Math 19 E
Spring 2019
Exam 2
March 20

Name:	

PRACTICE EXAM

This exam contains 7 pages and 6 questions. Total of points is 100. For full credit you must show your work. Partial credit may be given for incorrect solutions if sufficient work is shown. Messy/unorganized answers may be penalized, even if correct.

Grade Table (for teacher use only)

Question	Points	Score	
1	40		
2	10		
3	10		
4	20		
5	10		
6	10		
Total:	100		

<u>HONORS PLEDGE</u> (sign after exam is completed): I have neither given nor received aid on this exam, nor have I observed a violation of the UVM Code of Academic Integrity.

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- 1. (40 points) Calculate the derivatives of the following functions.
 - (a) (8 points)

$$h(x) = 3(2x^2 + 5x - 8)^4$$

(b) (8 points)

$$h(x) = 10\ln(1-7x)$$

(c) (8 points)

$$h(x) = \frac{1 - e^x}{1 + e^x}$$

(d) (8 points)

$$h(x) = x^2 \ln(x)$$

(e) (8 points)

$$h(x) = 5xe^{2x}$$

- 2. (10 points) For the function $h(x) = 5xe^{2x}$ from Problem 1(e),
 - (a) (5 points) For what value(s) of x will the tangent line to h(x) be horizontal?

(b) (5 points) Find the equation of the tangent line to h(x) when x = 0.

- 3. (10 points)
 - (a) (5 points) Suppose $h(x) = \frac{f(x)}{g(x)}$ and suppose we know that f(1) = 1, f'(1) = 4, g(1) = 2, and g'(1) = 7. Calculate h'(1).

(b) (5 points) Consider the function T(x) defined as

$$T(x) = \ln\left(\frac{x^3 f(x)}{g(x)}\right).$$

Find T'(x). Hint 1: use properties of logarithms to simplify (otherwise you have to do product + quotient rule = yikes!!!). Hint 2: your answer will involve f'(x) and g'(x) due to chain rule.

- 4. (20 points) For the implicit curve defined by the equation: $y^4 3y^3 + x^3 = 6$
 - (a) (10 points) Use implicit differentiation to find $\frac{dy}{dx}$.

(b) (5 points) Find the equation of the tangent line at the point (2,1).

(c) (5 points) For what value(s) of x will the tangent line to the curve be horizontal.

- 5. (10 points) One of these two problems (but not both) will appear on the exam!
 - A 40-foot ladder is placed against a wall. If the top of the ladder is sliding down the wall at 3 feet per second, at what rate is the bottom of the ladder moving away from the wall when the bottom of the ladder is 22 feet away from the wall?

• The radius of a spherical balloon is increasing at the rate of 6 centimeters per minute. How fast is the volume changing when the radius is 24 centimers?

Note: the formula for the volume V of a sphere with radius r is given by

$$V = \frac{4}{3}\pi r^3.$$

6. (10 points) Find the intervals on which f(x) is increasing and the intervals on which f(x) is decreasing.

$$f(x) = 3x^3 - 9x$$

Hint: make a sign chart for the derivative of f.