Design of Digital Circuits
Lecture 21: SIMD Processors II and Graphics Processing Units

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New Course: Bachelor's Seminar in Comp Arch

- Fall 2018
- 2 credit units

- **Rigorous seminar on fundamental and cutting-edge topics in computer architecture**

- Critical presentation, review, and discussion of seminal works in computer architecture
  - We will cover many ideas & issues, analyze their tradeoffs, perform critical thinking and brainstorming

- Participation, presentation, report and review writing
- Stay tuned for more information

Agenda for Today & Next Few Lectures

- Single-cycle Microarchitectures
- Multi-cycle and Microprogrammed Microarchitectures
- Pipelining
- Issues in Pipelining: Control & Data Dependence Handling, State Maintenance and Recovery, …
- Out-of-Order Execution
- Other Execution Paradigms

Readings for Today

- Peleg and Weiser, "MMX Technology Extension to the Intel Architecture," IEEE Micro 1996.

- Lindholm et al., "NVIDIA Tesla: A Unified Graphics and Computing Architecture," IEEE Micro 2008.

Other Approaches to Concurrency (or Instruction Level Parallelism)

Approaches to (Instruction-Level) Concurrency

- Pipelining
- Out-of-order execution
- Dataflow (at the ISA level)
- Superscalar Execution
- VLIW
- Fine-Grained Multithreading
- SIMD Processing (Vector and array processors, GPUs)
- Decoupled Access Execute
- Systolic Arrays

SIMD Processing:
Exploiting Regular (Data) Parallelism

Recall: Flynn's Taxonomy of Computers

- Mike Flynn, "Very High-Speed Computing Systems," Proc. of IEEE, 1966

- SISD: Single instruction operates on single data element
- SIMD: Single instruction operates on multiple data elements
  - Array processor
  - Vector processor
- MISD: Multiple instructions operate on single data element
  - Closest form: systolic array processor, streaming processor
- MIMD: Multiple instructions operate on multiple data elements (multiple instruction streams)
  - Multiprocessor
  - Multithreaded processor

Recall: SIMD Processing

- Single instruction operates on multiple data elements
  - In time or in space
- Multiple processing elements

- Time-space duality

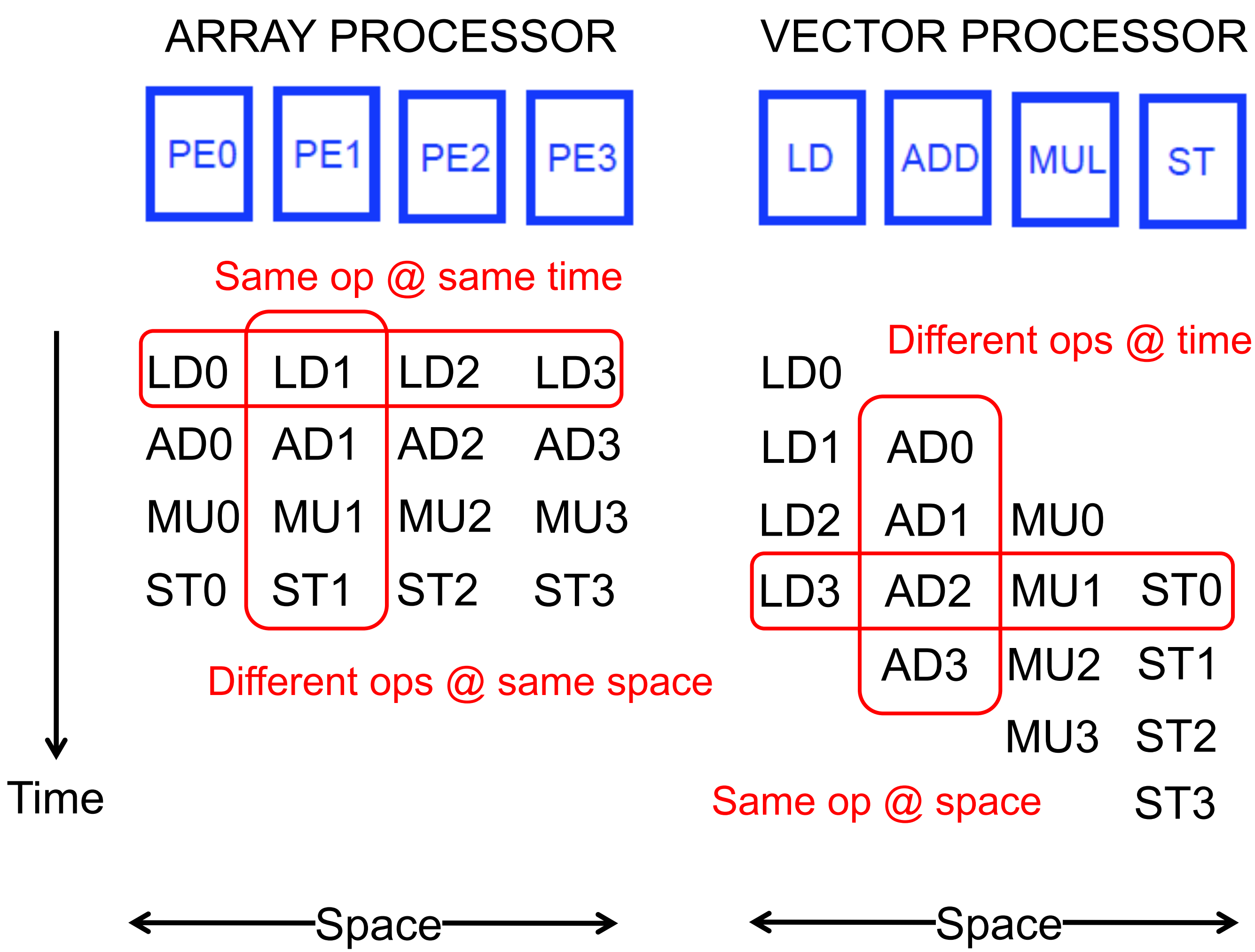
  - Array processor: Instruction operates on multiple data elements at the same time using different spaces

  - Vector processor: Instruction operates on multiple data elements in consecutive time steps using the same space

Recall: Array vs. Vector Processors

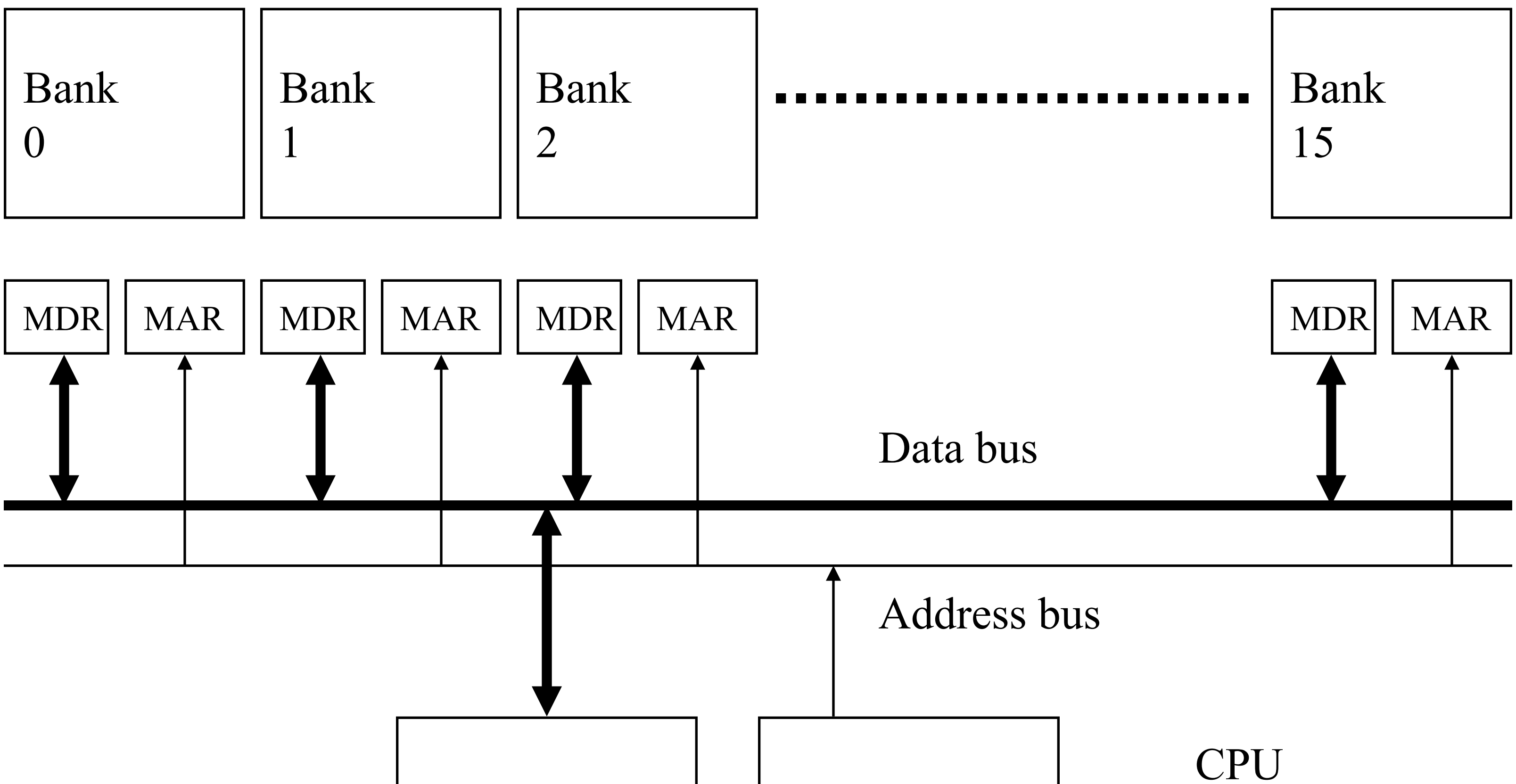
Instruction Stream

```
LD    VR ← A[3:0]
ADD   VR ← VR, 1
MUL   VR ← VR, 2
ST    A[3:0] ← VR
```



Recall: Memory Banking

- Memory is divided into banks that can be accessed independently; banks share address and data buses (to minimize pin cost)
- Can start and complete one bank access per cycle
- Can sustain N parallel accesses if all N go to different banks



Picture credit: Derek Chiou

Some Issues

- Stride and banking
  - As long as they are *relatively prime* to each other and there are enough banks to cover bank access latency, we can sustain 1 element/cycle throughput

- Storage of a matrix
  - Row major: Consecutive elements in a row are laid out consecutively in memory
  - Column major: Consecutive elements in a column are laid out consecutively in memory
  - You need to change the stride when accessing a row versus column

Matrix Multiplication

- A and B, both in row-major order

A_0	0	1	2	3	4	5
	6	7	8	9	10	11

$A_{4x6}\ B_{6x10} \rightarrow C_{4x10}$

Dot products of rows and columns of A and B

B_0	0	1	2	3	4	5	6	7	8	9
	10	11	12	13	14	15	16	17	18	19
	20									
	30									
	40									
	50									

- A: Load A_0 into vector register V_1
  - Each time, increment address by one to access the next column
  - Accesses have a stride of 1
- B: Load B_0 into vector register V_2
  - Each time, increment address by 10
  - Accesses have a stride of 10

Different strides can lead to bank conflicts

How do we minimize them?

Minimizing Bank Conflicts

- More banks

- Better data layout to match the access pattern
  - Is this always possible?

- Better mapping of address to bank
  - E.g., randomized mapping
  - Rau, "Pseudo-randomly interleaved memory," ISCA 1991.

Recall: Questions (II)

- What if vector data is not stored in a strided fashion in memory? (irregular memory access to a vector)
  - Idea: Use indirection to combine/pack elements into vector registers
  - Called scatter/gather operations

Gather/Scatter Operations

Want to vectorize loops with indirect accesses:

```
for (i=0; i<N; i++)
    A[i] = B[i] + C[D[i]]
```

Indexed load instruction (*Gather*)

```
LV vD, rD          # Load indices in D vector
LVI vC, rC, vD     # Load indirect from rC base
LV vB, rB          # Load B vector
ADDV.D vA,vB,vC    # Do add
SV vA, rA          # Store result
```

Gather/Scatter Operations

- Gather/scatter operations often implemented in hardware to handle sparse vectors (matrices)
- Vector loads and stores use an index vector which is added to the base register to generate the addresses

- *Scatter* example

Index Vector	Data Vector (to Store)	Stored Vector (in Memory)	
0	3.14	Base+0	3.14
2	6.5	Base+1	X
6	71.2	Base+2	6.5
7	2.71	Base+3	X
		Base+4	X
		Base+5	X
		Base+6	71.2
		Base+7	2.71

Array vs. Vector Processors, Revisited

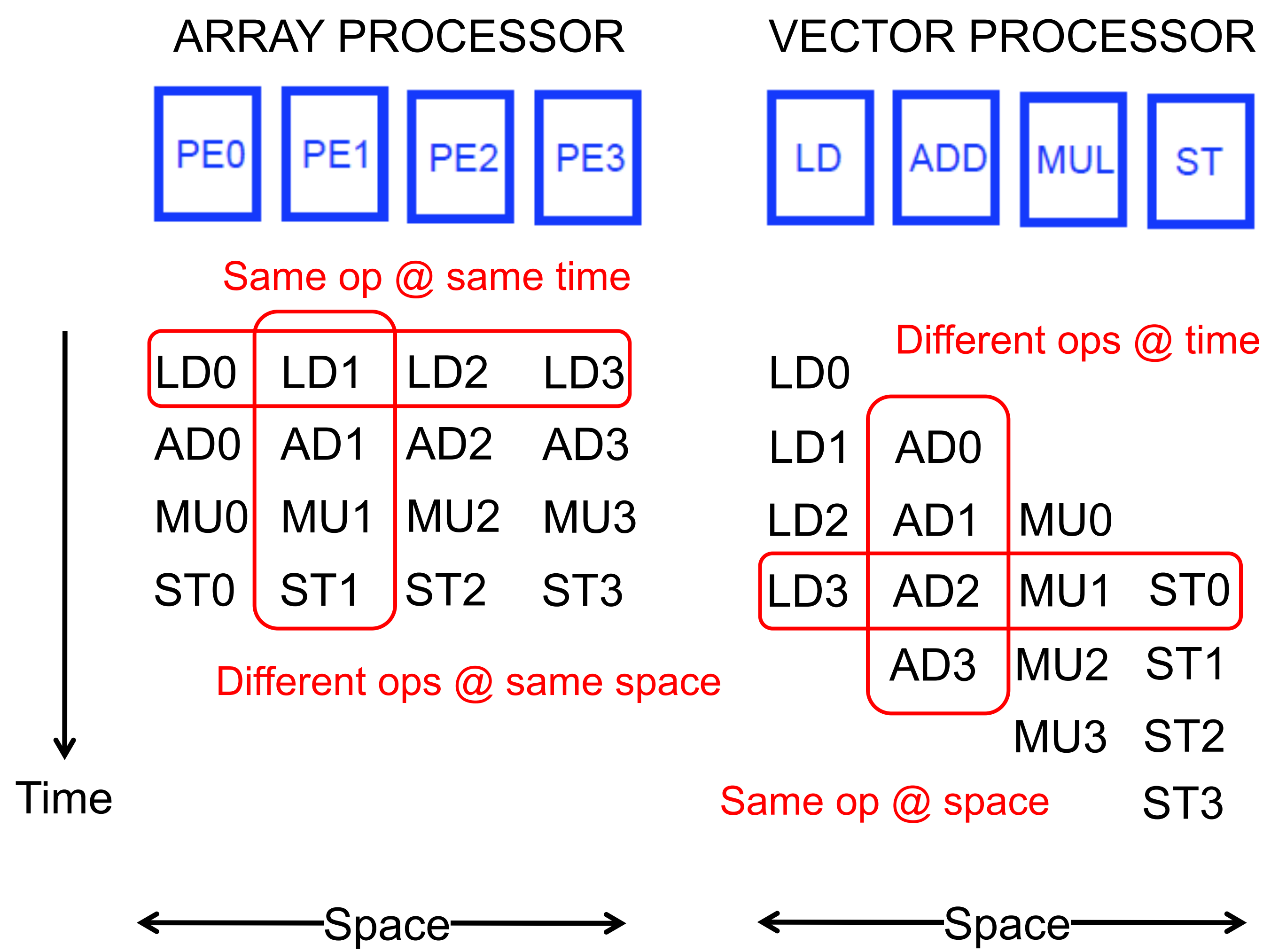
- Array vs. vector processor distinction is a "purist's" distinction

- Most "modern" SIMD processors are a combination of both
  - They exploit data parallelism in both time and space
  - GPUs are a prime example we will cover in a bit more detail

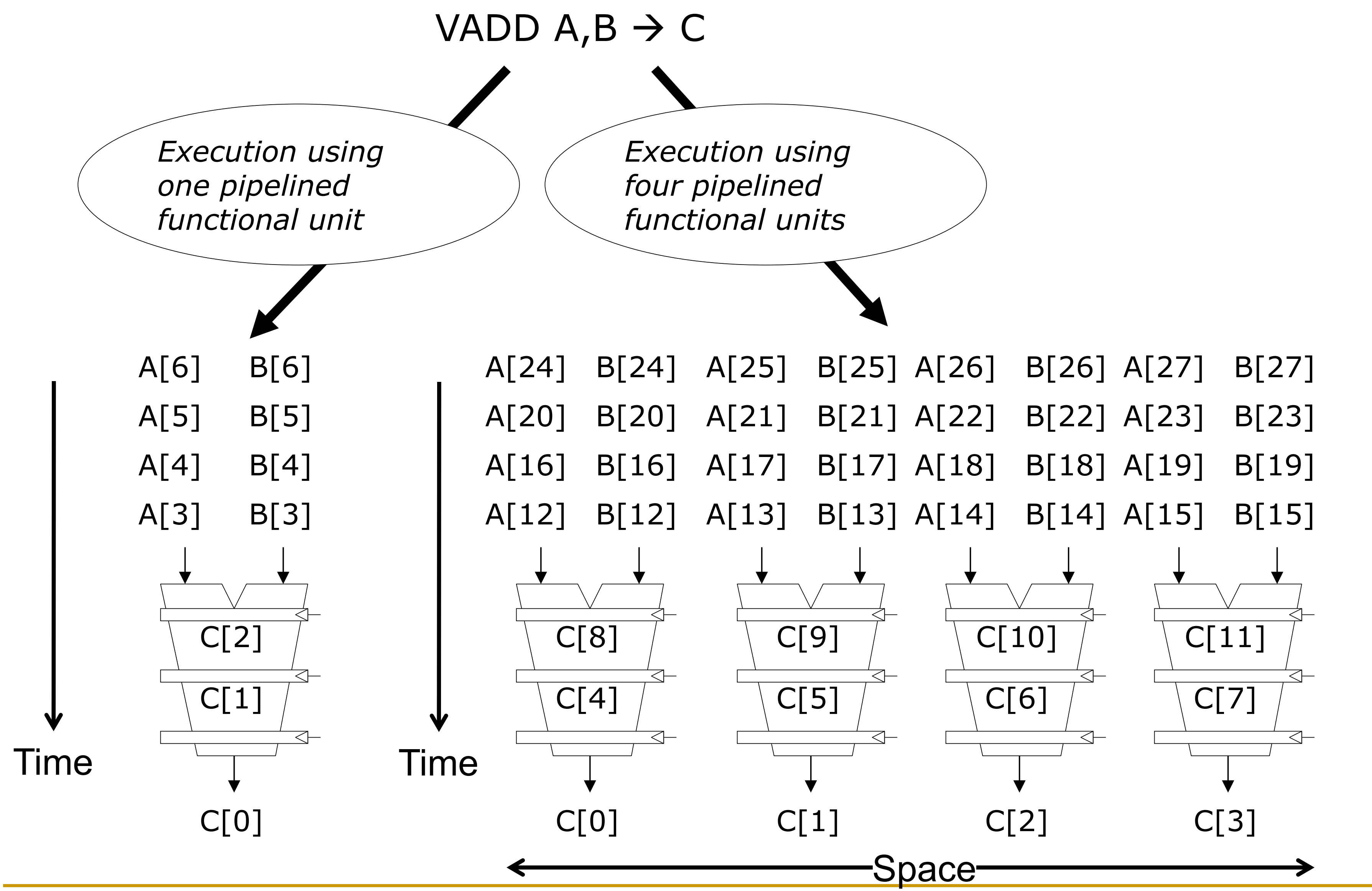
Recall: Array vs. Vector Processors

Instruction Stream

LD VR ← A[3:0]
ADD VR ← VR, 1
MUL VR ← VR, 2
ST A[3:0] ← VR

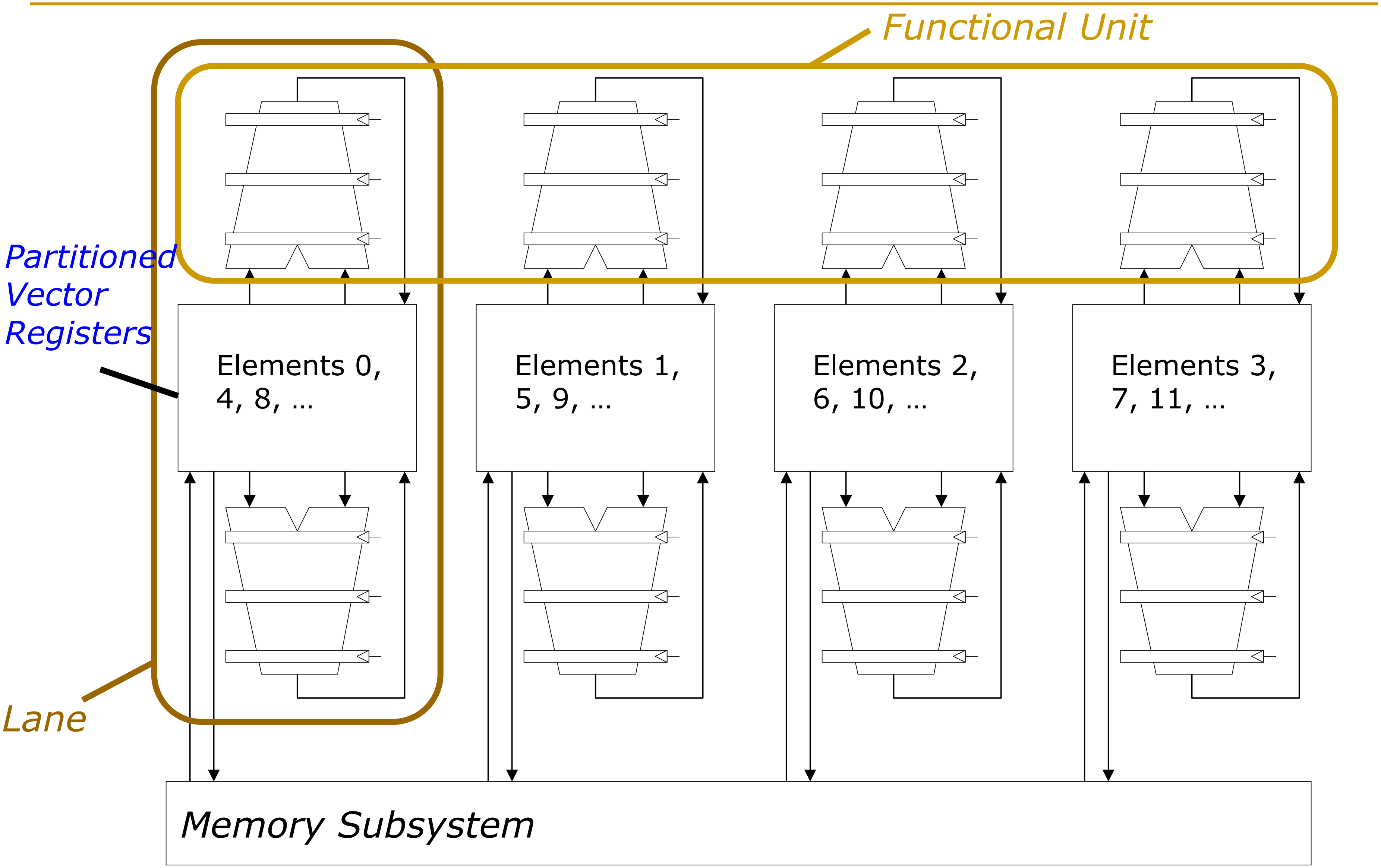


Vector Instruction Execution



Slide credit: Krste Asanovic

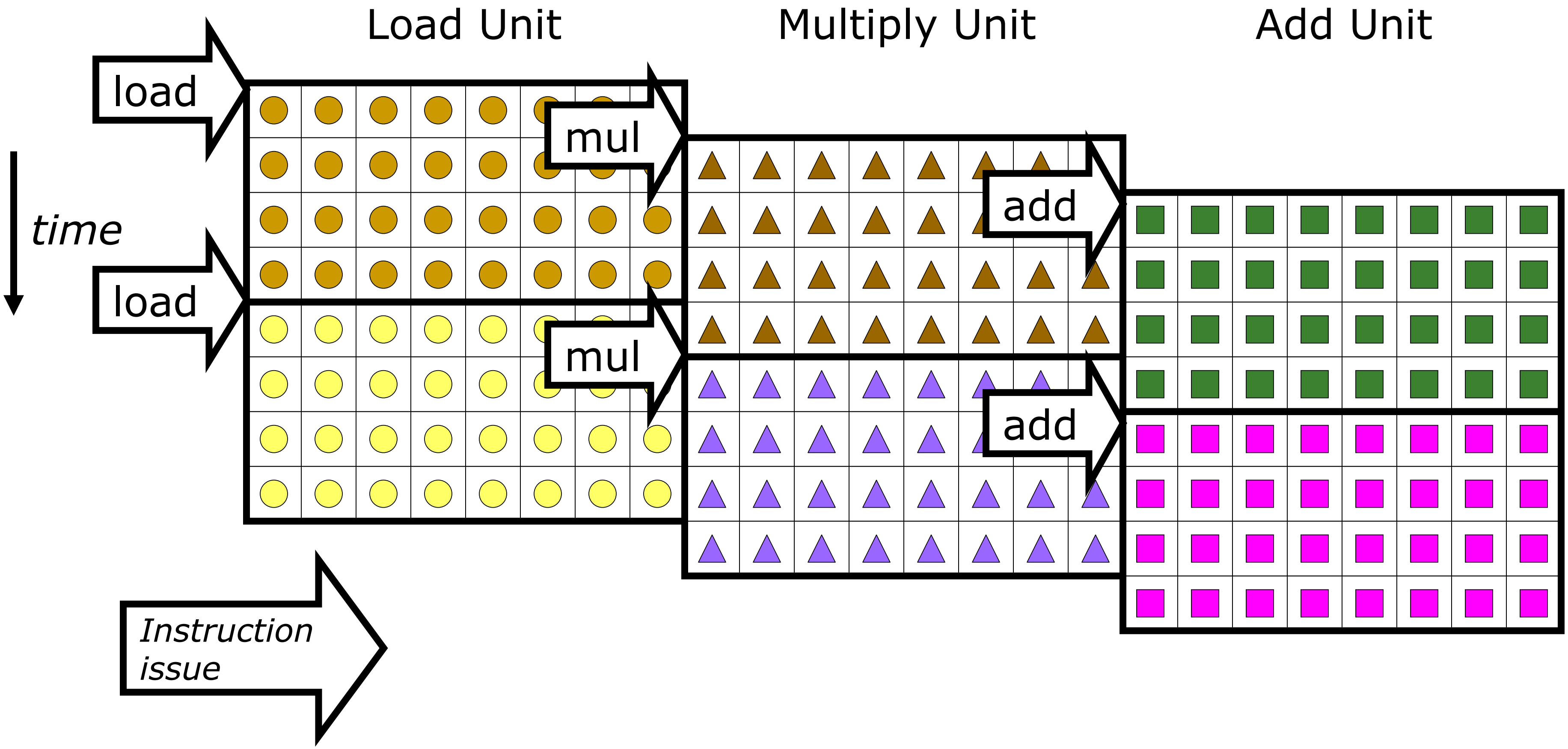
Vector Unit Structure



Vector Instruction Level Parallelism

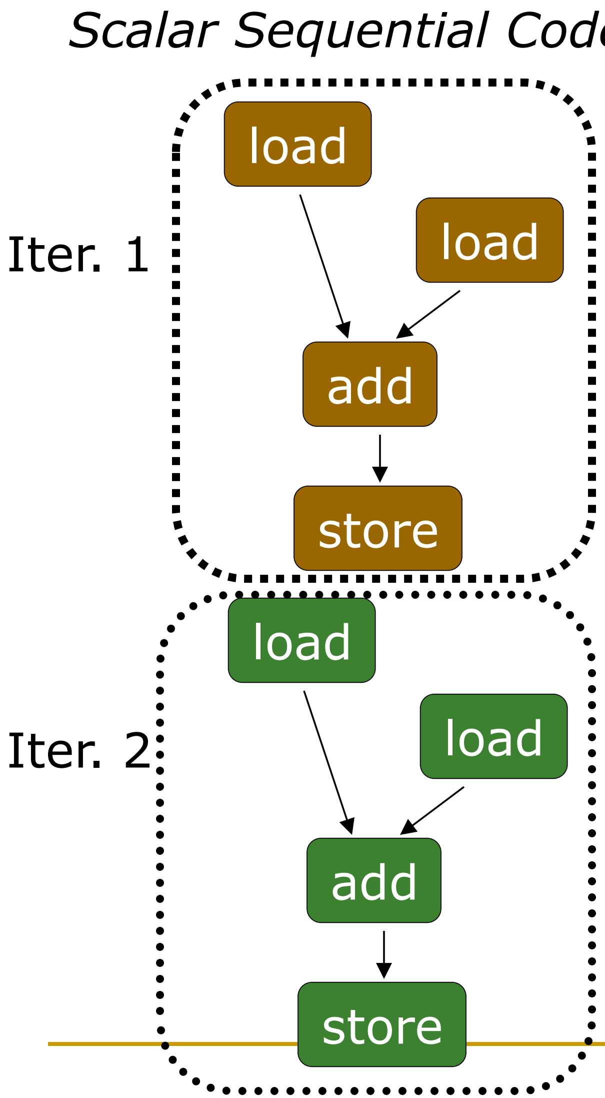
Can overlap execution of multiple vector instructions

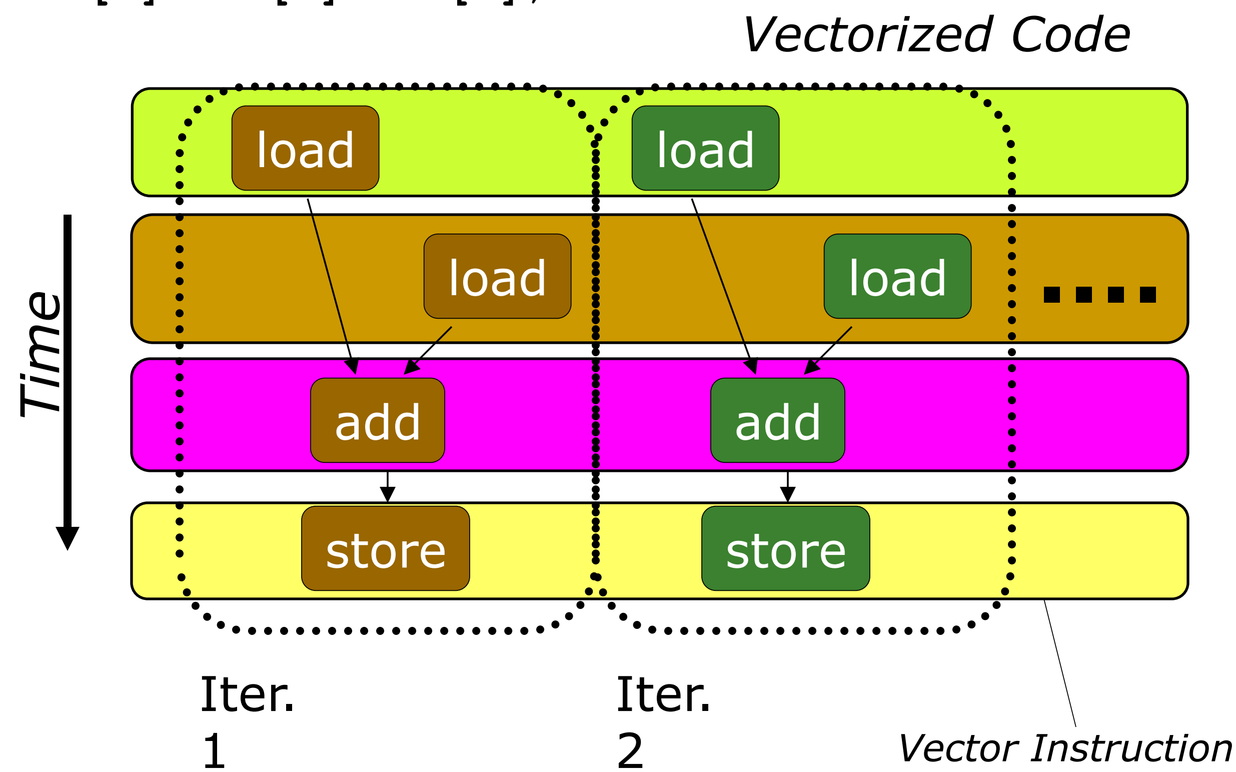
- Example machine has 32 elements per vector register and 8 lanes
- Completes 24 operations/cycle while issuing 1 vector instruction/cycle



Automatic Code Vectorization

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```





Vectorization is a compile-time reordering of operation sequencing
⇒ requires extensive loop dependence analysis

Vector/SIMD Processing Summary

- Vector/SIMD machines are good at exploiting regular data-level parallelism
  - Same operation performed on many data elements
  - Improve performance, simplify design (no intra-vector dependencies)

- Performance improvement limited by vectorizability of code
  - Scalar operations limit vector machine performance
  - Remember Amdahl's Law
  - CRAY-1 was the fastest SCALAR machine at its time!

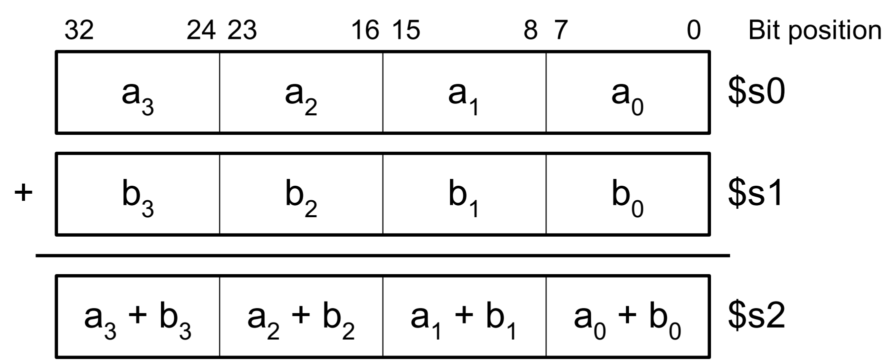
- Many existing ISAs include (vector-like) SIMD operations
  - Intel MMX/SSEn/AVX, PowerPC AltiVec, ARM Advanced SIMD

SIMD Operations in Modern ISAs

SIMD ISA Extensions

- Single Instruction Multiple Data (SIMD) extension instructions
  - Single instruction acts on multiple pieces of data at once
  - Common application: graphics
  - Perform short arithmetic operations (also called *packed arithmetic*)
- For example: add four 8-bit numbers
- Must modify ALU to eliminate carries between 8-bit values

```
padd8 $s2, $s0, $s1
```



Intel Pentium MMX Operations

- Idea: One instruction operates on multiple data elements simultaneously
  - *À la* array processing (yet much more limited)
  - Designed with multimedia (graphics) operations in mind

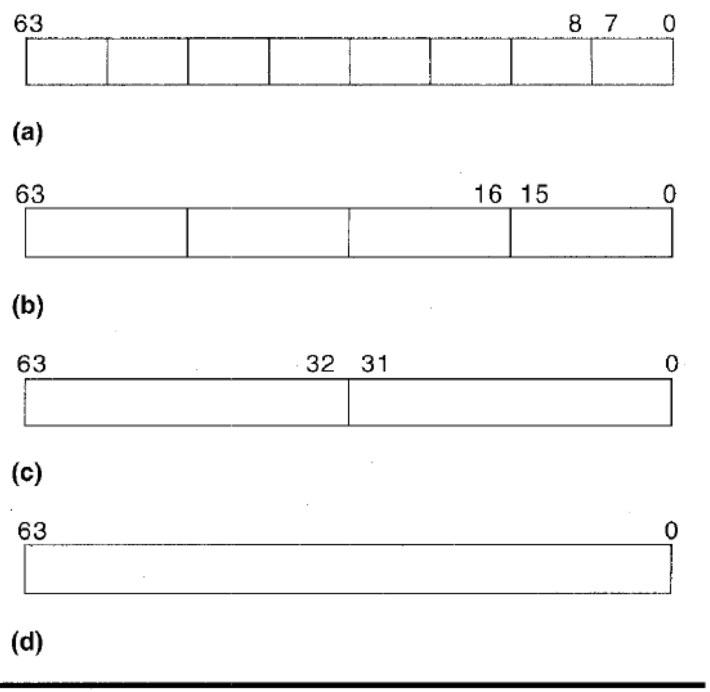


Figure 1. MMX technology data types: packed byte (a), packed word (b), packed doubleword (c), and quadword (d).

No VLEN register
Opcode determines data type:
8 8-bit bytes
4 16-bit words
2 32-bit doublewords
1 64-bit quadword

Stride is always equal to 1.

Peleg and Weiser, "MMX Technology Extension to the Intel Architecture," IEEE Micro, 1996.

MMX Example: Image Overlaying (I)

- Goal: Overlay the human in image 1 on top of the background in image 2


```
for (i=0; i<image_size; i++) {
if (x[i] == Blue)  new_image[i] =y[i];
        else new_image[i] = x[i];
}
```

Figure 8. Chroma keying: image overlay using a background color.

PCMPEQB MM1, MM3

MM1	Blue	Blue	Blue	Blue	Blue	Blue	Blue	Blue
MM3	X7!=blue	X6!=blue	X5=blue	X4=blue	X3!=blue	X2!=blue	X1=blue	X0=blue
MM1	0x0000	0x0000	0xFFFF	0xFFFF	0x0000	0x0000	0xFFFF	0xFFFF

Bitmask

Figure 9. Generating the selection bit mask.

Peleg and Weiser, "MMX Technology Extension to the Intel Architecture," IEEE Micro, 1996.

MMX Example: Image Overlaying (II)

PAND MM4, MM1 — Y = Blossom image

MM4	Y_7	Y_6	Y_5	Y_4	Y_3	Y_2	Y_1	Y_0
MM1	0x0000	0x0000	0xFFFF	0xFFFF	0x0000	0x0000	0xFFFF	0xFFFF
MM4	0x0000	0x0000	Y_5	Y_4	0x0000	0x0000	Y_1	Y_0

PANDN MM1, MM3 — X = Woman's image

MM1	0x0000	0x0000	0xFFFF	0xFFFF	0x0000	0x0000	0xFFFF	0xFFFF
MM3	X_7	X_6	X_5	X_4	X_3	X_2	X_1	X_0
MM1	X_7	X_6	0x0000	0x0000	X_3	X_2	0x0000	0x0000

POR MM4, MM1

MM4	X_7	X_6	Y_5	Y_4	X_3	X_2	Y_1	Y_0

Figure 10. Using the mask with logical MMX instructions to perform a conditional select.

```
Movq      mm3, mem1   /* Load eight pixels from
                         woman's image
Movq      mm4, mem2   /* Load eight pixels from the
                         blossom image
Pcmpeqb   mm1, mm3
Pand      mm4, mm1
Pandn     mm1, mm3
Por       mm4, mm1
```

Figure 11. MMX code sequence for performing a conditional select.

Peleg and Weiser, "MMX Technology Extension to the Intel Architecture," IEEE Micro, 1996.

GPUs (Graphics Processing Units)

GPUs are SIMD Engines Underneath

- The instruction pipeline operates like a SIMD pipeline (e.g., an array processor)
- However, the programming is done using threads, NOT SIMD instructions
- To understand this, let's go back to our parallelizable code example
- But, before that, let's distinguish between
  - Programming Model (Software)

    vs.
  - Execution Model (Hardware)

Programming Model vs. Hardware Execution Model

- Programming Model refers to how the programmer expresses the code
  - E.g., Sequential (von Neumann), Data Parallel (SIMD), Dataflow, Multi-threaded (MIMD, SPMD), …

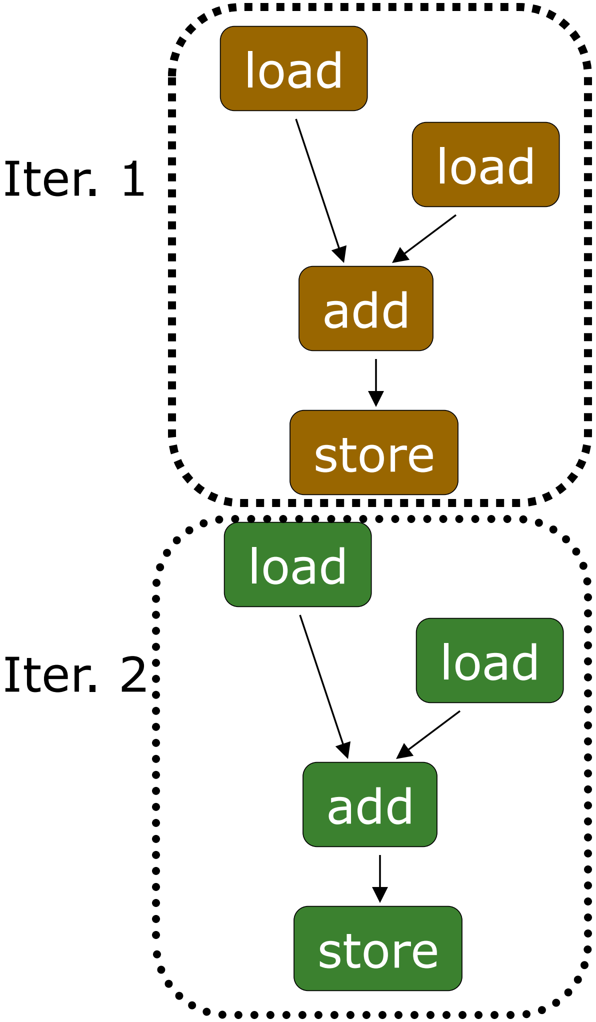
- Execution Model refers to how the hardware executes the code underneath
  - E.g., Out-of-order execution, Vector processor, Array processor, Dataflow processor, Multiprocessor, Multithreaded processor, …

- Execution Model can be very different from the Programming Model
  - E.g., von Neumann model implemented by an OoO processor
  - E.g., SPMD model implemented by a SIMD processor (a GPU)

How Can You Exploit Parallelism Here?

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```

Scalar Sequential Code



Let's examine three programming options to exploit instruction-level parallelism present in this sequential code:

1. Sequential (SISD)

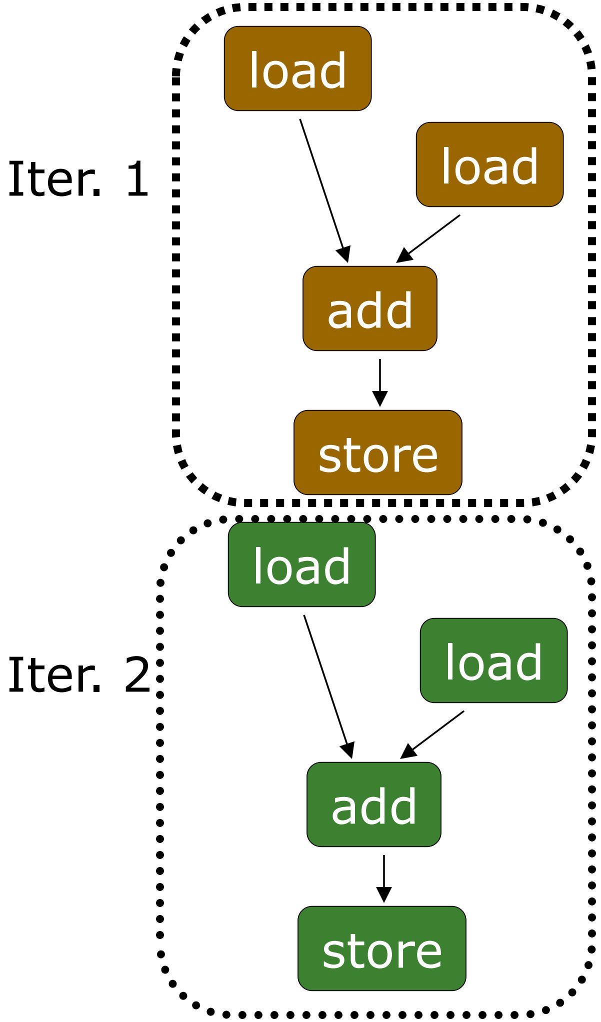
2. Data-Parallel (SIMD)

3. Multithreaded (MIMD/SPMD)

Prog. Model 1: Sequential (SISD)

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```

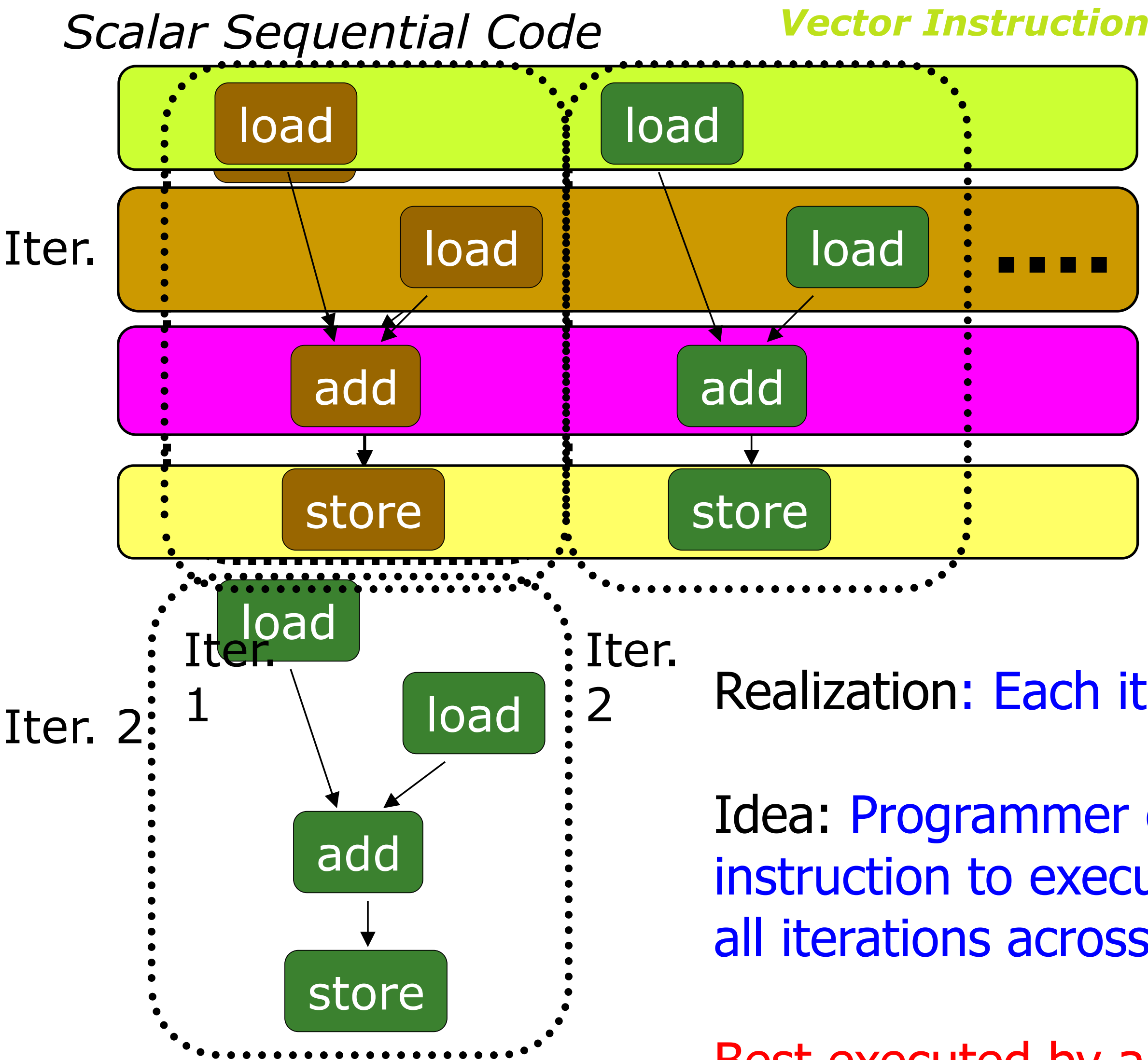
Scalar Sequential Code



- Can be executed on a:
- Pipelined processor
- Out-of-order execution processor
  - Independent instructions executed when ready
  - Different iterations are present in the instruction window and can execute in parallel in multiple functional units
  - In other words, the loop is dynamically unrolled by the hardware
- Superscalar or VLIW processor
  - Can fetch and execute multiple instructions per cycle

Prog. Model 2: Data Parallel (SIMD)

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```



Vectorized Code

VLD A → V1

VLD B → V2

VADD V1 + V2 → V3

VST V3 → C

Realization: Each iteration is independent

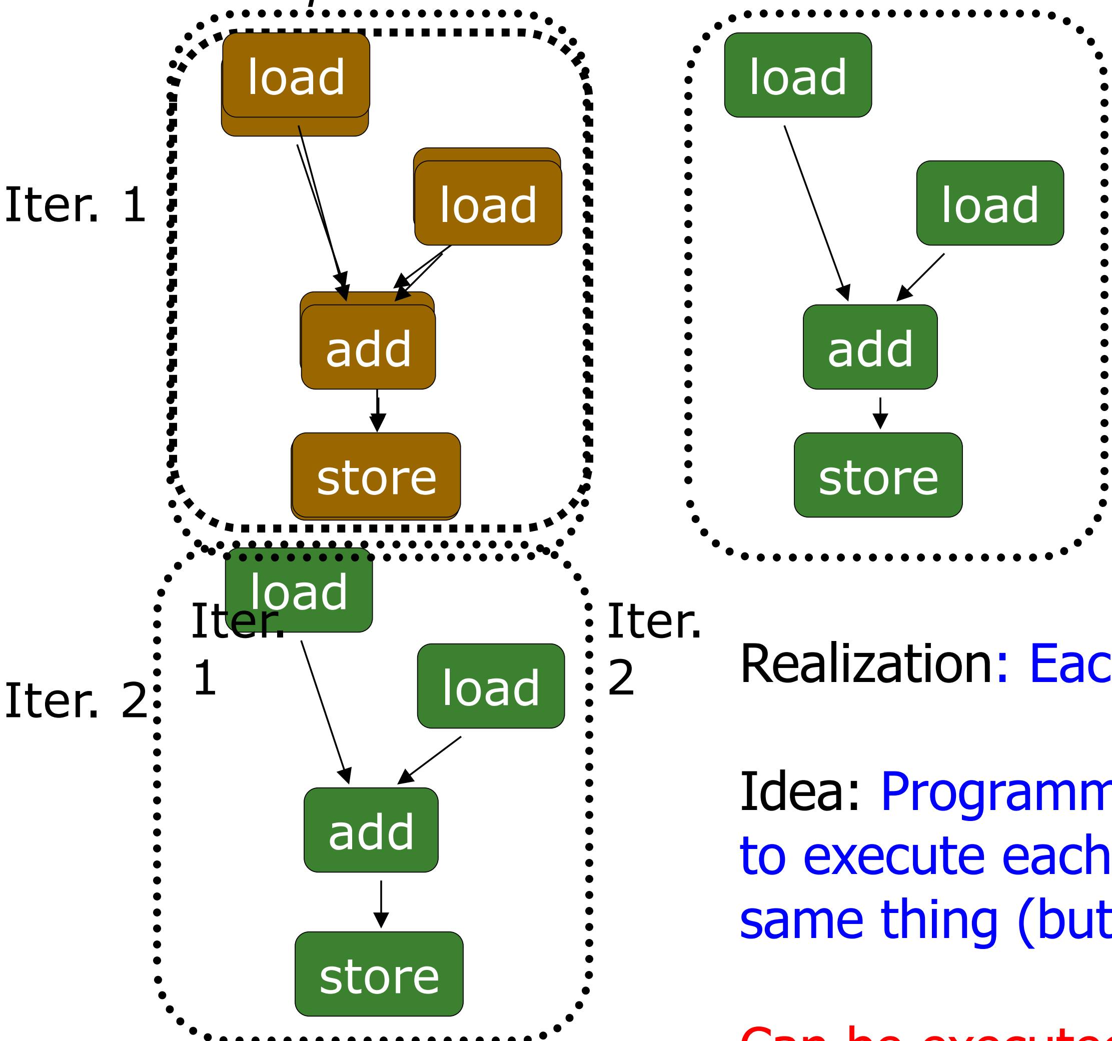
Idea: Programmer or compiler generates a SIMD instruction to execute the same instruction from all iterations across different data

Best executed by a SIMD processor (vector, array)

Prog. Model 3: Multithreaded

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```

Scalar Sequential Code



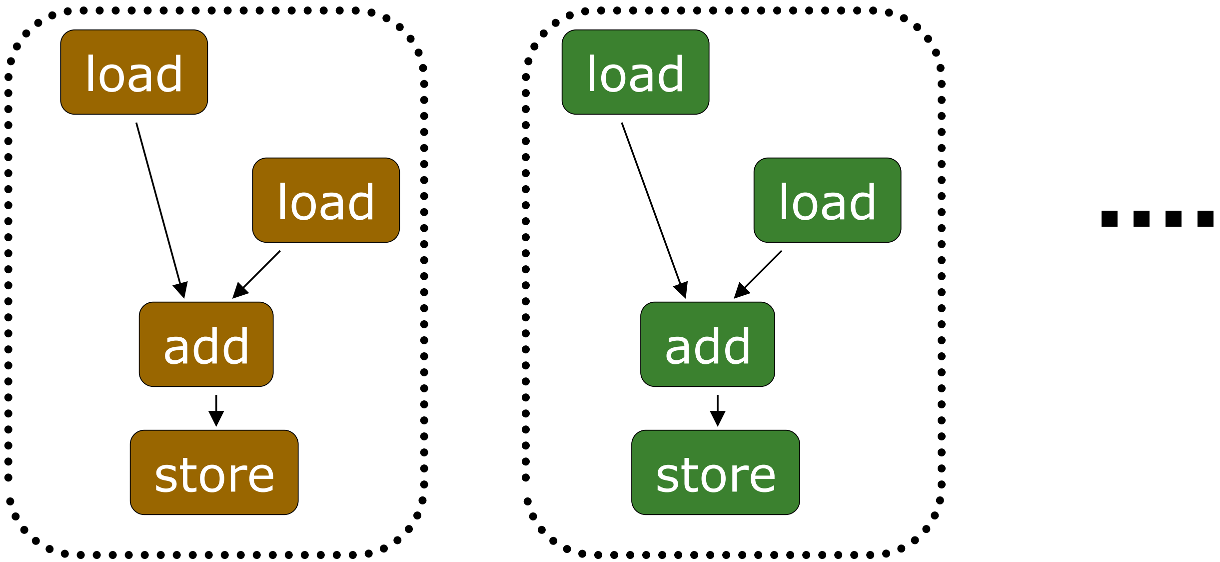
Realization: Each iteration is independent

Idea: Programmer or compiler generates a thread to execute each iteration. Each thread does the same thing (but on different data)

Can be executed on a MIMD machine

Prog. Model 3: Multithreaded

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```



Iter. 1

Iter. 2

Realization: Each iteration is independent

This particular model is also called:

SPMD: Single Program Multiple Data

Can be executed on a SIMT machine

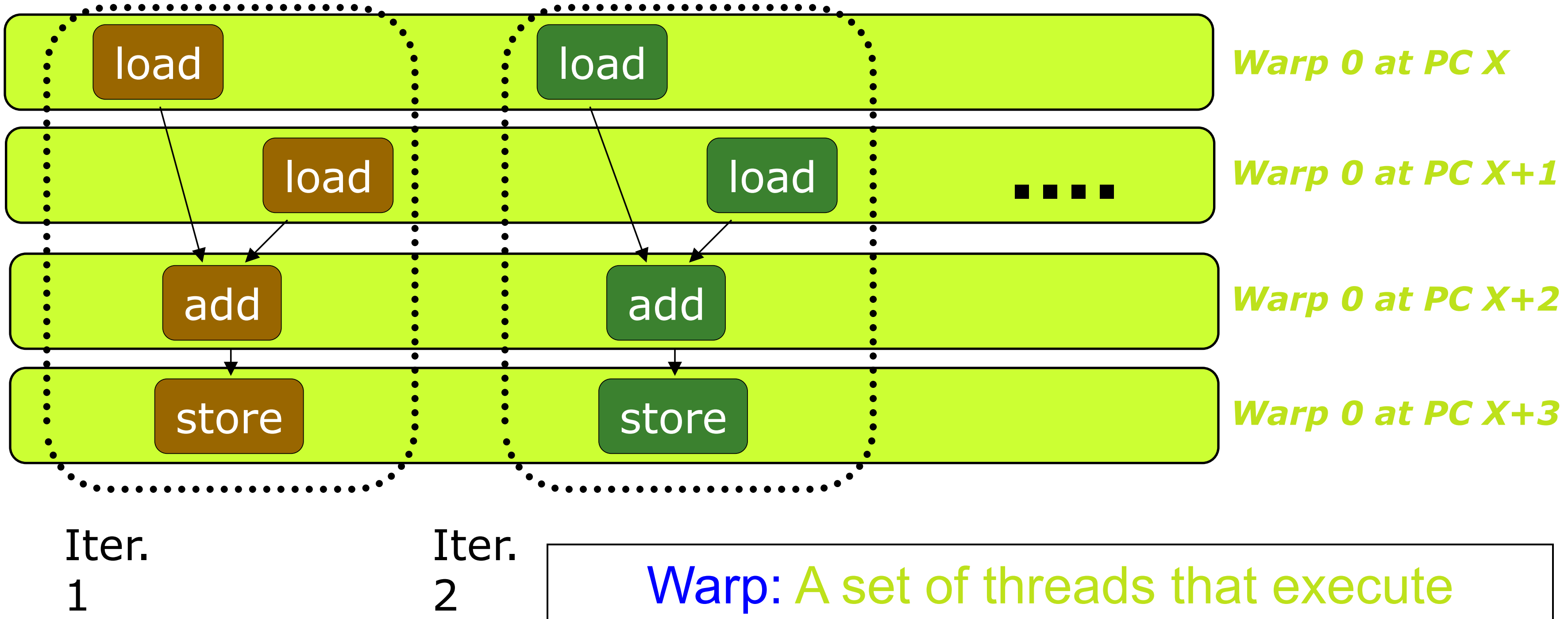
Single Instruction Multiple Thread

A GPU is a SIMD (SIMT) Machine

- Except it is **not** programmed using SIMD instructions
- It is programmed using threads (SPMD programming model)
  - Each thread executes the same code but operates a different piece of data
  - Each thread has its own context (i.e., can be treated/restarted/executed independently)
- A set of threads executing the same instruction are dynamically grouped into a **warp (wavefront)** by the hardware
  - A warp is essentially a SIMD operation formed by hardware!

SPMD on SIMT Machine

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```



Warp: A set of threads that execute the same instruction (i.e., at the same PC)

This particular model is also called:

SPMD: Single Program Multiple Data

A GPU executes it using the SIMT model:
Single Instruction Multiple Thread

Graphics Processing Units

SIMD not Exposed to Programmer (SIMT)

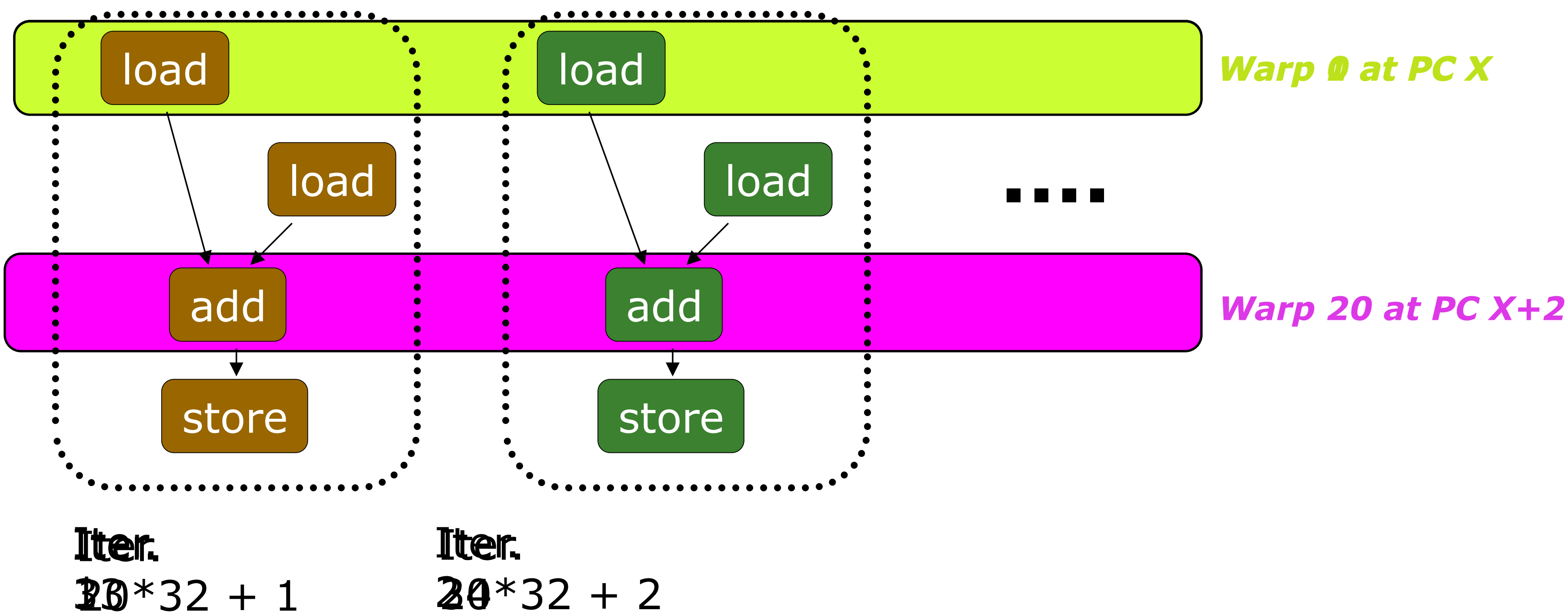
SIMD vs. SIMT Execution Model

- SIMD: A single sequential instruction stream of SIMD instructions → each instruction specifies multiple data inputs
  - [VLD, VLD, VADD, VST], VLEN
- SIMT: Multiple instruction streams of scalar instructions → threads grouped dynamically into warps
  - [LD, LD, ADD, ST], NumThreads
- Two Major SIMT Advantages:
  - Can treat each thread separately → i.e., can execute each thread independently (on any type of scalar pipeline) → MIMD processing
  - Can group threads into warps flexibly → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing

Multithreading of Warps

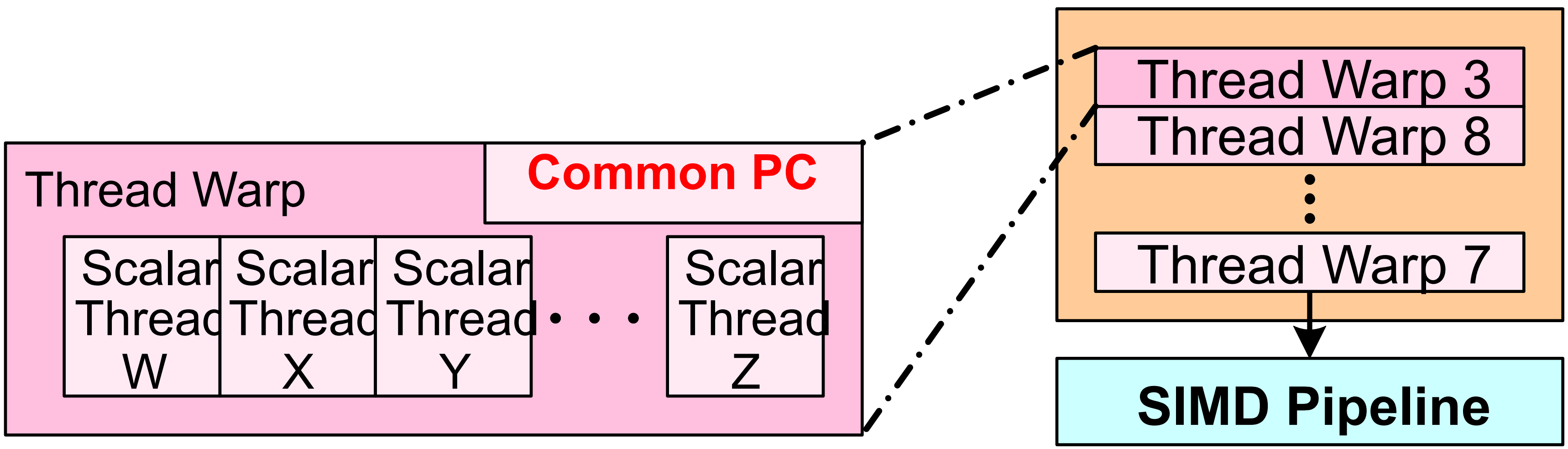
```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```

- Assume a warp consists of 32 threads
- If you have 32K iterations, and 1 iteration/thread → 1K warps
- Warps can be interleaved on the same pipeline → Fine grained multithreading of warps

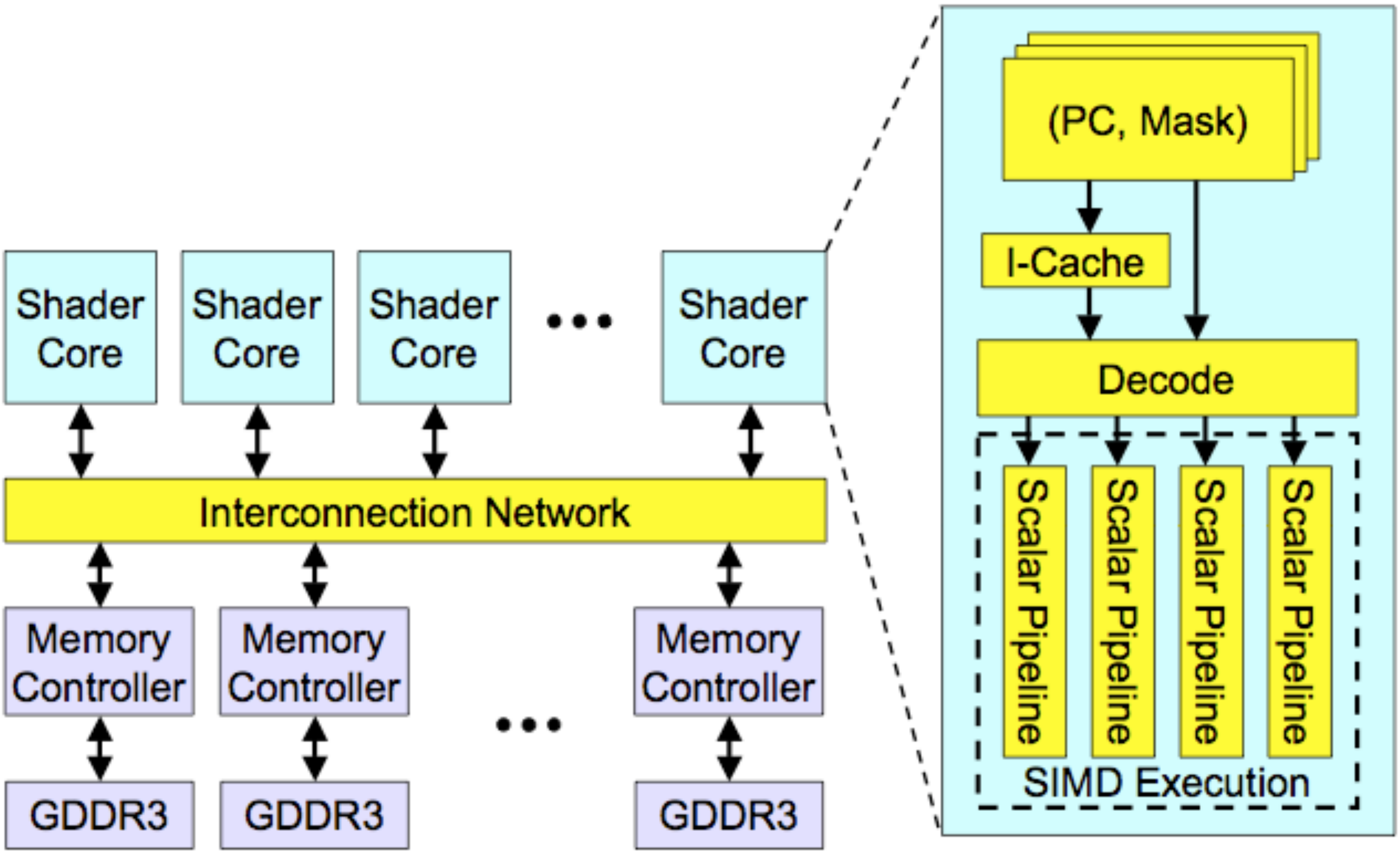


Warps and Warp-Level FGMT

- Warp: A set of threads that execute the same instruction (on different data elements) → SIMT (Nvidia-speak)
- All threads run the same code
- Warp: The threads that run lengthwise in a woven fabric …

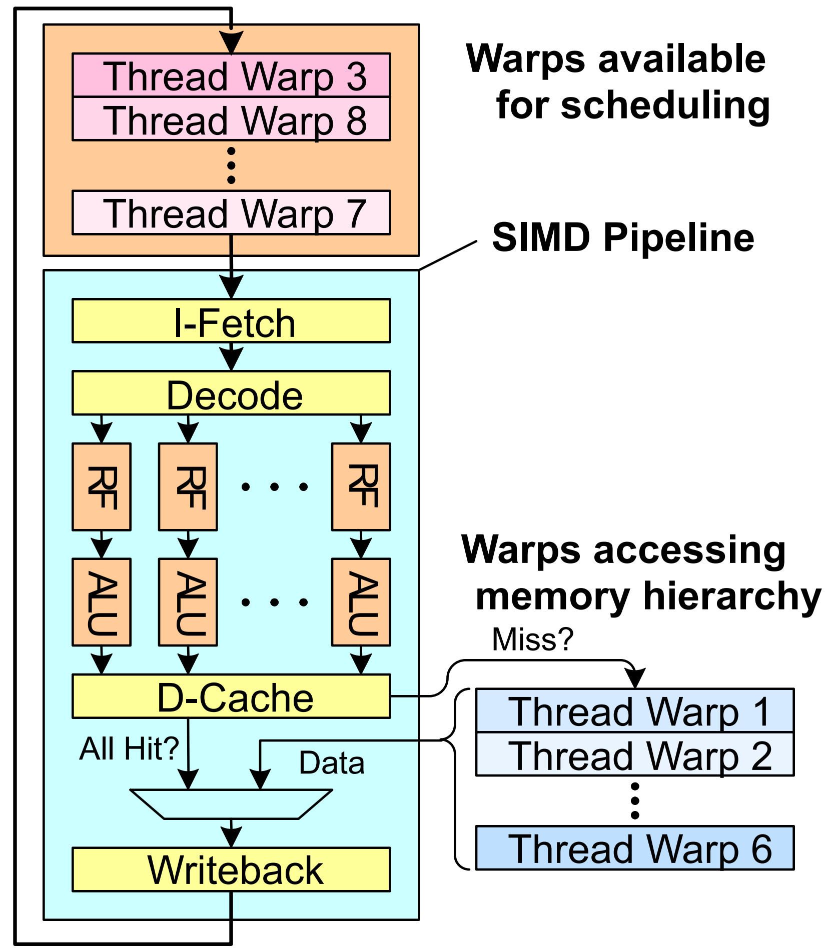


High-Level View of a GPU

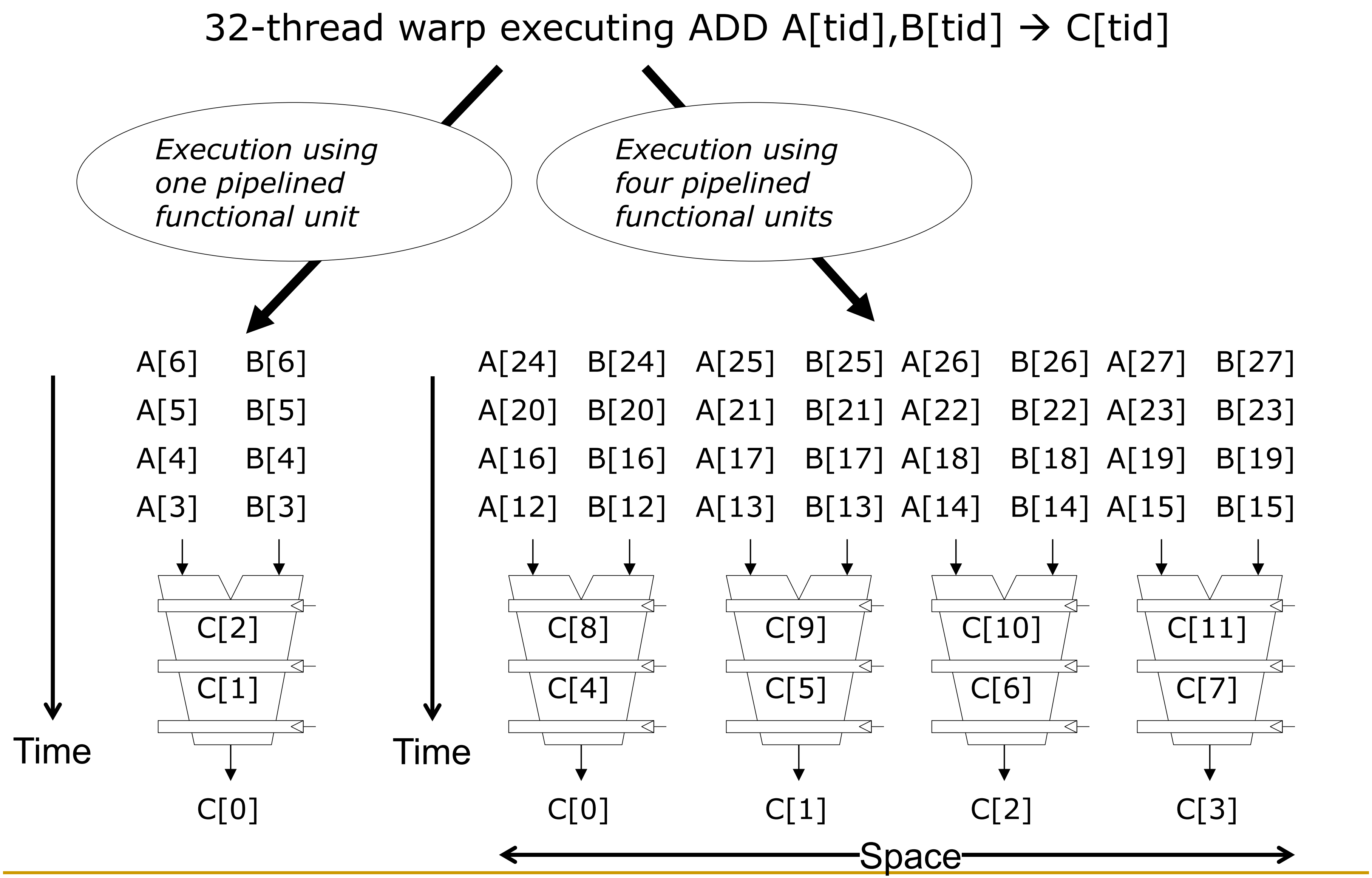


Latency Hiding via Warp-Level FGMT

- Warp: A set of threads that execute the same instruction (on different data elements)
- Fine-grained multithreading
  - One instruction per thread in pipeline at a time (No interlocking)
  - Interleave warp execution to hide latencies
- Register values of all threads stay in register file
- FGMT enables long latency tolerance
  - Millions of pixels

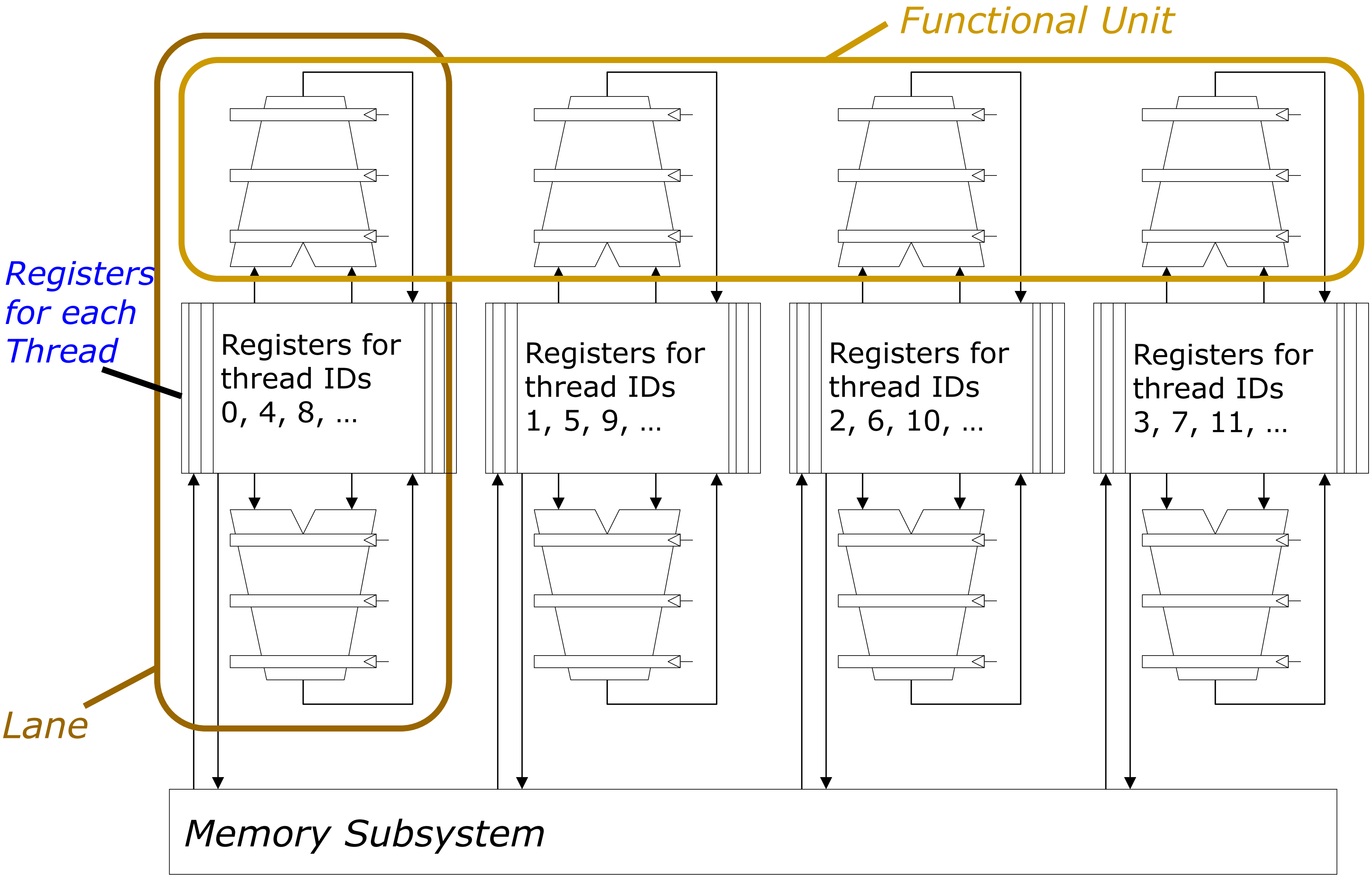


Warp Execution (Recall the Slide)



Slide credit: Krste Asanovic

SIMD Execution Unit Structure

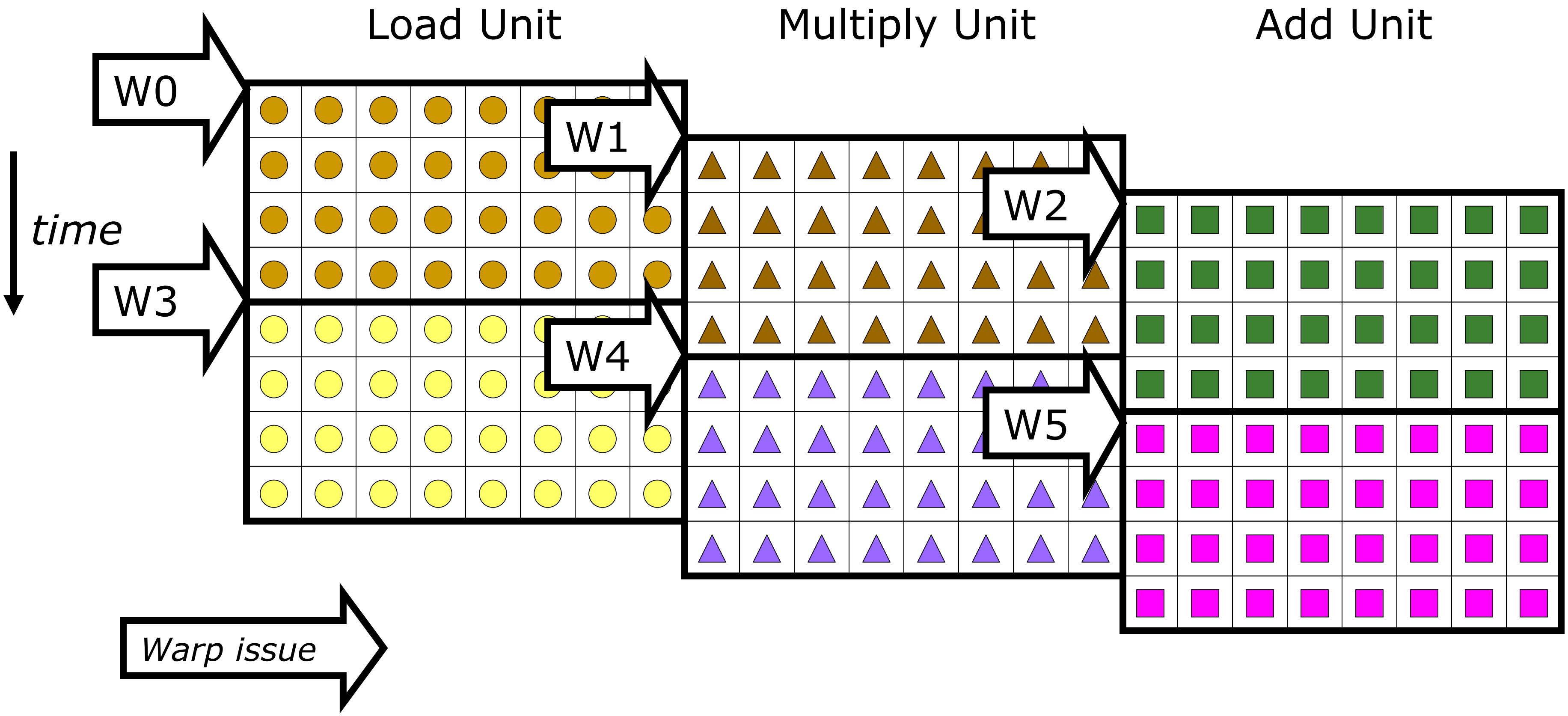


Slide credit: Krste Asanovic

Warp Instruction Level Parallelism

Can overlap execution of multiple instructions

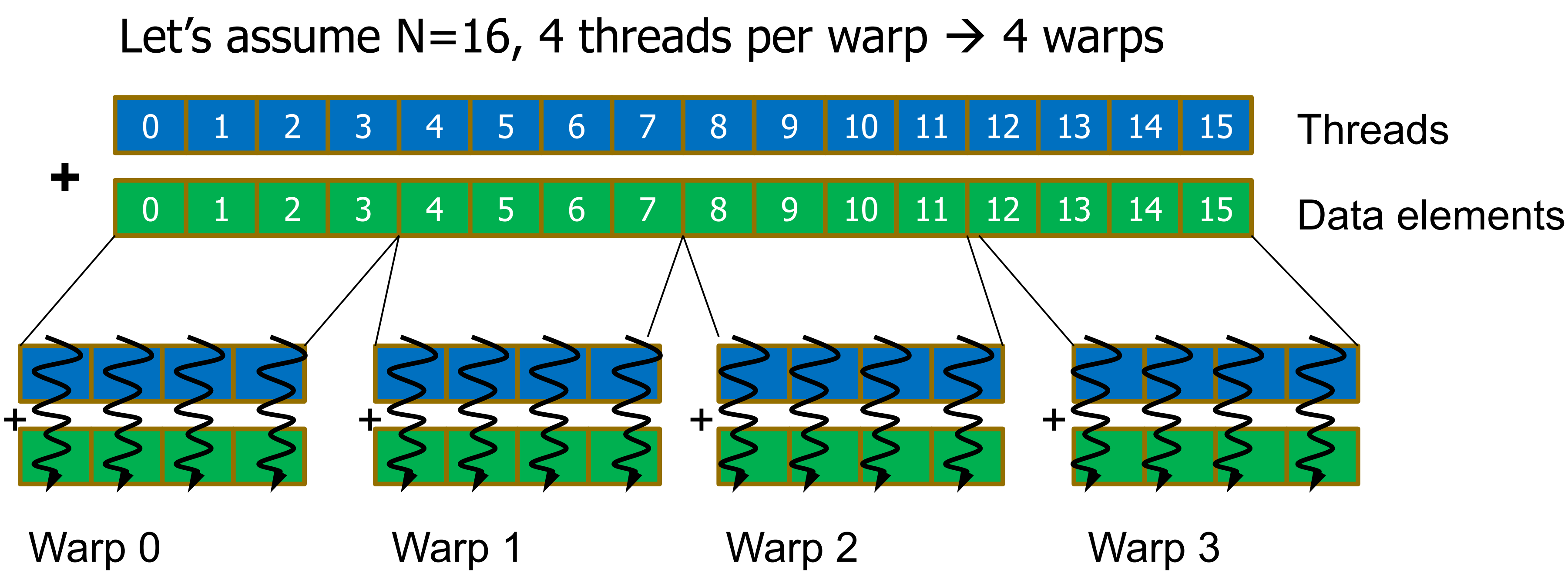
- Example machine has 32 threads per warp and 8 lanes
- Completes 24 operations/cycle while issuing 1 warp/cycle



Slide credit: Krste Asanovic

SIMT Memory Access

- Same instruction in different threads uses thread id to index and access different data elements



Sample GPU SIMT Code (Simplified)

CPU code

```
for (ii = 0; ii < 100000; ++ii) {
C[ii] = A[ii] + B[ii];
}
```

CUDA code

```
// there are 100000 threads
__global__ void KernelFunction(…) {
  int tid = blockDim.x * blockIdx.x + threadIdx.x;
  int varA = aa[tid];
  int varB = bb[tid];
  C[tid] = varA + varB;
}
```

Slide credit: Hyesoon Kim

Sample GPU Program (Less Simplified)

CPU Program

```
void add matrix
 ( float *a, float* b, float *c, int N) {
   int index;
   for (int i = 0; i < N; ++i)
      for (int j = 0; j < N; ++j) {
         index = i + j*N;
         c[index] = a[index] + b[index];
        }
 }

int main () {

  add matrix (a, b, c, N);
}
```

GPU Program

```
__global__  add_matrix
  ( float *a, float *b, float *c, int N) {
int i = blockIdx.x *  blockDim.x + threadIdx.x;
Int j = blockIdx.y * blockDim.y  + threadIdx.y;
int index = i + j*N;
 if (i < N && j < N)
   c[index] = a[index]+b[index];
}

Int main() {
  dim3 dimBlock( blocksize, blocksize) ;
  dim3 dimGrid (N/dimBlock.x, N/dimBlock.y);
  add_matrix<<<dimGrid, dimBlock>>>( a, b, c, N);
}
```

Warp-based SIMD vs. Traditional SIMD

- Traditional SIMD contains a single thread
  - Sequential instruction execution; lock-step operations in a SIMD instruction
  - Programming model is SIMD (no extra threads) → SW needs to know vector length
  - ISA contains vector/SIMD instructions

- Warp-based SIMD consists of multiple scalar threads executing in a SIMD manner (i.e., same instruction executed by all threads)
  - Does not have to be lock step
  - Each thread can be treated individually (i.e., placed in a different warp) → programming model not SIMD
    - SW does not need to know vector length
    - Enables multithreading and flexible dynamic grouping of threads
  - ISA is scalar → SIMD operations can be formed dynamically
  - Essentially, it is SPMD programming model implemented on SIMD hardware

SPMD

- Single procedure/program, multiple data
  - This is a programming model rather than computer organization

- Each processing element executes the same procedure, except on different data elements
  - Procedures can synchronize at certain points in program, e.g. barriers

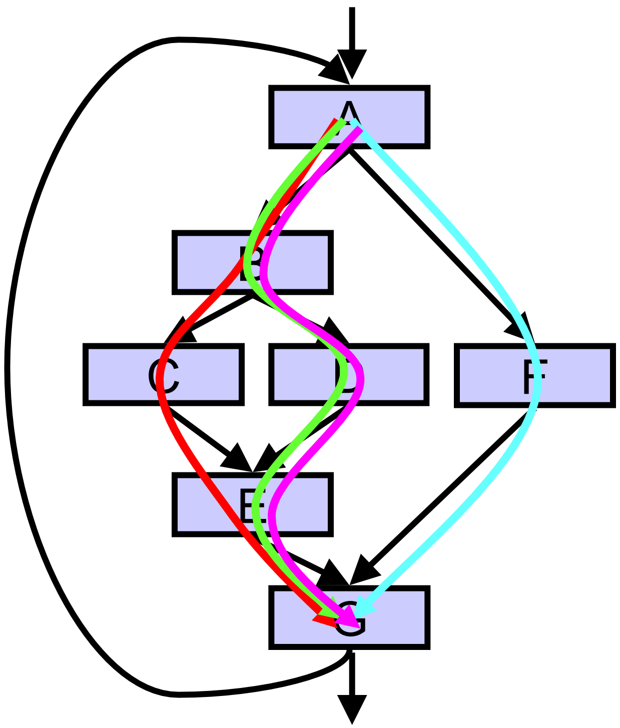
- Essentially, multiple instruction streams execute the same program
  - Each program/procedure 1) works on different data, 2) can execute a different control-flow path, at run-time
  - Many scientific applications are programmed this way and run on MIMD hardware (multiprocessors)
  - Modern GPUs programmed in a similar way on a SIMD hardware

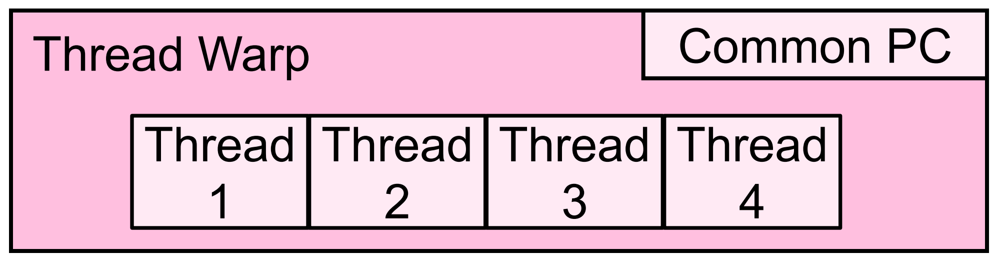
SIMD vs. SIMT Execution Model

- SIMD: A single sequential instruction stream of SIMD instructions → each instruction specifies multiple data inputs
  - [VLD, VLD, VADD, VST], VLEN
- SIMT: Multiple instruction streams of scalar instructions → threads grouped dynamically into warps
  - [LD, LD, ADD, ST], NumThreads
- Two Major SIMT Advantages:
  - Can treat each thread separately → i.e., can execute each thread independently on any type of scalar pipeline → MIMD processing
  - Can group threads into warps flexibly → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing

Threads Can Take Different Paths in Warp-based SIMD

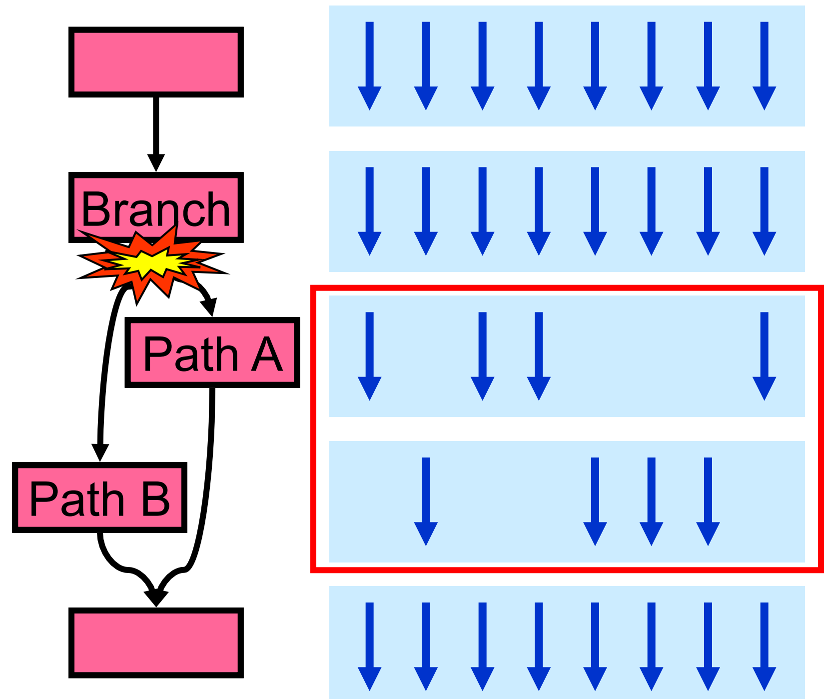
- Each thread can have conditional control flow instructions
- Threads can execute different control flow paths





Control Flow Problem in GPUs/SIMT

- A GPU uses a SIMD pipeline to save area on control logic
  - Groups scalar threads into warps
- Branch divergence occurs when threads inside warps branch to different execution paths



This is the same as conditional/predicated/masked execution. Recall the Vector Mask and Masked Vector Operations?

Slide credit: Tor Aamodt

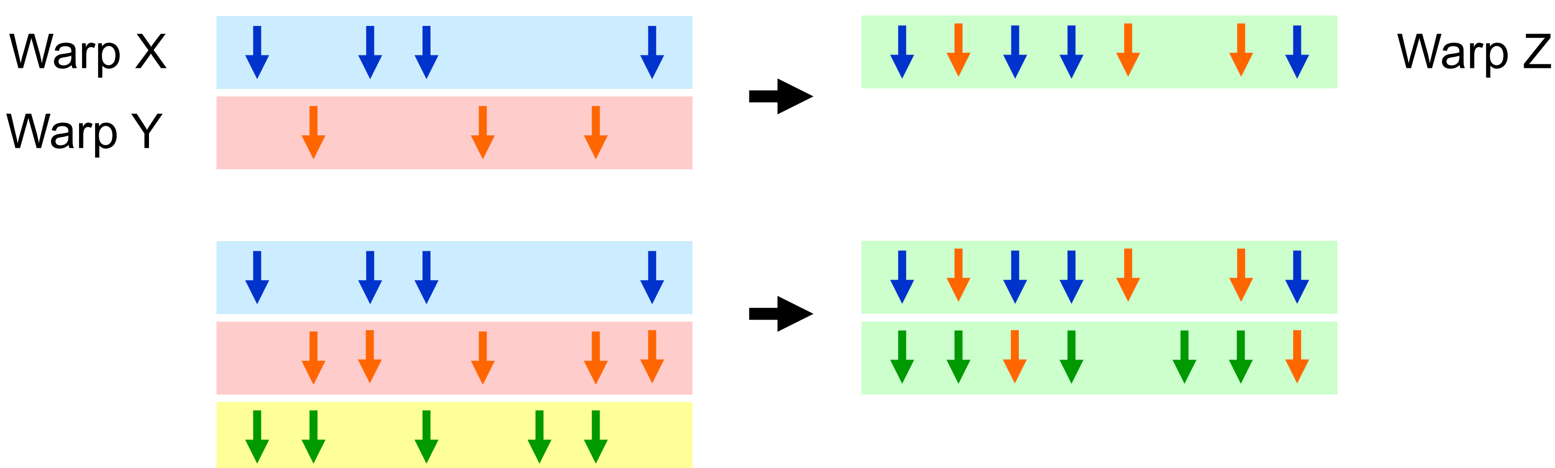
Remember: Each Thread Is Independent

- Two Major SIMT Advantages:
  - Can treat each thread separately → i.e., can execute each thread independently on any type of scalar pipeline → MIMD processing
  - Can group threads into warps flexibly → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing

- If we have many threads
- We can find individual threads that are at the same PC
- And, group them together into a single warp dynamically
- This reduces "divergence" → improves SIMD utilization
  - SIMD utilization: fraction of SIMD lanes executing a useful operation (i.e., executing an active thread)

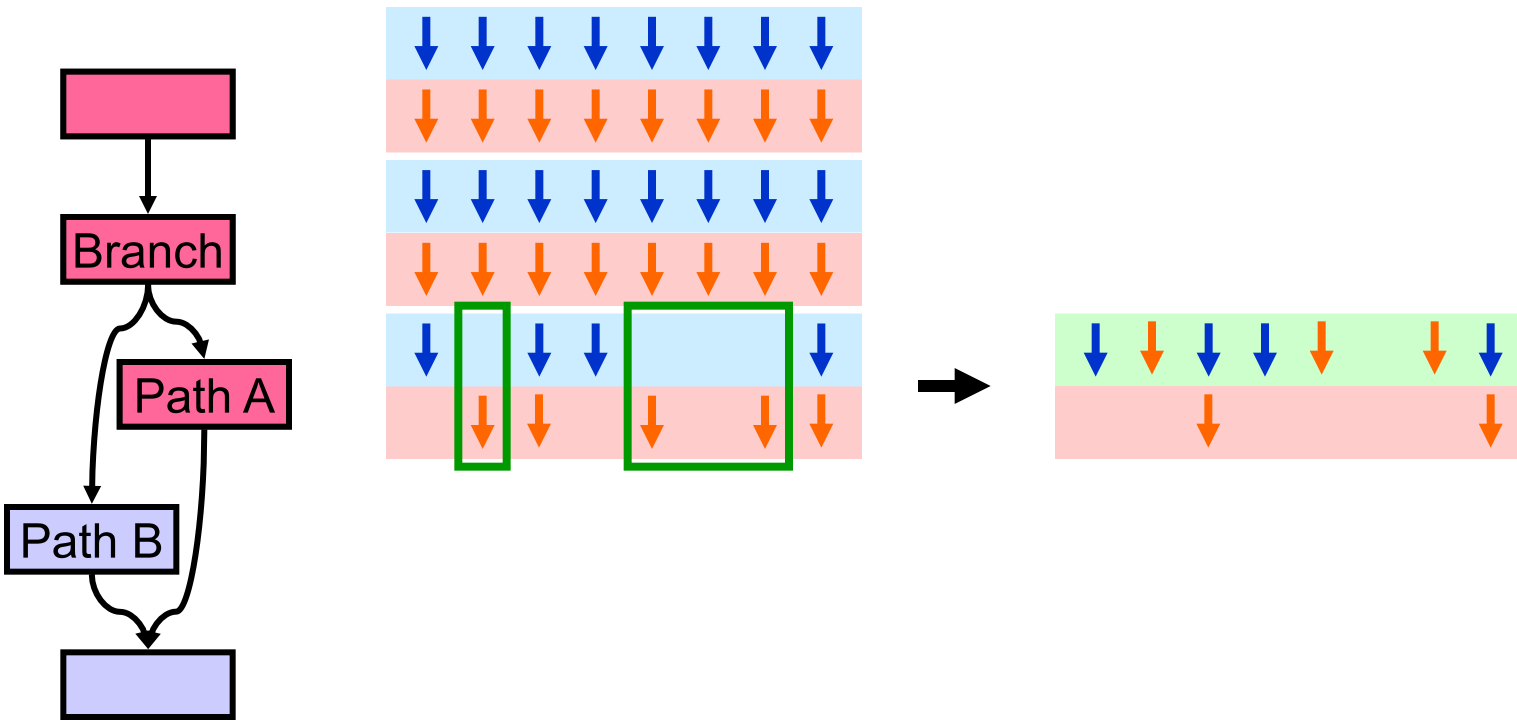
Dynamic Warp Formation/Merging

- Idea: Dynamically merge threads executing the same instruction (after branch divergence)
- Form new warps from warps that are waiting
  - Enough threads branching to each path enables the creation of full new warps



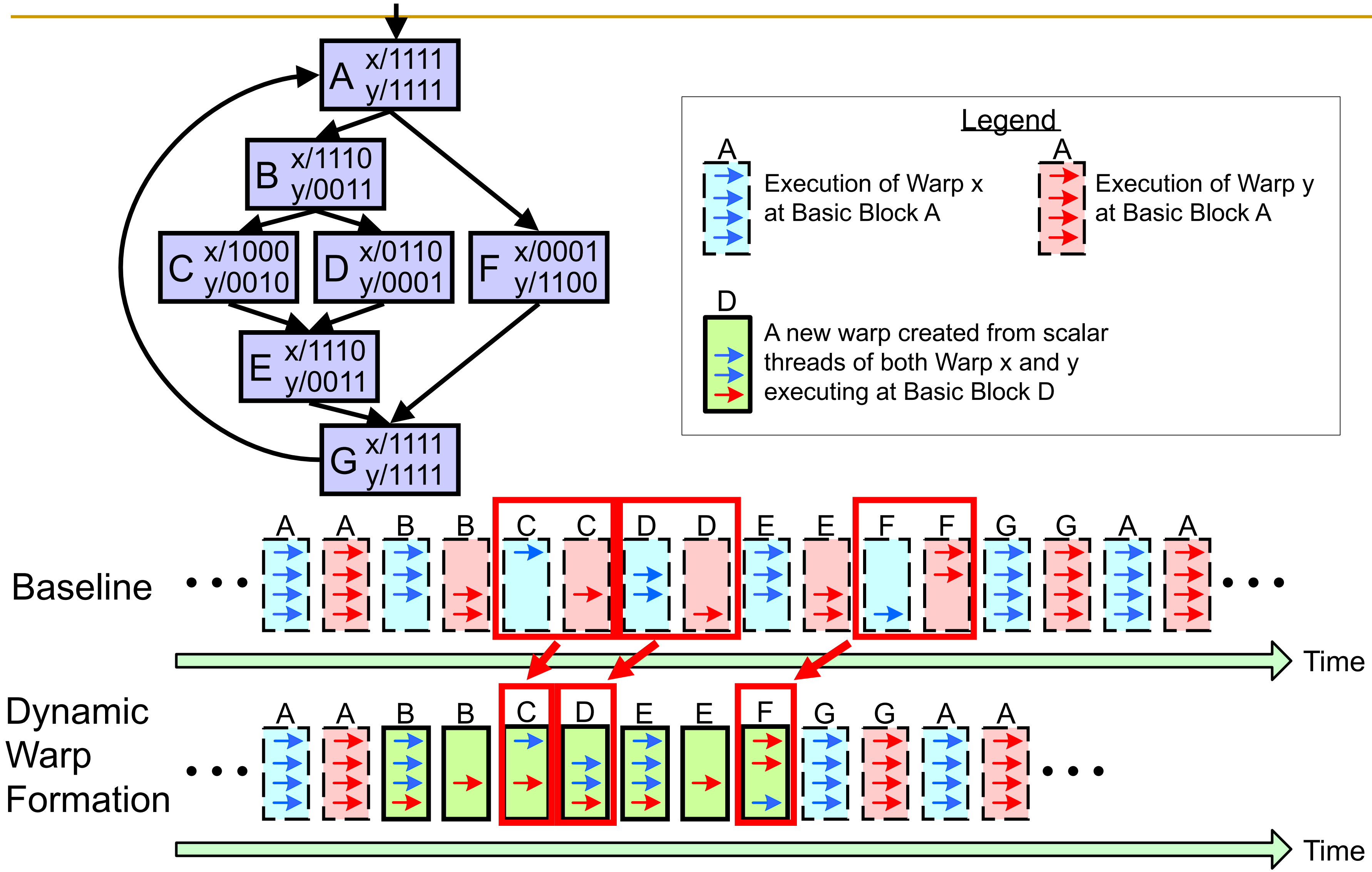
Dynamic Warp Formation/Merging

- Idea: Dynamically merge threads executing the same instruction (after branch divergence)



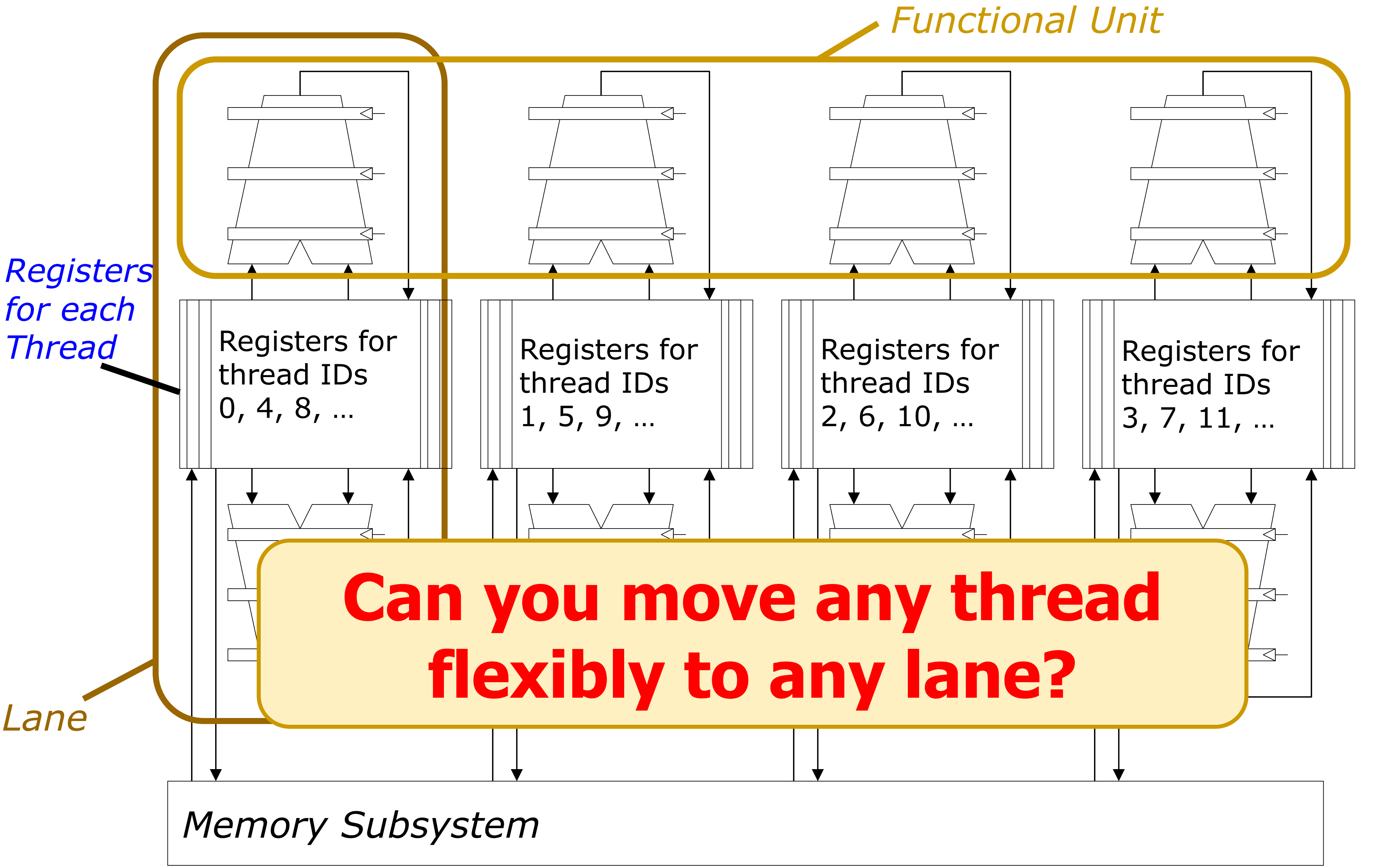
- Fung et al., "Dynamic Warp Formation and Scheduling for Efficient GPU Control Flow," MICRO 2007.

Dynamic Warp Formation Example



Slide credit: Tor Aamodt

Hardware Constraints Limit Flexibility of Warp Grouping



Slide credit: Krste Asanovic

Design of Digital Circuits
Lecture 21: SIMD Processors II and Graphics Processing Units

Dr. Juan Gómez Luna
Prof. Onur Mutlu
ETH Zurich

Spring 2018

17 May 2018

We did not cover the following slides in lecture. These are for your preparation for the next lecture.

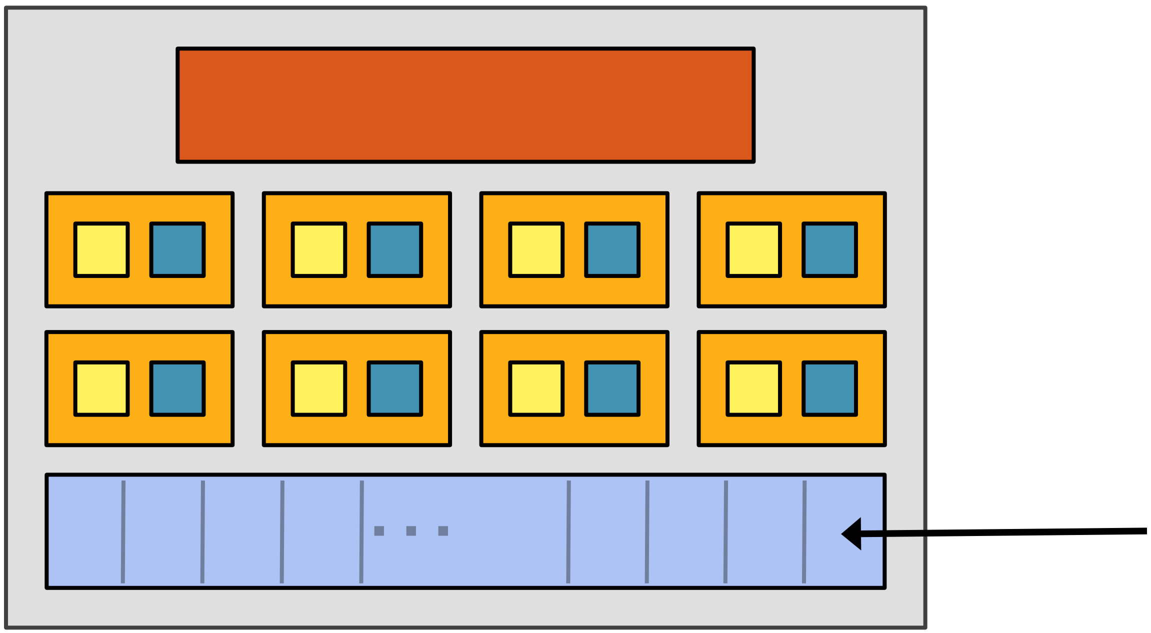
An Example GPU

NVIDIA GeForce GTX 285

- NVIDIA-speak:
  - 240 stream processors
  - “SIMT execution”
- Generic speak:
  - 30 cores
  - 8 SIMD functional units per core

Slide credit: Kayvon Fatahalian

NVIDIA GeForce GTX 285 "core"



64 KB of storage for thread contexts (registers)

= SIMD functional unit, control shared across 8 units

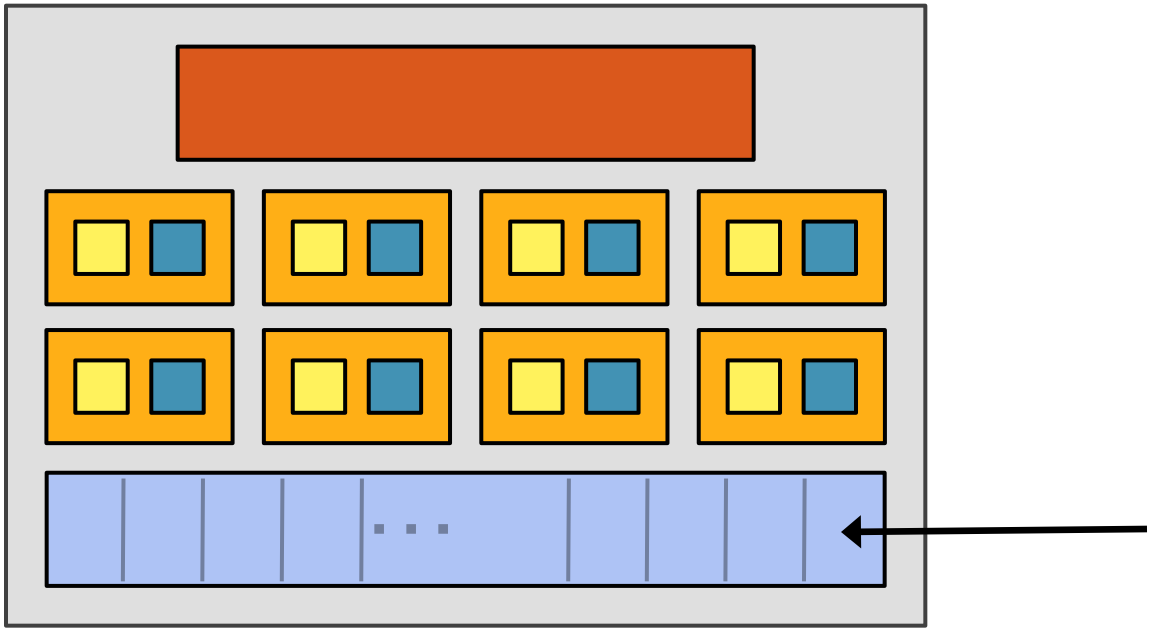
= multiply-add

= multiply

= instruction stream decode

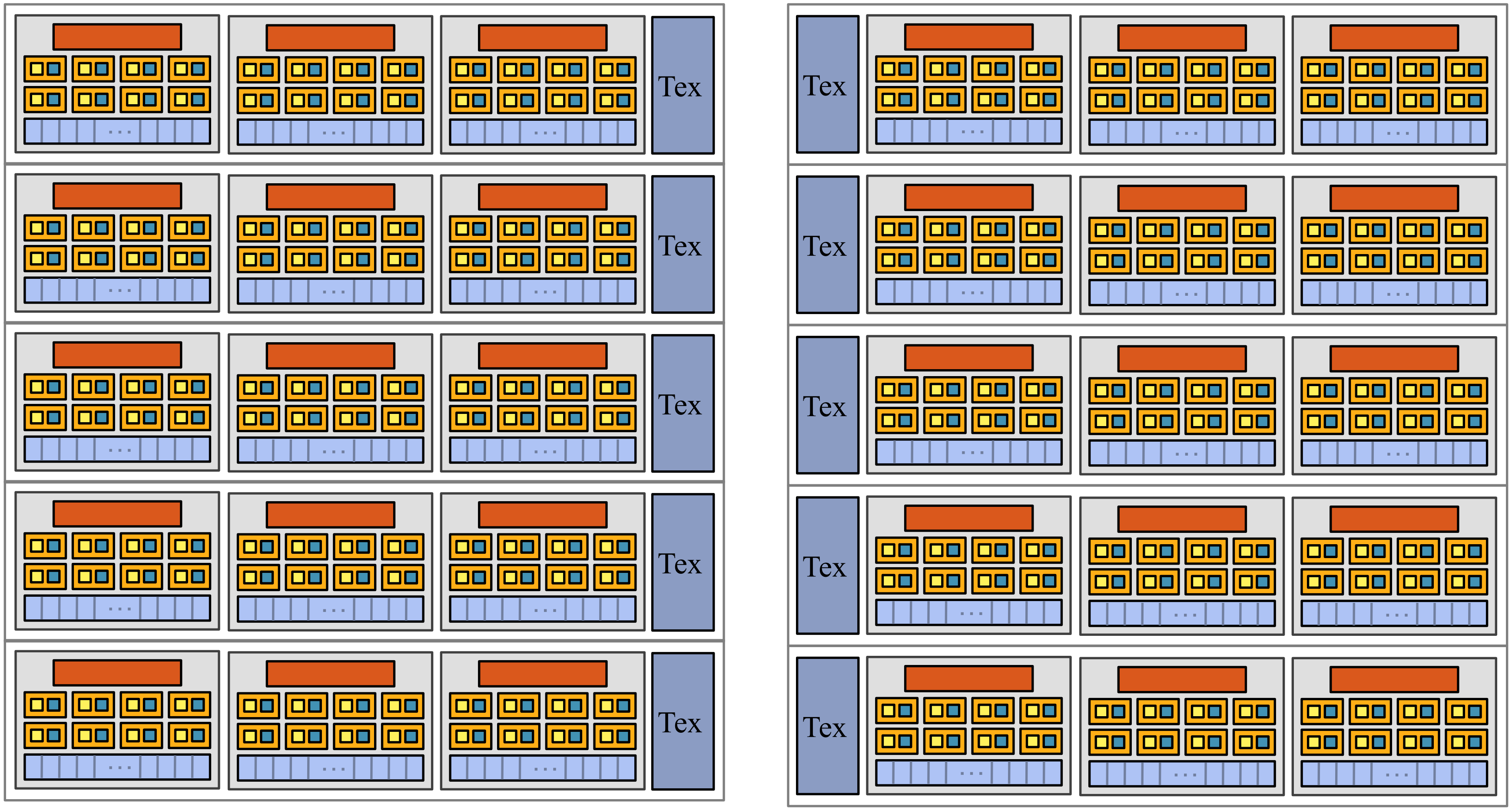
= execution context storage

NVIDIA GeForce GTX 285 "core"



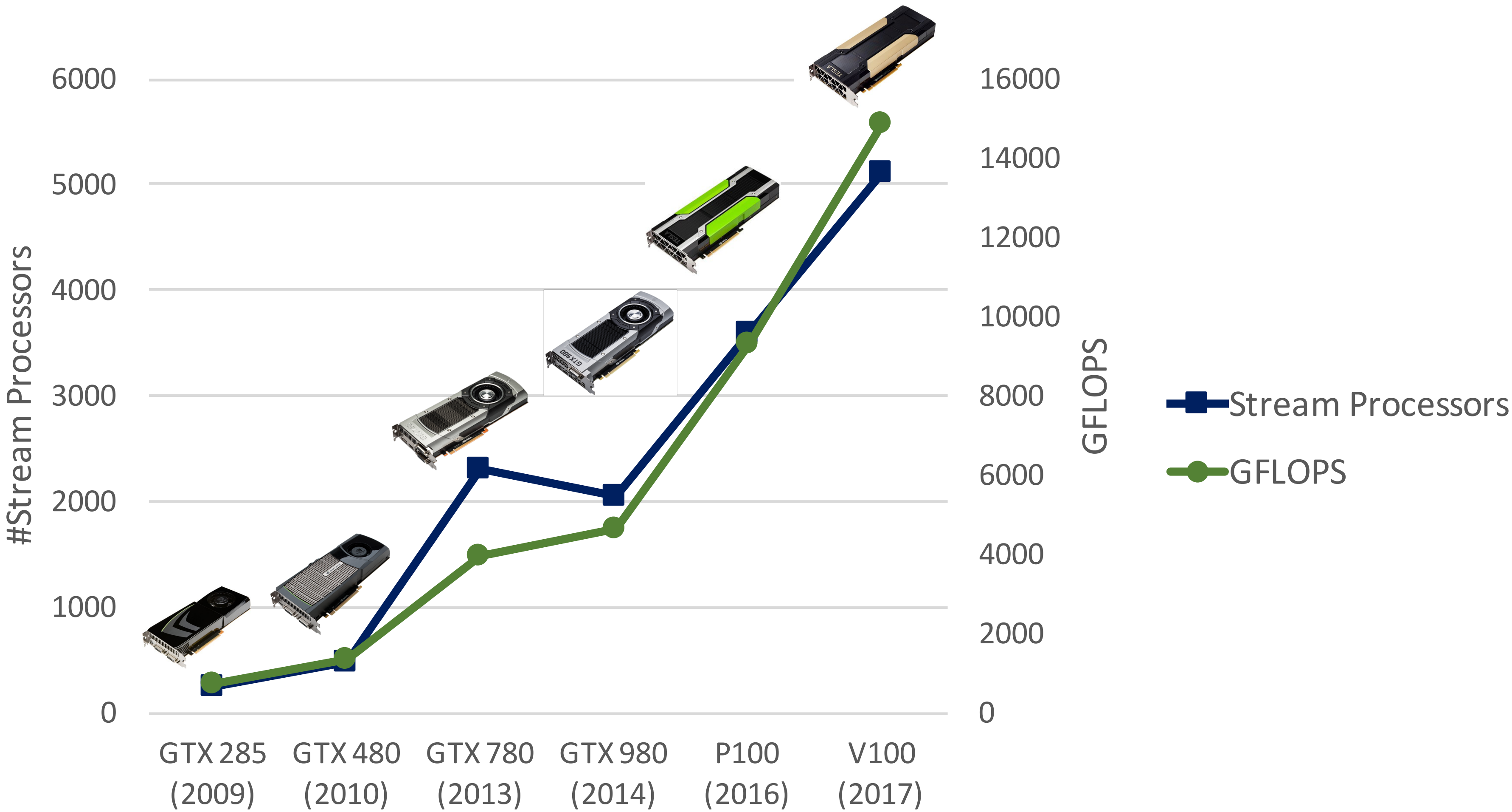
- Groups of 32 threads share instruction stream (each group is a Warp)
- Up to 32 warps are simultaneously interleaved
- Up to 1024 thread contexts can be stored

NVIDIA GeForce GTX 285



30 cores on the GTX 285: 30,720 threads

Evolution of NVIDIA GPUs



NVIDIA V100

- NVIDIA-speak:
  - 5120 stream processors
  - “SIMT execution”

- Generic speak:
  - 80 cores
  - 64 SIMD functional units per core

  - Tensor cores for Machine Learning

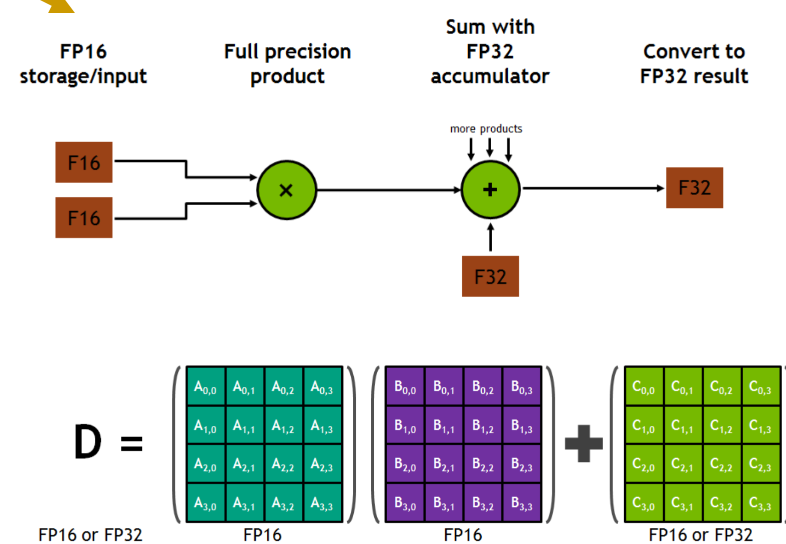
NVIDIA V100 Block Diagram

https://devblogs.nvidia.com/inside-volta/

80 cores on the V100

NVIDIA V100 Core

15.7 TFLOPS Single Precision
7.8 TFLOPS Double Precision
125 TFLOPS for Deep Learning (Tensor cores)



https://devblogs.nvidia.com/inside-volta/