

## Assignment 2: Coding Question

● Graded

### Student

Tyler NGUYEN

### Total Points

100 / 100 pts

### Autograder Score

30.0 / 30.0

### Passed Tests

Test empty() (1/1)

Test randomly generated elements (8/8)

Test member() with delete() (2/2)

Whitebox test (16/16)

Test member() (1/1)

Test tiny tree { 2, 1, 3 } (2/2)

### Question 2

#### Manual Grading

70 / 70 pts

✓ - 0 pts Correct

- 70 pts Late submission

- 70 pts Incorrect or can not be complied

- 33 pts Only pass 14/30 cases

- 42 pts Only pass 12/30 cases

- 56 pts Only pass 6/30 cases

- 60 pts Only pass 4/30 cases

- 63 pts Only pass 3/30 cases

- 65 pts Only pass 2/30 cases

- 68 pts Only pass 1/30 cases

+ 1 pt Provide a constructor that does not take any arguments and initialize the tree to an empty one.

+ 1 pt Implement empty

+ 1 pt Implement insert

+ 1 pt Implement delete

+ 1 pt Implement member

+ 1 pt Implement toString()

+ 1 pt Implement preorder tree walk

## Autograder Results

Test empty() (1/1)

Test randomly generated elements (8/8)

Test member() with delete() (2/2)

Whitebox test (16/16)

Test member() (1/1)

Test tiny tree { 2, 1, 3 } (2/2)

## Submitted Files

```
1  /*
2  author: Tyler Nguyen UCID: 30158563
3  date: October 28, 2023
4  description: RedBlackTree class that implements Dictionary and its methods as well as some helper
5  functions
6  */
7
8  package ca.ucalgary.cpsc331.a2;
9
10 public class RedBlackTree implements Dictionary {
11
12     private static final boolean RED = true; //constant to represent the colour red
13     private static final boolean BLACK = false; //constant to represent the colour black
14
15     private class Node {
16         Node parent;
17         Node left;
18         Node right;
19         boolean red;
20         int key;
21
22         /**
23          * constructor to create a new node
24          * @param key, which is the value to be stored in the node
25          */
26         Node(int key) {
27             this.key = key;
28             this.red = RED;
29             this.parent = null;
30             this.left = NIL;
31             this.right = NIL;
32         }
33     }
34     private Node root;
35     private Node NIL; //will act as sentinel for the tree
36
37     /**
38      * constructor for the Red Black Tree
39      * initializes the tree with a NIL node
40      */
41     public RedBlackTree() {
42         NIL = new Node(-1);
43         NIL.red = BLACK;
44         NIL.left = null;
45         NIL.right = null;
46         root = NIL;
47     }
48 }
```

```

49  /**
50   * will check if the tree is empty
51   *
52   * @return true if the tree is indeed empty and false if not empty
53   */
54  @Override
55  public boolean empty() {
56      return root == NIL;
57  }
58
59  /**
60   * will search the tree to find the node with a given key through recursion
61   *
62   * @param node the node that is being searched
63   * @param key the value that is being searched
64   * @return the node that contains the that we are searching for if found and NIL if cant be found
65   */
66  private Node search(Node node, int key) {
67      if (node == NIL) { //checking if the node is empty/NULL
68          return NIL;
69      }
70      if (key < node.key) {
71          return search(node.left, key); //search in the left subtree of the current node
72      } else if (key > node.key) {
73          return search(node.right, key); //search in the right subtree of the current node
74      }
75      return node; //current node's key is the key being searched
76  }
77
78  /**
79   * does a left rotation on the given node x in the tree
80   *
81   * @param x the that is going to be rotated
82   */
83  private void rotateLeft(Node x) {
84      Node y = x.right; //storing the nodes right child into y
85      x.right = y.left;
86      if (y.left != NIL) { //checking if y's left child is empty/NULL
87          y.left.parent = x;
88      }
89      y.parent = x.parent;
90      if (x.parent == null) {
91          root = y;
92      } else if (x == x.parent.left) { //if x is a left child of its parent then update x's parents
93          //left child to be y
94          x.parent.left = y;
95      } else {
96          //otherwise x is a right child of its parent then update x's parents right child to be y
97          x.parent.right = y;
98      }
99      y.left = x; //make x to be the left child of y
100     x.parent = y; //make x to have y as its parent

```

```

101 }
102
103 /**
104  * does a right rotation on the given node y in the tree
105  *
106  * @param y the that is going to be rotated
107  */
108 private void rotateRight(Node y) {
109     Node x = y.left; //storing the nodes left child into x
110     y.left = x.right;
111     if (x.right != NIL) { //checking if x's right child is empty/NULL
112         x.right.parent = y;
113     }
114     x.parent = y.parent;
115     if (y.parent == null) {
116         root = x;
117     } else if (y == y.parent.right) { //if y is a right child of its parent then update y's
118         //parents right child to be x
119         y.parent.right = x;
120     } else {
121         //otherwise y is a left child of its parent then update y's parents left child to be x
122         y.parent.left = x;
123     }
124     x.right = y; //make y to be the right child of x
125     y.parent = x; //make y to have x as its parent
126 }
127
128 /**
129  * fixes the possible red black tree property violations after the insertion of a new node k
130  *
131  * @param k the newly inserted node that may violate the red black tree properties
132  */
133 private void insertFixUp(Node k) {
134     Node u; //uncle node
135     while (k.parent != null && k.parent.red) { //fixing tree while the parent of k is a red colour
136         if (k.parent == k.parent.parent.right) { //if the parent of k's parent is the right child
137             //of its parent
138             u = k.parent.parent.left;
139             if (u.red) { //case 1, where the uncle is red, thus violating the red black tree property
140                 u.red = BLACK;
141                 k.parent.red = BLACK;
142                 k.parent.parent.red = RED;
143                 k = k.parent.parent;
144             } else { //case 2, where k is the left child of its parent
145                 if (k == k.parent.left) {
146                     k = k.parent;
147                     rotateRight(k);
148                 } //case 3, where k is the right child of its parent
149                 k.parent.red = BLACK;
150                 k.parent.parent.red = RED;
151                 rotateLeft(k.parent.parent);
152             }

```

```

153     } else { //same as before cases but when k's parent is the left child of its parent
154         u = k.parent.parent.right;
155
156         if (u.red) {
157             u.red = BLACK;
158             k.parent.red = BLACK;
159             k.parent.parent.red = RED;
160             k = k.parent.parent;
161         } else {
162             if (k == k.parent.right) {
163                 k = k.parent;
164                 rotateLeft(k);
165             }
166             k.parent.red = BLACK;
167             k.parent.parent.red = RED;
168             rotateRight(k.parent.parent);
169         }
170     }
171     if (k == root) { //exit the loop if the root is reached
172         break;
173     }
174 }
175 root.red = BLACK; //enforces the fact that the root of the tree is black to preserve the
176                     //red black tree property
177 }
178
179 /**
180  * inserts a new node with the given key k into the tree
181  *
182  * @param k the key that is to be inserted
183  * @return true only if the insertion is successful and false the key trying to be inserted
184  *         already exists in the tree
185  */
186 @Override
187 public boolean insert(int k) {
188     Node node = new Node(k); //creates a new node for the input key
189     if (search(this.root, k) != NIL) { //checks if the input key already exists
190         return false; //key already exists so insertion fails
191     }
192
193     //standard binary search tree insert procedure
194     Node temp = root;
195     Node parent = null;
196     while (temp != NIL) {
197         parent = temp;
198         if (node.key < temp.key) {
199             temp = temp.left;
200         } else {
201             temp = temp.right;
202         }
203     }
204     node.parent = parent; //setting the parent of the newly created node

```

```

205
206     if (parent == null) {
207         root = node; //now if tree is empty then make the new node the root
208     } else if (node.key < parent.key) {
209         parent.left = node; //if new nodes is less than the parent then insert it as the left child
210     } else {
211         parent.right = node; //otherwise insert it as the right child since it is greater than parent
212     }
213
214     node.left = NIL; //initializing the new nodes children to NIL
215     node.right = NIL;
216
217
218     insertFixUp(node); //fixing the possible violations of the red black tree properties
219         //after the insertion
220     return true; //insertion is successful
221 }
222 /**
223  * fixes the possible red black tree property violations after the deletion of a new node x
224  *
225  * @param x the node for where the red black tree properties need to be fixed
226  */
227 private void deleteFix(Node x) {
228     Node s; //sibling node
229     while (x != root && x.red == BLACK) { //fixing tree while x is not the root and is black
230         if (x.parent != null && x == x.parent.left) {
231             s = x.parent.right;
232             //enforcing the sentinel is correct if needed
233             if (s == null){
234                 s = NIL;
235             }
236             if (s.left == null){
237                 s.left = NIL;
238             }
239             if (s.right == null){
240                 s.right = NIL;
241             }
242             if (s.red == RED) { //case 1: the sibling is red so we need to rotate it left and
243                 //recolour
244                 s.red = BLACK;
245                 x.parent.red = RED;
246                 rotateLeft(x.parent);
247                 s = x.parent.right;
248             }
249
250             if (s.left.red == BLACK && s.right.red == BLACK) {
251                 //case 2: both the left and right child of the sibling are black so we have
252                 //to move the violation up the tree
253                 s.red = RED;
254                 x = x.parent;
255             } else {
256                 if (s.right.red == BLACK) {

```

```

257         //case 3: right child of sibling is black so we need to rotate it right and
258         //recolour
259         s.left.red = BLACK;
260         s.red = RED;
261         rotateRight(s);
262         s = x.parent.right;
263     }
264     //case 4: keep recolouring and rotate left
265     s.red = x.parent.red;
266     x.parent.red = BLACK;
267     s.right.red = BLACK;
268     rotateLeft(x.parent);
269     x = root;
270 }
271 } else if (x.parent != null) { //same as before cases but when x is a right child of its parent
272     s = x.parent.left;
273     if (s == null){
274         s = NIL;
275     }
276     if (s.left == null){
277         s.left = NIL;
278     }
279     if (s.right == null){
280         s.right = NIL;
281     }
282     if (s.red == RED) {
283         s.red = BLACK;
284         x.parent.red = RED;
285         rotateRight(x.parent);
286         s = x.parent.left;
287     }
288
289     if (s.right.red == BLACK && s.left.red == BLACK) {
290         s.red = RED;
291         x = x.parent;
292     } else {
293         if (s.left.red == BLACK) {
294             s.right.red = BLACK;
295             s.red = RED;
296             rotateLeft(s);
297             s = x.parent.left;
298         }
299
300         s.red = x.parent.red;
301         x.parent.red = BLACK;
302         s.left.red = BLACK;
303         rotateRight(x.parent);
304         x = root;
305     }
306 }
307 }
308 x.red = BLACK;

```



```

309     }
310
311     /**
312     * gets the node which has the minimum key in the tree at the given node
313     *
314     * @param node the root node of the subtree to find the minimum key
315     * @return the node that has the minimum key in the subtree
316     */
317     private Node minimum(Node node) {
318         while (node.left != NIL) { //traverses to the left most child
319             node = node.left;
320         }
321         return node; //returns the minimum key in the subtree
322     }
323
324     /**
325     * replaces the subtree that is rooted at given node u with other subtree rooted at given node v
326     * in the red black tree
327     *
328     * @param u the node that has the subtree that will be replaced
329     * @param v the node that has the subtree that will replace u's subtree
330     */
331     private void transplant(Node u, Node v) {
332         if (u.parent == null) { //if the given node u is the root then set v to the root
333             root = v;
334         } else if (u == u.parent.left) { //if the given node u is a left child of its parent
335             //then make the left child of u's parent to v
336             u.parent.left = v;
337         } else { //if the given node u is a right child of its parent then make the right child of
338             //u's parent to v
339             u.parent.right = v;
340         }
341         v.parent = u.parent; //now update the parent of v to be the parent of u
342     }
343
344     /**
345     * delete the node with key k from the red black tree
346     *
347     * @param k the key of the node that is to be deleted
348     * @return true if sucessful in deletion and otherwise false if the key does not exist
349     */
350     @Override
351     public boolean delete(int k) {
352         Node node = search(root, k); //searching for the given input k in the tree
353         if (node == NIL) {
354             return false; //key does not exist in the tree so deletion will fail
355         }
356
357         Node y = node;
358         boolean yOriginalColor = y.red;
359         Node x;
360

```

```

361
362     if (node.left == NIL) { //case of where the node has either one child either left or right
363         x = node.right;
364         transplant(node, node.right);
365     } else if (node.right == NIL) {
366         x = node.left;
367         transplant(node, node.left);
368     } else { //case of where the node has both its left and right children
369         y = minimum(node.right);
370         yOriginalColor = y.red; //need to keep the original colour of y before changes
371         x = y.right;
372         if (y.parent == node) {
373             x.parent = y;
374         } else {
375             transplant(y, y.right);
376             y.right = node.right;
377             y.right.parent = y;
378         }
379         transplant(node, y);
380         y.left = node.left; //connecting y to the left subtree of node
381         y.left.parent = y;
382         y.red = node.red; //preserving the colour of node in y
383     }
384     if (yOriginalColor == BLACK) { //now fix any red black tree properties if the original
385         //colour of y was black
386         deleteFix(x);
387     }
388     return true; //successful deletion
389 }
390
391 /**
392  * determines if the node that has the key k exists in the red black tree
393  *
394  * @param k the key to search for in the tree
395  * @return true if k was found in the tree and otherwise false if not found
396  */
397 @Override
398 public boolean member(int k) {
399     return search(root, k) != NIL; //uses the search helper method to find if key k exists
400 }
401
402 /**
403  * will create a string representation of the red black tree that uses preorder traversal
404  *
405  * @return the representation of the red black tree that is in a form of a string
406  */
407 @Override
408 public String toString() {
409     StringBuilder result = new StringBuilder(); //making a StringBuilder to represent the string
410     preOrder(root, "*", result); //uses the preOrder helper method to
411     return result.toString();
412 }

```

```
413
414 /**
415  * achieves a preorder traversal of the red black tree and constructs a string representation of
416  * the structure of the tree with its node colours
417  *
418  * @param node the current node that is in the traversal
419  * @param address the address string which indicates the path to the current node
420  * @param result the result of the tree's string representation
421  */
422 private void preOrder(Node node, String address, StringBuilder result) {
423     if (node != NIL) { //if the node is not NIL then it appends the node's address, its colour
424         //either red or black and the key to the result
425         result.append(address).append(":");
426         result.append(node.red ? "red:" : "black:").append(node.key).append("\n");
427         preOrder(node.left, address + "L", result); //traverses the left subtree
428         preOrder(node.right, address + "R", result); //traverses the right subtree
429     }
430 }
431 }
432
```