KINEMATICS

Particle Rectilinear Motion Variable a:

$$v = v_0 + a_c t$$

$$s = s_0 + v_0 t + \frac{1}{2} a_c t^2$$

$$v^2 = v_0^2 + 2a_c (s - s_0)$$

Particle Curvilinear Motion

$r, z, \theta \ Coordinates$:

 $a_z = \ddot{z}$

$$\begin{array}{lll} v_r = \dot{r} & v_\theta = r\dot{\theta} & v_z = \dot{z} \\ a_r = \ddot{r} - r\dot{\theta}^2 & a_\theta = r\ddot{\theta} + 2\dot{r}\dot{\theta} \end{array}$$

$$-r\theta^2$$
 $a_\theta = r\theta + 2i$

n, t, b Coordinates:

$$a_t = \dot{v} = v \frac{\mathrm{d}v}{\mathrm{d}s}$$

$$a_n = \frac{v^2}{\rho}$$
 $\rho = \frac{[1 + (dy/dx)^2]^{3/2}}{|\frac{d^2y}{2}|}$

$$a = \sqrt{(a_n)^2 + (a_t)^2}$$

Relative Motion

$$v_A = v_B + v_{A/B}$$
$$a_A = a_B + a_{A/B}$$

Rigid Body Motion About a Fixed Axis

 $Variable \alpha$: $\omega = \frac{d\theta}{dt}$ $\alpha = \frac{d\omega}{dt}$ $\alpha d\theta = \omega d\omega$ Constant $\alpha = \alpha_c$:

$$\omega = \omega_0 + \alpha_c t$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha_c t^2$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha_c t$$

$$\omega^2 = \omega_0^2 + 2\alpha_c (\theta - \theta_0)$$
For Point P:

$s = \theta r \ v = \omega r \ a_t = \alpha r \ a_n = \omega^2 r$

KINETICS Mass Moment of Inertia $I = \int r^2 dm$

Parallel Axis Theorem:

 $I = I_G + md^2$ Rad. of Gyration: $k = \sqrt{\frac{I}{m}}$

$$\frac{n, t, o \, Coordinates :}{dv}$$

$$t = \dot{v} = v \frac{\mathrm{d}v}{\mathrm{d}s}$$

$$n = \frac{v^2}{\rho} \qquad \rho = \frac{[1 + (\mathrm{d}y/\mathrm{d}x)^2]^{3/2}}{\mathrm{d}^2y}$$

$$n = \frac{v^2}{\rho} \qquad \rho = \frac{[1 + (\mathrm{d}y/\mathrm{d}x)^2]^{3/2}}{|\frac{\mathrm{d}^2 y}{\mathrm{d}x^2}|}$$

Motion: Translating Axes $\mathbf{v}_B = \mathbf{v}_A + \mathbf{v}_{B/A(pin)}$ $\mathbf{a}_B = \mathbf{a}_A + \mathbf{a}_{B/A(pin)}$

Relative General Plane

Relative General Plane Motion: Trans. and Rot. Axes

$$\begin{aligned} \mathbf{v}_B &= \mathbf{v}_A + \Omega \times \mathbf{r}_{B/A} + (\mathbf{v}_{B/A})_{xyz} \\ \mathbf{a}_B &= \mathbf{a}_A + \dot{\Omega} \times \mathbf{r}_{B/A} + \Omega \times \\ (\Omega \times \mathbf{r}_{B/A}) + 2\Omega \times (\mathbf{v}_{B/A})_{xyz} + \\ (\mathbf{a}_{B/A})_{xyz} \end{aligned}$$

Equations of Motion $\frac{Particle: \mathbf{F} = m\mathbf{a}}{Rigid\ Body\ (Plane\ Motion):}$	$\frac{Spring: U_S = -(\frac{1}{2}ks_2^2 - \frac{1}{2}ks_1^2)}{\frac{Couple\ Moment:}{} U_M = M\Delta\theta}$	Conservation of Linear Momentum $\Sigma(syst.\ m{f v})_1 = \Sigma(syst.\ m{f v})_2$
$\Sigma F_x = m(a_G)_x$ $\Sigma F_y = m(a_G)_y$ $\Sigma M = I_G \alpha$	Power and Efficiency $P = \frac{dU}{dt} = \mathbf{F} \cdot \mathbf{v}$ $\epsilon = \frac{P_{out}}{P_{in}} = \frac{U_{out}}{U_{in}}$	$\frac{Coefficient\ of\ Restitution:}{e = \frac{(v_B)_2 - (v_A)_2}{(v_A)_1 - (v_B)_1}}$
Principle of Work and	$e - P_{in} - U_{in}$	Duin sink of America
Energy $T_1 + \Sigma U_{1-2} = T_2$	Conservation of Energy $T_1 + V_1 = T_2 + V_2$	Principle of Angular Impulse and Momentum Particle:
Kinetic Energy $Particle: T = \frac{1}{2}mv^2$ $Rigid Body:$ $T = \frac{1}{2}mv_G^2 + \frac{1}{2}I_G\omega^2$	$\begin{aligned} & Potential \; Energy : \\ & \overline{V} = V_g + V_e, \; where \; V_g = \pm Wy, \\ & V_e = \frac{1}{2}ks^2 \end{aligned}$	$\begin{split} &(\mathbf{H}_{O})_{1} + \Sigma \int \mathbf{M}_{O} \; \mathrm{d}t = (\mathbf{H}_{O})_{2} \\ &where \; H_{O} = (d)(mv) \\ &\underline{Rigid \; Body \; (Plane \; Motion) :} \\ &(\mathbf{H}_{G})_{1} + \Sigma \int \mathbf{M}_{G} \; \mathrm{d}t = (\mathbf{H}_{G})_{2} \\ &where \; H_{G} = I_{G} \omega \end{split}$
Work $ \begin{array}{l} Variable\ Force:\\ U_F = \int F\cos\theta\mathrm{ds}\\ \underline{Constant\ Force:}\\ U_F = (F_c\cos\theta)\Delta s \end{array} $	Principle of Linear Impulse and Momentum $\frac{Particle:}{m\mathbf{v}_1 + \sum \int F \mathrm{d}t = m\mathbf{v}_2}$ $\frac{Rigid Body:}{m\mathbf{v}_1 + \sum \int F \mathrm{d}t = m\mathbf{v}_2}$	$(\mathbf{H}_O)_1 + \Sigma \int \mathbf{M}_O \mathrm{d}t = (\mathbf{H}_O)_2$ where $H_O = I_O \omega$ Conservation of Angular Momentum
$\underline{Weight:}\ U_W = -W\Delta y$	$m(\mathbf{v}_G)_1 + \Sigma F \mathrm{d}t = m(\mathbf{v}_G)_2$	$\Sigma(syst. \mathbf{H})_1 = \Sigma(syst. \mathbf{H})_2$