

$(not(\leq (+ (f(x1)(0)) (* (-1)) (x3))) (-1)))$
 Proof/Definition of a!1
 $(not(\geq (+ (f(x1)(0)) (* (-1)) (x3))) (0)))$
 Proof/Definition of a!2
 $(= (\geq (f(x1)(0)) (x3)) (\geq (+ (f(x1)(0)) (* (-1)) (x3))) (0)))$
 Proof/Definition of a!3

$$\frac{(\geq (-x3)(f(x1)(0))) (1))}{\text{definition}} \quad \text{asserted}$$

 Proof/Definition of a!5
 $(= (-x3)(f(x1)(0))) (+ (x3) (* (-1)) (f(x1)(0))))$
 Proof/Definition of a!6
 $(\geq (+ (x3) (* (-1)) (f(x1)(0)))) (1))$
 Proof/Definition of a!7
 $(= (+ (x3) (* (-1)) (f(x1)(0)))) (+ (* (-1)) (f(x1)(0))) (x3)))$
 Proof/Definition of a!9
 $(\geq (+ (* (-1)) (f(x1)(0))) (x3)) (1))$
 Proof/Definition of a!10

$$\frac{(\geq (f(x1)(0)) (x3))}{\text{definition}} \quad \frac{(\geq (f(x1)(0)) (x3))}{\text{asserted}} \quad \frac{(a!3)}{\text{rewrite}} \quad \frac{(\geq (+ (f(x1)(0)) (* (-1)) (x3))) (0))}{\text{definition}} \quad \text{mp}$$

 Proof/Definition of a!4
 $(= (\geq (-x3)(f(x1)(0))) (1)) (a!7))$
 Proof/Definition of a!8
 $(= (a!10) (\leq (+ (f(x1)(0)) (* (-1)) (x3))) (-1)))$
 Proof/Definition of a!11
 $(= (a!7) (\leq (+ (f(x1)(0)) (* (-1)) (x3))) (-1)))$
 Proof/Definition of a!12

$$\frac{(\geq (f(x1)(0)) (x3))}{\text{definition}} \quad \frac{(a!6)}{\text{rewrite}} \quad \frac{(a!8)}{\text{monotonicity}} \quad \frac{(a!7)}{\text{mp}} \quad \frac{(a!9)}{\text{rewrite}} \quad \frac{(= (a!7) (a!10))}{\text{definition}} \quad \frac{(a!11)}{\text{rewrite}} \quad \frac{(a!12)}{\text{trans}} \quad \frac{(\leq (+ (f(x1)(0)) (* (-1)) (x3))) (-1))}{\text{definition}} \quad \text{mp}$$

 Proof/Definition of a!13

$$\frac{(or(a!1)(a!2))}{\text{th-lemma}} \quad \frac{(a!4)}{\text{definition}} \quad \frac{(a!13)}{\text{definition}} \quad \frac{(false)}{\text{definition}} \quad \text{unit-resolution}$$