

* Basics of R software:

1. R is a statistical software for data analysis and computing.
2. It is a software by which effective handling and outcome is possible.
3. It is capable of graphical display.
4. It is a free software.

$$1) 2^2 + 1 - 5 \cdot 1 + 4 \cdot 5 + 6 \div 5$$

$$\Rightarrow 2^2 \cdot 2 + abs(-5) + 4 \cdot 5 + 6 / 5$$

[1] 30.2

$$2) x = 20, y = 2x, z = x + y, \sqrt{z} = ?$$

$$> x = 20$$

$$y = 2 * x$$

$$z = x + y$$

$$sqrt(z)$$

[1] > 7.7459 (-)

$$3) x = 10, y = 15, z = 5$$

Find $x + y = z$; $x \cdot y \cdot z$; \sqrt{xyz} , round (15)

$$> x = 10$$

$$> y = 15$$

$$> z = 5$$

$$> x + y + z$$

[1] 30.

"> a = $x^*y \times 2$
 $\geq a$
 $[1] > 250.$

"> sqrt(a)
 $[1] > 27.38613$

"> round(a)
 $[1] > 27$

Q.4. A vector in R software is denoted by

i.) $x = c(2, 3, 5, 7) 1_2$

$[1] > x$
 $[1] > 4 9 25 47$

ii.) $x = c(2, 3, 5, 7)^T c(2, 4)$

$[1] > x$
 $[1] > 2 7 25 34 3$

iii.) $x = c(2, 3, 5, 7)^T c(2, 3)$

$[1] > x$
 $[1] >$ warning message

iv.) $x = c(1, 2, 3, 4, 5, 6)^T c(2, 3, 9)$

$[1] > x$
 $[1] > 1 6 16 125 1296.$

"> u $(2, 1, 2, 3, 1, 4) 1_3$
 $[1] > u$
 $[1] > 63 69 3 31$

"> n = $c(2, 1, 2, 3, 1, 4) * c(-2, -3, -5, 1, -2)$
 $[1] > n$
 $[1] > -42 -69 -5 -28$

"> u = $c(2, 1, 3, 5, 7) + c(-2, -3, -1, 0)$
 $[1] > u$
 $[1] > 0 0 4 7$

"> u = $((2, 3, 5, 7)) 1_2$
 $[1] > u$
 $[1] > 1.0 1.5 2.5 3.5$

Q.5) Find the sum, product, square of sum a product for the given values.

$> i = c(4, 9, 2, 5, 7, 8, 3, 6, 15, 12, 10, 9, 8, 13, 14$

$> s = sum(i)$
 $> p = prod(i)$

$> s = sum(i)$
 $> p = prod(i)$

$> s$
 $> p$
 $> s$
 $> sqrt(s)$
 $> sqrt(p)$

$> s$
 $> p$
 $> s$
 $> sqrt(s)$
 $> sqrt(p)$

Q.6) Find the sum, product, max, min value

$n = c(2, 8, 9, 11, 10, 7, 6) 1_2$

$> sum(n)$
 $[1] > 55$

$> product(n)$
 $[1] > 4425975632$

No 030

Practical - 2

035.

$\geq \max(n)$

$\geq \min(n)$

$x \sim \text{matrix}(\text{row}=4, \text{ncol}=2, \text{data} = ((12, 2, 4, 5, 8)))$

$$\begin{bmatrix} [1,1] & [1,2] \\ [2,1] & 2 \\ [3,1] & 7 \\ [4,1] & 8 \end{bmatrix}$$

$$\rightarrow \begin{bmatrix} y & y \\ 2 & 0 \end{bmatrix} + \begin{bmatrix} 6 & 1/2 \\ 4 & 7 \end{bmatrix}$$

y

$x \sim \text{matrix}(\text{row}=3, \text{ncol}=3, \text{data} = ((4, 5, 6, 7, 8, 9, 10, 25)))$

$y \sim \text{matrix}(\text{row}=3, \text{ncol}=3, \text{data} = ((6, 4, 5, 11, 12, 6, 9)))$

x

$$\begin{bmatrix} [1,1] & [1,2] & [1,3] \\ [2,1] & 5 & 0 \\ [3,1] & 6 & 2 \end{bmatrix}$$

$$\rightarrow y \begin{bmatrix} [1,1] & [1,2] & [1,3] \\ [2,1] & 4 & 0 \\ [3,1] & 6 & 2 \end{bmatrix}$$

$$\rightarrow x \neq 2$$

$$\begin{bmatrix} [1,1] & [1,2] & [1,3] \\ [2,1] & 6 & 11 \\ [3,1] & 4 & 12 \\ [4,1] & 5 & 8 \end{bmatrix}$$

- * Binomial distribution
- a. Toss a coin 10 times $P(\text{heads}) = 0.5$. Let x be the number of heads. Find the probability.
 - i.) Seven heads
 - ii.) Four heads
 - iii.) Atmost four heads
 - iv.) Atleast six heads.
 - v.) No Heads
 - vi.) All heads.
- Also find expectation and variance

At least = 1 - p(below)
Atmost = p(below)

n = Total number of trials

$p = P(\text{success})$

$q = P(\text{failure})$

$x = \text{number of success out of } n$

$P(x) = {}^n C_x p^x q^{n-x}$

$E(x) = np$

$V(x) = np^2$

Binomial (n, n, p) = $P(x=n)$

$n \neq p \neq q$

Binomial (n, n, p)

* Exercise

Q. Toss a coin 10 times $P(\text{heads}) = 0.5$. Let

x be the number of heads.

Find the probability.

i.) Seven heads

ii.) Four heads

iii.) Atmost four heads

iv.) Atleast six heads.

v.) No Heads

vi.) All heads.

Practical - no. 3.

Q.1 Check the following are p.m.f () or not

(i)	x	1	2	3	4	5
	$p(x)$	0.2	0.5	-0.5	0.4	0.4

(ii)	x	10	20	30	40	50
	$p(x)$	0.3	0.2	0.3	0.1	0.1

(iii)	x	0	1	2	3	4
	$p(x)$	0.4	0.2	0.3	0.2	0.1

Solutions :-

$$(i) \quad 0 \leq p(x) \leq 1$$

$$(ii) \quad \sum p(x) = 1$$

(1). Since, it not satisfy the first condition.

Solutions:-

(2) Since all the value of $p(x)$ are more than zero and less than one, 1st condition is satisfied.

$$\sum p(x) = p(10) + p(20) + p(30) + p(40) + p(50)$$

$$\Rightarrow \text{prob} = (0.3, 0.2, 0.3, 0.1, 0.1)$$

$$\Rightarrow \text{sum (prob)}$$

$$[1] \quad 1$$

i. Since both the conditions are satisfied it is a p.m.f

(3) Since all the value of $p_2(n)$ is between 0 to 1, therefore, condition 1 is satisfied.
But

$$\begin{aligned} \sum p(n) &= p(0) + p(1) + p(2) + p(3) + p(4) \\ &= 0.4 + 0.2 + 0.3 + 0.2 + 0.1 \\ &= 1.2. \end{aligned}$$

If it is more than 1
It does not satisfy condition 2
Hence, not proof. prob

$$\begin{aligned} > \text{prob} &= (0.4, 0.2, 0.3, 0.2, 0.1) \\ [1] &\sum(\text{prob}) = 1.2 \end{aligned}$$

\therefore It's not satisfy second condition
 \therefore It's not a p.m.f.

Q2: Following is the p.m.f of x
 $x = 1, 2, 3, 4, 5$
 $P(x) = 0.1, 0.15, 0.2, 0.3, 0.25$
 Find the mean and variance of x .

x	$P(x)$	$xP(x)$	$x^2 P(x)$
1	0.1	0.1	0.1
2	0.15	0.3	0.6
3	0.2	0.6	1.8
4	0.3	1.2	4.8
5	0.5	1.25	6.25

$$\sum xP(x) = \sum x^2 P(x) = 13.55$$

$$\text{Var} = V(x) = \sum x^2 P(x) - [E(x)]^2$$

$$= 13.55 - 3.45^2$$

$$= 1.6475$$

```

> x=c(1,2,3,4,5)
> prob=c(0.1,0.15,0.2,0.3,0.25)
> a=x*prob
> a
[1] 0.10 0.30 0.60 1.20 1.25
  
```

```

> b=(x^2)*prob
> b
[1] 0.10 0.60 1.80 4.80 6.25
  
```

10

$$> \text{mean} = \text{sum}(a)$$

> mean

$$[1] 3.45$$

$$> \text{mean} = \text{sum}(b)$$

> mean

$$[1] 13.55$$

$$> \text{var} = \text{sum}(b^a) - \text{mean}^{12}$$

> var

$$[1] 1.6475$$

Q3. Find mean and variance of n

$$x = 5, 10, 15, 20, 25$$

$$P(x) = 0.1, 0.3, 0.25, 0.25, 0.15$$

$$\rightarrow > n = c(5, 10, 15, 20, 25)$$

$$> \text{prob} = c(0.1, 0.3, 0.2, 0.25, 0.15)$$

$$> a = x * \text{prob}$$

> a

$$[1] 0.5 \quad 3.0 \quad 3.0 \quad 5.0 \quad 3.75$$

$$> \text{mean} = \text{sum}(a)$$

> mean

$$[1] 4.1525$$

$$> b = (* 12) * \text{prob}$$

$$[1] 2.50$$

$$> \text{var} = \text{sum}(b) - \text{mean}^{12}$$

$$> 38.6875$$

$$100.00$$

$$93.25$$

> var
> C1 38.6825

C1

510

[1] 0.2 0.5 0.3 0.2 0.9 1.2

[1] plot(x,a,"s")

[1]

? a = curveon(prob)
> [1] a = 0.4, 0.7, 0.9, 1.0 .1
> plot(x,a,"r")

[1] ~~p(x) = 0, x < 0~~
~~= 0.2, 0 ≤ x < 2~~
~~= 0.5, 2 ≤ x < 4~~
~~= 0.2, 4 ≤ x < 6~~
~~= 0.9, 6 ≤ x < 8~~
~~= 1.0, x ≥ 8~~

?
ii) Find c.d.f and draw the graph
X
p(x) 0 2 4 6 8
0.2 0.3 0.2 0.2 0.1

$P(x) = 0 \quad x < 0$

$= 0.2 \quad 0 \leq x < 2$
 $= 0.5 \quad 2 \leq x < 4$
 $= 0.7 \quad 4 \leq x < 6$
 $= 0.9 \quad 6 \leq x < 8$
 $= 1.0 \quad x \geq 8$

> x = (0, 2, 4, 6, 8)
> p_x = (0, 2, 0.3, 0.2, 0.2, 0.1)
> a = curveon(p_x)

-> a

Practical - 2.

Binomial distribution

1. Suppose there are twelve MCQs in an English Question paper. Each question has five answers and only one is correct. Find a probability of having
 - i) four correct answers.
 - ii) almost four correct answers
 - iii) at least three correct answers

2. Find the complete distribution where $a = 5$ and $p = 0.1$.

3. Find the probability of exactly ten success out of 100 trials with $p = 0.1$.

4. X follow binomial distribution with $a = 12$ and $p = 0.25$. Find
 - i) $P(X \leq 5)$
 - ii) $P(X > 7)$
 - iii) $P(5 < X < 7)$

5. There are 10 members in a community. Probability of attending a meeting of any member is 0.7

seven and more members present in a meeting.

A salesman has a twenty person probability of making a sale to a customer. On a typical day he will meet 30 customers what minimum number of sales he will make with 88% probability.

For $n=10$ and $p=0.6$ Find the binomial probability and plot the graph of p.m.f and c.d.f.

Note:-

$$1) P(X=x) = \text{dbinom}(\frac{x, n}{n-x}, p)$$

$$2) P(X \leq x) = (\text{probability of atleast value}) \\ = \text{pbisnom}(x, n, p)$$

$$3) P(X > n) \rightarrow (\text{probability of atleast }) \\ = 1 - \text{pbisnom}(n, n, p)$$

$$4) \text{If } x \text{ is unknown and probability is given was } z \text{ bisnom}(p, n, p)$$

> $\text{dbinom}(10, 100, 0.1)$
 [1] 0.1316653

740

Solutions:-

[1] $n = 12$
 $p = 0.15$

ptm>

> $\text{dbinom}(4, 12, 0.15)$
 [1] 0.1328756

[1] $\text{pbinom}(4, 12, 0.15)$
 [1] 0.9274445

[1] $1 - \text{pbinom}(2, 12, 0.15)$
 [1] 0.4416543

[5] $m = 10$
 $p = 0.9$

> $\text{pbinom}(6, 10, 0.9)$
 [1] 0.9872098

[2]> $n = 5$
 $p = 0.1$

> $\text{dbinom}(1, 5, 0.1)$
 [1] 0.32805
> $\text{dbinom}(3, 5, 0.1)$
 [1] 0.0081
> $\text{dbinom}(5, 5, 0.1)$
 [1] 0.05
> $\text{dbinom}(0, 5, 0.1)$
 [1] 0.59047

3)> $x = 10$
> $n = 10$
> $p = 0.1$
> $\text{pbinom}(0, 10, 0.1)$
[1] 0.5831555

110

```
> n = 10
> p = 0.6
> x = 0:n
```

```
> bp = dbinom(x, n, p)
> bp
[1] 0.0001048576 0.0015228640 0.0106168320
```

```
0.0424673280 0.1114267360 0.2149908980
```

```
[6] 0.2006581248 0.2508226560
```

```
0.1209323520 0.0403107840
```

```
0.1209323520
```

```
[11] 0.0060466176
[11] d=data.frame("x.values=x", "probability"=bp)
```

```
> point(d)
```

```
(1) x.x.value x. p probability
```

```
1 x.values=x 0.0001048576
```

```
2 x.values=x 0.0015228640
```

```
3 x.values=x 0.0106168320
```

```
4 x.values=x 0.0424673280
```

```
5 x.values=x 0.1114267360
```

```
6 x.values=x 0.2149908980
```

```
7 x.values=x 0.2508226560
```

```
8 x.values=x 0.1209323520
```

```
9 x.values=x 0.0403107840
```

```
10 x.values=x 0.0060466176
```

```
11 x.values=x
```

It follows binomial distribution
parameter

By M.A.K

5.10

Practical 4

$$P(X=n) = (P^n) P^X q^{n-2}$$

[$n=8$, $P=0.6$, $q=0.4$] - given

$$\begin{aligned} \textcircled{i} \quad P(X=7) &= {}^8C_7 (0.6)^7 (0.4)^0 \\ &= {}^8C_7 \times 0.2799 * 0.4 \\ &= 0.02799 \times 0.4 \\ &= 0.08956 \end{aligned}$$

$$\begin{aligned} \textcircled{ii} \quad P(X \leq 3) &= P(0) + P(1) + P(2) + P(3) \\ &= {}^8C_0 (0.6)^0 (0.4)^8 + {}^8C_1 (0.6)^1 (0.4)^{8-1} + {}^8C_2 \\ &\quad (0.6)^2 \\ &= 1 \times 1 \times 0.00065536 + 8 \times 0.6 \times 0.0016384 \times \\ &\quad 28 \times 0.36 \times 0.004096 + 56 \times 0.26 \times 0.07204 \\ &= 0.1736204 \end{aligned}$$

$$\begin{aligned} \textcircled{iii} \quad P(X=2 \text{ or } 3) &= P(2) + P(3) \\ &= {}^8C_2 (0.6)^2 + 1 (0.6)^2 + {}^8C_3 (0.6)^3 (0.4)^3 \\ &= 28 \times 0.36 \times 0.004096 + 56 + 0.21670.024 \\ &= 0.04128 + 0.12384 \\ &= 0.16515612. \end{aligned}$$

Practical - 5

Q

Normal distribution

- Q 1) $\Phi(p(x \leq 7))$
 > pnorm(7, 10, 2)
 cat(p(x > 12))
 > 1 - pnorm(12, 10, 2)

- (ii) $p(5 \leq x \leq 12)$
 > pnorm(12, 10, 2) - pnorm(5, 10, 2)
 (17) 0.835135

- (iii) $p(x < 1) = 0.4$
 > k = qnorm(0.4, 10, 2)

- > k = qnorm(0.4, 10, 2)

cat(k)

0.93306

- Q 2) $p_1 = \text{pnorm}(110, 100, 6)$
 cat("p(x \leq 110) is = ", p1)

- $p(x \leq 110) = 0.7522096$

- (iv) $p_2 = 1 - \text{pnorm}(105, 100, 6)$

- cat("1 - p(x > 105) is = ", p2)

- $1 - p(x > 105) = 0.2028284$

- (v) $p_3 = \text{pnorm}(92, 100, 6)$

- cat("p(x < 92) is = ", p3)

- $p(x < 92) = 0.91211225$

- cat("p(x < 92) = 0.91211225, pnorm(92, 100, 6) = ", p3)

- (vi) $p_4 = \text{pnorm}(110, 100, 6) - \text{pnorm}(95, 100, 6)$
 cat("p(95 \leq x \leq 110) is = ", p4)

- $p(95 \leq x \leq 110) = 0.7498813$
 cat("p(x < k) = 0.9 = ", k)
 $p(x < k) = 0.9 = 102.6893$.

Q 3) A random variable x follows normal distribution with $\mu = 10$, $\sigma = 2$ find:

- (i) $P(x \leq 7)$
 (ii) $P(x > 12)$
 (iii) $P(5 \leq x \leq 12)$
 (iv) $P(x < t) = 0.4$

- (i) $X \sim N(10, 13)$
 $\sigma = \sqrt{13}$

- (ii) $p(x \leq 110)$
 (iii) $p(x > 105)$
 (iv) $p(x \leq 92)$
 (v) $p(95 \leq x \leq 110)$

- v. $P(x < k) = 0.9$.
 v. $P(x < k) = 0.9$.

Q1

Q1) $x \sim N(10, 3)$
Generate 10 random variable find the
sample mean, median, variance &
standard deviation

Q2) Plot the standard normal curve

$x = seq(-3, 3, by = 0.1)$

$y = dnorm(x)$
 $plot(x, y, xlab = "values", ylab = "probability",$
main: "standard normal curve")

Q3) $x \sim N(50, 10^2)$

Find i) $P(x \leq 60)$

ii) $P(x > 65)$

iii) $P(45 \leq x \leq 60)$

→ Solutions:-

$p_1 = pnorm(60, 50, 10)$

$cat("P(x \leq 60) is = ", p_1)$

$P(x \leq 60) = 0.8413447$

$p_2 = 1 - pnorm(65, 50, 10)$

$cat("P(x > 65) is = ", p_2)$

$P(x > 65) = 0.668072$

$p_3 = pnorm(60, 50, 10)$

$cat("P(45 \leq x \leq 60) is = ", pnorm(45, 50, 10))$

$P(45 \leq x \leq 60) = 0.532871 P_3$

Practical - 6.

Aim: Z and T distribution sum
S.I. Check the hypotheses

A simple of size = 400 is selected and the sample mean is 20.2 and the standard derivation is 2.25.

Test at 5 person level of significant

$\rightarrow H_0: \mu = 20$ against $H_1: \mu \neq 20$.

$$m_0 = 20; m_x = 20.2, s_d = 2.25, n = 400$$

$$\rightarrow H_0 = H_1$$

$$\rightarrow z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$$

$$\rightarrow z_{cal}$$

$$[1] 1.0777778$$

$$\rightarrow \text{cat}("z_{calculated} is ", z_{cal})$$

$$\rightarrow pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$$

$$\rightarrow pvalue$$

$$[1] 0.075477036$$

$$> 0.05$$

Pvalue is greater than 0.05 we accept

$$H_0: \mu = 20$$

[2] We want to test the hypothesis that the sample of size 100 has a mean of 275 and standard deviation of 5% level of significance.

$H_0: \mu = 250$, $H_1: \mu \neq 250$. A test of the hypothesis at 5% level of significance.

$$\rightarrow H_0: \mu = 250$$

$$\rightarrow H_1: \mu \neq 250$$

(1) $\alpha = 0.05$

```

> zcal = (nx - n0) / (sd / sqrt(n))
> zcal
[1] 8.333333
> cat("Z calculated is = ", zcal)
Z calculated is = 8.333333
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0
    
```

Since, pvalue is less than 0.05, we reject H_0 .

p-value? ~~Are~~ \neq 0.05 we reject H_0 .

Q3] We want to test the hypothesis that $H_0: p = 0.2$ against $H_1: p < 0.2$ population proportion in the sample of 100 is reduced than the sample proportion is called 0.125. Test the hypothesis at 5% level of significance.

Practical 2

Topic: Large sample test

Q. A study of noise level in two hospital is done following data is calculated first sample mean = 61.2 standard deviation = 3.4 second sample mean = 61.1 standard deviation = 3.8, Test $H_0: \mu_1 = \mu_2$ at 1% level of significance.

Q.1 Two random sample of single 1000 and 2000 drawn from two population with a standard duration 2 and 3 respectively. Test the hypothesis that two population means equal or not at 5%.

level of significance. Sample means are 67 and 68 respectively

$\rightarrow H_0: \mu_1 = \mu_2$ against $\mu_1 \neq \mu_2$

μ_1 = population 1st mean

μ_2 = population 2nd mean

$m\chi_1$ = mean of sample first

$m\chi_2$ = mean of sample second.

s_{d1} = standard deviation 1st

s_{d2} = standard deviation 2nd.

$\rightarrow n_1 = 1000$

$\rightarrow n_2 = 2000$

$m\chi_1 = 67$

$m\chi_2 = 68$

$s_{d1} = 2$

$s_{d2} = 3$

$\rightarrow z_{cal} = (m\chi_1 - m\chi_2) / \sqrt{(s_{d1}^2/n_1) + (s_{d2}^2/n_2)}$

$\rightarrow z_{cal} = (67 - 68) / \sqrt{(2^2/1000) + (3^2/2000)}$

$\rightarrow z_{cal} = -1.311$

$\rightarrow p-value = 2 * (1 - pnorm(z_{cal}))$

$\rightarrow p-value = 2 * (1 - pnorm(-1.311))$

$\rightarrow p-value = 0.258006$

Since pvalue is greater than 0.01, we accept H_0 i.e. $\mu_1 = \mu_2$

Q.2) From each of two population of orange, the following sample are collected. Test whether proportion of Bad orange are equal or not

First sample size = 250

No. of bad orange in the first sample = 140 and second sample 200.

$\rightarrow p-value = 2 * (1 - pnorm(z_{cal}))$

$\rightarrow p-value = 0.125000$

$\rightarrow p-value = 0.125000$

(e) The following are the two independent sample from the two population regarding equality of two population mean of SI. LOS
 Sample 1: 74, 77, 74, 73, 74, 79, 72, 72, 75, 79, 74, 75
 76, 76, 76
 Sample 2: 72, 76, 74, 70, 70, 78, 70, 72, 75, 79, 74, 75
 78, 72, 74, 70.

Soln:-

- $H_0: \mu_1 = \mu_2$ against $\mu_1 < \mu_2$ or
 $\mu_1 = (79, 77, 76, 76)$
- $\mu_1 = \text{length}(x_1)$
- $\mu_1 = \text{mean}(x_1)$

? variance($\mu_1 - 1$) * var(x_1) / n_1

? variance
 $\sum_{i=1}^{12} b_i^2 - 4S^2$

? sd1 = sqrt(variance)
 26.1

[1] 0.6714

- $\mu_2 = (72, 76, 74, 70)$
- $\mu_2 = \text{length}(x_2)$
- $\mu_2 = \text{mean}(x_2)$

variance = $(m_2 - 1) * \text{var}(x_2) / n_2$
 covariance
 [1] 0.6163
 $\Rightarrow s_{d2} = \sqrt{\text{variance}}$
 $\Rightarrow s_{d2}$

[1] 0.7850

$t(0) = (m_{\bar{x}_1} - m_{\bar{x}_2}) / (\sqrt{s_{d1}^2 / n_1} + (s_{d2}^2 / n_2))$

[1] 1.5757

?cat("calculated is: ", tval)
 calculated is 1.5757

t.test(x1, x2) = 1.57

pvalue = 0.1387

AM

t-test(x)

One sample t-test

data: x
 $t = 24.029$ df = 14 p-value = 8.819e

alternative hypothesis: true mean is not equal to 0 as
 confidence interval:

91.37475

Sample estimates:

mean of x : 100.3333

Since, p-value is less than 0.05 we reject

0.2] > g1 = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)

> g2 = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

> t.test(g1, g2).

data: g1 and g2
 $t = 2.2573$ df = 16.376, p-value = 0.03798
 alternative hypothesis: true difference in mean is not equal to 0.166205

Sample estimate: mean of g1
 mean of g2

i] A random sample of 15 observation is given by 80, 100, 110, 105, 122, 170, 120, 110, 101, 88, 83, 95, 89, 107, 125.
 Does this data support the assumption i.e popular mean = 100.

$\Rightarrow H_0: \mu = 100$

x = c(80, 100, 110, 105, 122, 70, 120, 110, 101, 88, 83,

89, 107, 125)

t.test(x)

One sample t-test

data: x
 $t = 24.029$ df = 14 p-value = 8.819e

alternative hypothesis: true mean is not equal to 0 as
 confidence interval:

91.37475

Sample estimates:

mean of x : 100.3333

Since, p-value is less than 0.05 we reject

0.2] > g1 = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)

> g2 = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

> t.test(g1, g2).

data: g1 and g2
 $t = 2.2573$ df = 16.376, p-value = 0.03798
 alternative hypothesis: true difference in mean is not equal to 0.166205

Sample estimate: mean of g1
 mean of g2

Since p value is greater than 0.05 we accept the null hypothesis.

057

Q3) Two type of medicines are used on the weight reducing program to reducing their weight after using the medicine given below:

med A = 10, 12, 13, 11, 14

med B = 8, 9, 12, 14, 15, 10, 9

Is there a significance difference in the efficiency of the medicines.

No H₀: μ_A

> x = ((10, 12, 13, 11, 14))

> y = ((8, 9, 12, 14, 15, 10, 9))

t-test(x, y)

data: x and y

z = 0.80384, df = 9.7591, p-value = 0.4106

alternative hypothesis: true difference in means is not equal to 9.5 percent confidence interval:

-1.781171

Sample estimates:

mean of x mean of y

12

11

Since, p-value is more than 0.05 we accept

H0: μ_A = μ_B at 1% LSD.

Q4) Observation is noted to whether the program is effective or not before and after the program is effective or not.

Before: 120, 125, 115, 130, 123, 119, 122, 127, 129, 118

After: 111, 118, 107, 110, 115, 112, 112, 110, 119, 112

H₀: There is no significant difference in weight.

H₁: The diet program reduce weight.

> x = ((120, 125, 115, 130, 123, 119, 122, 127, 129, 118))

> y = ((111, 118, 107, 110, 115, 112, 112, 110, 119, 112))

t-test(x, y, paired = T, alternative = "less")

data: x and y

t = 1.7, df = 9, p-value = 1

alternative hypothesis: true difference in means is less than 0 as percent confidence interval:

inf = 9.416551

Sample estimates

mean of the difference

8.5

Q5) Sample(A) = 66, 67, 75, 76, 82, 84, 85, 90, 92
Sample(B) = 64, 66, 74, 75, 82, 85, 87, 91, 93, 95, 97
Test the population mean are equal as not.

> x = ((66, 67, 75, 76, 82, 84, 85, 90, 92))

> y = ((64, 66, 74, 75, 82, 85, 87, 91, 93, 95, 97))

t-test(x, y)

data: x and y
 $t = -6.63738$, $p\text{value} = 0.0124$, difference in mean
 alternative hypothesis: true difference in mean is
 greater than 0 as percentage confidence interval

-12.653192
 6.953192
 large population is 52. The standard deviation
 against the hypothesis that the
 Los (Level of significance)

level aim - Large and small sample spaces
 the arithmetic mean of a sample of 100 item from a
 against an alternative $p\text{value}$ more than 5% at 5%
 Los (Level of significant)

large population is 52. The standard deviation

In a big city 350 out of 400 males are found to be
 smokers. Thus, this information supports that exactly
 half of the males in the city are smokers. Test
 at 1%. Los

Sample estimate
 mean of x mean of y
 80 83
 since, p-value is greater than 0.05 we accept H_0
 as 1%. level of significance.

4. A sample of size 400 was drawn and the sample
 mean is 99. Test at 5% LOS that the samples
 come from a population with mean 100 and var
 64.

5. The flowers stems are selected and the heights
 found to be centimeter. $63, 63, 68, 69, 71,$
 $72, 74, 77, 78$

> $y = \{74, 77, 78\}$
 $\text{t-test}(x, y, \text{paired=T}, \text{alternative}=\text{"greater"})$
 data: x and y
 $t = -4.4691, df = 9, p\text{value} = 0.9972$

alternative hypothesis: true difference in mean is
 greater than 0 as percent confidence interval.
 -5.076637

Sample estimate
 mean of the difference

-3.6.

6. Two random two samples were drawn from the
 normal populations and their value are $A = 66,$
 $75, 76, 82, 84, 88, 90, 92$.
 $B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97$
 test whether the population have a same
 variance at 5%. Los.

Solution:

$H_0: \mu_1 = \mu_2$ against

1st

> n = 100
> m1 = 52
> m0 = 55

> zcal = $\frac{(m1 - m0)}{\sqrt{m1 + m0}} \sqrt{n}$

[1] -4.285714

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 1.082153e-05

pvalue < 0.05 we rejected

2. $H_0: \mu_1 = \mu_2$ against $H_0: \mu_1 \neq \mu_2$

> p = 0.5
> p = 350 / 400

> p
[1] 0.5

> n = 700
> Q = 1 - p
> Q

[2] 0.5
> zcal = (p - Q) / (sqrt(p * Q / n))

> zcal

0.0
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.014

> zcal
[1] 2.082731

> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.03721511

Since, pvalue < 0.05
we reject pvalue

95 percent confidence interval: 060
 69.6649 71.6292

 Sample estimator
 mean of X
 68.14286

 4B. $H_0: \mu_1 = \mu_2$
 $n = 400$
 $m_1 = 99$
 $m_0 = 100$
 $\text{variance} = 64$
 $sd = \sqrt{\text{variance}}$
 $[1] 8$
 $z_{\text{val}} = (m_1 - m_0) / (sd / \sqrt{n})$
 $[1] -2.5$
 $pvalue = 2 * (1 - pnorm(\text{abs}(z_{\text{val}})))$
 $pvalue$
 $[1] 0.01241933$

 Since, $pvalue < 0.05$

 we reject $H_0: \mu_1 = \mu_2$

 ⑥ $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$
 $x = c(66, 67, \dots, 90, 92)$
 $y = c(64, 66, \dots, 95, 97)$
 $f = f.var.test(x, y)$
 f

F test to compare two variance

data: x and y
 $F = 0.70686$, num df = 8, denom df = 10, pvalue = 0.6351
 alternative hypothesis: true ratio of variance is
 not equal to 1.

 95 percent confidence interval:
 0.1833612 3.0360393

Sample estimate
 ratio of variance
 0.4068567

 $\mu_0: \mu_1 = \mu_2$
 $t = 4.754$, df = 6, p-value = 5.522e-09

alternative hypothesis: true mean is not equal to 0.

$H_0: \mu_1 = H_0$ against $\mu_1 \neq \mu_2$
 p value > 0.05 we accept $H_0: \mu_1 = \mu_2$

ANOVA & CHI-SQ

060

- Q1. Use the following data to test whether the cleanliness of home and cleanliness of child is independent or not.

		Clean	Dirty
		50	20
C.C.		Family clean 80	Family dirty 35

Solution No. 1 (as C.R.)

> $x = \{ 40, 80, 35, 50, 20, 45 \}$

> m=3

> n=2

> y=matrix(x, nrow=m, ncol=n)

> y

[1,1] [1,2]

40 50

80 20

35 45

50 35

20 45

45 35

> p.v=chisq.test(y)

> p.v.

Pearson's Chi-squared test with Yates' continuity correction

data=

y

X-squared=25.646, df=1, P-value=2.698e-06.

Since P-value is less than 0.05, we reject

Hence, child cleanliness and Home cleanliness are dependent

061

- Q2. Use the following data to find a vaccination and a particular disease are independent or not.

		Given	Not Given
		aff	Not aff
Vac.		20	50

Solution No. Vac & a Dis

> x= ((20, 25, 15, 35))

> m=2

> n=2

> y=matrix(x, nrow=m, ncol=n)

> y

[1,1] [1,2]

20 30

25 35

15 35

35 35

> p.v=chisq.test(y)

> p.v.

Pearson's Chi-squared test with Yates' continuity correction

data=

y

X-squared=0, df=1, P-value=1.

Since, P-value is more than 0.05, we accept
Hence, child cleanliness & the vaccine
and disease independence or each other

Q3. Perform a ANOVA for the following data

varieties

A
B
C
D

Observation

53, 55, 53
60, 58, 57, 56
52, 54, 54, 55

Soluⁿ- No. The mean of the varieties are equal

```
> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 58, 57, 56)
> x4 = c(52, 54, 54, 55)
```

* H₀: The average life of four brands is same.
test the hypothesis that the average life of four brands is same.

```
> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "values" "ind"
> oneway.test(values~ind, data=d, var.equal=T)
```

* H₀: The average life of four brands is same.
H₁: The average life of four brands is not same.
Test the hypothesis that the average life of four brands is not same.

```
One-way analysis of means
data: values and ind
F = 3.326, num df = 3, denom df = 9, p-value = 0.0483
Call:
```

```
anova = anova(values~ind, data=d)
```

> anova

Call:

```
aov(formula=values~ind, data=d)
```

Residual standard error: 2.11023

Estimated effects may be unbalanced.

Terms	Sum of squares	Deg. of freedom	Ind residuals	Residuals
Residual		3	7	1.5000062
Standard error:				1.470246
Estimated effects may be unbalanced.				

> one-way test (values wind data = d, var equal = T)
one-way analysis of means

data: values and ind
 $f = 6.8415$, num df = 3, denom df = 20, p-value = 0.003.

Pearson's Chi-squared test
 χ^2 -squared = 39.726, df = 2, p-value = 2.364e-07

Since, p-value is less than 0.5 it rejected

b. One thousand student of a college graded according to their IQ and economic condition of their home. Check what is there any association between IQ and the economic condition of the home.

IQ	High	Low
Prod.	460	140
	330	200
Low	240	160

Solv: No: IQ & EC.

> x = c(460, 330, 240, 140, 200, 160)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = w)

> y

[1,1] [1,2]

460 140

330 200

[2,1] 240 160

[3,1] 780 180

> pch = chisq.test(y)

> pch.

Q.4 Following are the 12 questions
 $64, 57, 12, 12, 1, 25, 20, 2, 1, 32, 32, 12, 2, 5, 2, 4, 2, 6$
 $63, 65, 60, 8, 9, 6, 1, 4, 1, 48, 51, 61, 62$
 Using wilcoxon sign rank test test the hypothesis
 that the population median is greater than 60 at 5%.
 Null hypothesis: true population median is 60.
 Alternative hypothesis: true population median is greater than 60.

```
> x = c(15, 12, 12, 1, 25, 20, 2, 1, 32, 32, 12, 2, 5, 2, 4, 2, 6)
> y = wilcox.test(x, alt = "greater", mu = 60)
> wilcox.test(x, alt = "less", mu = 60)
data: x
V = 48, p-value = 0.9132
alternative hypothesis: true location is less than 60
```

> x = c(65, 65, 60, 8, 9, 6, 1, 7, 1, 58, 51, 62)

> wilcox.test(x, alt = "greater", mu = 60)
 Wilcoxon signed rank test with continuity correction

data: x
 $p\text{-value} = 0.09092$

alternative hypothesis: true location is greater than 60

Q.5 Following are the observations

15, 17, 12, 4, 25, 20, 2, 1, 32, 28, 12, 2, 5, 2, 4, 2, 6.

Use the wilcoxon sign

```
data: x
V = 35, p-value = 0.7127
alternative hypothesis: true location is not equal to 25.
```

Ans