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Assignment 2

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Download all python codes from

https://github.com/tyagio/AI1103/tree/main/assignment2/codes

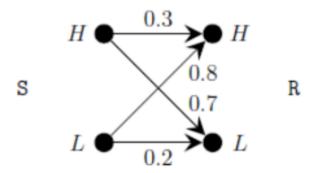
and latex-tikz codes from

https://github.com/tyagio/AI1103/tree/main/assignment2/assignment2.tex

1 Problem

A sender(S) transmits a signal, which can be one of two kinds: H and L with probabilities 0.1 and 0.9 respectively, to a receiver (R).

In the graph below,the weight of an edge(u,v) is the probability of receiving v when u is transmitted,where u,v \in {H,L}.For example the probability that the received signal is L given the transmitted signal is H is 0.7.



If the received signal is H, the probability that the transmitted signal was H is _____ ?

2 Solution

Let $A \in \{0, 1\}$ represent the random variable, where 0 represents H being transmitted, 1 represents L being transmitted.

Let $B \in \{0, 1\}$ represent the random variable, where 0 represents H being received, 1 represents L being received.

TABLE 0: Probability for random variables

Pr(A=0)	0.1	Pr(A=1)	0.9
$\Pr\left(B = 0 A = 0\right)$	0.3	$\Pr\left(B = 0 A = 1\right)$	0.8
$\Pr\left(B=1 A=0\right)$	0.7	$\Pr\left(B=1 A=1\right)$	0.2

Now we need to find Pr(A = 0|B = 0)Using Bayes theorem

$$\Pr(A = 0|B = 0) = \frac{\Pr(A = 0) \times \Pr(B = 0|A = 0)}{\sum_{i=0}^{1} \Pr(A = i) \times \Pr(B = 0|A = i)}$$
(2.0.1)

Putting in values given in question

$$\Pr(A = 0|B = 0) = \frac{1}{25} = 0.04 \tag{2.0.2}$$

The probability that transmitted signal was H is 0.04