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- pn Junction Current
- Generation–Recombination Currents
- High-Level Injection

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pn Junction Current

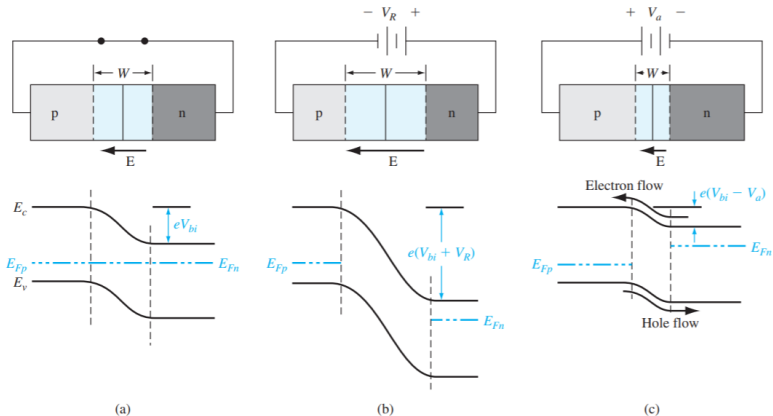


Figure: A pn junction and its associated energy-band diagram for (a) zero bias, (b) reverse bias, and (c) forward bias

pn Junction Current

The ideal current-voltage relationship of a pn junction is derived on the basis of four assumptions. (The last assumption has three parts, but each part deals with current.) They are:

1. The abrupt depletion layer approximation applies. The space charge regions have abrupt boundaries, and the semiconductor is neutral outside of the depletion region.
2. The Maxwell-Boltzmann approximation applies to carrier statistics.
3. The concepts of low injection and complete ionization apply.
- 4a. The total current is a constant throughout the entire pn structure.
- 4b. The individual electron and hole currents are continuous functions through the pn structure.
- 4c. The individual electron and hole currents are constant throughout the depletion region.

Boundary Conditions

An expression for the built-in potential barrier was derived in the last chapter and was given by Equation (7.10) as

$$V_{bi} = V_t \ln \left(\frac{N_a N_d}{n_i^2} \right)$$

If we divide the equation by $V_t = kT/e$, take the exponential of both sides, and then take the reciprocal, we obtain

$$\frac{n_i^2}{N_a N_d} = \exp \left(\frac{-eV_{bi}}{kT} \right)$$

no

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99

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Boundary Conditions

The potential barrier V_{bi} in Equation can be replaced by $(V_{bi} - V_a)$ when the junction is forward biased. Equation becomes

$$n_p = n_{n0} \exp\left(\frac{-e(V_{bi} - V_a)}{kT}\right) = n_{n0} \exp\left(\frac{-eV_{bi}}{kT}\right) \exp\left(\frac{+eV_a}{kT}\right)$$

If we assume low injection, the majority carrier electron concentration n_{n0} , for example, does not change significantly. However, the minority carrier concentration, n_p , can deviate from its thermal-equilibrium value n_{p0} by orders of magnitude. Using Equation, we can write Equation as

$$n_p = n_{p0} \exp\left(\frac{eV_a}{kT}\right)$$

$$(M)$$

Consider a silicon pn junction at $T = 300$ K. Assume the doping concentration in the n region is $N_d = 10^{16} \text{ cm}^{-3}$ and the doping concentration in the p region is $N_a = 6 \times 10^{15} \text{ cm}^{-3}$, and assume that a forward bias of 0.60 V is applied to the pn junction. Calculate the minority carrier concentrations at the edge of the space charge regions in a forward-biased pn junction.

Example 1 Solution

$$n_p(-x_p) = n_{po} \exp\left(\frac{eV_a}{kT}\right) \quad \text{and} \quad p_n(x_n) = p_{no} \exp\left(\frac{eV_a}{kT}\right)$$

The thermal-equilibrium minority carrier concentrations are

$$n_{po} = \frac{n_i^2}{N_a} = \frac{(1.5 \times 10^{10})^2}{6 \times 10^{15}} = 3.75 \times 10^4 \text{ cm}^{-3}$$

$$p_{no} = \frac{n_i^2}{N_d} = \frac{(1.5 \times 10^{10})^2}{10^{16}} = 2.25 \times 10^4 \text{ cm}^{-3}$$

We then have

$$n_p(-x_p) = 3.75 \times 10^4 \exp\left(\frac{0.60}{0.0259}\right) = 4.31 \times 10^{14} \text{ cm}^{-3}$$

$$p_n(x_n) = 2.25 \times 10^4 \exp\left(\frac{0.60}{0.0259}\right) = 2.59 \times 10^{14} \text{ cm}^{-3}$$

Minority Carrier Distribution

We developed, in Chapter 6, the ambipolar transport equation for excess minority carrier holes in an n region. This equation, in one dimension, is

$$D_p \frac{\partial^2 (\delta p_n)}{\partial x^2} - \mu_p E \frac{\partial (\delta p_n)}{\partial x} + g' - \frac{\delta p_n}{\tau_{p0}} = \frac{\partial (\delta p_n)}{\partial t}$$

In the n region for $x > x_n$, we have that $E = 0$ and $g' = 0$. If we also assume steady state so $\partial (\delta p_n) / \partial t = 0$, then Equation reduces to

$$\frac{d^2 (\delta p_n)}{dx^2} - \frac{\delta p_n}{L_p^2} = 0 \quad (x > x_n)$$

where $L_p^2 = D_p \tau_{p0}$.

Minority Carrier Distribution

For the same set of conditions, the excess minority carrier electron concentration in the p region is determined from

$$\frac{d^2(\delta n_p)}{dx^2} - \frac{\delta n_p}{L_n^2} = 0 \quad (x < x_p)$$

where $L_n^2 = D_n \tau_{n0}$. The general solution to Equation 1 is

$$\delta p_n(x) = p_n(x) - p_{n0} = Ae^{x/L_p} + Be^{-x/L_p} \quad (x \geq x_n)$$

and the general solution to Equation 2 is

$$\delta n_p(x) = n_p(x) - n_{p0} = Ce^{x/L_n} + De^{-x/L_n} \quad (x \leq -x_p)$$

Minority Carrier Distribution

The excess carrier concentrations are then found to be, for
 $(x \geq x_n)$,

$$\delta p_n(x) = p_n(x) - p_{n0} = p_{n0} \left[\exp \left(\frac{eV_a}{kT} \right) - 1 \right] \exp \left(\frac{x_n - x}{L_p} \right)$$

and, for $(x \leq -x_p)$,

$$\delta n_p(x) = n_p(x) - n_{p0} = n_{p0} \left[\exp \left(\frac{eV_a}{kT} \right) - 1 \right] \exp \left(\frac{x_p + x}{L_n} \right)$$

Minority Carrier Distribution

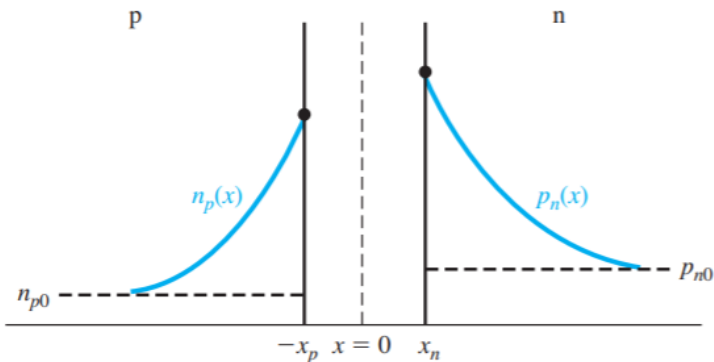


Figure: Steady-state minority carrier concentrations in a pn junction under forward bias.

Minority Carrier Distribution

In Chapter 6, we discussed the concept of quasi-Fermi levels, which apply to excess carriers in a nonequilibrium condition. Since excess electrons exist in the neutral p region and excess holes exist in the neutral n region, we can apply quasi-Fermi levels to these regions. We had defined quasi-Fermi levels in terms of carrier concentrations as

$$p = p_o + \delta p = n_i \exp \left(\frac{E_{Fi} - E_{Fp}}{kT} \right)$$

and

$$n = n_o + \delta n = n_i \exp \left(\frac{E_{Fn} - E_{Fi}}{kT} \right)$$

Combining them, we can write

$$np = n_i^2 \exp \left(\frac{E_{Fn} - E_{Fp}}{kT} \right)$$

Minority Carrier Distribution

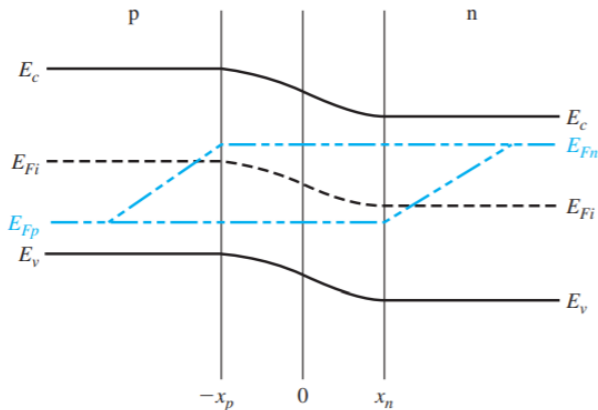


Figure: Quasi-Fermi levels through a forward-biased pn junction.

Ideal pn Junction Current

$$J_p(x_n) = \frac{eD_p p_{n0}}{L_p} \left[\exp\left(\frac{eV_a}{kT}\right) - 1 \right]$$

$$J_n(-x_p) = \frac{eD_n n_{p0}}{L_n} \left[\exp\left(\frac{eV_a}{kT}\right) - 1 \right]$$

The total current density in the pn junction is then

$$J = J_p(x_n) + J_n(-x_p) = \left[\frac{eD_p p_{n0}}{L_p} + \frac{eD_n n_{p0}}{L_n} \right] \left[\exp\left(\frac{eV_a}{kT}\right) - 1 \right]$$

Ideal pn Junction Current

We may define a parameter J_s as

$$J_s = \left[\frac{eD_p p_{n0}}{L_p} + \frac{eD_n n_{p0}}{L_n} \right]$$

so that Equation may be written as

$$J = J_s \left[\exp \left(\frac{eV_a}{kT} \right) - 1 \right]$$

Example 2

Consider a GaAs pn junction diode at $T = 300$ K. The parameters of the device are $N_d = 2 \times 10^{16} \text{ cm}^{-3}$, $N_a = 8 \times 10^{15} \text{ cm}^{-3}$, $D_n = 210 \text{ cm}^2/\text{s}$, $D_p = 8 \text{ cm}^2/\text{s}$, $\tau_{no} = 10^{-7} \text{ s}$, and $\tau_{po} = 5 \times 10^{-8} \text{ s}$. Determine the ideal reverse-saturation current density.

Example 2 Solution

The ideal reverse-saturation current density is given by

$$J_s = \frac{eD_n n_{p0}}{L_n} + \frac{eD_p p_{n0}}{L_p}$$

which may be rewritten as

$$\begin{aligned} J_s &= en_i^2 \left[\frac{1}{N_a} \sqrt{\frac{D_n}{\tau_{no}}} + \frac{1}{N_d} \sqrt{\frac{D_p}{\tau_{po}}} \right] \\ &= (1.6 \times 10^{-19}) (1.8 \times 10^6)^2 \\ &\quad \times \left[\frac{1}{8 \times 10^{15}} \sqrt{\frac{210}{10^{-7}}} + \frac{1}{2 \times 10^{16}} \sqrt{\frac{8}{5 \times 10^{-8}}} \right] \\ J_s &= 3.30 \times 10^{-18} \text{ A/cm}^2 \end{aligned}$$

Ideal I-V characteristic

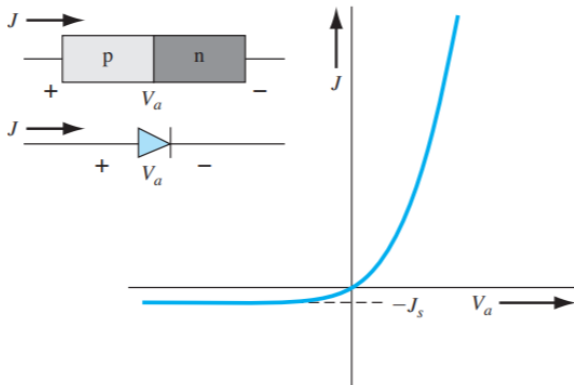


Figure: Ideal I-V characteristic of a pn junction diode

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Reverse-Biased Generation Current

$$R = \frac{-n_i}{\tau_{p0} + \tau_{n0}}$$

If we define a new lifetime as the average of τ_{p0} and τ_{n0} , or

$$\tau_0 = \frac{\tau_{p0} + \tau_{n0}}{2}$$

then the recombination rate can be written as

$$R = \frac{-n_i}{2\tau_0} \equiv -G$$

Reverse-Biased Generation Current

The negative recombination rate implies a generation rate, so G is the generation rate of electrons and holes in the space charge region. The generation current density may be determined from

$$J_{\text{gen}} = \int_0^W eGdx$$

where the integral is over the space charge region. If we assume that the generation rate is constant throughout the space charge region, then we obtain

$$J_{\text{gen}} = \frac{en_i W}{2\tau_0}$$

Forward-Bias Recombination Current

The recombination current density may be calculated from

$$J_{\text{rec}} = \int_0^W eRdx$$

where again the integral is over the entire space charge region. In this case, however, the recombination rate is not a constant through the space charge region. We have calculated the maximum recombination rate at the center of the space charge region, so we may write

$$J_{\text{rec}} = ex' \frac{n_i}{2\tau_0} \exp\left(\frac{eV_a}{2kT}\right)$$

where x' is a length over which the maximum recombination rate is effective. However, since τ_0 may not be a well-defined or known parameter, it is customary to write

$$J_{\text{rec}} = \frac{eWn_i}{2\tau_0} \exp\left(\frac{eV_a}{2kT}\right) = J_{r0} \exp\left(\frac{eV_a}{2kT}\right)$$

Total Forward-Bias Current

In general, the diode current-voltage relationship may be written as

$$I = I_s \left[\exp \left(\frac{eV_a}{nkT} \right) - 1 \right]$$

where the parameter n is called the ideality factor. For a large forward-bias voltage, $n \approx 1$ when diffusion dominates, and for low forward-bias voltage, $n \approx 2$ when recombination dominates. There is a transition region where $1 < n < 2$.

Example 3

Consider a silicon pn junction diode at $T = 300$ K with parameters $N_a = 2 \times 10^{15} \text{ cm}^{-3}$, $N_d = 8 \times 10^{16} \text{ cm}^{-3}$, $D_p = 10 \text{ cm}^2/\text{s}$, $D_n = 25 \text{ cm}^2/\text{s}$, and $\tau_0 = \tau_{p0} = \tau_{n0} = 10^{-7} \text{ s}$. The diode is forward biased at $V_a = 0.35 \text{ V}$.

- Calculate the ideal diode current density.
- Find the forward-biased recombination current density.
- Determine the ratio of recombination current to the ideal diffusion current.

Example 3 Solution

(a)

$$J \cong J_s \exp\left(\frac{V_a}{V_t}\right)$$

$$\begin{aligned} J_s &= en_i^2 \left[\frac{1}{N_a} \sqrt{\frac{D_n}{\tau_{no}}} + \frac{1}{N_d} \sqrt{\frac{D_p}{\tau_{po}}} \right] \\ &= (1.6 \times 10^{-19}) (1.5 \times 10^{10})^2 \\ &\quad \times \left[\frac{1}{2 \times 10^{15}} \sqrt{\frac{25}{10^{-7}}} + \frac{1}{8 \times 10^{16}} \sqrt{\frac{10}{10^{-7}}} \right] \\ J_s &= 2.891 \times 10^{-10} \text{ A/cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Then } J &\cong (2.891 \times 10^{-10}) \exp\left(\frac{0.35}{0.0259}\right) \\ &= 2.137 \times 10^{-4} \text{ A/cm}^2 \end{aligned}$$

Example 3 Solution

$$\begin{aligned} \text{(b) } V_{bi} &= (0.0259) \ln \left[\frac{(2 \times 10^{15})(8 \times 10^{16})}{(1.5 \times 10^{10})^2} \right] \\ &= 0.7068 \text{ V} \end{aligned}$$

We find

$$\begin{aligned} W &= \left\{ \frac{2(11.7)(8.85 \times 10^{-14})(0.7068 - 0.35)}{1.6 \times 10^{-19}} \right. \\ &\quad \times \left. \left[\frac{2 \times 10^{15} + 8 \times 10^{16}}{(2 \times 10^{15})(8 \times 10^{16})} \right] \right\}^{1/2} \\ &= 4.865 \times 10^{-5} \text{ cm} \end{aligned}$$

Example 3 Solution

Then

$$J_{rec} = \frac{en_i W}{2\tau_o} \exp\left(\frac{V_a}{2V_t}\right)$$

$$= \frac{(1.6 \times 10^{-19}) (1.5 \times 10^{10}) (4.865 \times 10^{-5})}{2(10^{-7})} \times \exp\left[\frac{0.35}{2(0.0259)}\right]$$

$$J_{rec} = 5.020 \times 10^{-4} \text{ A/cm}^2$$

(c)

$$\frac{J_{rec}}{J} = \frac{5.020 \times 10^{-4}}{2.137 \times 10^{-4}} = 2.35$$

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High-Level Injection

As the forward-bias voltage increases, the excess carrier concentrations increase and may become comparable or even greater than the majority carrier concentration.

$$np = n_i^2 \exp\left(\frac{V_a}{V_t}\right)$$

Under high-level injection, we may have $\delta n > n_o$ and $\delta p > p_o$ so that Equation becomes approximately

$$(\delta n)(\delta p) \cong n_i^2 \exp\left(\frac{V_a}{V_t}\right)$$

$$\delta n = \delta p \cong n_i \exp\left(\frac{V_a}{2V_t}\right)$$

The diode current is proportional to the excess carrier concentration so that, under high-level injection, we have

$$I \propto \exp\left(\frac{V_a}{2V_t}\right)$$

High-Level Injection

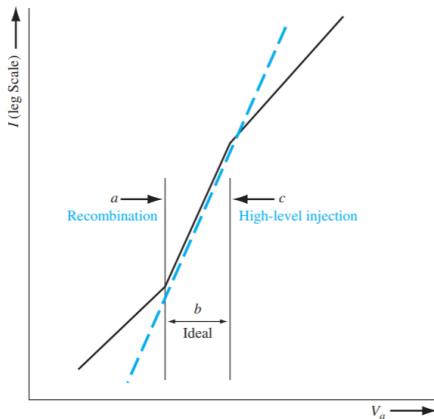


Figure: Forward-bias current versus voltage from low forward bias to high forward bias

