Plane

and Rot.

General

Motion: Translating Axes

 $\mathbf{v}_B = \mathbf{v}_A + \Omega \times \mathbf{r}_{B/A} + (\mathbf{v}_B/A)_{xyz}$ $\mathbf{a}_B = \mathbf{a}_A + \dot{\Omega} \times \mathbf{r}_{B/A} + \Omega \times$

 $(\Omega \times \mathbf{r}_B/A) + 2\Omega \times (\mathbf{v}_{B/A})_{xyz} +$

Mass Moment of Inertia

 $\mathbf{v}_B = \mathbf{v}_A + \mathbf{v}_{B/A(pin)}$

 $\mathbf{a}_B = \mathbf{a}_A + \mathbf{a}_{B/A(pin)}$

Relative General

Motion: Trans.

Engineering Mechanics: Dynamics

KINEMATICS

Rectilinear Motion Variable a:

$$\frac{v + ds}{v = \frac{ds}{dt}} \quad a = \frac{dv}{dt} \quad a ds = v dv$$

$$\frac{Constant \ a = a_c :}{v = v_0 + a_c t}$$

$$s = s_0 + v_0 t + \frac{1}{2} a_c t^2$$

 $v^2 = v_0^2 + 2a_c (s - s_0)$

Curvilinear Motion x, y, z Coordinates:

$$v_x = \dot{x}$$
 $v_y = \dot{y}$ $v_z = \dot{z}$
 $a_x = \ddot{x}$ $a_y = \ddot{y}$ $a_z = \ddot{z}$

$r, z, \theta \ Coordinates$:

$$a_r = \ddot{r} - r\theta^2 a_\theta = r\theta +$$
 $n, t, b \ Coordinates:$

$$\frac{n, t, b \ Coordinates :}{a_t = \dot{v} = v \frac{\mathrm{d}v}{\mathrm{d}t}}$$

 $a_n = \frac{v^2}{\rho}$ $\rho = \frac{\left[1 + \left(\frac{\mathrm{d}y}{\mathrm{d}x}\right)^2\right]^{3/2}}{\left|\frac{\mathrm{d}^2y}{\mathrm{d}x^2}\right|}$ $a = \sqrt{(a_n)^2 + (a_t)^2}$

 $Variable \alpha$:

 $\omega = \omega_0 + \alpha_0 t$

 $For\ Point\ P$:

Relative Motion

 $v_A = v_B + v_{A/B}$

 $la_A = a_B + a_{A/B}$

Rigid Body Motion About

a Fixed Axis

 $\omega = \frac{d\theta}{dt}$ $\alpha = \frac{d\omega}{dt}$ $\alpha d\theta = \omega d\omega$

Constant $\alpha = \alpha_c$:

 $\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha_c t^2$

 $\omega^2 = \omega_0^2 + 2\alpha_c(\tilde{\theta} - \theta_0)$

 $s = \theta r \ v = \omega r \ a_t = \alpha r \ a_n = \omega^2 r$

Parallel Axis Theorem : $I = I_G + md^2$ Rad. of Gyration: $k = \sqrt{\frac{I}{m}}$

Relative

Axes

 $(\mathbf{a}_{B/A})_{xyz}$

KINETICS

 $I = \int r^2 dm$

Equations of Motion $\frac{Particle: \mathbf{F} = m\mathbf{a}}{Rigid\ Body\ (Plane\ Motion):}$	$ \begin{array}{ c c c } Spring: U_S = -(\frac{1}{2}ks_2^2 - \frac{1}{2}ks_1^2) \\ \hline Couple \ Moment: U_M = M\Delta\theta \end{array} $	$ \begin{array}{ccc} \textbf{Conservation} & \textbf{of} & \textbf{Linear} \\ \textbf{Momentum} & \\ \Sigma(syst.\ m\mathbf{v})_1 = \Sigma(syst.\ m\mathbf{v})_2 \end{array} $
$egin{array}{ll} ar{\Sigma}F_x = m(a_G)_x & \Sigma F_y = m(a_G)_y \\ \Sigma M = I_G lpha & & & & & & \\ & & & & & & & \\ & & & & $	Power and Efficiency $P = \frac{dU}{dt} = \mathbf{F} \cdot \mathbf{v}$ $\epsilon = \frac{P_{out}}{P_{in}} = \frac{U_{out}}{U_{in}}$	$\frac{Coefficient \ of \ Restitution:}{e = \frac{(v_B)_2 - (v_A)_2}{(v_A)_1 - (v_B)_1}}$
Energy		Principle of Angular
$T_1 + \Sigma U_{1-2} = T_2$ Kinetic Energy $\underbrace{Particle:}_{C} T = \frac{1}{2}mv^2$ $\underbrace{Rigid\ Body:}_{C} T = \frac{1}{2}mv_G^2 + \frac{1}{2}I_G\omega^2$	Conservation of Energy $T_1+V_1=T_2+V_2$ $Potential\ Energy:$ $\overline{V}=V_g+V_e,\ where\ V_g=\pm Wy,$ $V_e=\frac{1}{2}ks^2$	$\begin{array}{l} \textbf{Impulse and Momentum} \\ \underline{Particle:} \\ (\mathbf{H}_O)_1 + \Sigma \int \mathbf{M}_O \ \mathrm{d}t = (\mathbf{H}_O)_2 \\ where \ H_O = (d)(mv) \\ \underline{Rigid \ Body \ (Plane \ Motion):} \\ (\mathbf{H}_G)_1 + \Sigma \int \mathbf{M}_G \ \mathrm{d}t = (\mathbf{H}_G)_2 \\ where \ H_G = I_G \omega \end{array}$
Work $\frac{Variable\ Force:}{U_F = \int F\cos\theta\mathrm{d}s}$	Principle of Linear Impulse and Momentum Particle:	$\begin{aligned} (\mathbf{H}_O)_1 + \Sigma \int \mathbf{M}_O \mathrm{d}t &= (\mathbf{H}_O)_2 \\ where H_O &= I_O \omega \end{aligned}$
$Constant\ Force:$ $U_F = (F_c cos\ \theta) \Delta s$ $Weight: U_W = -W \Delta y$	$\overline{m\mathbf{v}_1 + \Sigma \int F dt} = m\mathbf{v}_2$ $\frac{Rigid Body}{m(\mathbf{v}_G)_1 + \Sigma F} dt = m(\mathbf{v}_G)_2$	