

$n_i = 2$ per subject

$P = \#$ of fixed effects

$b_i =$ random intercept $q=1$

$$R_i = \sigma^2 I_{2 \times 2}$$

$$Y_i = X_i \beta + Z_i b_i + \epsilon_i$$

Y_i is 2×1

$$\epsilon_i = 2 \times 1$$

$$X_i = 2 \times p$$

$$Z_i = 2 \times p$$

Q: Develop expressions for $E[b_i | Y_i]$ and $\text{var}(b_i | Y_i)$

$$\begin{pmatrix} Y_i \\ b_i \end{pmatrix} \sim \text{MVN} \left(\begin{pmatrix} \mu_i \\ 0 \end{pmatrix}, \begin{bmatrix} \Sigma_i & Z_i G \\ G Z_i^T & G \end{bmatrix} \right)$$

$$E[b_i^T | Y_i^T] = \mu_2 + \Sigma_{21} \Sigma_{11}^{-1} (Y_i - \mu_1)$$

$$E[b_i^T | Y_i^T] = 0 + G Z_i^T \Sigma_i^{-1} (Y_i - \mu_i)$$

$$\text{var}(b_i | Y_i) = \Sigma_{22} - \Sigma_{21} \Sigma_{11}^{-1} \Sigma_{12}$$

$$= G - G Z_i^T \Sigma_i^{-1} Z_i G$$

Need explicit expressions -b

(2)

of parameters = 10 = 3 fixed effects + 1 from R + 6 from G

Effect	Estimate	sd error
Intercept	21.397	0.5676
time-0	2.478	0.1205
time-on	0.407	0.1579

significant digits should be the same in the table.

w/ time-0 = after menarche
time-on = before menarche

$$G_{3 \times 3} = \begin{bmatrix} 45.9102 & (5.7657) \\ -3.6610 & (1.00) \\ 2.5686 & (1.2245) \end{bmatrix}$$

$$0.9012 (0.2721)$$

$$-0.1171 (0.2629)$$

$$1.6508 \\ (0.437)$$

note estimate (sd error)

$$R = 9.4304 (0.5444)$$

• covariance and correlation matrix see attached page 2.

• Graph see attached
Need to comment on graph -4

Q: Describe the correlation matrix

→ diagonal is 1

→ symmetric

→ 8×8

→ if looking at the upper triangle, each row decreases in corr as row # increases ("correlations decrease as time increases") ✓