

$$\int \frac{8-3x}{(x+1)(x^2-4x-5)} dx = \int \frac{8-3x}{(x+1)(x+1)(x-5)} dx$$

use partial
fractions

$$\frac{8-3x}{(x+1)^2(x-5)} = \frac{A}{x+1} + \frac{B}{(x+1)^2} + \frac{C}{x-5}$$

$$8-3x = A(x+1)(x-5) + B(x-5) + C(x+1)^2$$

$$x=5 \Rightarrow -7 = 36C$$

$$C = -7/36$$

$$x=-1 \Rightarrow 11 = -6B \Rightarrow B = -11/6$$

$$x=0 \Rightarrow 8 = -5A - 5B + C$$

$$8 = -5A + \frac{55}{6} - \frac{7}{36}$$

$$A = \frac{-\frac{55}{6} + \frac{7}{36} - 8}{5} = \frac{\frac{-49}{36}}{5} = \frac{-49}{180} = \frac{49}{180}$$

$$\int \frac{8-3x}{(x+1)(x^2-4x-5)} dx = \frac{49}{180} \int \frac{dx}{x+1} - \frac{11}{6} \int \frac{dx}{(x+1)^2} - \frac{7}{36} \int \frac{dx}{x-5}$$

$$= \frac{49}{180} \ln|x+1| + \frac{11}{6} \frac{1}{x+1} - \frac{7}{36} \ln|x-5| + C$$