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- $\mathbb{E}_{t+1}[a_i]$ and $\mathbb{V}_{t+1}[a_i]$ are referred to as the posterior beliefs

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These properties may not always be desirable, but they are intrinsic to Bayesianism