

CSC 220

10/20/2020

Grammar



$$L = \{ 0^n 1^n \mid n \in \mathbb{N} \}$$

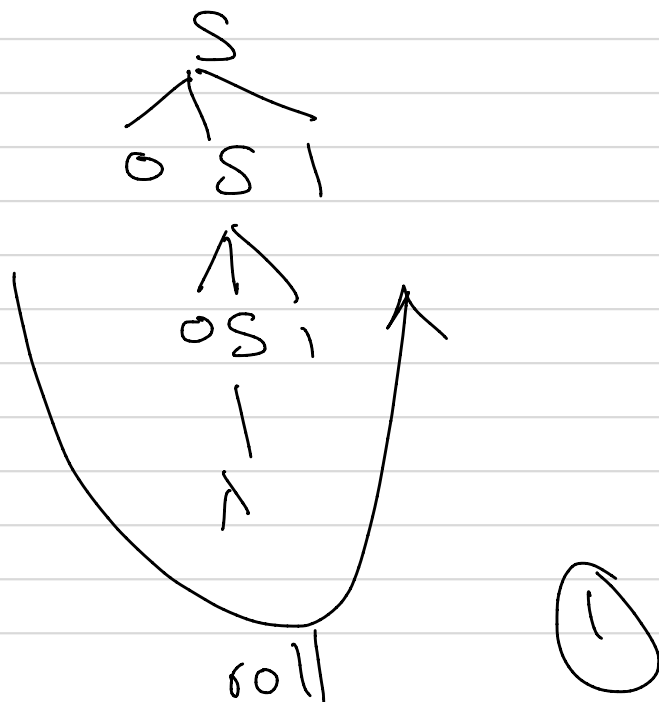
$$n=0 \quad 0^0 1^0 = \lambda \cdot \lambda = \lambda$$

$$n=1 \quad 01$$

$$n=2 \quad 0011$$

$$n=3 \quad 000111$$

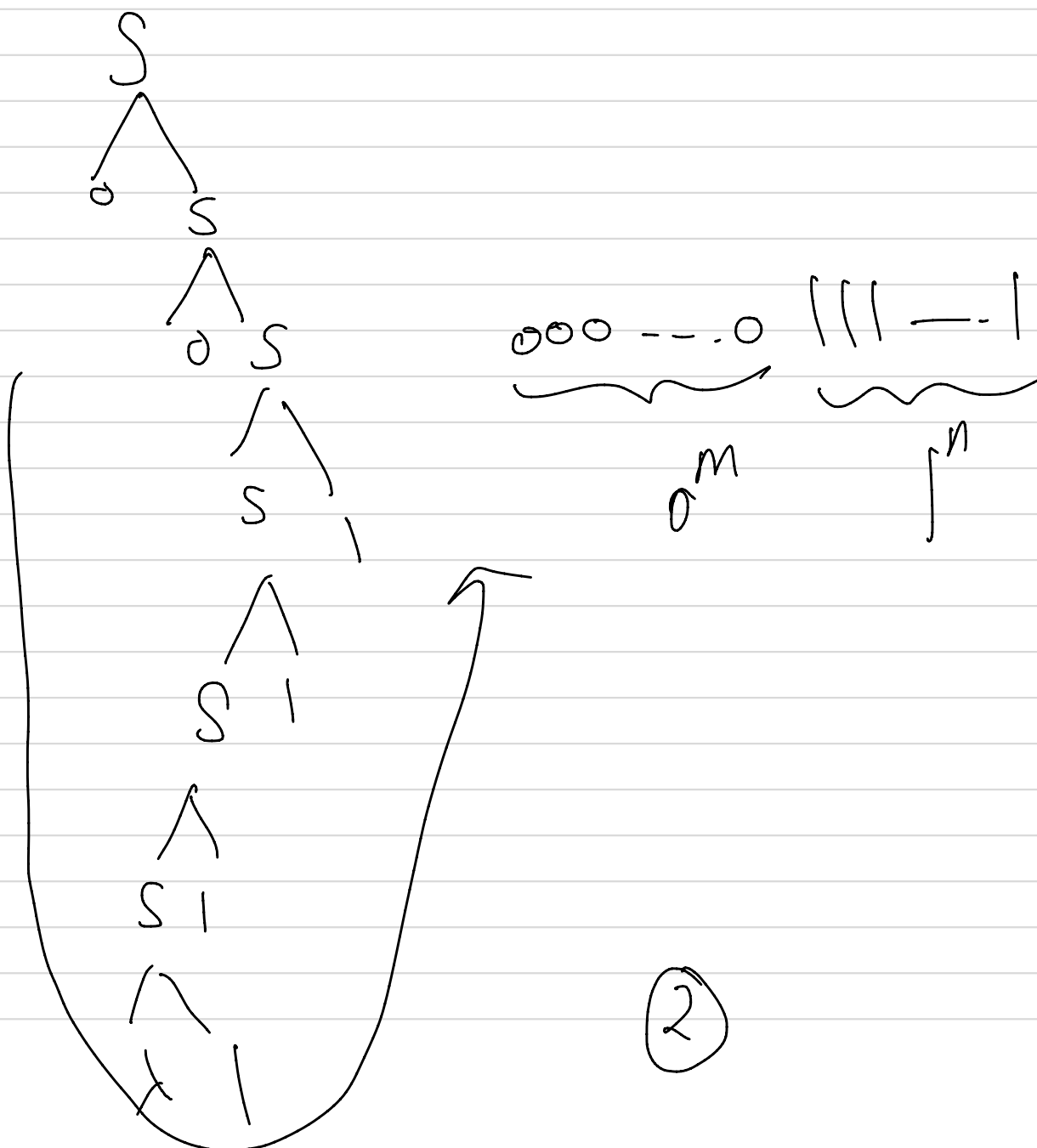
$$S \rightarrow \lambda \mid 0S1$$



$$L = \{ 0^m 1^n \mid m, n \in \mathbb{N} \}$$

$\lambda, 00001, 01111, \dots$

$$S \rightarrow \lambda \mid 0S \mid S1$$



$$L = \{ (000)^n \mid n \in \mathbb{N} \}$$

$$S \rightarrow \lambda \mid 000S$$

$$S \rightarrow 000S \rightarrow 000\lambda \quad 000$$

$$S \rightarrow 000S \rightarrow 000 \ 000S \rightarrow 000 \ 000 \lambda$$

;
;

③

Grammar for a lang. of even # of 0's no 1.

$\lambda, 00, 000 \notin L, 00 \in L, \dots$

$$S \rightarrow \lambda \mid 00S$$

Palindromes:

BOB, KAYAK, - - -

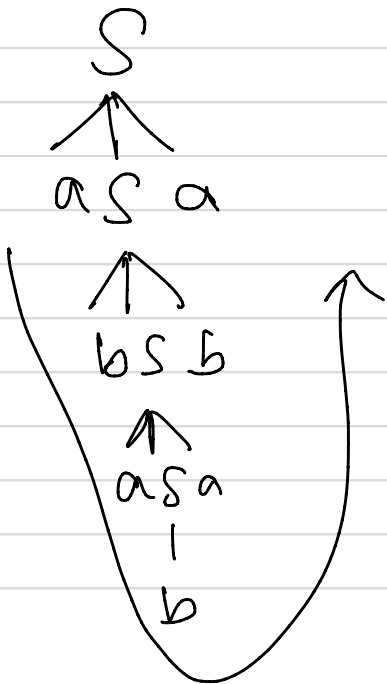
$$A = \{a, b\}$$
$$S \rightarrow a \mid b$$

but

aba ✓

bbabb ✓

—
(
—

$$S \rightarrow a|b|aSa|bSb$$


abababab

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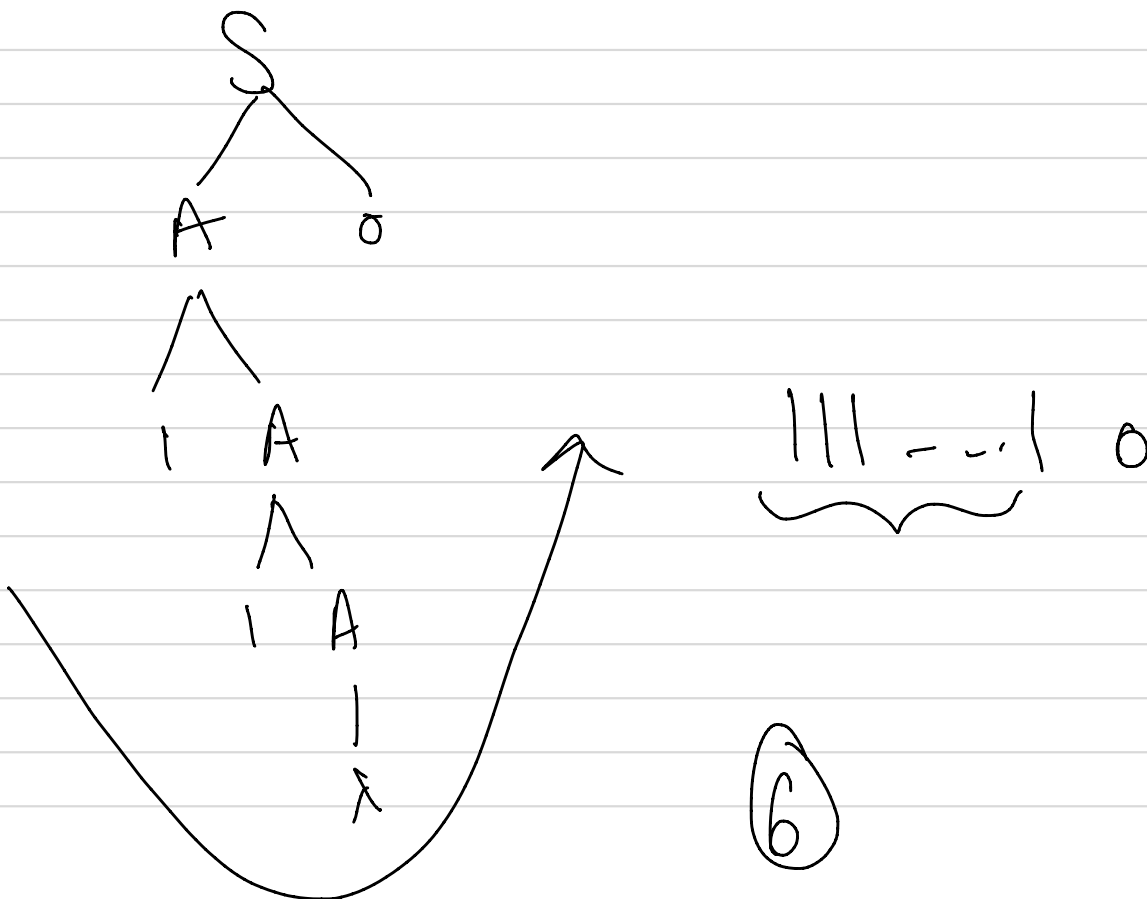
$$L = \{0^n \mid n \in \mathbb{N}\}$$

$$S \rightarrow 0S \mid \lambda$$

$$L = \{1^n 0 \mid n \in \mathbb{N}\}$$

$$S \rightarrow A0$$

$$A \rightarrow 1A \mid \lambda$$



$$L = \{ a^n b^m c^m d^{2n} \mid n \geq 0, m \geq 0 \}$$

$$m \geq 0 \Rightarrow a^0 b^0 c^0 d^0$$

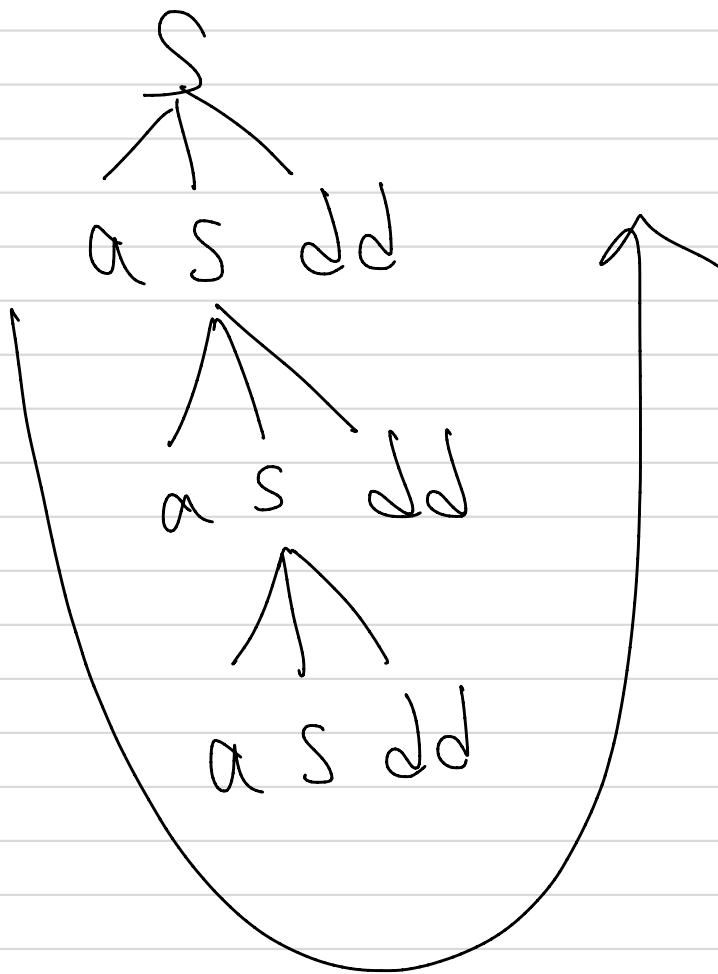
$$bc \in L$$

$$\underbrace{aa \dots a}_n \quad bc \quad \underbrace{ddd}_{2n}$$

$$S \rightarrow aSdd \mid A$$

$$A \rightarrow bc \mid bAc$$

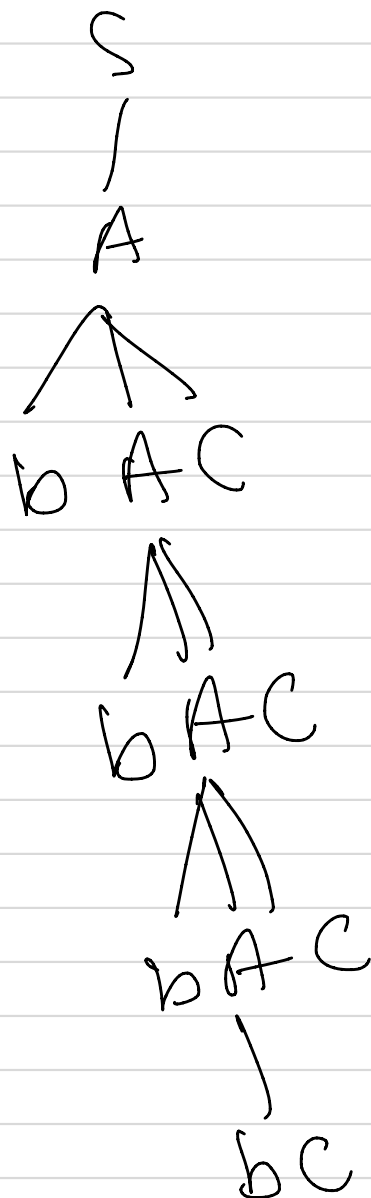
⑦

$$S \rightarrow aSdd$$


for each $a \rightarrow \text{dd}$



$S \rightarrow A \rightarrow bAC$



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$$L = \{a^n b^n\}$$

$$S \rightarrow aa \mid bb$$

$$L = \{aa, bb\}^*$$

$$S \rightarrow aaS \mid bbs \mid \lambda$$

$$L = \{ a b^n c \mid n \in \mathbb{N} \}$$

$ac, abc, abbc, abbbc, \dots$

$$S \rightarrow aBC$$

$$B \rightarrow \cancel{A} / bB$$

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