## 1- General Concepts:

1-T 2-T 3-F 4-F 5-F 6-F 7-F 8-T 9-F 10-T 11-F 12-T

13-part of 14- does not infer false statements 15- derives any sentence that is entailed

16- valid 17- a  $\land \neg b$  18- horn 19- backward 20-tautology

#### 2- Truth tables:

a)

А	В	С	А∧В	$\alpha$ = (A $\wedge$ B) V	¬C	A ∨ ¬C	вУс	KB= (A ∨ ¬C) ∧ (B ∨ C)
Т	Т	Т	Т	Т	F	Т	Т	Т
Т	Т	F	Т	Т	Т	Т	Т	Т
Т	F	Т	F	Т	F	Т	Т	Т
Т	F	F	F	F	Т	Т	F	F
F	Т	Т	F	Т	F	F	Т	F
F	Т	F	F	F	Т	Т	Т	Т
F	F	Т	F	Т	F	F	Т	F
F	F	F	F	F	Т	Т	F	F

Rubrics: each row one point.

b) No, in the colored row, the KB is true but  $\,lpha\,$  is not. So KB does not entail  $\,lpha\,$  .

Rubrics: no partial credit.

### 3- Propositional logic

a) 
$$\neg ((A \Rightarrow B) \Rightarrow (((P^B) \Rightarrow Q) \lor R))$$
  
 $\neg (\neg (A \Rightarrow B) \lor (\neg (P^B) \lor Q \lor R))$   
 $\neg (\neg (\neg A \lor B) \lor (\neg P \lor \neg B \lor Q \lor R))$ 

$$(\neg A \lor B) \land P \land B \land \neg Q \land \neg R$$

b)

- Modus tollens on 3,4  $\Rightarrow$  ¬study (2 points)
- And Introduction on 6,7  $\Rightarrow$  HomewykDueNextWeek  $\land$  HighWeightageOfHomewyk (11)

Modus Ponens on 2,11 ⇒ WvkOnHW (4 points)

• Modus tollens on 1,8  $\Rightarrow$  ¬ExamNextWeek (12)

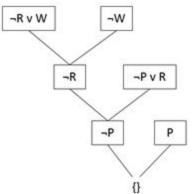
Modus tollens on  $5,12 \Rightarrow \neg StudyBreak$  (4 points)

Rubrics: every method except using inference rules got half points. Not mentioning the name of the inference rule is -1 in each part.

c) To prove W, we add ¬W to the KB:

$$KB : \neg W, P, \neg Q, \neg P \lor R, \neg Q \lor W, \neg W \lor P, \neg R \lor W$$

Rubrics: other solutions also exist.



#### **4- First Order Logic**

1- (blue texts are the answer with this assumption that fails(x,y,z) also implies that takes(x,y,z)

a)  $\forall$  x,z ( (Student(x)  $\land$  Semester(z))  $\Rightarrow$   $\exists$  y,t ( Course(y)  $\land$  Course(t)  $\land$  Takes(x,y,z)  $\land$  Takes(x,t,z)  $\land$  y $\neq$ t))

b)  $\exists x \text{ (Student(x) } \land \text{ takes(x,History,S2015) } \land \text{ Failed(x, History,S2015) } \land \forall y \text{ (Student(y) } \land \text{ takes(y,History,S2015) } \land \text{ Failed(y, History,S2015)} \Rightarrow x = y \text{ ))}$ 

 $\exists x (Student(x) \land Failed(x, History, S2015) \land \forall y (Student(y) \land Failed(y, History, S2015) \Rightarrow x = y))$ 

 $\exists$  x (Student(x)  $\land$  Failed(x, History,S2015)  $\land$   $\forall$  y (x $\neq$ y  $\land$  Student(y)  $\Rightarrow$  ¬Failed(y, History,S2015) ))

c)  $\neg \exists x (Student(x) \land takes(x,Chemistry,S2015) \land Failed(x,Chemistry,S2015)) \land \exists y (Student(y) \land takes(y,History,S2015) \land Failed(y,History,S2015))$ 

 $\neg \exists x (Student(x) \land Failed(x, Chemistry, S2015)) \land \exists y (Student(y) \land Failed(y, History, S2015))$ 

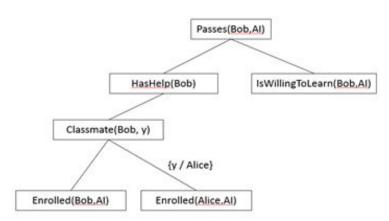
d)  $\forall$  x,z (Student(x)  $\land$  Semester(z)  $\land$  Takes(x, Analysis,z)  $\Rightarrow$  Takes(x, Geometry,z))

 $\forall$  x,z (Student(x)  $\land$  Semester(z)  $\land$  Takes(x, Analysis,z)  $\Rightarrow$   $\exists$  y (Semester(y)  $\land$  Takes(x, Geometry,y)))

e)  $\neg \exists x,z \in Student(x) \land Semester(z) \land takes(x, Analysis,z) \land takes(x, History,z))$ 

Rubrics:Every subquestion is 3 pts. Making at most 1 error in predicate or parameter or quantifier or logical connectives, especially Student() Course() Semester(), can only get 1 pt. (more than 1 error will get 0 since it's required basic knowledge of FOL)

2-



Rubrics:Didn't use backward chaining method -4. Missing unification -2. Missing any box -2. Parameter error -1. Up to -10.

3- not complete due to infinite loops. When a loop is detected, suspend the loop branch and try other branches until getting this subgoal or no solution.

Rubrics: NO is 1pt. Explain 2pts. You can get full points if you explain it right without say No.

4- Algorithms exist that return YES to every entailed sentence, but no algorithm exists that also returns NO to every nonentailed sentence

#### Rubrics:no partial

# 5-Planning

- 1-4
- 2- E, F
- 3- E
- 4- If we add an ordering constraint to F, so that it occurs before B. (Multiple possible answer, like add one more B between EC, but no change order of BEC and no remove any steps)

Rubrics:no partial Q1-Q4

5- No, For example if we go to finish from F, g will not be true.

Rubrics:NO is 1pt. Good justification 1pt