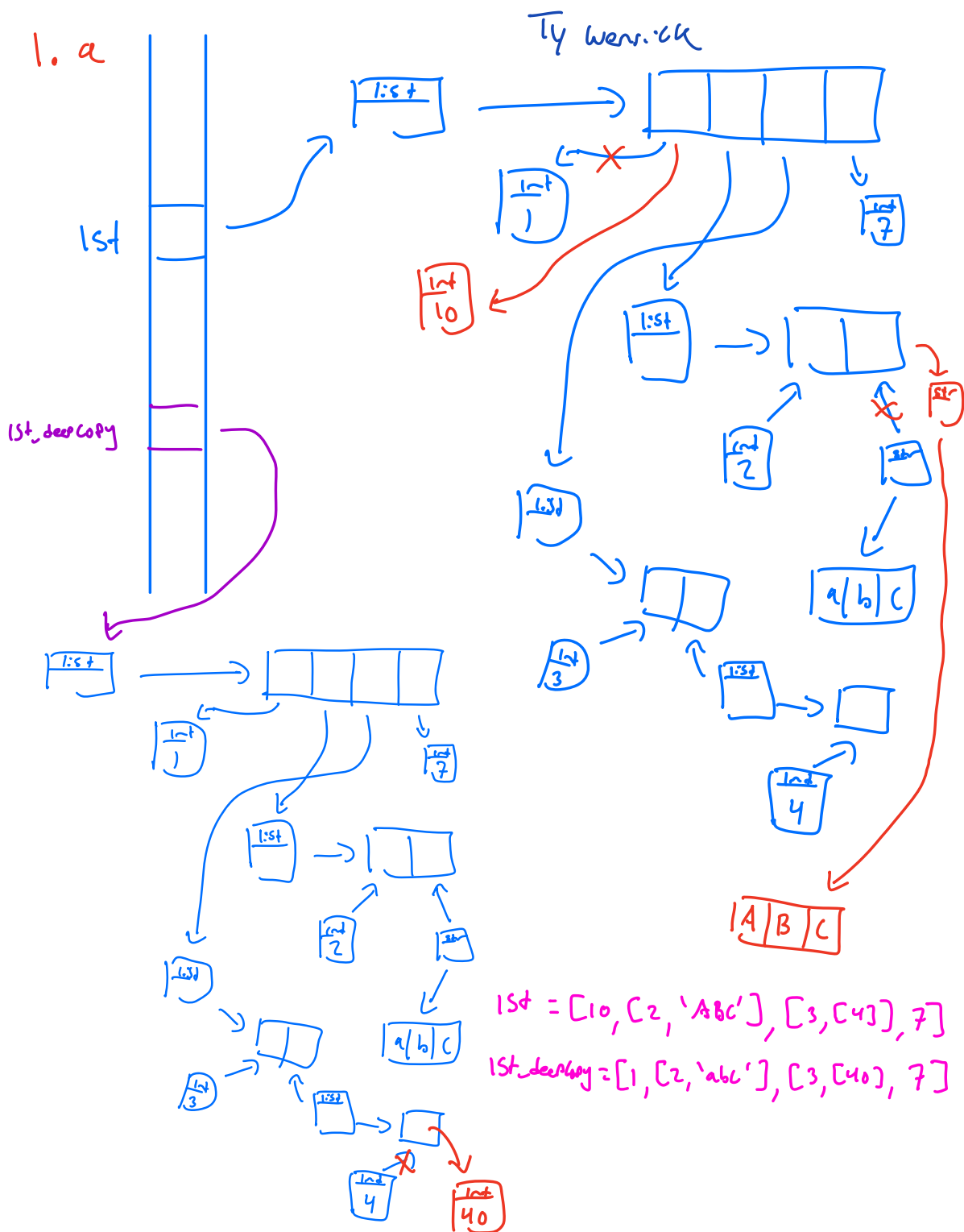


1. a



$$b. \frac{n^2-1}{n+1} \text{ is } O(n)$$

$$\frac{n^2-1}{n+1} < c * n$$

for all $n > n_0$

$$n-1 < c * n$$

$$n < 2 * n + 1$$

$$c=2 \quad n_0=1$$

$$c. \frac{n^2+1}{n+1} < c * n$$

$$n^2+1 < c * n(n+1)$$

$$n^2+1 < c(n^2+n)$$

$$n^2+1 < n^2 + n$$

$$c=1 \quad n_0=1$$

$$d. \sqrt{5n^2-3n+2} \quad \Theta(n)$$

$$\text{Big } O \quad d=\sqrt{5} \quad n_0=1(\sqrt{5}-3.16)$$

S

Ran out of time for this question.

3. a) $8n^2(\sqrt{n})$ is $O(n^3)$

TRUE

$$8n^2(\sqrt{n}) \leq C * n^3 \quad \text{for all } n \geq n_0$$

$$8n^2(\sqrt{n}) \leq 8n^3$$

$$8n^{2.5} \leq 8n^3$$

$$C = 8 \quad n_0 = 1$$

b) $8n^2(\sqrt{n})$ is $\Theta(n^3)$

False

n gets infinitely larger
no tight bound

c. TRUE

$$16 \log(n^2) + 2 \leq C * \log(n)$$

$$16 * 2 \log(n) + 2 \leq C * \log(n)$$

4. Given n numbers

$$1 + 1 + 1 + 1 + 1 \dots + 1 = n = \Theta(n)$$

$$n + n + n + n \dots + n = n^2 = \Theta(n^2)$$

$$1 + 2 + 3 + 4 + 5 \dots + n = \frac{n(n+1)}{2} = \Theta(n^2)$$

Given $\log(n)$ numbers where $n < 2$

$$1 + 2 + 4 + 8 + \dots + n$$

time
limit
up

$$\text{adding Powers of 2} \quad \underline{2^{n-1}} = \Theta(n)$$

notes

$$n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \frac{n}{16} \dots + 1 = \Theta(n)$$

$$n \left(1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} \dots + \frac{1}{n} \right) \quad n \left(1 + 1 \cdot \frac{1}{2} \right) = 2n-1$$

$$2n-1$$

```

5. def func(lst):
    a) for i in range(len(lst)):
        if (len(lst) % 2 == 0):
            return

```

$O(n)$ because $\text{len}(\text{lst})$ doesn't change
can be odd number

```

b) def func(lst):
    for i in range(len(lst)):
        if (len(lst) % 2 == 0):
            print(":", i)
        else:
            return

```

$O(n)$

6. constant $f(n)$

log $\log(n)$

sqrt \sqrt{n}

linear $f(n)$

linear log $\sqrt{\log(n)}$

quadratic $f(n^2)$

cubic $f(n^3)$

factorial $f(n!)$

7. def func1(n)

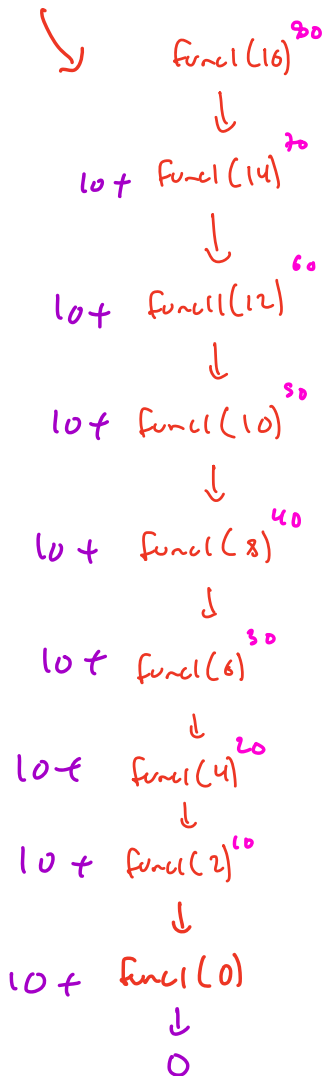
n = 16

a) if (n <= 1):
return 0

else:

return 10 + func1(n-2)

Call
Stack



func1(16)

outputs:

80

n-2

$\Theta(n)$

b) def func2(n): # n=16

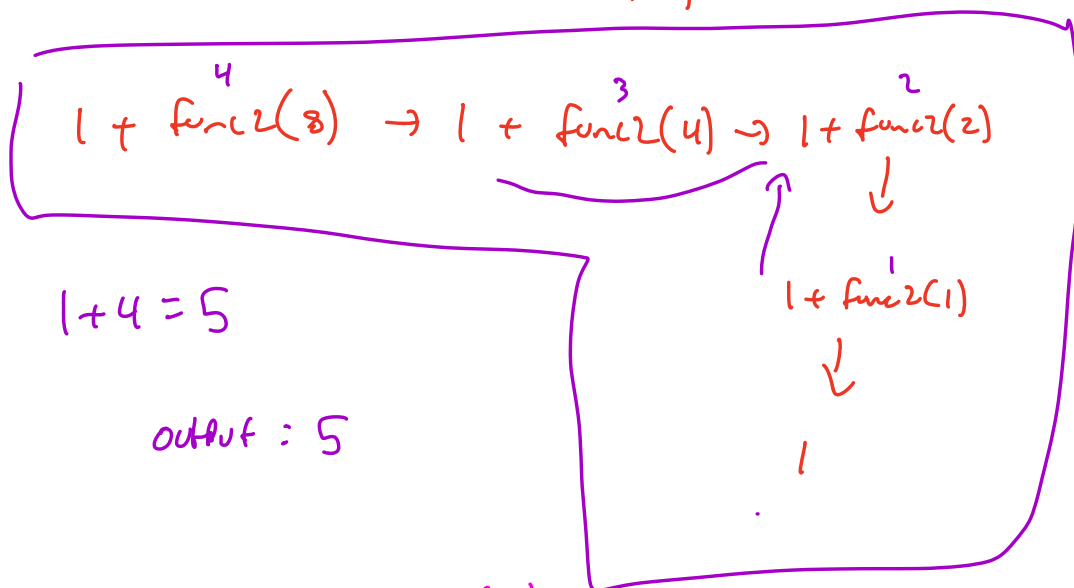
if (n <= 1):

return 1

$\frac{n}{2}$

else:

return 1 + func2(n//2)



$\Theta(n)$

Coding

1. `def reverse_list(lst):`

`return [i for i in lst[::-1]]`

2. `def reverse_list(lst, low = None, high = None):`

`if low is None:`

`low = 0`

`if high is None:`

`high = len(lst) - 1`

`while low < high:`

`lst[low], lst[high] = lst[high], lst[low]`

`low += 1`

`high -= 1`

2. def move_zeros(nums):

last_zero = 0

for i in range(len(nums)):

if nums[i] != 0:

nums[i], nums[last_zero] =

nums[last_zero],

nums[i]

←
→

0, 1, 0, 3, 13, 0

~~x~~ ~~x~~

1, 0, 0, 3, 13, 0
~~x~~

1, 3, 0, 0, 13, 0

1, 3, 13, 0, 0, 0

3. a. `def find_missing(lst):`
 `for num in range(len(lst)+1):`
 `if num not in lst:`
 `return num`

b. `def find_missing(lst):`
 `if lst[0] != 0:`
 `return 0`

 `for i in range(1, len(lst)):`
 `if lst[i] - lst[i-1] > 1:`
 `return lst[i] - 1`

 `return len(lst)`

```

3.C    def find_missing(list):
        total = sum(list)

        for num in range(len(list) + 1):
            total -= num

        return -total

```

```

4,    def sum_to(n):                # n = 3
        if n < 0:
            return 0
        else:
            return n + sum_to(n-1)

```

for $n=3$

$3 + \text{sum_to}(2) \rightarrow 2 + \text{sum_to}(1)$

↙

$3 + 2 + 1 + 0 = 6$

$1 + \text{sum_to}(0)$

↙

$0 + \text{sum_to}(-1) \rightarrow 0$

```

                    srt_lst
5. def binary_search(↓, low, high, val):
    if low > high:
        return None

    mid = (low + high) // 2

    if srt_lst[mid] == val:
        return mid

    elif srt_lst[mid] < val:
        return binary_search(srt_lst, val, mid+1,
                               high)
    else:
        return binary_search(srt_lst, val, mid-1, high)

```

6. `def find_max(lst):`
 `if len(lst) == 1:`
 `return lst[0]`
 `prev = find_max(lst[1:])`
 `if prev > lst[0]:`
 `return prev`
 `return lst[0]`

a,

↗

define runtime

`def find_max(lst, low, high):`
 `if low == high:`
 `return lst[low]`
 `curr_max = find_max(lst, low+1, high)`
 `if curr_max < lst[low]:`
 `curr_max = lst[low]`
 `return curr_max`

b,

7.

Solution on lab

```
def VL_Count(word, low, high):
```

```
    if low >= high:
```

```
        if word[low] in "aeiouAEIOU":
```

```
            return (1, 0)
```

```
        return (0, 1)
```

```
    else:
```

```
        prev = VL_Count(word, low+1, high)
```

```
        if word[low] in "aeiouAEIOU":
```

```
            return (prev[0] + 1, prev[1])
```

```
        return (prev[0], prev[1] + 1)
```