

Announcements

• HW 1 Due Thurs

Jan 29th 11:59 PM

(Do before quiz)

• Quiz 1 Thurs Jan

29th in discussion

• Lecture Review

◦ Def) Population

The population is the entire group being studied, of size N

◦ Def) Sample

A sample is a subset of the population which we draw data from, size n

$$\{x_1, x_2, \dots, x_n\}$$

$$\{x_1, x_2, x_3, x_4\}$$

◦ Example)

You conduct study, average height UI undergrad

by sampling 100 people on Pentacrest

Population: UI undergrads

Sample: 100 people on Pentacrest

o Def) Parameter

A parameter is a numerical summary of the population

o Def) Statistic

A statistic is a numerical summary of the sample

o Ex)

Parameter μ = average

height of all underground

Statistic \bar{x} = average

height of 100 people

on Pentacrest

o Def) Sample Mean

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i \quad \Sigma x_i$$

"balance point of the
data"

• Example) 5 people

pool money together

$$\{10, 5, 3, 7, 20\}$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$= \frac{1}{5} \sum_{i=1}^5 x_i$$

$$= \frac{1}{5} [10 + 5 + 3 + 7 + 20]$$

$$= \frac{1}{5} [45] = 9$$

• Def) Median

"middle" of the data

half the data is below
median, half above

• Example

$$\text{Data} = \{1, 2, 3, 6, 7, 8\}$$

$$\frac{3+6}{2} = \frac{9}{2} = 4.5 = \text{median}$$

$$\text{Data} = \{1, 2, 3, 7, 8\}$$

Median = 3

• Def) Mode

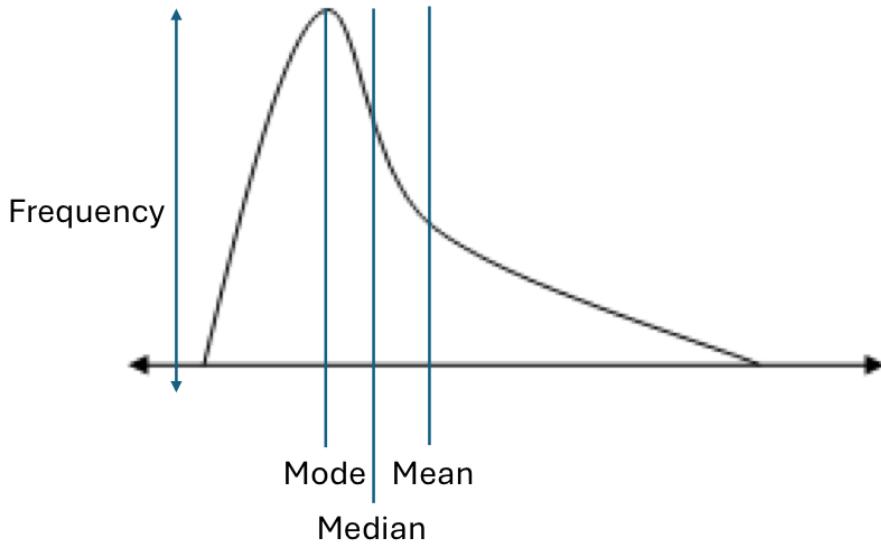
Data Point that "appears" most often

• Examples

$$\text{Data} = \{1, 2, 2, 2, 3, 3, 5\}$$

Mode = 2

This graph is said to have right-skew. Think of it as “right-tailed.” Where is the mean, median, and mode on this graph?



Problem 1: Two samples are drawn and listed below:

$$\text{List A: } \{47, 48, 49, 50, 51, 52, 53\} \quad n = 7$$
$$\text{List B: } \{20, 30, 40, 50, 60, 70, 80\}$$

a. What is the sample mean of each list?

b. What is the sample median of each list?

(a)

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$
$$= \frac{1}{7} \left[47 + 48 + \dots + 53 \right]$$

$$\bar{x} = \frac{1}{7}[350] = 50$$

List B, $\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$

$$\bar{x} = \frac{1}{7}[350] = 50$$

(b) $\bar{x} = \frac{1}{7}[47, 48, 49, 50, 51, 52, 53]$
 $= 50$

Def) Population Variance

$$\sigma^2 = \frac{1}{N} \sum (x_i - \mu)^2$$

represents the "spread"
of the data

$$\mu = \text{Population mean} = \frac{1}{N} \sum_{i=1}^N x_i$$

Def) Sample Variance

$$s^2 = \frac{1}{n-1} \sum (x_i - \bar{x})^2$$

$\frac{1}{n-1}$ instead of $\frac{1}{n}$

Bessel's correction
error in estimating \bar{x} instead
of μ causes sample
variance to be too small

c Def) Population &

Sample SD

$$\sigma = \sqrt{\sigma^2}, S = \sqrt{S^2}$$

Calculate the "typical distance"

from the mean"

List A: {47, 48, 49, 50, 51, 52, 53}

List B: {20, 30, 40, 50, 60, 70, 80}

c. Without calculating, which list do you expect to have a lower sample standard deviation?

d. What is the sample variance of each list? (Feel free to use Excel)

e. What is the sample standard deviation of each list?

f. What is $\sum x_i$ of each list?

(c) Standard Deviation is
"average spread" of
Data. List A has lower
Standard Deviation

(f)

$$\bar{x} = \frac{1}{n} \sum x_i, \sum x_i = 350$$

Problem 2: Answer the following summation problems:

$$x_1 = 9, x_2 = 9, x_3 = 12$$

a. Σx_i

b. $\Sigma(x_i - \bar{x})$

c. $\Sigma(x_i - \bar{x})^2$

(a) $\Sigma x_i, \sum_{i=1}^n x_i$

$$\sum x_i = \sum_{i=1}^3 x_i$$

$$= 9 + 9 + 12 = 30$$

(b) $\Sigma(x_i - \bar{x})$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$= \frac{1}{3} \sum_{i=1}^3 x_i$$

$$= \frac{1}{3}(30) = 10$$

(c) $\Sigma(x_i - \bar{x})^2$

$$= [(9-10)^2 + (9-10)^2 + (12-10)^2]$$

$$= [(-1)^2 + (-1)^2 + (2)^2] = 6$$

Problem 3: Mean, Median, and Mode Problems:

a. There are 3 exams in a particular semester where every exam is weighted equally. If you score an 87 and an 85, what do you need on the 3rd exam for your mean to be a 90?

b. Is it possible to have a larger sample size than a population size? Why or why not?

$$x_1 = 87, x_2 = 85, x_3 = ?$$

$$\bar{x} = 90$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i = \frac{1}{3} \sum x_i$$

$$90 = \frac{1}{3} [87 + 85 + x_3]$$

$$270 = [87 + 85 + x_3]$$

$$98 = x_3$$

(b) No, we can't draw a larger subset than the population

Problem 4: Calculate the sample variance by hand.

$$\{-5, 0, 5\}$$

$$S^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$(n=3)$

$$S^2 = \frac{1}{(3)-1} \sum_{i=1}^3 (x_i - \bar{x})^2$$
$$\bar{x} = \frac{1}{n} \sum x_i = \frac{1}{3} (-5+0+5)$$

$$S^2 = \frac{1}{2} \sum_{i=1}^3 (x_i - 0)^2$$
$$= \frac{1}{2} [(-5)^2 + 0^2 + 5^2]$$
$$= \frac{1}{2} [50] = 25$$