

Practical Work with Working Examples:

Bisection Method:

Output:

Instance 1:

$$f(x) = x^3 - 3x + 1$$

```
1 | Enter the values of a and b: 0 1
2 | The root is: 0.347321
```

Instance 2:

$$f(x) = x^3 - 2\sin(x)$$

```
1 | Enter the values of a and b: 0.5 2
2 | The root is: 1.236176
```

Lagrange's Method:

Instance 1:

x	$\frac{1}{3}$	$\frac{1}{4}$	1
f	2	-1	7

```
1 | Enter the number of data points: 3
2 | Enter the data points: 0.33 2
3 | 0.25 -1
4 | 1 7
5 | Input x at which interpolation is required: 0.5
6 | Interpolated function value at x = 0.50000 is 6.67288.
```

Instance 2:

x	-1	-2	2	4
$f(x)$	-1	-9	11	69

```
1 | Enter the number of data points: 4
2 | Enter the data points: -1 -1
3 | -2 -9
4 | 2 11
5 | 4 69
6 | Input x at which interpolation is required: 0
7 | Interpolated function value at x = 0.00000 is 1.00000.
```

Trapezoidal Method:

Instance 1:

Change the function in the program according to question.

$$\int_0^1 e^{-x^2} dx$$

```
1 Enter the lower limit of integration: 0
2 Enter the upper limit of integration: 1
3 Enter the number of subintervals: 5
4 The value of the integral is 0.74437.
```

Instance 2:

$$\int_0^\pi (3 \cos x + 5) dx \text{ with } n = 5$$

```
1 Enter the lower limit of integration: 0
2 Enter the upper limit of integration: 3.14
3 Enter the number of subintervals: 5
4 The value of the integral is 15.70462
```

Runge Kutta:

Instance 1

$$y' = y + \sin x$$
$$y(0) = 2$$

from $y(0) = 2$ we get initial values of x and y

```
1 Input initial values of x and y: 0 2
2
3 Input x at which y is required: 0.3
4
5 Input the number of steps: 0.1
6
7 1      0.100000      2.215508
8 2      0.200000      2.464138
9 3      0.300000      2.749218
10 Value of y at x = 0.300000 is 2.749218
```

Instance 2:

$$y' = y \cos x$$
$$y(0) = 1$$

Initial conditions here are 0 and 1

```
1 | Input initial values of x and y: 0 1
2 |
3 | Input x at which y is required: 0.5
4 |
5 | Input the number of steps: 0.25
6 |
7 | 1      0.250000      1.280688
8 | 2      0.500000      1.615127
9 | Value of y at x = 0.500000 is 1.615127
```
