```
# draw the figures illustrating maximum likelihood
x < -c(1, 3, 4, 6, 8, 9, 12)
y < -c(5, 8, 6, 10, 9, 13, 12)
windows (14,6)
par(mfrow=c(1,3))
plot(x, y, pch=21, bg="blue", ylim=c(0, 15))
abline(0,0.6793,col="red")
plot(x,y,pch=21,bg="blue",ylim=c(0,15))
abline(8,0.6793,col="red")
plot(x,y,pch=21,bg="blue",ylim=c(0,15))
abline (lm(y\sim x))
abline(lm(y~x),col="blue")
plot(x,y,pch=21,bg="blue",ylim=c(0,15))
abline(4.8273,1.5,col="red")
plot(x,y,pch=21,bg="blue",ylim=c(0,15))
abline(4.8273,0.2,col="red")
plot(x,y,pch=21,bg="blue",ylim=c(0,15))
abline (lm(y~x))
abline(lm(y \sim x),col="blue")
# randomizing treatments for experimental design
treatments <- c("aloprin","vitex","formixin","panto","allclear")</pre>
   use sample to shuffle them for the active insects in dishes 1 to 5
sample(treatments)
# this produces a warning message because the same variable name
# appears in two attached dataframes
first.frame <- read.csv("c:\\temp\\test.pollute.csv")</pre>
second.frame <- read.csv("c:\\temp\\ozone.data.csv")</pre>
attach(first.frame)
attach (second.frame)
# this is how you should avoid this kind of problem
first.frame <- read.csv("c:\\temp\\test.pollute.csv")</pre>
second.frame <- read.csv("c:\\temp\\ozone.data.csv")</pre>
attach(first.frame)
# this is where you work on the information from first.frame.
# Then when you are finished
# ......
detach(first.frame)
attach (second.frame)
```

```
# read data from a file called worms.csv to create a
# dataframe called worms
worms <- read.csv("c:\\temp\\worms.csv")</pre>
names (worms)
attach (worms)
worms
# all rows, just columns 1 to 3
worms[,1:3]
# all columns just rows 5 to 15
worms[5:15,]
\# all columns but only selected rows (area > 3 and slope < 3)
worms[Area>3 & Slope <3,]</pre>
# sort the rows by increasing area
worms[order(Area),]
# only the columns with numeric data
worms [order (Area), c(2,3,5,7)]
# sort into decending order with just two columns
worms[rev(order(worms[,5])),c(5,7)]
# using tapply with a specified dataframe
with(worms, tapply(Worm.density, Vegetation, mean))
# using aggregate to summarise multiple variables by facor levels
aggregate (worms[,c(2,3,5,7)],list(Vegetation),mean)
aggregate(worms[,c(2,3,5,7)],list(Community=Vegetation),mean)
# multiple explanatory variables
aggregate (worms [,c(2,3,5,7)],
      list(Moisture=Damp, Community=Vegetation), mean)
# aggregate and tapply compared
with(worms, tapply(Slope, list(Damp, Vegetation), mean))
# plotting your data
data <- read.csv("c:\\temp\\das.csv")</pre>
attach (data)
```

```
head (data)
# finding the identity of the outlier
which (y > 10)
y[50]
# plots with categorical explanatory variables
yields <- read.csv("c:\\temp\\fertyield.csv")</pre>
attach(yields)
head(yields)
table(treatment)
which(treatment == "nitogen")
# scatterplots
data <- read.csv("c:\\temp\\scatter.csv")</pre>
attach (data)
head(data)
plot(x,y,pch=21,bg="red")
# box and whisker plots
data <- read.csv("c:\\temp\\weather.data.csv")</pre>
attach (data)
head(data)
plot(factor(month), upper)
# data for coplot
data <- read.csv("c:\\temp\\coplot.csv")</pre>
attach (data)
head(data)
# scale the plotting area to accommodate two plots side by side
windows (7,4)
par(mfrow=c(1,2))
plot(x, y)
plot(z, y)
# using coplot
windows (7,7)
coplot(y~x|z,pch=16,panel=panel.smooth)
# factorial data
data <- read.csv("c:\\temp\\np.csv")</pre>
attach (data)
head (data)
windows (7,4)
par(mfrow=c(1,2))
plot(nitrogen, yield, main="N")
plot(phosphorus, yield, main="P")
```

```
# Chapter 3
yvals <- read.csv("c:\\temp\\yvalues.csv")</pre>
attach(yvals)
hist(y)
# arithmetic mean
total <- sum(y)</pre>
n <- length(y)</pre>
( ybar <- total/n )</pre>
arithmetic.mean <- function(x) sum(x)/length(x)</pre>
data <-c(3,4,6,7)
arithmetic.mean(data)
arithmetic.mean(y)
mean(y)
# median
sorted <- sort(y)</pre>
length(y)/2
ceiling (length (y)/2)
sorted[20]
sorted[ceiling(length(y)/2)]
sort(y)[ceiling(length(y)/2)]
y.even <- y[-1]
length(y.even)
sort(y.even)[19]
sort(y.even)[20]
(sort(y.even)[19]+sort(y.even)[20])/2
38%%2
39%%2
med <- function(x) {</pre>
modulo <- length(x)%%2</pre>
if (modulo == 0)
(sort(x) [ceiling(length(x)/2)] + sort(x) [ceiling(1+length(x)/2)])/2
else sort(x) [ceiling(length(x)/2)]
med(y)
med(y.even)
median(y)
median(y.even)
```

```
# geometric mean

100000^0.2
insects <- c(1,10,1000,10,1)
mean(insects)

exp(mean(log(insects)))

# harmonic mean

v <- c(1,2,4,1)
length(v)/sum(1/v)

1/mean(1/v)</pre>
```

```
# Variance
y \leftarrow c(13,7,5,12,9,15,6,11,9,7,12)
plot(y, ylim=c(0, 20))
# range
range(y)
plot(1:11, y, ylim=c(0,20), pch=16, col="blue")
lines(c(4.5, 4.5), c(5, 15), col="brown")
lines(c(4.5, 3.5), c(5, 5), col="brown", lty=2)
lines (c(4.5, 5.5), c(15, 15), col="brown", lty=2)
# residuals
plot(1:11, y, ylim=c(0, 20), pch=16, col="blue")
abline(h=mean(y),col="green")
for (i in 1:11) lines(c(i,i), c(mean(y), y[i]), col="red")
# sum of squares
y - mean(y)
y - mean(y))^2
sum((y - mean(y))^2)
# variance
variance <- function (x) sum((x-mean(x))^2)/(length(x)-1)
variance(y)
var(y)
# ozone example
ozone <- read.csv("c:\\temp\\gardens.csv")</pre>
attach (ozone)
ozone
mean(gardenA)
gardenA - mean(gardenA)
(gardenA - mean(gardenA))^2
sum((gardenA - mean(gardenA))^2)
sum((gardenA - mean(gardenA))^2)/9
mean(gardenB)
gardenB - mean(gardenB)
(gardenB - mean(gardenB))^2
sum((gardenB - mean(gardenB))^2)
sum((gardenB - mean(gardenB))^2)/9
mean(gardenC)
```

```
gardenC - mean(gardenC)
(gardenC - mean(gardenC))^2
sum((gardenC - mean(gardenC))^2)
sum((gardenC - mean(gardenC))^2)/9
var(gardenC)/var(gardenB)
# critical value of Fisher's F
2*(1 - pf(10.667, 9, 9))
var.test(gardenB, gardenC)
# sample size
plot(c(0,32),c(0,15),type="n",xlab="Sample size",ylab="Variance")
for (df in seq(3,31,2)) {
for( i in 1:30){
x <- rnorm(df,mean=10,sd=2)</pre>
points(df, var(x)) }}
# standard error of a mean
sqrt(var(gardenA)/10)
sqrt(var(gardenB)/10)
sqrt(var(gardenC)/10)
# quantiles of the t distribution
qt(.025,9)
qt(.975,9)
qt(.995,9)
qt(.9975,9)
qt(.975,9)*sqrt(1.33333/10)
# bootstrap intervals
data <- read.csv("c:\\temp\\skewdata.csv")</pre>
attach (data)
names (data)
plot(c(0,30),c(0,60),type="n",xlab="Sample size",
ylab="Confidence interval")
for (k in seq(5,30,3)){
a <- numeric(10000)</pre>
for (i in 1:10000) {
a[i] <- mean(sample(values, k, replace=T))</pre>
```

```
points(c(k,k),quantile(a,c(.025,.975)),type="b",pch=21,bg="red")
}

quantile(a,c(.025,.975))

xv <- seq(5,30,0.1)
yv <- mean(values)+1.96*sqrt(var(values)/xv)
lines(xv,yv,col="blue")
yv <- mean(values)-1.96*sqrt(var(values)/xv)
lines(xv,yv,col="blue")

yv <- mean(values)-qt(.975,xv)*sqrt(var(values)/xv)
lines(xv,yv,lty=2,col="green")
yv <- mean(values)+qt(.975,xv)*sqrt(var(values)/xv)
lines(xv,yv,lty=2,col="green")</pre>
```

```
# single samples
data <- read.csv("c:\\temp\\example.csv")</pre>
attach (data)
names (data)
summary(y)
boxplot(y)
hist(y)
# rug plot
length(table(y))
plot(range(y),c(0,10),type="n",xlab="y values",ylab="")
for (i in 1:100) lines(c(y[i],y[i]),c(0,1),col="blue")
# designing a histogram
(max(y)-min(y))/10
diff(range(y))/11
# the game of craps
score <- 2:12
ways <-c(1,2,3,4,5,6,5,4,3,2,1)
( game <- rep(score, ways) )
sample(game, 1)
outcome <- numeric(10000)</pre>
for (i in 1:10000) outcome[i] <- sample(game, 1)</pre>
hist(outcome, breaks=(1.5:12.5))
mean.score <- numeric(10000)</pre>
for (i in 1:10000) mean.score[i] <- mean(sample(game, 3))</pre>
hist(mean.score,breaks=(1.5:12.5))
mean (mean.score)
sd(mean.score)
xv < - seq(2, 12, 0.1)
yv <- 10000*dnorm(xv, mean(mean.score), sd(mean.score))</pre>
hist(mean.score,breaks=(1.5:12.5),ylim=c(0,3000),col="yellow", main="")
lines(xv,yv,col="red")
# standard normal disribution
standard.deviations \leftarrow seq(-3,3,0.01)
pd <- dnorm(standard.deviations)</pre>
plot(standard.deviations,pd,type="l",col="blue")
pnorm(-2)
pnorm(-1)
1-pnorm(3)
qnorm(c(0.025,0.975))
```

```
# shading the tails of the standard normal distribution
xv < -seq(-3, 3, 0.01)
yv<-dnorm(xv)
plot(c(-3,3),c(0,0.3),xlim=c(-
3,3),ylim=c(0,0.4),type="n",ylab="pd",xlab="standard deviations")
polygon(c(1.96, 1.96, -1.96, -
1.96, xv[105:496]),c(yv[496],0,0,yv[105],yv[105:496]),col="green")
polygon(c(-1.96,-1.96,xv[1],xv[1:104]),c(yv[104],0,0,yv[1:104]),col="red")
polygon(c(xv[601],xv[601],1.96,1.96,xv[497:601]),c(yv[601],0,0,yv[496:601])
, col="red")
text(0,0.2,"95%",cex=2)
lines(xv,yv,col="blue")
# calculations with the sandard normal distribution
ht <- seq(150, 190, 0.01)
plot(ht,dnorm(ht,170,8),type="l",col="brown",
ylab="Probability density",xlab="Height")
pnorm(-1.25)
pnorm(1.875)
1 - pnorm(1.875)
pnorm(1.25) - pnorm(-0.625)
# drawing a panel of four normal distributions
par(mfrow=c(2,2))
ht <- seq(150, 190, 0.01)
pd <- dnorm(ht, 170, 8)
plot(ht,dnorm(ht,170,8),type="l",col="brown",
ylab="Probability density",xlab="Height")
plot(ht,dnorm(ht,170,8),type="l",col="brown",
ylab="Probability density",xlab="Height")
yv <- pd[ht<=160]</pre>
xv \leftarrow ht[ht <= 160]
xv < -c(xv, 160, 150)
yv <- c(yv,yv[1],yv[1])</pre>
polygon(xv,yv,col="orange")
plot(ht,dnorm(ht,170,8),type="l",col="brown",
ylab="Probability density",xlab="Height")
xv \leftarrow ht[ht>=185]
yv \leftarrow pd[ht>=185]
xv < -c(xv, 190, 185)
yv < -c(yv, yv[501], yv[501])
polygon(xv,yv,col="blue")
plot(ht,dnorm(ht,170,8),type="l",col="brown",
ylab="Probability density", xlab="Height")
xv \leftarrow ht[ht>=160 \& ht <= 180]
yv \leftarrow pd[ht>=160 \& ht <= 180]
```

```
xv < -c(xv, 180, 160)
yv <- c(yv,pd[1],pd[1])</pre>
polygon(xv,yv,col="green")
# plots for skewness
data <- read.csv("c:\\temp\\skewdata.csv")</pre>
attach (data)
qqnorm(values)
qqline(values, lty=2)
# speed of light data
light <- read.csv("c:\\temp\\light.csv")</pre>
attach(light)
names(light)
hist(speed)
summary(speed)
wilcox.test(speed, mu=990)
a <- numeric(10000)
for(i in 1:10000) a[i] <- mean(sample(speed,replace=T))</pre>
hist(a)
# student's t distribution
plot(c(0,30),c(0,10),type="n",
xlab="Degrees of freedom",ylab="Students t value")
lines(1:30,qt(0.975,df=1:30),col="red")
abline(h=1.96,lty=2,col="green")
xvs < - seq(-4, 4, 0.01)
plot(xvs, dnorm(xvs), type="l",
ylab="Probability density",xlab="Deviates")
lines(xvs, dt(xvs, df=5), col="red")
qt(0.975,5)
# skewness
skew <- function(x){</pre>
m3 <- sum((x-mean(x))^3)/length(x)
s3 \leftarrow sqrt(var(x))^3
m3/s3 }
hist(values, main="", col="green")
skew(values)
skew(values)/sqrt(6/length(values))
1 - pt(2.949, 28)
skew(sqrt(values))/sqrt(6/length(values))
skew(log(values))/sqrt(6/length(values))
# kurtosis
kurtosis <- function(x) {</pre>
```

```
m4 <- sum((x-mean(x))^4)/length(x)
s4 <- var(x)^2
m4/s4 - 3 }
kurtosis(values)
kurtosis(values)/sqrt(24/length(values))</pre>
```

```
# code 7
          Regression
# text figure
plot(c(0,10),c(0,100),xlab="",ylab="",type="n")
lines (c(0,10),c(80,10),lwd=2)
# intercept = 80
lines (c(0,0),c(0,80),col="green")
lines (c(0,-10),c(80,80),col="red")
\# slope = -7
lines (c(2,8),c(24,24),col="brown")
lines (c(2,2),c(66,24),col="blue")
# tannin example
reg.data <- read.csv("c:\\temp\\tannin.csv")</pre>
attach(reg.data)
names(reg.data)
plot(tannin, growth, pch=21, bg="blue")
lm(growth~tannin)
abline(lm(growth~tannin),col="green")
fitted <- predict(lm(growth~tannin))</pre>
fitted
lines (c(0,0),c(12,11.7555555))
# residuals
for (i in 1:9)
lines (c(tannin[i],tannin[i]),c(growth[i],fitted[i]),col="red")
# estimating the maximum likelihood slope
b < -seq(-1.43, -1, 0.002)
sse <- numeric(length(b))</pre>
for (i in 1:length(b)) {
a <- mean(growth)-b[i]*mean(tannin)</pre>
residual <- growth - a - b[i]*tannin
sse[i] <- sum(residual^2)</pre>
plot(b, sse, type="l", ylim=c(19, 24))
arrows (-1.216, 20.07225, -1.216, 19, col="red")
abline (h=20.07225, col="green", lty=2)
lines(b, sse)
b[which(sse==min(sse))]
# corrected sums of squares
SSX <- sum(tannin^2)-sum(tannin)^2/length(tannin)
SSY <- sum(growth^2)-sum(growth)^2/length(growth)
SSXY <- sum(tannin*growth) -sum(tannin) *sum(growth)/length(tannin)
```

```
# box 7.5 figure
plot(c(0,10),c(0,10),xlab="",ylab="",type="n")
abline (h=5, lty=2)
lines (c(0,10),c(8,2))
text(2, 6.2, expression(hat(y) - bar(y)))
text(2, 8.45, expression(y - hat(y)))
arrows (7, 5, 7, 9.5, code=3, length=0.1)
arrows (1, 5, 1, 7.4, code=3, length=0.1)
arrows (1, 9.5, 1, 7.4, code=3, length=0.1)
points(1,9.5,pch=16)
text(8,7.4,expression(y - bar(y)))
text(0.2, 5, expression(bar(y)))
text(.2,7.4, expression(hat(y)))
text(.2,9.5,"y")
# regreesion model in R
model <- lm(growth~tannin)</pre>
summary(model)
summary.aov(model)
par(mfrow=c(2,2))
plot(model)
# a non-linear relationship
par(mfrow=c(1,1))
data <- read.csv("c:\\temp\\decay.csv")</pre>
attach (data)
names (data)
plot(time, amount, pch=21, col="blue", bg="green")
abline(lm(amount~time),col="red")
summary(lm(amount~time))
plot(time, log(amount), pch=21, col="blue", bg="red")
abline(lm(log(amount)~time),col="blue")
model <- lm(log(amount)~time)</pre>
summary(model)
par(mfrow=c(1,1))
plot(time, amount, pch=21, col="blue", bg="green")
xv < - seq(0,30,0.25)
yv \leftarrow 94.38536 * exp(-0.068528 * xv)
lines(xv, yv, col="red")
# shapes of quadratic relationships
par(mfrow=c(2,2))
curve(4+2*x-0.1*x^2,0,10,col="red",ylab="y")
curve(4+2*x-0.2*x^2,0,10,col="red",ylab="y")
curve(12-4*x+0.3*x^2,0,10,col="red",ylab="y")
curve(4+0.5*x+0.1*x^2,0,10,col="red",ylab="y")
```

```
model2 <- lm(amount~time)</pre>
model3 <- lm(amount~time+I(time^2))</pre>
summary(model3)
AIC (model2, model3)
anova (model2, model3)
# non-linear regression using nls
deer <- read.csv("c:\\temp\\jaws.csv")</pre>
attach(deer)
names (deer)
par(mfrow=c(1,1))
plot(age,bone,pch=21,bg="lightgrey")
model <- nls(bone \sim a-b*exp(-c*age), start=list(a=120, b=110, c=0.064))
summary(model)
model2 <- nls(bone \sim a*(1-exp(-c*age)), start=list(a=120,c=0.064))
anova(model, model2)
av < -seq(0,50,0.1)
bv <- predict(model2,list(age=av))</pre>
lines(av,bv,col="blue")
summary(model2)
null.model <- lm(bone ~ 1)</pre>
summary.aov(null.model)
# generalized additive models GAM
library(mgcv)
hump <- read.csv("c:\\temp\\hump.csv")</pre>
attach(hump)
names (hump)
model <- gam(y \sim s(x))
plot(model,col="blue")
points(x,y-mean(y),pch=21,bg="red")
summary(model)
```

```
# one-way anova
oneway <- read.csv("c:\\temp\\oneway.csv")</pre>
attach (oneway)
names (oneway)
plot(1:20,ozone,ylim=c(0,8),ylab="y",xlab="order",pch=21,bg="red")
abline(h=mean(ozone),col="blue")
for(i in 1:20) lines(c(i,i),c(mean(ozone),ozone[i]),col="green")
plot(1:20,ozone,ylim=c(0,8),ylab="y",xlab="order",
pch=21,bg=as.numeric(garden))
abline(h=mean(ozone[garden=="A"]))
abline(h=mean(ozone[garden=="B"]),col="red")
index <- 1:length(ozone)</pre>
for (i in 1:length(index)){
if (garden[i] == "A" )
     lines(c(index[i],index[i]),c(mean(ozone[garden=="A"]),ozone[i]))
else
     lines(c(index[i],index[i]),c(mean(ozone[garden=="B"]),ozone[i]),
col="red")
SSY <- sum((ozone-mean(ozone))^2)</pre>
SSY
sum((ozone[garden=="A"]-mean(ozone[garden=="A"]))^2)
sum((ozone[garden=="B"]-mean(ozone[garden=="B"]))^2)
qf(0.95,1,18)
1-pf(15.0,1,18)
summary(aov(ozone~garden))
plot(aov(ozone~garden))
cbind(ozone[garden=="A"],ozone[garden=="B"])
tapply(ozone, garden, sum)
mean (ozone[garden=="A"]) -mean (ozone)
mean (ozone[garden=="B"]) -mean (ozone)
mean(ozone[garden=="A"])
mean(ozone[garden=="B"]) -mean(ozone[garden=="A"])
# plots for anova
comp <- read.csv("c:\\temp\\competition.csv")</pre>
attach (comp)
names (comp)
plot(clipping, biomass, xlab="Competition treatment",
ylab="Biomass",col="lightgrey")
heights <- tapply(biomass,clipping,mean)</pre>
barplot(heights, col="green", ylim=c(0,700),
ylab="mean biomass",xlab="competition treatment")
```

```
# error bars
error.bars <- function(y,z) {
x <- barplot(y,plot=F)</pre>
n <- length(y)
for (i in 1:n)
arrows(x[i],y[i]-z,x[i],y[i]+z,code=3,angle=90,length=0.15)
model <- aov(biomass~clipping)</pre>
summary(model)
table(clipping)
se < -rep(28.75, 5)
error.bars(heights, se)
ci <- se*qt(.975,5)
barplot(heights, col="green", ylim=c(0,700),
ylab="mean biomass",xlab="competition treatment")
error.bars(heights,ci)
lsd \leftarrow qt(0.975,10)*sqrt(2*4961/6)
lsdbars \leftarrow rep(lsd,5)/2
barplot(heights, col="green", ylim=c(0,700),
ylab="mean biomass",xlab="competition treatment")
error.bars(heights, lsdbars)
# fatorial experiments
weights <- read.csv("c:\\temp\\growth.csv")</pre>
attach(weights)
barplot(tapply(gain, list(diet, supplement), mean), beside=T)
labels <- levels(diet)</pre>
shade <-c(0.2, 0.6, 0.9)
barplot(tapply(gain, list(diet, supplement), mean), beside=T,
ylab="weight gain",xlab="supplement",ylim=c(0,30))
legend(locator(1), labels, gray(shade))
tapply(gain, list(diet, supplement), mean)
model <- aov(gain~diet*supplement)</pre>
summary(model)
tapply(gain, list(diet, supplement), length)
x \leftarrow as.vector(barplot(tapply(gain, list(diet, supplement), mean),
beside=T, ylim=c(0,30))
y <- as.vector(tapply(gain, list(diet, supplement), mean))</pre>
z \leftarrow rep(0.656, length(x))
for( i in 1:length(x) )
arrows(x[i],y[i]-z[i],x[i],y[i]+z[i],length=0.05,code=3,angle=90)
legend(locator(1), labels, gray(shade))
model <- lm(gain~diet+supplement)</pre>
```

```
summary(model)
supp2 <- factor(supplement)</pre>
levels(supp2)
model2 <- lm(gain~diet+supp2)</pre>
anova (model, model2)
# split plot experiments
yields <- read.csv("c:\\temp\\splityield.csv")</pre>
attach(yields)
names (yields)
model <-
aov(yield~irrigation*density*fertilizer+Error(block/irrigation/density))
summary(model)
interaction.plot(fertilizer,irrigation,yield)
interaction.plot(density,irrigation,yield)
# random effects and pseudoreplication
rats <- read.csv("c:\\temp\\rats.csv")</pre>
attach(rats)
names(rats)
Treatment <- factor(Treatment)</pre>
Rat <- factor(Rat)</pre>
Liver <- factor(Liver)</pre>
# this is the wrong way to do the analysis
model <- aov(Glycogen~Treatment)</pre>
summary(model)
# this is the right way to do the analysis
yv <- tapply(Glycogen, list(Treatment, Rat), mean)</pre>
( yv <- as.vector(yv) )</pre>
treatment <- factor(c(1,2,3,1,2,3))
model <- aov(yv~treatment)</pre>
summary(model)
# variance components analysis
model2 <- aov(Glycogen~Treatment+Error(Treatment/Rat/Liver))</pre>
summary(model2)
```

```
# analysis of covariance
compensation <- read.csv("c:\\temp\\ipomopsis.csv")</pre>
attach(compensation)
names (compensation)
plot(Root, Fruit, pch=16, col="blue")
plot(Grazing,Fruit,col="lightgreen")
# the wrong analysis (not controlling for initial size)
summary(aov(Fruit~Grazing))
# the correct anocova
model <- lm(Fruit~Root*Grazing)</pre>
summary.aov(model)
model <- lm(Fruit~Grazing*Root)</pre>
summary.aov(model)
model2 <- lm(Fruit~Grazing+Root)</pre>
anova(model, model2)
summary.lm(model2)
plot(Root, Fruit, pch=21, bg=(1+as.numeric(Grazing)))
legend(locator(1),c("grazed","ungrazed"),col=c(2,3),pch=16)
abline(-127.829,23.56,col="blue")
abline(-127.829+36.103,23.56,col="blue")
```

```
# multiple regression
ozone.pollution <- read.csv("c:\\temp\\ozone.data.csv")</pre>
attach(ozone.pollution)
names (ozone.pollution)
pairs (ozone.pollution, panel=panel.smooth)
library(mgcv)
par(mfrow=c(2,2))
model <- gam(ozone~s(rad)+s(temp)+s(wind))</pre>
plot(model,col= "blue")
par(mfrow=c(1,1))
library(tree)
model <- tree(ozone~.,data=ozone.pollution)</pre>
plot (model)
text (model)
model1 <- lm(ozone~temp*wind*rad+I(rad^2)+I(temp^2)+I(wind^2))</pre>
summary(model1)
model2 <- update(model1,~. - temp:wind:rad)</pre>
summary(model2)
model3 <- update(model2,~. - wind:rad)</pre>
summary(model3)
model4 <- update(model3,~. - temp:wind)</pre>
summary(model4)
model5 <- update(model4,~. - I(rad^2))</pre>
summary(model5)
model6 <- update(model5,~. - temp:rad)</pre>
summary(model6)
plot (model6)
# start all over again with a new transfrmation of the response
model7 <- lm(log(ozone)~temp*wind*rad+I(rad^2)+I(temp^2)+I(wind^2))</pre>
model8 <- step(model7)</pre>
summary(model8)
plot (model8)
# a more tricky example
pollute <- read.csv("c:\\temp\\sulphur.dioxide.csv")</pre>
attach(pollute)
names (pollute)
pairs (pollute, panel=panel.smooth)
par(mfrow=c(1,1))
library(tree)
model <- tree(Pollution~.,data=pollute)</pre>
plot(model)
```

```
text (model)
model1 <-
lm(Pollution~Temp+I(Temp^2)+Industry+I(Industry^2)+Population+I(Population^
2) +Wind+I (Wind^2) +Rain+I (Rain^2) +Wet.days+I (Wet.days^2))
summary(model1)
model2 <- step(model1)</pre>
summary(model2)
model3 <- update(model2, ~.- Rain-I(Wind^2))</pre>
summary(model3)
interactions <- c("ti", "tp", "tw", "tr", "td", "ip", "iw",</pre>
"ir", "id", "pw", "pr", "pd", "wr", "wd", "rd")
sample(interactions)
model4 <-
lm(Pollution~Temp+Industry+Population+Wind+Rain+Wet.days+Wind:Rain+Wind:Wet
.days+Industry:Wet.days+Industry:Rain+Rain:Wet.days)
model5 <-
lm(Pollution~Temp+Industry+Population+Wind+Rain+Wet.days+Population:Rain+Te
mp:Population+Population:Wind+Temp:Industry+Industry:Wind)
model6 <-
lm(Pollution~Temp+Industry+Population+Wind+Rain+Wet.days+Temp:Wind+Populati
on:Wet.days+Temp:Rain+Temp:Wet.days+Industry:Population)
model7 <-
lm(Pollution~Temp+Industry+Population+Wind+Rain+Wet.days+Wind:Rain+Wind:Wet
.days+Population:Wind+Temp:Rain)
summary(model7)
model8 <- update(model7, ~.-Temp:Rain)</pre>
summary(model8)
model9 <- update(model8,~.-Population:Wind)</pre>
summary(model9)
plot(model9)
model10 <- update(model9,~. + Wind:Rain:Wet.days)</pre>
summary(model10)
```

- # generalised linear models
- # there is no R code in this chapter

```
#count data
# regression
clusters <- read.csv("c:\\temp\\clusters.csv")</pre>
attach(clusters)
names(clusters)
plot (Distance, Cancers, pch=21, bg="lightblue")
model1 <- glm(Cancers~Distance, poisson)</pre>
summary(model1)
model2 <- glm(Cancers~Distance, quasipoisson)</pre>
summary(model2)
xv <- 0:100
yv <- 0.186865-0.006138*xv
y <- exp(yv)
lines(xv,y,col="red")
y <- predict(model2,list(Distance=xv), type="response")</pre>
lines(xv,y,col="red")
# categorical explanatory vaariables
count <- read.csv("c:\\temp\\cells.csv")</pre>
attach (count)
names (count)
table(cells)
tapply(cells, smoker, mean)
tapply(cells, weight, mean)
tapply(cells,sex,mean)
tapply(cells,age,mean)
model1 <- glm(cells~smoker*sex*age*weight,poisson)</pre>
summary(model1)
model2 <- glm(cells~smoker*sex*age*weight,quasipoisson)</pre>
summary(model2)
model3 <- update(model2, ~. -smoker:sex:age:weight)</pre>
model4 <- update(model3, ~. -sex:age:weight)</pre>
anova (model4, model3, test="F")
model5 <- update(model4, ~. -smoker:sex:age)</pre>
anova(model5, model4, test="F")
model6 <- update(model5, ~. -smoker:age:weight)</pre>
anova(model6, model5, test="F")
Despite 1-star significance for one of the interaction terms, this was not
significant either, so we leave it out.
model7 <- update(model6, ~. -smoker:sex:weight)</pre>
```

```
anova (model7, model6, test="F")
model8 <- update(model7, ~. -smoker:age)</pre>
anova(model8, model7, test="F")
model9 <- update(model8, ~. -sex:weight)</pre>
anova(model9, model8, test="F")
model10 <- update(model9, ~. -age:weight)</pre>
anova (model10, model9, test="F")
model11 <- update(model10, ~. -smoker:sex)</pre>
anova (model11, model10, test="F")
model12 <- update(model11, ~. -sex:age)</pre>
anova (model12, model11, test="F")
model13 <- update(model11, ~. -smoker:weight)</pre>
anova (model13, model11, test="F")
tapply(cells, list(smoker, weight), mean)
tapply(cells, list(sex, age), mean)
barplot(tapply(cells,list(smoker,weight),mean),beside=T)
weight <- factor(weight,c("normal","over","obese"))</pre>
barplot(tapply(cells,list(smoker,weight),mean),beside=T)
barplot(tapply(cells,list(smoker,weight),mean),beside=T)
legend(locator(1),c("non smoker","smoker"),fill=gray(c(0.2,0.8)))
# comlex contingency tables
induced <- read.csv("c:\\temp\\induced.csv")</pre>
attach(induced)
names (induced)
model <- glm(Count~Tree*Aphid*Caterpillar,family=poisson)</pre>
model2 <- update(model , ~ . - Tree:Aphid:Caterpillar)</pre>
anova(model, model2, test="Chi")
model3 <- update(model2 , ~ . - Aphid:Caterpillar)</pre>
anova (model3, model2, test="Chi")
# the wrong way of doing it
wrong <- glm(Count~Aphid*Caterpillar,family=poisson)</pre>
wrong1 <- update(wrong,~. - Aphid:Caterpillar)</pre>
anova(wrong, wrong1, test="Chi")
tapply(Count, list(Tree, Caterpillar), sum)
# ancova with count data
species <- read.csv("c:\\temp\\species.csv")</pre>
attach(species)
names(species)
plot(Biomass, Species, pch=21, bg=(1+as.numeric(pH)))
```

```
model <- lm(Species~Biomass*pH)</pre>
summary(model)
abline(40.60407,-2.80045,col="red")
abline(40.60407-22.75667,-2.80045-0.02733,col="green")
abline(40.60407-11.57307,-2.80045+0.23535,col="blue")
model <- glm(Species~Biomass*pH, poisson)</pre>
summary (model)
model2 <- glm(Species~Biomass+pH, poisson)</pre>
anova (model, model2, test="Chi")
plot(Biomass, Species, pch=21, bg=(1+as.numeric(pH)))
xv < - seq(0,10,0.1)
length(xv)
acidity <- rep("low",101)</pre>
yv <- predict(model,list(Biomass=xv,pH=acidity),type="response")
lines(xv,yv,col="green")
acidity <- rep("mid",101)</pre>
yv <- predict(model,list(Biomass=xv,pH=acidity),type="response")</pre>
lines(xv, yv, col="blue")
acidity <- rep("high",101)</pre>
yv <- predict(model,list(Biomass=xv,pH=acidity),type="response")</pre>
lines(xv, yv, col="red")
# frquency distributions
case.book <- read.csv("c:\\temp\\cases.csv")</pre>
attach(case.book)
names(case.book)
frequencies <- table(cases)</pre>
frequencies
mean(cases)
windows (7,4)
par(mfrow=c(1,2))
barplot(frequencies, ylab="Frequency", xlab="Cases",
col="red", main="observed")
barplot(dpois(0:10,1.775)*80, names=as.character(0:10),
ylab="Frequency", xlab="Cases", col="blue", main="expected")
var(cases)/mean(cases)
negbin <- function(x,u,k)</pre>
    (1+u/k)^{(-k)}*(u/(u+k))^x*gamma(k+x)/(factorial(x)*gamma(k))
xf <- numeric(11)
for (i in 0:10) xf[i+1] \leftarrow negbin(i, 0.8, 0.2)
barplot(xf)
```

```
mean(cases)^2/(var(cases)-mean(cases))
expected <- dnbinom(0:10, size=0.8898, mu=1.775) *80
both <- numeric(22)</pre>
both[1:22 %% 2 != 0] <- frequencies
both[1:22 %% 2 == 0] <- expected
labels <- character(22)</pre>
labels[1:22 %% 2 == 0] <- as.character(0:10)
barplot(both,col=rep(c("lightgray","darkgray"),11),names=labels,ylab="Frequ
ency",xlab="Cases")
legend(locator(1),c("Observed","Expected"), fill=c("lightgray","darkgray"))
cs <- factor(0:10)
levels(cs)[6:11] <- "5+"
levels(cs)
ef <- as.vector(tapply(expected,cs,sum))</pre>
of <- as.vector(tapply(frequencies,cs,sum))</pre>
sum((of-ef)^2/ef)
1 - pchisq(2.581842,3)
```

```
# proportion data
# logistic regression
numbers <- read.csv("c:\\temp\\sexratio.csv")</pre>
numbers
attach(numbers)
windows (7, 4)
par(mfrow=c(1,2))
p <- males/(males+females)</pre>
plot(density,p,ylab="Proportion male")
plot(log(density),p,ylab="Proportion male")
y <- cbind(males, females)</pre>
model <- glm(y~density,binomial)</pre>
summary(model)
model <- glm(y~log(density),binomial)</pre>
summary(model)
xv < - seq(0,6,0.1)
plot(log(density),p,ylab="Proportion male",pch=21,bg="blue")
lines(xv, predict(model, list(density=exp(xv)),
type="response"),col="brown")
# catagorical explanatory variables
germination <- read.csv("c:\\temp\\germination.csv")</pre>
attach(germination)
names (germination)
y <- cbind(count , sample-count)
model <- glm(y ~ Orobanche * extract, binomial)</pre>
summary(model)
model <- glm(y ~ Orobanche * extract, quasibinomial)</pre>
model2 <- update(model, ~ . - Orobanche:extract)</pre>
anova (model, model2, test="F")
anova(model2,test="F")
model3 <- update(model2, ~ . - Orobanche)</pre>
anova(model2, model3, test="F")
coef(model3)
1/(1+1/(\exp(-0.5122)))
1/(1+1/(exp(-0.5122+1.0574)))
tapply(predict(model3, type="response"), extract, mean)
p <- count/sample</pre>
tapply(p,extract,mean)
as.vector(tapply(count,extract,sum))/
```

```
as.vector(tapply(sample, extract, sum))
# ancova with proportion data
props <- read.csv("c:\\temp\\flowering.csv")</pre>
attach (props)
names (props)
y <- cbind(flowered, number-flowered)</pre>
pf <- flowered/number</pre>
pfc <- split(pf,variety)</pre>
dc <- split(dose, variety)</pre>
plot(dose,pf,type="n",ylab="Proportion flowered")
points(jitter(dc[[1]]), jitter(pfc[[1]]), pch=21, bg="red")
points(jitter(dc[[2]]),jitter(pfc[[2]]),pch=22,bg="blue")
points(jitter(dc[[3]]),jitter(pfc[[3]]),pch=23,bg="gray")
points(jitter(dc[[4]]),jitter(pfc[[4]]),pch=24,bg="green")
points(jitter(dc[[5]]),jitter(pfc[[5]]),pch=25,bg="yellow")
model1 <- glm(y~dose*variety,binomial)</pre>
summary(model1)
model2 <- glm(y~dose*variety,quasibinomial)</pre>
summary(model2)
model3 <- glm(y~dose+variety,quasibinomial)</pre>
anova (model2, model3, test="F")
xv < - seq(0,32,0.25)
length(xv)
yv <- predict(model3,list(dose=xv,variety=rep("A",129)),type="response")</pre>
lines(xv, yv, col="red")
yv <- predict(model3,list(dose=xv,variety=rep("B",129)),type="response")</pre>
lines(xv, yv, col="blue")
yv <- predict(model3,list(dose=xv,variety=rep("C",129)),type="response")</pre>
lines(xv,yv,col="gray")
yv <- predict(model3,list(dose=xv,variety=rep("D",129)),type="response")</pre>
lines(xv, yv, col="green")
yv <- predict(model3,list(dose=xv,variety=rep("E",129)),type="response")</pre>
lines(xv,yv,col="yellow")
```

```
# binary response variables
island <- read.csv("c:\\temp\\isolation.csv")</pre>
attach(island)
names (island)
[1] "incidence" "area"
                               "isolation"
model1 <- glm(incidence~area*isolation,binomial)</pre>
model2 <- glm(incidence~area+isolation,binomial)</pre>
anova(model1, model2, test="Chi")
summary(model2)
windows (7,4)
par(mfrow=c(1,2))
xv < - seq(0, 9, 0.01)
modela <- glm(incidence~area, binomial)</pre>
modeli <- glm(incidence~isolation,binomial)</pre>
yv <- predict(modela,list(area=xv),type="response")</pre>
plot(area,incidence,pch=21,bg="yellow")
lines(xv,yv,col="blue")
xv2 < - seq(0,10,0.1)
yv2 <- predict(modeli,list(isolation=xv2),type="response")</pre>
plot(isolation, incidence, pch=21, bg="yellow")
lines(xv2, yv2, col="red")
ac <- cut(area,3)</pre>
ic <- cut(isolation, 3)</pre>
tapply(incidence, ac, sum)
tapply(incidence, ic, sum)
table(ac)
table(ic)
tapply(incidence,ac,sum) / table(ac)
tapply(incidence,ic,sum) / table(ic)
xv < - seq(0, 9, 0.01)
yv <- predict(modela, list(area=xv), type="response")</pre>
plot(area,incidence,pch=21,bg="yellow")
lines(xv, yv, col="blue")
d <- (max(area) - min(area))/3
left <- \min(area) + d/2
mid <- left+d
right <- mid+d
xva <- c(left,mid,right)</pre>
pa <- as.vector(tapply(incidence,ac,sum) / table(ac))</pre>
se <- sqrt(pa*(1-pa)/table(ac))
xv < - seq(0, 9, 0.01)
yv <- predict(modela,list(area=xv),type="response")</pre>
lines(xv, yv, col="blue")
points (xva, pa, pch=16, col="red")
for (i in 1:3) lines(c(xva[i], xva[i]),
```

```
c(pa[i]+se[i],pa[i]-se[i]),col="red" )
xv2 < - seq(0,10,0.1)
yv2 <- predict(modeli,list(isolation=xv2),type="response")</pre>
plot(isolation, incidence, pch=21, bg="yellow")
lines(xv2, yv2, col="red")
d <- (max(isolation)-min(isolation))/3</pre>
left <- min(isolation)+d/2</pre>
mid <- left+d
right <- mid+d
xvi <- c(left,mid,right)</pre>
pi <- as.vector(tapply(incidence,ic,sum) / table(ic))</pre>
se <- sqrt(pi*(1-pi)/table(ic))</pre>
points(xvi,pi,pch=16,col="blue")
for (i in 1:3) lines(c(xvi[i],xvi[i]),
c(pi[i]+se[i],pi[i]-se[i]),col="blue" )
# binary ancova
infection <- read.csv("c:\\temp\\infection.csv")</pre>
attach(infection)
names(infection)
windows (7,4)
par(mfrow=c(1,2))
plot(infected,weight,xlab="Infection",ylab="Weight",col="lightblue")
plot(infected,age,xlab="Infection",ylab="Age", col="lightgreen")
table (infected, sex)
model <- glm(infected~age*weight*sex,family=binomial)</pre>
summary(model)
model2 <- step(model)</pre>
summary(model2)
model3 <- update(model2,~.-age:weight)</pre>
anova(model2, model3, test="Chi")
model4 <- update(model2, ~.-age:sex)</pre>
anova (model2, model4, test="Chi")
model5 <- glm(infected~age+weight+sex,family=binomial)</pre>
summary(model5)
model6 <- glm(infected~age+weight+sex+I(weight^2)+I(age^2),family=binomial)</pre>
summary(model6)
library (mgcv)
model7 <- gam(infected~sex+s(age)+s(weight),family=binomial)</pre>
plot.gam(model7)
model8 <- glm(infected~sex+age+I(age^2)+</pre>
I((weight-12) * (weight>12)), family=binomial)
summary (model8)
model9 <- update(model8, ~.-sex)</pre>
```

```
anova (model8, model9, test="Chi")
model10 <- update (model8, ~.-I(age^2))
anova (model8, model10, test="Chi")
summary (model9)</pre>
```

```
# age at death data
mortality <- read.csv("c:\\temp\\deaths.csv")</pre>
attach (mortality)
names (mortality)
tapply (death, treatment, mean)
tapply(death, treatment, var)
model <- glm(death~treatment, Gamma)</pre>
summary(model)
detach (mortality)
# survival analysis with censoring
library(survival)
sheep <- read.csv("c:\\temp\\sheep.deaths.csv")</pre>
attach (sheep)
names (sheep)
plot(survfit(Surv(death, status)~group), col=c(2,3,4),
xlab="Age at death (months)")
model <- survreg(Surv(death, status) ~weight*group, dist="exponential")</pre>
summary(model)
model2 <- survreg(Surv(death, status) ~weight+group, dist="exponential")</pre>
anova(model, model2, test="Chi")
model3 <- survreg(Surv(death, status) ~group, dist="exponential")</pre>
anova (model2, model3, test="Chi")
model4 <- survreg(Surv(death, status)~1, dist="exponential")</pre>
anova(model3, model4, test="Chi")
summary (model3)
model3 <- survreg(Surv(death, status)~group, dist="exponential")</pre>
model4 <- survreg(Surv(death, status)~group, dist="extreme")</pre>
model5 <- survreg(Surv(death, status) ~group, dist="gaussian")</pre>
model6 <- survreg(Surv(death, status)~group, dist="logistic")</pre>
anova (model3, model4, model5, model6)
tapply(predict(model3, type="response"), group, mean)
tapply(death,group,mean)
```