

# Formal Lang Assignment 1

Tyler Tracy

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1. The intersection is  $\{3\}$
2. The union is  $\{1,2,3,a,b\}$
3.  $A/B = \{1,2\}$
4.  $B/A = \{a,b\}$
5. Power set of  $A = \{\{1\}, \{2\}, \{3\}, \{1,2\}, \{1,3\}, \{2,3\}, \{1,2,3\}\}$
6. Power set of  $B = \{\{a\}, \{b\}, \{3\}, \{a,b\}, \{a,3\}, \{b,3\}, \{a,b,3\}\}$

Truth Table for  $A \implies B$

$A$	$B$	$A \rightarrow B$
$T$	$T$	$T$
$T$	$F$	$F$
$F$	$T$	$T$
$F$	$F$	$T$

Proof by induction:

$$(n+1)^*n = 2^*(1+2+\dots+n)$$

$$@ n = 1 : (1+1)^*1 = 2^*(1) = 2$$

$$@ n = k+1 : (k+2)^*(k+1) = 2^*(1+2+\dots+k+k+1)$$

$$(k+2)^*(k+1) = (k+1)^*k + 2^*(k+1)$$

$$(k+2)^*(k+1) = (k+2)^*(k+1)$$