

**1. [8%] General AI Knowledge and Application.**

1	<input type="radio"/> T	<input type="radio"/> F
2	<input type="radio"/> T	<input type="radio"/> F
3	<input type="radio"/> T	<input type="radio"/> F
4	<input type="radio"/> T	<input type="radio"/> F
5	<input type="radio"/> T	<input type="radio"/> F
6	<input type="radio"/> T	<input type="radio"/> F
7	<input type="radio"/> T	<input type="radio"/> F
8	<input type="radio"/> T	<input type="radio"/> F

**T, 1).** [1%]

**F, 2).** [1%]

**F, 3).** [1%]

**F, 4).** [1%]

**T, 5).** [1%]

**T, 6).** [1%]

**F, 7).** [1%]

**T, 8).** [1%]

**2.[16%] Multiple Choice**

1. (abce)
2. (abd)
3. (ad)
4. (b)
5. (c)
6. (a)
7. (bde)
8. (b)

### **3.[23%] MDPs and RL: Mini-Grids**

#### **3A. [1%]**

10

(No partial credits)

#### **3B. [1%]**

2

(No partial credits)

#### **3C. [1%]**

1

(No partial credits)

#### **3D. [1%]**

4

(No partial credits)

#### **3E. [1%]**

10/8

Or

1.25

(No partial credits)

#### **3F. [2%]**

$$1/\sqrt{10} \leq \gamma \leq 1$$

Or

$$1/\sqrt{10} < \gamma \leq 1$$

Or

$$1/\sqrt{10} < \gamma$$

Or

$$\gamma^2 > 0.1$$

Or

$$\gamma^2 \geq 0.1$$

(No partial credits)

**3G. [1%]**

10

(No partial credits)

**3H. [1%]**

4

(No partial credits)

**3I. [1%]**

10/8

Or

1.25

(No partial credits)

**3J. [1%]**

Never.(1pt, no partial credits)

There is always only a  $1/2$  probability of success on any movement action, so while  $V_k$  will asymptotically approach  $V^*$ , it won't ever equal it. Consider the square right next to the exit, which we'll call C:  $V_{k+1}(C) = 10/2 + (1/2) * V_k(C)$ .

**3K. [1%]**

$1/8$

Or

0.125

(No partial credits)

**3L. [1%]**

$1/8$

Or

0.125

(No partial credits)

**3M. [1%]**

4

(No partial credits)

**3N. [2%]**

$$16/2 + 4/2 = 10$$

(No partial credits)

**30. [2%]**

4

(No partial credits)

**3P. [2%]**

16

(No partial credits)

**4.[18%] Bayes Net**

**4A.[3%]**

$$P(+g)P(+a \mid +g)P(+b)P(+s \mid +b, +a) = (0.1)(1.0)(0.4)(1.0) = 0.04$$

Full credit if expression is correct. -0.5 if the final answer is incorrect.

**4B.[3%]**

$$P(+a) = P(+a \mid +g)P(+g) + P(+a \mid -g)P(-g) = (1.0)(0.1) + (0.1)(0.9) = 0.19$$

Full credit if expression is correct. -0.5 if the final answer is incorrect.

**4C.[3%]**

$P(+a \mid +b) = P(+a) = 0.19$  The first equality holds true as we have  $A \perp\!\!\!\perp B$ , which can be inferred from the graph of the Bayes' net.

Full credit if expression is correct. -0.5 if the final answer is incorrect.

**4D.[3%]**

$$\begin{aligned} P(+a \vee +b \mid +s) &= 1 - P(-a, -b \mid +s) = 1 - \frac{P(-a, -b, +s)}{P(+s)} = 1 - \frac{P(+s \mid -a, -b)P(-a)P(-b)}{P(+s)} \\ &= 1 - \frac{P(+s \mid -a, -b)P(-a)P(-b)}{P(+s \mid +a+b)P(+a)P(+b) + P(+s \mid +a-b)P(+a)P(-b) + P(+s \mid -a+b)P(-a)P(+b) + P(+s \mid -a-b)P(-a)P(-b)} \\ &= 1 - \frac{0.1*0.81*0.6}{1.0*0.19*0.4 + 0.9*0.19*0.6 + 0.8*0.81*0.4 + 0.1*0.81*0.6} \approx 0.9001 \end{aligned}$$

Full credit if expression is correct. -0.5 if the final answer is incorrect. Expansion of all the terms carry 1 point each.

**4E.[3%]**

$$P(+g|+a) = \frac{P(+g)P(+a|+g)}{P(+g)P(+a|+g) + P(-g)P(+a|-g)} = 0.5263$$

$$P(+g|+a) \text{ (1\%)}, \frac{P(+g)P(+a|+g)}{P(+g)P(+a|+g) + P(-g)P(+a|-g)} \text{ (2\%)}, 0.5263 \text{ is optional.}$$

You can still get 1%, if you write part of the  $\frac{P(+g)P(+a|+g)}{P(+g)P(+a|+g) + P(-g)P(+a|-g)}$ .

You get 3% if you calculate 0.5263 correctly.

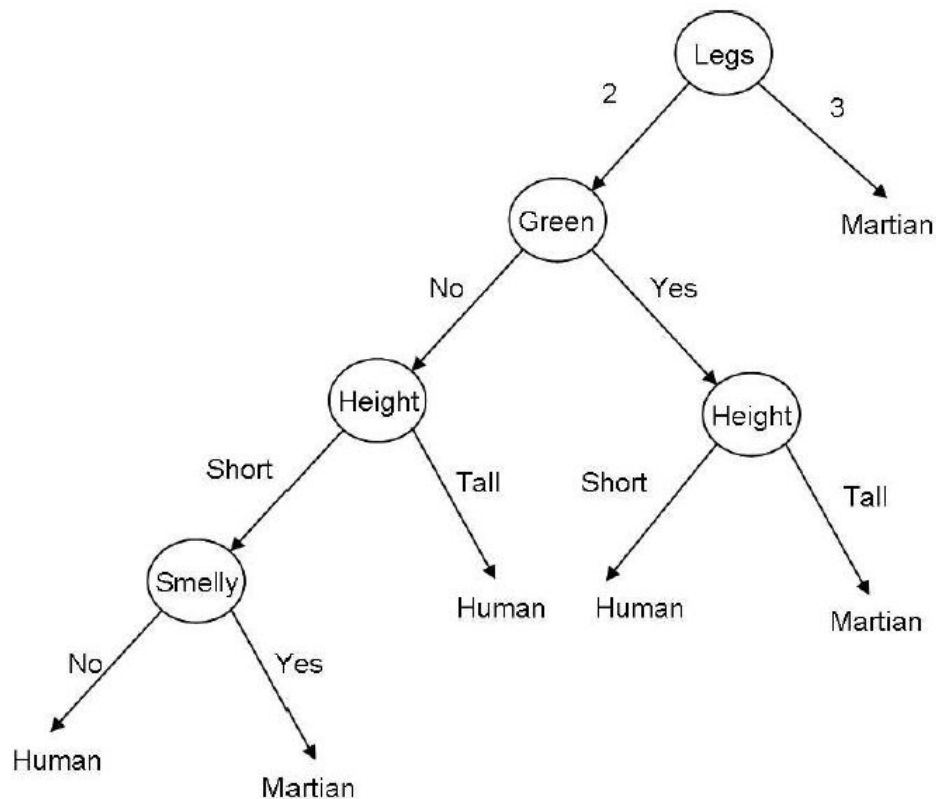
**4F.[3%]**

$P(+g|+b) = P(+g) = 0.1$  The first equality holds true as we have  $G \perp\!\!\!\perp B$ , which can be inferred from the graph of the Bayes' net.

$P(+g|+b)$  (1%),  $P(+g)$  (2%), 0.1 is optional.

You get 3% if you calculate 0.1 correctly.

**5.[20%] Decision Tree****5A.[8%]**



0.5 point off for every incorrect leaf.

2 points for getting Legs as the root node, because that a grasp of information gain, and then back to 1 point for the other branches.

All deductions up to 8 points total.

**5B. [6%]**

Only the disjunction of conjunctions for Martians was required.

$(\text{Legs}=3) \vee$

$(\text{Legs}=2 \wedge \text{Green}=\text{Yes} \wedge \text{Height}=\text{Tall}) \vee$

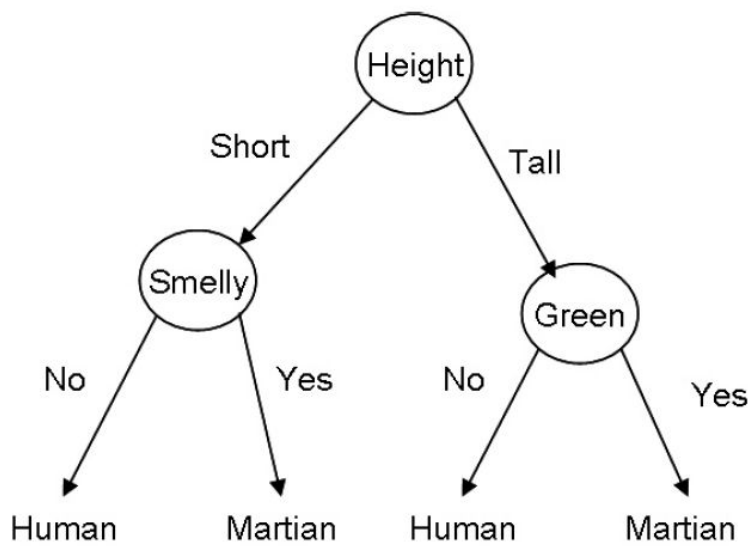
$(\text{Legs}=2 \wedge \text{Green}=\text{No} \wedge \text{Height}=\text{Short} \wedge \text{Smelly}=\text{Yes})$

partial credit: 2 points each line.

**5C. [6%]**

$(\text{Green}=\text{Yes} \wedge \text{Height}=\text{Tall}) \vee (\text{Smelly}=\text{Yes} \wedge \text{Height}=\text{Short})$  These conjunctive rules share the height term, so a depth-2 tree is possible. See the figure below.

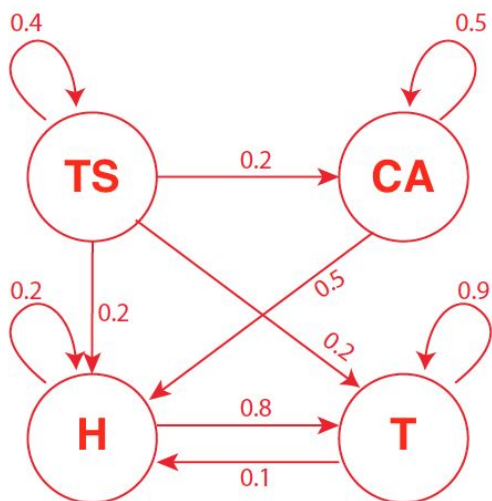
If only give the “yes” answer without correct explanation, no partial credits.



## 6.[18%] HMM

### 6A. [8%]

(Green=Yes ^ Height=Tall) V (Smelly=



	$TS_{t+1}$	$CA_{t+1}$	$H_{t+1}$	$T_{t+1}$
$TS_t$	0.4	0.2	0.2	0.2
$CA_t$	0	0.5	0.5	0
$H_t$	0	0	0.2	0.8
$T_t$	0	0	0.1	0.9

**Partial Credits:**

- Total 4 Points for the markov chain graph with 1 point for each entry(node).
- 4 points for the transition probability table - 1 point for each entry in the table.

**6B. [4%]**

	$P(X_0)$	$P(X_{Mon})$	$P(X_{Tue})$
TS	0	0	$0*0.4+0.5*0+0.5*0+0*0 = 0$
CA	1	0.5	$0*0.2+0.5*0.5+0.5*0+0*0 = 0.25$
H	0	0.5	$0*0.2+0.5*0.5+0.5*0.2+0*0.1 = 0.35$
T	0	0	$0*0.2+0.5*0+0.5*0.8+0*0.9 = 0.4$

**Partial Credits - 0.5 points for each correct probability(total 8) computed in the table.  $0.5 * 8 = 4$**

**6C. [6%]**



The goal is to compute the stationary distribution. From the Markov chain it is obvious that  $P_{\infty}(TS) = 0$  and  $P_{\infty}(CA) = 0$ . Let  $x = P_{\infty}(H)$  and  $y = P_{\infty}(T)$ .

Then the definition of stationarity implies

$$x = 0.2x + 0.1y$$

$$y = 0.8x + 0.9y$$

Since we must have  $x \geq 0$  and  $y \geq 0$ , we can choose any  $x > 0$  and solve for  $y$ . For example,  $x = 1$  yields  $y = 8$ , which normalized results in  $x = P_{\infty}(H) = 1/9$  and  $y = P_{\infty}(T) = 8/9$ .

**Partial Credits:**

**2 Points for pointing out the equations.**

**2 Points for computing the probability.**

**2 Points for the logic.**