## FP.1 Match 3D Objects

Implement the method "matchBoundingBoxes", which takes as input both the previous and the current data frames and provides as output the ids of the matched regions of interest (i.e. the boxID property). Matches must be the ones with the highest number of keypoint correspondences.

Solution: The data structure std::map<int, std::map<int, int>> was used for recording the occurrences of all the potential matched bounding box candidates. In that, the first keys (outer map) were box IDs from previous frame, the second keys (inner map) were the matched one(s) from current frame, the last values were the respective occurrences.

## FP.2 Compute Lidar-based TTC

Compute the time-to-collision in second for all matched 3D objects using only Lidar measurements from the matched bounding boxes between current and previous frame.

Solution: The below table shows the TTCs computed from lidar point data for all frames.

| #  | Distance in X | TTC lidar |
|----|---------------|-----------|
| 1  | 7.913         | 12.9722   |
| 2  | 7.849         | 12.264    |
| 3  | 7.793         | 13.9161   |
| 4  | 7.741         | 14.8865   |
| 5  | 7.678         | 12.1873   |
| 6  | 7.577         | 7.50199   |
| 7  | 7.555         | 34.3404   |
| 8  | 7.515         | 18.7875   |
| 9  | 7.468         | 15.8894   |
| 10 | 7.414         | 13.7297   |
| 11 | 7.344         | 10.4914   |
| 12 | 7.272         | 10.1      |
| 13 | 7.194         | 9.22307   |
| 14 | 7.129         | 10.9678   |
| 15 | 7.042         | 8.09422   |
| 16 | 6.963         | 8.81392   |
| 17 | 6.896         | 10.2926   |
| 18 | 6.814         | 8.30978   |

## FP.3 Associate Keypoint Correspondences with Bounding Boxes

Prepare the TTC computation based on camera measurements by associating keypoint correspondences to the bounding boxes which enclose them. All matches which satisfy this condition must be added to a vector in the respective bounding box.

Solution: This feature was implemented in clusterKptMatchesWithROI (). The function used a shrink factor to scale down the overall size of the bounding box as some key points close to the edges should not be included, i.e. key points from lane markers or surrounding vehicles. The function also calculated a mean Euclidean distance between all matched key points, which was then being used to remove mis-matched outliers.

# FP.4 Compute Camera-based TTC

Compute the time-to-collision in second for all matched 3D objects using only keypoint correspondences from the matched bounding boxes between current and previous frame.

Solution: This feature was implemented in computeTTCCamera (). The median of all distance ratios was used to remove outliers. More outliers reduction methods and results were shown in the last section.

| #  | FAST+BRISK TTC |
|----|----------------|
| 1  | 12.1074        |
| 2  | 10.5933        |
| 3  | 14.0617        |
| 4  | 12.7493        |
| 5  | 55.5457        |
| 6  | 12.9517        |
| 7  | 12.6532        |
| 8  | 11.0928        |
| 9  | 11.591         |
| 10 | 11.1959        |
| 11 | 13.0815        |
| 12 | 11.7126        |
| 13 | 11.7494        |
| 14 | 11.3088        |
| 15 | 13.5299        |
| 16 | 10.3481        |
| 17 | 7.4008         |

18 8.95851

### FP.5 Performance Evaluation 1

Find examples where the TTC estimate of the Lidar sensor does not seem plausible. Describe your observations and provide a sound argumentation why you think this happened.

Solution: In the lidar TTC computation, the closest distance values to preceding vehicle were heavily used. There were several cases these values were way off. The below table shows the 1st, 2nd and 3rd closest lidar points from each image frame and the last column shows the delta distance between the 1st and 2nd points.

| #  | Closest Dis | 2nd Closest Dis | 3rd Closet Dis | Delta dis |
|----|-------------|-----------------|----------------|-----------|
| 1  | 7.913       | 7.913           | 7.916          | 0         |
| 2  | 7.849       | 7.85            | 7.851          | 0.001     |
| 3  | 7.793       | 7.803           | 7.804          | 0.01      |
| 4  | 7.685       | 7.741           | 7.744          | 0.056     |
| 5  | 7.638       | 7.678           | 7.683          | 0.04      |
| 6  | 7.577       | 7.58            | 7.581          | 0.003     |
| 7  | 7.555       | 7.558           | 7.56           | 0.003     |
| 8  | 7.475       | 7.515           | 7.515          | 0.04      |
| 9  | 7.434       | 7.468           | 7.47           | 0.034     |
| 10 | 7.393       | 7.414           | 7.415          | 0.021     |
| 11 | 7.205       | 7.344           | 7.349          | 0.139     |
| 12 | 7.272       | 7.273           | 7.274          | 0.001     |
| 13 | 7.194       | 7.195           | 7.195          | 0.001     |
| 14 | 7.129       | 7.131           | 7.134          | 0.002     |
| 15 | 7.042       | 7.043           | 7.045          | 0.001     |
| 16 | 6.827       | 6.963           | 6.966          | 0.136     |
| 17 | 6.896       | 6.897           | 6.897          | 0.001     |
| 18 | 6.814       | 6.815           | 6.816          | 0.001     |

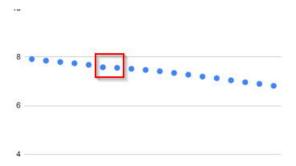
As shown in the below plot, we could argue that an idea lidar cluster shows a tight pattern and the delta distances shall stay below than 0.005.

When the delta distance was greater than 0.02, the point cluster started to show some degree of outliers. These distances were labeled with orange in the above table.

The extreme cases were where the delta distances were around 0.139 (labeled with red in table), the lidar points in these cases were way off, as demonstrated as below.

In the implementation, two approaches were taken to handle the outliers. First, all lidar points in the current bounding box were sorted in ascending order based on the distances in X direction. Then, the "tightness" was checked based on the distances among the k closest points. If the closest point were too far away from the rest, it would not be used. The next closest point would be examined, etc. This would take care of the single or double outlier(s) cases. Second, if there were multiple outliers, the mean distance in "X" direction were calculated from the lidar points in a calibratable index range, which was then used in TTC computation. The reason of not using the whole data set was that it would inevitably make the resulting distance further than the true value.

The result was shown previously in solution 2, there was a case, the resulting TTC was much longer than the rest, that was caused by two lidar measurements from two successive frames that were very closed. All distance measurements were plotted as below.



#### FP.6 Performance Evaluation 2

Run several detector / descriptor combinations and look at the differences in TTC estimation. Find out which methods perform best and also include several examples where camera-based TTC estimation is way off. As with Lidar, describe your observations again and also look into potential reasons.

Solution: Taking the FAST detector plus BRISK descriptor as an example, upon examination of detected key points, it's clear that a portion of them located in the top right corner area does not belong to the preceding vehicle. They came from a front vehicle of the right lane.

To solve this issue, in addition to applying a shrink factor to the bounding box, the key points that enclosed by multiple bounding boxes were labeled in a vector<int> matchIndexMultiBox, thus, not to be used in the camera TTC computation. This vector was determined in matchBoundingBoxes(), as iterations over all key points were done there for other reasons anyways. The below table shows the matches that were eliminated by each outlier removal approach. About 10 – 20 key point matches per frame will not be used in final TTC computation, leaving 50 – 60 matches to be used for TTC using this detector/descriptor combination.

| # | All matches in bb | After Removal of multi-bb enclosed | After Removal of mean – dis outlier |
|---|-------------------|------------------------------------|-------------------------------------|
| 1 | 59                | 49                                 | 48                                  |
| 2 | 68                | 60                                 | 59                                  |
| 3 | 79                | 67                                 | 63                                  |
| 4 | 70                | 60                                 | 58                                  |
| 5 | 66                | 50                                 | 49                                  |
| 6 | 70                | 61                                 | 60                                  |
| 7 | 79                | 64                                 | 62                                  |
| 8 | 74                | 57                                 | 55                                  |
| 9 | 76                | 58                                 | 57                                  |

| 10 | 75 | 62 | 61 |
|----|----|----|----|
| 11 | 68 | 68 | 67 |
| 12 | 89 | 76 | 73 |
| 13 | 90 | 71 | 68 |
| 14 | 86 | 72 | 68 |
| 15 | 80 | 65 | 64 |
| 16 | 88 | 63 | 62 |
| 17 | 91 | 67 | 65 |
| 18 | 85 | 58 | 57 |

The below table shows a camera based TTC computation comparison, in row five, the TTC was way longer than the rest when only mean distance outlier removal approach was used, and it was shortened by removing key points that were enclosed by multiple bounding boxes, but that was still an error TTC. The error could be coming from inaccurate key points detection.

|    | FAST+BRISK TTC                | FAST+BRISK TTC                 |
|----|-------------------------------|--------------------------------|
| #  | After Remove distance outlier | After Remove multi-bb enclosed |
| 1  | 12.2507                       | 12.1074                        |
| 2  | 11.5744                       | 10.5933                        |
| 3  | 14.1877                       | 14.0617                        |
| 4  | 12.9486                       | 12.7493                        |
| 5  | 89.6625                       | 55.5457                        |
| 6  | 12.3381                       | 12.9517                        |
| 7  | 11.8431                       | 12.6532                        |
| 8  | 10.6219                       | 11.0928                        |
| 9  | 11.7216                       | 11.591                         |
| 10 | 12.0135                       | 11.1959                        |
| 11 | 12.9492                       | 13.0815                        |
| 12 | 11.8227                       | 11.7126                        |
| 13 | 11.1224                       | 11.7494                        |
| 14 | 11.3432                       | 11.3088                        |
| 15 | 10.615                        | 13.5299                        |

| 16 | 12.1318 | 10.3481 |
|----|---------|---------|
| 17 | 7.45952 | 7.4008  |
| 18 | 8.96193 | 8.95851 |

The following tables documented all the camera based TTC computation results from all detector/ descriptor combinations. It's worth mentioned that the ORB gave the most amount of matched key points, SIFT detector found very accurate key points, AKAZE also performed well. They generally gave better key points than the rests. HARRIS detector, on the other hand, was not able to generate enough key point matches, thus no reliable computation can be done.

| SHITOMASI | BRISK   | BRIEF   | ORB     | FREAK   | SIFT    |
|-----------|---------|---------|---------|---------|---------|
| 1         | 12.8433 | 13.1872 | 13.1872 | 12.4657 | 12.7376 |
| 2         | 12.5842 | 12.2338 | 13.0927 | 12.9602 | 13.0927 |
| 3         | 12.5261 | 12.7493 | 12.5261 | 11.1762 | 12.5261 |
| 4         | 12.5425 | 13.4653 | 11.8277 | 12.561  | 12.9209 |
| 5         | 12.5574 | 13.1229 | 13.3604 | 12.981  | 13.0927 |
| 6         | 33.8072 | 51.093  | 51.093  | 33.4116 | 51.093  |
| 7         | 11.4035 | 17.4326 | 12.1842 | 12.7924 | 13.0836 |
| 8         | 48.7022 | 28.5716 | 34.5924 | 16.5133 | 34.5924 |
| 9         | 11.2406 | 11.322  | 10.7655 | 11.0326 | 11.322  |
| 10        | 12.2185 | 12.7782 | 13.0192 | 12.7    | 12.7782 |
| 11        | 11.1985 | 11.4051 | 11.3267 | 11.1395 | 11.4035 |
| 12        | 11.5372 | 11.9352 | 11.9445 | 11.5091 | 11.2932 |
| 13        | 10.8276 | 11.2589 | 10.8928 | 11.1144 | 10.8928 |
| 14        | 11.0007 | 11.4653 | 12.0086 | 9.97271 | 11.4653 |
| 15        | 7.7695  | 10.5009 | 9.30722 | 7.85835 | 10.2604 |
| 16        | 11.8009 | 10.6538 | 11.6088 | 12.1502 | 11.6088 |
| 17        | 10.6613 | 10.7978 | 10.7978 | 10.9456 | 10.7978 |
| 18        | 9.28292 | 10.2624 | 10.2624 | 10.8955 | 10.2624 |

Table 1 SHITOMASI + descriptors

| FAST | BRISK   | BRIEF   | ORB     | FREAK   | SIFT |
|------|---------|---------|---------|---------|------|
| 1    | 12.1074 | 11.9837 | 12.5923 | 11.6137 | 12.3 |

| 2  | 10.5933 | 11.4902 | 11.0927 | 11.9104 | 11.9321 |
|----|---------|---------|---------|---------|---------|
| 3  | 14.0617 | 15.4031 | 18.6767 | 13.6059 | 16.7148 |
| 4  | 12.7493 | 13.0998 | 13.4766 | 12.863  | 14.0808 |
| 5  | 55.5457 | 50.7164 | 136.717 | 43.1884 | 68.4601 |
| 6  | 12.9517 | 77.6257 | 55.9788 | 12.162  | 200.697 |
| 7  | 12.6532 | 13.3187 | 14.2267 | 12.6921 | 13.1858 |
| 8  | 11.0928 | 12.2852 | 11.5331 | 11.0924 | 11.8359 |
| 9  | 11.591  | 13.0071 | 12.0205 | 12.0205 | 12.9845 |
| 10 | 11.1959 | 11.9099 | 12.0364 | 11.3906 | 11.8211 |
| 11 | 13.0815 | 13.3065 | 16.7096 | 12.6239 | 13.8047 |
| 12 | 11.7126 | 11.9242 | 11.9242 | 12.3725 | 11.9904 |
| 13 | 11.7494 | 11.4287 | 12.4822 | 10.8341 | 11.4982 |
| 14 | 11.3088 | 12.3029 | 10.8823 | 11.6034 | 12.0391 |
| 15 | 13.5299 | 12.1787 | 10.8165 | 13.6029 | 11.8915 |
| 16 | 10.3481 | 10.1821 | 9.93405 | 10.4347 | 10.3473 |
| 17 | 7.4008  | 6.75334 | 10.4317 | 9.3235  | 7.26423 |
| 18 | 8.95851 | 9.86412 | 9.86412 | 10.7611 | 9.9403  |

Table 2 FAST + descriptors

| BRISK | BRISK   | BRIEF   | ORB     | FREAK   | SIFT    |
|-------|---------|---------|---------|---------|---------|
| 1     | 15.9129 | 13.2224 | 16.3066 | 11.3707 | 12.4207 |
| 2     | 24.4151 | 20.9711 | 18.9895 | 23.0196 | 16.7499 |
| 3     | 15.8779 | 14.1962 | 16.9161 | 15.4904 | 15.8622 |
| 4     | 14.2406 | 19.1127 | 16.124  | 13.6877 | 13.3158 |
| 5     | 38.1267 | 26.3307 | 23.0541 | 44.3614 | 61.1804 |
| 6     | 16.7515 | 16.1906 | 16.118  | 22.3342 | 12.7797 |
| 7     | 19.1964 | 18.1101 | 19.3314 | 17.7165 | 15.3729 |
| 8     | 17.8414 | 19.3001 | 18.7714 | 19.8115 | 19.4443 |
| 9     | 11.5134 | 18.0849 | 15.425  | 14.5459 | 14.6713 |
| 10    | 14.1491 | 11.4253 | 12.2923 | 12.1302 | 13.1305 |
| 11    | 13.4277 | 12.3646 | 13.5246 | 15.2564 | 14.0951 |
| 12    | 10.9403 | 15.9454 | 13.0255 | 11.8212 | 10.7941 |
| 13    | 10.7798 | 11.6277 | 10.3467 | 11.452  | 11.1499 |
| 14    | 13.7096 | 13.9751 | 14.6538 | 15.134  | 13.8841 |

| 15 | 11.0309 | 11.22   | 14.9521 | 11.6512 | 12.2551 |
|----|---------|---------|---------|---------|---------|
| 16 | 9.505   | 7.86839 | 9.4925  | 9.22807 | 8.94255 |
| 17 | 8.50294 | 10.1215 | 9.3229  | 9.08344 | 9.04073 |
| 18 | 9.61413 | 10.6804 | 10.9098 | 9.78683 | 9.25336 |

Table 3 BRISK + descriptors

| ORB | BRISK   | BRIEF   | ORB     | FREAK   | SIFT    |
|-----|---------|---------|---------|---------|---------|
| 1   | 23.9207 | 15.4892 | 16.1274 | 12.6614 | 14.2986 |
| 2   | 32.2936 | 16.5993 | 18.0406 | 11.5734 | 24.5336 |
| 3   | 19.7281 | 17.2944 | 14.3531 | 17.5533 | 15.1742 |
| 4   | 21.1512 | 15.5643 | 23.8041 | 12.7957 | 29.0782 |
| 5   | 23.7453 | 25.7587 | 27.5727 | 36.8389 | 52.139  |
| 6   | 34.5787 | 20.575  | 38.4812 | 14.4876 | 34.0743 |
| 7   | 18.0892 | 18.9894 | 14.588  | 10.7095 | 13.4362 |
| 8   | 19.1167 | 27.0044 | 31.4144 | 12.254  | 19.1372 |
| 9   | 18.7106 | 24.9116 | 13.493  | 11.1959 | 18.7485 |
| 10  | 13.3132 | 13.9011 | 13.7573 | 11.0672 | 13.221  |
| 11  | 13.1788 | 16.0621 | 16.5708 | 12.3778 | 17.4819 |
| 12  | 11.8607 | 20.1078 | 12.103  | 10.5461 | 11.1317 |
| 13  | 10.9981 | 13.8013 | 11.1106 | 10.6361 | 10.9953 |
| 14  | 10.845  | 10.8414 | 9.94925 | 10.8548 | 10.1379 |
| 15  | 11.9564 | 12.7403 | 15.6288 | 10.5824 | 12.7915 |
| 16  | 10.7964 | 10.5342 | 12.1821 | 8.96083 | 10.4772 |
| 17  | 9.59573 | 7.93232 | 9.39934 | 9.9032  | 9.56353 |
| 18  | 11.0525 | 11.9304 | 11.6118 | 11.0636 | 10.3248 |

Table 4 ORB + descriptors

| AKAZA | BRISK   | BRIEF   | ORB     | FREAK   | AKAZA   | SIFT    |
|-------|---------|---------|---------|---------|---------|---------|
| 1     | 12.8674 | 14.3489 | 12.764  | 13.2783 | 13.0126 | 12.8887 |
| 2     | 18.0855 | 18.2275 | 17.5173 | 17.7972 | 18.2301 | 18.6185 |
| 3     | 13.8423 | 14.0742 | 14.0557 | 14.4235 | 13.4534 | 13.9644 |
| 4     | 15.7624 | 14.8159 | 15.9847 | 14.2269 | 14.9035 | 15.7008 |
| 5     | 15.5579 | 16.3677 | 16.4395 | 15.5546 | 16.5989 | 16.8226 |

| 6  | 14.5293 | 14.4861 | 14.8422 | 14.3618 | 14.6603 | 15.0743 |
|----|---------|---------|---------|---------|---------|---------|
| 7  | 15.5947 | 17.3746 | 18.0491 | 15.7868 | 15.5947 | 15.9267 |
| 8  | 15.1575 | 14.5395 | 15.092  | 14.9208 | 14.6588 | 14.3626 |
| 9  | 20.4919 | 19.2508 | 18.7237 | 19.2747 | 16.4397 | 16.4263 |
| 10 | 13.1195 | 12.9979 | 13.1755 | 13.3247 | 13.4701 | 11.8933 |
| 11 | 12.4589 | 12.6803 | 12.3819 | 12.5336 | 11.9858 | 12.2092 |
| 12 | 12.4338 | 12.3051 | 12.977  | 12.8802 | 11.2962 | 11.433  |
| 13 | 9.78058 | 9.67199 | 10.1297 | 9.98508 | 10.2621 | 10.2181 |
| 14 | 11.5389 | 10.6412 | 10.5235 | 9.87759 | 11.6386 | 11.8647 |
| 15 | 11.8063 | 10.1472 | 9.88102 | 11.0593 | 9.81721 | 9.80535 |
| 16 | 9.46654 | 9.12905 | 9.09654 | 9.18654 | 9.10158 | 9.24892 |
| 17 | 9.1857  | 8.85196 | 9.06825 | 8.71978 | 8.95599 | 9.11708 |
| 18 | 8.45773 | 8.52705 | 8.68989 | 8.45728 | 8.59675 | 8.68923 |

Table 5 AKAZE + descriptors

| SIFT  | BRISK   | BRIEF   | FREAK   | SIFT    |
|-------|---------|---------|---------|---------|
| 311 1 | אכואום  | DIVILI  | INLAN   | 311 T   |
| 1     | 14.153  | 12.8427 | 16.3746 | 12.5555 |
| 2     | 14.3015 | 12.8452 | 14.3094 | 13.3381 |
| 3     | 14.6315 | 15.8301 | 15.605  | 13.1739 |
| 4     | 22.057  | 22.0046 | 22.9581 | 18.6291 |
| 5     | 14.5191 | 14.9068 | 19.0701 | 14.5191 |
| 6     | 11.4815 | 16.6981 | 18.0626 | 10.6541 |
| 7     | 13.3351 | 13.3351 | 14.0692 | 13.036  |
| 8     | 15.226  | 15.2357 | 15.2207 | 14.2712 |
| 9     | 13.1391 | 12.7337 | 13.0491 | 12.7265 |
| 10    | 11.7037 | 11.7095 | 11.8755 | 11.7037 |
| 11    | 12.3936 | 13.616  | 13.5712 | 12.0321 |
| 12    | 10.0053 | 10.5955 | 10.0141 | 10.5833 |
| 13    | 10.0363 | 10.2173 | 10.004  | 10.0917 |
| 14    | 9.3534  | 9.06884 | 9.0966  | 9.3534  |
| 15    | 10.1176 | 10.4542 | 9.85732 | 9.43508 |
| 16    | 8.6137  | 8.71978 | 8.6137  | 9.06923 |

| 17 | 9.36582 | 9.28811 | 9.53635 | 8.61572 |
|----|---------|---------|---------|---------|
| 18 | 10.8816 | 9.90599 | 13.4881 | 9.76798 |

Table 6 SIFT + descriptors