

Announcements

• HW 1 Due Thurs

Jan 29th 11:59 PM

(Do before quiz)

• Quiz 1 Thurs Jan

29th in discussion

• Lecture Review

• Def) Population

The population is the entire group being studied, of size N

• Def) Sample

A sample is a subset of the population which we draw data from, size n

$$\{X_1, X_2, \dots, X_n\}$$

• Example) $\{X_1, X_2, X_3, X_4\}$

You conduct study, average height UI undergrads by sampling 100 people on Pentacrest

Population: UI undergrads

Sample: 100 people on Pentacrest

- Def) Parameter

A parameter is a numerical summary of the population

- Def) Statistic

A statistic is a numerical summary of the sample

- Ex)

Parameter μ = average height of UI undergrads

Statistic \bar{X} = average height of 100 people on Pentacrest

- Def) Sample Mean

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i \quad \sum X_i$$

"balance point of the data"

• Example) 5 people
pool money together

$\{10, 5, 3, 7, 20\}$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$= \frac{1}{5} \sum_{i=1}^5 x_i$$

$$= \frac{1}{5} [10 + 5 + 3 + 7 + 20]$$

$$= \frac{1}{5} [45] = 9$$

• Def) Median

"middle" of the data

half the data is below
median, half above

• Example

data = $\{ \cancel{1}, \cancel{2}, 3, 6, \cancel{7}, \cancel{8} \}$

$$\frac{3+6}{2} = \frac{9}{2} = 4.5 = \text{median}$$

data = $\{ \cancel{1}, \cancel{2}, 3, \cancel{7}, \cancel{8} \}$

median = 3

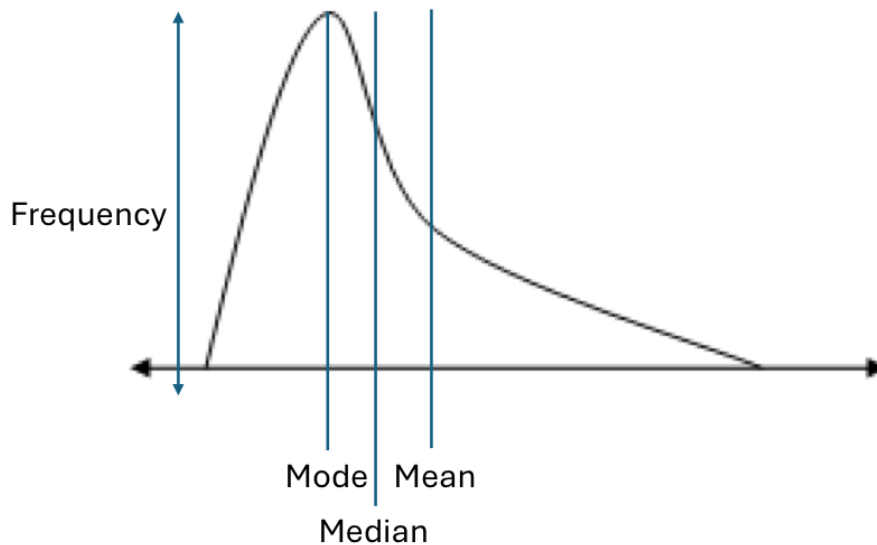
• Def) Mode
data point that "appears"
most often

• Example

data = $\{ 1, 2, 2, 2, 3, 3, 5 \}$

mode = 2

This graph is said to have right-skew. Think of it as “right-tailed.”
Where is the mean, median, and mode on this graph?



Problem 1: Two samples are drawn and listed below:

List A: {47, 48, 49, 50, 51, 52, 53}

List B: {20, 30, 40, 50, 60, 70, 80}

$n = 7$

a. What is the sample mean of each list?

b. What is the sample median of each list?

(a)

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$$

$$= \frac{1}{7} [47 + 48 + \dots + 53]$$

$$= \frac{1}{7} [350] = 50$$

list B, $\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$

$$= \frac{1}{7} [350] = 50$$

(b)

~~{47, 48, 49, 50, 51, 52, 53}~~

$$= 50$$

• Def) Population Variance

$$\sigma^2 = \frac{1}{N} \sum (x_i - \mu)^2$$

represents the "spread" of the data

$$\mu = \text{Population mean} = \frac{1}{N} \sum_{i=1}^N x_i$$

• Def) Sample Variance

$$s^2 = \frac{1}{n-1} \sum (x_i - \bar{x})^2$$

$\frac{1}{n-1}$ instead of $\frac{1}{n}$

Bessel's correction
error in estimating \bar{x} instead
of μ causes sample
variance to be too small

• Def) Population &
Sample SD

$$\sigma = \sqrt{\sigma^2}, \quad s = \sqrt{s^2}$$

Calculate the "typical distance
from the mean"

List A: {47, 48, 49, 50, 51, 52, 53}

List B: {20, 30, 40, 50, 60, 70, 80}

c. Without calculating, which list do you expect to have a lower sample standard deviation?

d. What is the sample variance of each list? (Feel free to use *Excel*)

e. What is the sample standard deviation of each list?

f. What is $\sum x_i$ of each list?

(c) Standard deviation is "average spread" of data. List A has lower standard deviation

(f)

$$\bar{x} = \frac{1}{n} \sum x_i, \sum x_i = 350$$

Problem 2: Answer the following summation problems:

$$x_1 = 9, x_2 = 9, x_3 = 12$$

a. $\sum x_i$

b. $\sum (x_i - \bar{x})$

c. $\sum (x_i - \bar{x})^2$

$$(a) \sum x_i, \sum_{i=1}^n x_i$$

$$\sum x_i = \sum_{i=1}^3 x_i$$

$$= 9 + 9 + 12 = 30$$

$$(b) \sum (x_i - \bar{x})$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$= \frac{1}{3} \sum_{i=1}^3 x_i$$

$$= \frac{1}{3} (30) = 10$$

$$(c) \sum (x_i - \bar{x})^2$$

$$= [(9-10)^2 + (9-10)^2 + (12-10)^2]$$

$$= [(-1)^2 + (-1)^2 + (2)^2] = 6$$

Problem 3: Mean, Median, and Mode Problems:

- a. There are 3 exams in a particular semester where every exam is weighted equally. If you score an 87 and an 85, what do you need on the 3rd exam for your mean to be a 90?
- b. Is it possible to have a larger sample size than a population size? Why or why not?

$$X_1 = 87, X_2 = 85, X_3 = ?$$

$$\bar{X} = 90$$

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i = \frac{1}{3} \sum X_i$$

$$90 = \frac{1}{3} [87 + 85 + X_3]$$

$$270 = [87 + 85 + X_3]$$

$$98 = X_3$$

(b) No, we can't draw a larger subset than the population

Problem 4: Calculate the sample variance by hand.

~~$\{-5, 0, 5\}$~~

$$S^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$(n=3)$

$$S^2 = \frac{1}{(3)-1} \sum_{i=1}^3 (x_i - \bar{x})^2$$

$$\bar{x} = \frac{1}{n} \sum x_i = \frac{1}{3} (-5 + 0 + 5)$$

$$= 0$$
$$S^2 = \frac{1}{2} \sum_{i=1}^3 (x_i - 0)^2$$

$$= \frac{1}{2} [(-5)^2 + 0^2 + 5^2]$$

$$= \frac{1}{2} [50] = 25$$