



请验证以下表格

$$SGN(x) = \begin{cases} 1, x > 0 \\ -1, x = 0 \\ -1, x < 0 \end{cases}$$

表：感知机训练过程

迭代次数	x	y	\hat{y}	w
0	(3.7, -10.5, 27.49)	+1	-1	(0, 0, 0)
1	(4.8, 0.13, 21.75)	-1	+1	(3.7, -10.5, 27.49)
2	(4.9, 1.25, 22.31)	-1	+1	(-1.1, -10.63, 5.74)
3	(4.8, 0.13, 21.75)	-1	-1	(-6., -11.88, -16.57)
4	(3.7, -10.5, 27.49)	+1	-1	(-6., -11.88, -16.57)
5	(4.9, 1.25, 22.31)	-1	+1	(-2.3, -22.38, 10.92)
6	(3.7, -10.5, 27.49)	+1	-1	(-7.2, -23.63, -11.39)
7	(4.9, 1.25, 22.31)	-1	+1	(-3.5, -34.13, 16.1)
8	(4.8, 0.13, 21.75)	-1	-1	(-8.4, -35.38, -6.21)
9	(3.7, -10.5, 27.49)	+1	+1	(-8.4, -35.38, -6.21)
10	(4.9, 1.25, 22.31)	-1	-1	(-8.4, -35.38, -6.21)
11	(4.8, 0.13, 21.75)	-1	-1	(-8.4, -35.38, -6.21)

通过代码验证如下

```
import numpy as np

n = 3

data_x = [
    [3.7, -10.5, 27.49],
    [4.8, 0.13, 21.75],
    [4.9, 1.25, 22.31],
    [4.8, 0.13, 21.75],
    [3.7, -10.5, 27.49],
    [4.9, 1.25, 22.31],
    [3.7, -10.5, 27.49],
    [4.9, 1.25, 22.31],
    [4.8, 0.13, 21.75],
    [3.7, -10.5, 27.49],
    [4.9, 1.25, 22.31],
    [4.8, 0.13, 21.75]]

data_y = [1, -1, -1, -1, 1, -1, 1, -1, -1, 1, -1, -1]

data_x = np.array(data_x)
data_y = np.array(data_y)
```

```
def SGN(x):
    if x > 0:
        return 1
    else:
        return -1
```

```
w = [0, 0, 0]
w = np.array(w)
result = []

for k in range(12):
    # print("k:", k)
    x = data_x[k]
    y = data_y[k]
    wx = np.dot(w, x)
    # print("w^T * x:", wx)
    y_est = SGN(wx)
    # print("y_estimate:", y_est)
    if y_est * y <= 0:
        w = np.add(w, y*x)
    # print("w:", w)
    # print()

    result.append((k, wx, y_est, w))

for (k, wx, y_est, w) in result:
    print(f"k: {k}, w^T * x: {wx}, y_estimate: {y_est}, w: {w}")
```

```
k: 0, w^T * x: 0.00, y_estimate: -1, w: [ 3.7 -10.5 27.49]
k: 1, w^T * x: 614.30, y_estimate: 1, w: [ -1.1 -10.63 5.74]
k: 2, w^T * x: 109.38, y_estimate: 1, w: [ -6. -11.88 -16.57]
k: 3, w^T * x: -390.74, y_estimate: -1, w: [ -6. -11.88 -16.57]
k: 4, w^T * x: -352.97, y_estimate: -1, w: [ -2.3 -22.38 10.92]
k: 5, w^T * x: 204.38, y_estimate: 1, w: [ -7.2 -23.63 -11.39]
k: 6, w^T * x: -91.64, y_estimate: -1, w: [ -3.5 -34.13 16.1 ]
k: 7, w^T * x: 299.38, y_estimate: 1, w: [ -8.4 -35.38 -6.21]
k: 8, w^T * x: -179.99, y_estimate: -1, w: [ -8.4 -35.38 -6.21]
k: 9, w^T * x: 169.70, y_estimate: 1, w: [ -8.4 -35.38 -6.21]
k: 10, w^T * x: -223.93, y_estimate: -1, w: [ -8.4 -35.38 -6.21]
k: 11, w^T * x: -179.99, y_estimate: -1, w: [ -8.4 -35.38 -6.21]
```