

**BIOSTATISTICS 767, Spring 2017**  
**Homework 5**

1. Problem 13.3.

Add 13.3.0: Present simple descriptive statistics and describe what they show.

Files: insomnia.\*

2. This problem was explained in class. For logistic regression with  $n$  independent Bernoulli 0/1 outcomes, after fitting by maximum-likelihood, the deviance ( $G^2$ ) can be expressed as a function of the estimates  $\hat{\beta}$  (or the fitted values) only, without the responses  $\{y_i\}$  appearing in the formula. i.e. If I give you ONLY the fitted values (just one column of numbers), and nothing else, you will be able to compute the deviance. The deviance is

$$G^2 = 2 \sum_{i=1}^n [y_i \log(y_i/\hat{\mu}_i) + (1 - y_i) \log\{(1 - y_i)/(1 - \hat{\mu}_i)\}],$$

where  $\hat{\mu}_i$  is the fitted value for the  $i$ -th observation.

What does  $G^2/n$  estimate?

What is the maximum possible value of  $G^2/n$ ?

Compute  $G^2$  for these vectors:

$$\hat{\mu}^\top = (0.4, 0.4, 0.4, 0.4, 0.4)$$

$$\hat{\mu}^\top = (0.05, 0.05, 0.1, 0.9, 0.9)$$

$$\hat{\mu}^\top = (0.01, 0.01, 0.01, 0.98, 0.99)$$

Comment.

Exercise (not homework, do not turn in):

For logistic regression with independent Bernoulli 0/1 outcomes, after fitting the model  $E[Y_i] = \mu$  (intercept only) by maximum-likelihood, compute the value of Pearson's  $X^2$ . Surprised?!