**Report from Lab nr 2 - Heat transfer**

1. **Introduction**

Thermodynamics is a part of physics that is about heat, particle movement and it’s macro properties. With parameters such as conductivity or specific heat capacity we can calculate the tranision of heat in diffrent scenarios such as: heat transfer on a space ship, heat transfer on in a house including air conditioning or heat transfer in a nuclear power plant. Thanks to such simulations we can better predict and construct crucial parts of modern technology.

1. **Laboratory outline**
   1. **Model coding**

Physical object that is being simulated is made out of two 30x30 matrixes. First one is responsible for distribution of the temperature, whereas the second one is responsible for preserving 1st and 2nd boundary conditions.

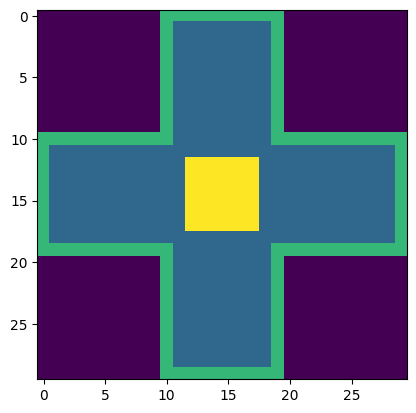


Figure 1 - Presentation of simulated object (yellow – heater, blue – object, green – Edge of object of constant temperature 10 degrees, purple – background without influence)

Obraz zawierający tekst, Czcionka, linia

Opis wygenerowany automatycznie

Above is the simplified heat transfer equation which will be used to calculate temperature in each cell in step n+1

Simplified mathematical equations describing heat transfer were implemented into python function:

def calc\_temp(self, T\_prev, T\_left, T\_right, T\_top, T\_down):

        dx = 3/self.resolution

        dy = dx

        p1 = T\_prev

        p2 = (self.K\*self.dt\*(T\_left-2\*T\_prev+T\_right))/(self.cw\*self.p\*dx\*\*2)

        p3 = (self.K\*self.dt\*(T\_top-2\*T\_prev+T\_down))/(self.cw\*self.p\*dy\*\*2)

        return p1 + p2 + p3

* 1. **First simple simulation**

First simulation was made for alumina material with following parameters:

Density : ρ=2700 kg/m3

Specific heat : cw=900 J/kgK

Thermal conductivity : K=237 W/mK

Obraz zawierający zrzut ekranu, tekst, diagram

Opis wygenerowany automatycznie

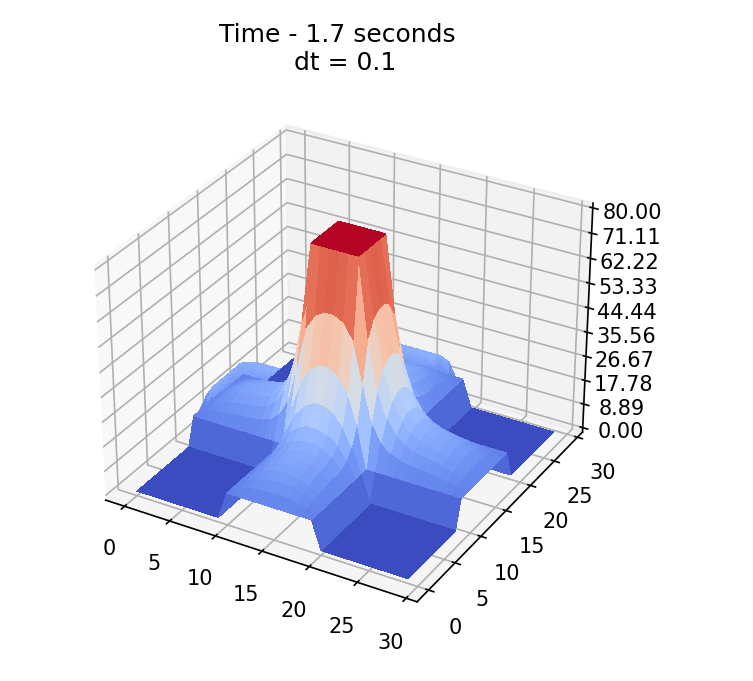
Graph 1 – Outcome of heat simulation of alumina

* 1. **Testing numerical stability**

Heat transfer simulations need to be provided with extreme caution, because of the numerical errors and possibility of ustability of a conducted simulation.

Obraz zawierający tekst, szkic, design

Opis wygenerowany automatycznieGraph 2 – Simulation conducted with dt = 0.4 (numerical instability)



Graph 3 – Simulation conducted with dt = 0.1 (numerical stability)

From conducted experiments dt > 0.2 is considared unstable and can (and most of the time will) lead to unstability of the simulation concluding in wrong results. Hence to that, it is crucial to set at least dt = 0.1, for ensuring stable simulation work.

* 1. **Stop condition (for copper, alumina and steel)**

Each metal has diffrent parameters that define how the heat is being distributed and how fast it is happening. In this section we simulate heat transfer for diffrent types of metals and try to evaluate how much time it takes for each metal to reach a stable state.

Stable state is defined by the following code:

def absolute\_mean(self):

        """

        Helper function to calculate change in heat distribution after single iteration

        """

        arr = np.absolute(self.shape - self.last\_shape)

        suma = np.sum(arr)

        return suma

    def stop\_condition(self) -> bool:

        """

        Function depneds wheather simualtion has ended or is still running

        """

        eps = 5 \* 10\*\*(-13)    #number not significant numerically

        if self.absolute\_mean() < eps:

            return True

        else:

            return False

Table 1, Time of heat simulation based on metal

|  |  |  |
| --- | --- | --- |
| Metal | Dt [s] | Time [s] |
| Alumina | 0.01 | 119.13 |
| Copper | 0.01 | 24.79 |
| Stainless steel | 0.01 | 2.26 |

From the above table we see steel is reaching thermal stability the fastest.

1. **Conclusion**

Heat transfer simulation is very important in variuos sciences and can be helpful to create and plan construction of lots of solutions. Nevertheless, it’s crucial to understand the capabilities and limitations of such simulation and to adress them properly. For example time step (dt) can’t be too big (or too small) to corectly conduct such simulation.

From the simulation we can see that choosing the right material is crucial as one can reach thermal stability almost 50x faster than the other one. It shows the magnitude of diffrence of conductivity between diffrent materials.

1. **References**

Model and whole code of the simulation is available at github:

https://github.com/tycjantyc/Modeling\_of\_Physical\_Systems/tree/main/lab2