### Axial Load

$$\underline{Normal\ Stress:}\ P = \frac{\sigma}{A}$$

$$\frac{Displacement:}{\delta = \int_{0}^{L} \frac{P(x) dx}{A(x)E}} \qquad \delta = \Sigma \frac{PI}{AI}$$

$$\delta = \Sigma \frac{PL}{AE}$$

### Torsion

 $\delta_T = \alpha \Delta T L$ 

#### Shear Stress in Circular Shaft:

$$\tau = \frac{T\rho}{J}$$
, where  $J = \frac{\pi}{2}c^4$  Solid cross section

$$J = \frac{\pi}{2} (c_o^4 - c_i^4) \text{ Tubular}$$

$$Power: P = T\omega = 2\pi fT$$

# $Angle\ of\ Twist:$ $\phi = \int_{-L}^{L} \frac{T(x)dx}{I(x)G}$

$$\phi = \Sigma \frac{TL}{LC}$$

#### Average Shear Stress in a Thin-Walled Tube:

$$\overline{\tau_{avg} = \frac{T}{2tA_m}}$$

Shear Flow: 
$$q = \tau_{avg}t = \frac{T}{2A_m}$$

### Bending

$$\underline{Normal\ Stress:}\ \sigma = \frac{M_y}{I}$$

$$Unsymmetric\ Bending:$$

$$\sigma = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\tan \alpha = \frac{I_z}{I_y} \tan \theta$$

#### Shear Average Direct Shear Stress:

$$\frac{\tau_{avg} = \frac{V}{A}}{\tau_{avg} = \frac{V}{A}}$$

$$\frac{Transverse\ Shear\ Stress\ :}{\tau = \frac{VQ}{A}}$$

Shear Flow:  $q = \tau t = \frac{VQ}{I}$ 

#### Stress in Thin-Walled Pressure Vessel

$$\frac{Cylinder: \sigma_1 = \frac{pr}{t}}{Sphere: \sigma_1 = \sigma_2 = \frac{pr}{2t}} \quad \sigma_2 = \frac{pr}{2t}$$

## Stress Transformation

Equations
$$\sigma_{x'} = \frac{\sigma_{x} + \sigma_{y}}{2} + \frac{\sigma_{x} - \sigma_{y}}{2} \cos 2\theta$$

$$+ \tau_{xy} \sin 2\theta$$

$$\tau_{x'y'} = -\frac{\sigma_{x} - \sigma_{y}}{2} \sin 2\theta$$

$$+ \tau_{xy} \cos 2\theta$$

$$\underline{Principle\ Stress}$$
:

$$\tan 2\theta_p = \frac{\tau_{xy}}{(\sigma_x - \sigma_y)/2}$$

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{(\frac{\sigma_x - \sigma_y}{2})^2 + \tau_{xy}^2}$$

|  | I.  | 1   |
|--|---|---|
| $\underline{Maximum\ In\text{-}Plane\ Shear}$  | $\gamma_{xy} = \frac{1}{G} \tau_{xy}$           | K = 0.5 Fixed ends  |
| $\underline{Stress}$ :   | $\gamma_{yz} = \frac{1}{G} \tau_{yz}$           | K = 0.7 Pinned and fixed ends   |
| $\tan 2\theta_s = -\frac{(\sigma_x - \sigma_y)/2}{\tau_{xy}}$                                      | $\gamma_{zx} = \frac{1}{C} \tau_{zx}$           |   |
| $\tau_{xy}$  | where $G = \frac{E}{2(1+\nu)}$                  | Critical Stress:  |
| $\tau_{max} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$                   | $2(1+\nu)$                                      |   |
| ¥ . 1  |   | $\sigma_{cr} = \frac{\pi^2 E}{(KL/r)^2}, \ r = \sqrt{I/A}$                                  |
| $\sigma_{avg} = \frac{\sigma_x + \sigma_y}{2}$   | Relations Between $w, V, M$                     | KL/r = Effective slenderness  |
|  | $\frac{dV}{dx} = w(x), \frac{dM}{dx} = V$       | ratio   |
| $Absolute\ Maximum\ Shear$   |   |   |
| $\overline{Stress}$ :  |   | Soant Formula   |
| $\tau_{abs\ max} = \frac{\sigma_{max}}{2}$   | Elastic Curve                                   | $Secant\ Formula: \sigma_{max} =$   |
|  | $\frac{1}{2} = \frac{M}{EI}$                    | $\frac{P}{A}\left[1 + \frac{ec}{-2}\sec\left(\frac{L}{2r}\sqrt{\frac{P}{EA}}\right)\right]$ |
| for $\sigma_{max}$ , $\sigma_{min}$ same sign  | P _==1  | , , , , , , , , , , , , , , , , , , ,   |
| $\sigma_{max} = \sigma_{mi}$   | $EI\frac{d^4v}{dx^4} = w(x)$                    | Energy Methods  |
| $	au_{abs\;max} = rac{\sigma_{max} - \sigma_{min}}{2}$  | 42  | 1   |
| for $\sigma_{max}$ , $\sigma_{min}$ opposite signs   | $EI\frac{\mathrm{d}^3 v}{\mathrm{d}x^3} = V(x)$ | Conservation of Energy:   |
|  | $EI\frac{\mathrm{d}^2 v}{\mathrm{d}x^2} = M(x)$ | $U_e = U_i$   |
| Motorial Property  | $dx^2$  |   |
| Material Property  |   | $Strain\ Energy:$   |
| Relations  |   | $U_i = \frac{N^2 L}{2AE}$ Constant axial load   |
| $\underline{Poisson's\ Ratio:}\ \nu = -\frac{\epsilon_{lat}}{\epsilon_{long}}$                     | Buckling  |   |
| $Generalized\ Hooke's\ Law:$   | Critical Axial Load:                            | $U_i = \int_0^L \frac{M^2 dx}{2EI}$ Bending moment  |
| $\frac{Generalized Hooke's Edd'.}{\epsilon_x = \frac{1}{E} [\sigma_x - \nu(\sigma_y + \sigma_z)]}$ | $P_{cr} = \frac{\pi^2 EI}{(KL)^2}$ , where      | 0   |
| E - 9  | K = 1 Pinned ends                               | $U_i = \int_0^L \frac{f_s v^2 dx}{2GA}$ Transverse shear                                    |
| $\epsilon_y = \frac{1}{E} [\sigma_y - \nu(\sigma_x + \sigma_z)]$                                   |   | $U_i = \int_0^L \frac{T^2 dx}{2GJ}$ Torsional moment  |
| $\epsilon_z = \frac{1}{E} [\sigma_z - \nu(\sigma_x + \sigma_y)]$                                   | K = 2 Free ends                                 | $\int_{0}^{\infty} \frac{1}{2GJ}$ Torsional moment  |