/assignment1.tex

1 Problem

Suppose that two cards are drawn at random from a deck of cards.Let X be the number of aces obtained.Then the value of E(X) is

- 1) 37/221
- 2) 5/13
- 3) 1/13
- 4) 2/13

2 Solution

Total number of cards =52 with 4 aces,48 non-ace's and we need to select 2 cards so X can be 0 ,1 or 2

Case 1: X = 0

$$Pr(X = 0) = \frac{\text{ways of selecting 2 non-ace's}}{\text{total ways of selecting 2 cards}}$$

$$Pr(X = 0) = \frac{\binom{48}{2}}{\binom{52}{2}} = \frac{24.47}{26.51}$$

Case 2: X = 1

$$Pr(X = 1) = \frac{\text{ways of selecting 1 ace and 1 non-ace}}{\text{total ways of selecting 2 cards}}$$

$$Pr(X = 1) = \frac{\binom{4}{1} \cdot \binom{48}{1}}{\binom{52}{2}} = \frac{48.4}{26.51}$$

Case 3: X = 2

$$Pr(X = 2) = \frac{\text{ways of selecting 2 aces}}{\text{total ways of selecting 2 cards}}$$

$$Pr(X = 2) = \frac{\binom{4}{2}}{\binom{52}{2}} = \frac{6}{26.51}$$

now we know that E(X) is given by

$$E(X) = \sum_{i=0}^{2} X.P(X)$$

X	0	1	2
P(X)	24.47 26.51	$\frac{48.4}{26.51}$	$\frac{6}{26.51}$
X.P(X)	0	<u>48.4</u> 26.51	26.51

$$\implies E(X) = \frac{48.4}{26.51} + \frac{12}{26.51} = \frac{192+12}{26.51} = \frac{2}{13}$$

Final answer E(x) = 2/13 or option 4