## **Summary Table for Statistical Techniques**

## **ESTIMATES**

Inference	Parameter	Statistic	Type of Data	Examples	Analysis	Conditions
Estimating a proportion	One population proportion p	sample proportion $\hat{p}$	categorical (binary)	What is the proportion of males in the world?  What is the proportion of students that smoke?	1-proportion Z-interval $\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$	n $\hat{p} \ge 10$ and n $(1-\hat{p}) \ge 10$
Estimating a mean	One population mean µ	sample mean $\frac{\overline{x}}{x}$	quantitative	What is the average weight of adults?  What is the average cholesterol level of adult females?	1-sample t-interval $\overline{x} \pm t^* \frac{s}{\sqrt{n}}$	data approximately normal or have a large sample size $(n \ge 30)$
Estimating the difference of two proportions	difference in two population proportions P <sub>1</sub> -P <sub>2</sub>	difference in two sample proportions $\hat{p}_1 - \hat{p}_2$	categorical (binary)	Are the percentages of male and female smokers different?  Are the percentages of upper- and lower- class binge drinkers different?	two-proportions Z-interval $(\hat{p}_1 - \hat{p}_2) \pm \\ z^* \times s.e{\hat{p}_1 - \hat{p}_2}$ See notes for s.e. formula	independent samples from the two populations $ n \ \hat{p} \ge 10 \ \text{and} \ (1-n) \ \hat{p} \ge 10 $ for each sample
Estimating the difference of two means	difference in two population means $\mu_1$ - $\mu_2$	difference in two sample means $\overline{x}_1 - \overline{x}_2$	quantitative	Are the mean GPAs of males and females different?  Do vitamin C takers get, on average, fewer colds than non vitamin C takers?	two-sample t-interval $(\overline{x}_1 - \overline{x}_2) \pm t^* \times s.e{\overline{x}_1 - \overline{x}_2}$ See text, page 445, for the s.e. of the difference	independent samples from the two populations data in each sample are about normal or large samples $(n_i \geq 30)$
Estimating a mean with paired data	mean of paired difference $\mu_D$	sample mean of difference $\overline{x}_d$	quantitative	Is there a difference in pulse rates, on the average, before and after exercise?	paired t-interval $\overline{x}_d \pm t^* \frac{s_d}{\sqrt{n}}$	differences approximately normal or $ \label{eq:continuous} $ have a large number of pairs $ (n \geq 30) $

## **TESTS**

Inference	Parameter	Statistic	Type of Data	Examples	Analysis	Conditions
Test about a mean	One population mean µ	sample mean $\bar{x}$	quantitative	Is the average GPA of juniors at Penn State higher than 3.0?  Is the average Winter temperature in State College less than 42°F?	$\begin{split} H_o \colon \mu &= \mu_o \\ H_a \colon \mu \neq \mu_o  \text{or} \ H_a \colon \mu > \mu_o \\ \text{or}  H_a \colon \mu < \mu_o \\ \text{The one sample t test:} \\ t &= \frac{\overline{x} - \mu_o}{\frac{s}{\sqrt{n}}} \\ H_o \colon p = p_o \end{split}$	data approximately normal or have a large sample size $(n \ge 30)$
Test about a proportion	One population proportion p	sample proportion $\hat{p}$	categorical (binary)	Is the proportion of females different from 0.5?  Is the proportion of students who fail Stat200 less than 0.1?	$\begin{aligned} H_o: p &= p_o \\ H_a: p &\neq p_o \text{ or } H_a: p > p_o \\ \text{or } H_a: p &< p_o \\ \text{The one proportion Z-test:} \end{aligned}$ $z &= \frac{\hat{p} - p_o}{\sqrt{\frac{p_o(1 - p_o)}{n}}}$	$n p_o \ge 10$ and $n (1-p_o) \ge 10$
Test to compare two means	difference in two population means $\mu_1$ - $\mu_2$	difference in two sample means $\overline{x}_1 - \overline{x}_2$	quantitative	Do the mean pulse rates of exercisers and non-exercisers differ?  Is the mean EDS score for dropouts greater than the mean EDS score for graduates?	$\begin{aligned} &H_0\colon \mu_1=\mu_2\\ &H_a\colon \mu_1\neq \mu_2  \text{or } H_a\colon \mu_1>\mu_2\\ &\text{or }  H_a\colon \mu_1<\mu_2\\ &\text{The two sample t test:} \\ &t=\frac{(\overline{x}_1-\overline{x}_2)-0}{s.e{\overline{x}_1-\overline{x}_2}}\\ &\text{See text, page 445, for the s.e. of the difference} \end{aligned}$	independent samples from the two populations data in each sample are about normal or large samples $(n_i \geq  30)$
Test about a mean with paired data	mean of paired difference $\mu_D$	sample mean of difference $\overline{x}_d$	quantitative	Is the difference in IQ of pairs of twins zero?  Are the pulse rates of people higher after exercise?	$H_{o}: \mu_{D} = 0$ $H_{a}: \mu_{D} \neq 0 \text{ or } H_{a}: \mu_{D} > 0$ $\text{or } H_{a}: \mu_{D} < 0$ $t = \frac{\overline{x}_{d} - \mu_{d}}{s_{d}}$	differences approximately normal or have a large number of pairs $(n \ge 30)$
Test to compare two proportions	difference in two population proportions p <sub>1</sub> -p <sub>2</sub>	difference in two sample proportions $\hat{p}_1 - \hat{p}_2$	categorical (binary)	Is the percentage of males with lung cancer higher than the percentage of females with lung cancer?  Are the percentages of upper- and lower-class binge drinkers different?	$\begin{aligned} &H_o\colon p_1=p_2\\ &H_a\colon p_1\neq p_2  \text{or } H_a\colon p_1>p_2\\ &\text{or } &H_a\colon p_1< p_2\\ &\text{The two proportion z test:} \end{aligned}$ $z=\frac{(\hat{p}_1-\hat{p}_2)-0}{s.e{\hat{p}_1-\hat{p}_2}}$ See notes for s.e. formula	independent samples from the two populations $\hat{p} \ge 10$ and $(1-n)$ $\hat{p} \ge 10$ for each sample (or at least 5 for a two-tailed test).

	Test to compare several means	Population means of the k populations $\mu_1, \mu_2, \dots, \mu_k$	Sample means of the $k$ populations $x_1, x_2, \dots, x_k$	quantitative	Is there a difference between the mean GPA of Freshman, Sophomore, Junior and Senior classes?	H <sub>o</sub> : $\mu_{1}=\mu_{2}=\cdots=\mu_{k}$ H <sub>a</sub> : not all the means are equal The F test for one-way ANOVA: $F = \frac{MS_{Between}}{MS_{Within}}$	each population is normally distributed independent samples from the k populations equal population standard deviations
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## RELATIONSHIPS

Inference	Parameter	Statistic	Type of Data	Examples	Analysis	Conditions
Test about a slope	slope of the population regression line β	sample estimate of the slope b	quantitative	Can height be used to predict weight?	$\begin{aligned} &H_{o} \colon \beta = 0 \\ &H_{a} \colon \beta \neq 0  \text{or } H_{a} \colon \beta > 0 \\ &\text{or } &H_{a} \colon \beta < 0 \\ &\text{The t test with n-2 degrees of freedom:} \\ &t = \frac{b-0}{s.e.(b)} \end{aligned}$	<ul> <li>relationship must be linear</li> <li>the error terms are normally distributed</li> <li>the errors terms have equal variances</li> <li>the error terms are independent of each other</li> </ul>
Association between categorical variables	relationship between two or more categorical variables	the observed counts in a two-way table	categorical	Is there a relationship between smoking and lung cancer?	$H_{o}$ : The two variables are not related $H_{a}$ : The two variables are related The chi-square statistic: $\chi^{2} = \sum_{\substack{all \ cells}} \frac{(Observed-Expected)^{2}}{Expected}$	- all expected counts must be at least 5
Association between two quantitative variables	ρ	Pearson's r	quantitative	Is there a linear relationship between height and weight of a person?	H <sub>o</sub> : $\rho = 0$ H <sub>a</sub> : $\rho \neq 0$ $t = \frac{r}{\sqrt{\frac{1 - r^2}{n - 2}}}$ n-2 degrees of freedom	- relationship must be linear