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- Overlay histogram of sampling distribution with fitted normal density

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- Show $m_N = \min_i \{X_i\}_{i=1}^N$ converges to Exponential if $X \sim$ Exponential