HW 13 GPT

April 19, 2023

```
[]: import torch
     import torch.nn as nn
     from torch.nn import functional as F
     # Hyperparameters.
     # I suggest you start with very small values, unless you have a strong PC or \square
      \rightarrow are running on the cluster
     batch_size = 64 # How many independent sequences will we process in parallel?
     block_size = 128 # What is the maximum context length for predictions?
     max_iters = 5000 # Max iterations we run the optimization
     # How often we evaluate across the optimization; every 500 iterations
     eval interval = 500
     learning_rate = 3e-4
     11 11 11
     Use 'mps' if on a mac as below:
     device = 'mps' if torch.backends.mps.is available() else 'cpu'
     device = 'cuda'
     # How many batches we use each time we evaluate
     eval_iters = 200
     \# d_model = 96
     # n_head = 6 # This implied that each head has a dimension for the key, query,
      \rightarrow and values of d_model / 6.
     \# n_layer = 6 \# This implies we have 6 turns to mix the embeddigs; this is "Nx"
      \rightarrow in the paper
     # dropout = 0.2
     d_model = 10
     n head = 2 # This implied that each head has a dimension for the key, query,
      \rightarrow and values of d_model / 6.
     n_layer = 2 # This implies we have 6 turns to mix the embeddigs; this is "Nx" \Box
      \rightarrow in the paper
```

```
dropout = 0.2

FILL_IN = "FILL_IN"

torch.manual_seed(1337)
```

[]: <torch._C.Generator at 0x27f547f9910>

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As usual, we read the text file and then get two dictionaries from char to idx and in reverse. char embeddings is what we will use here.

```
[]: with open('hemingway.txt', 'r', encoding='utf-8') as f:
         text = f.read()
     # Here are all the unique characters that occur in this text
     chars = sorted(list(set(text)))
     vocab_size = len(chars)
     # Create a mapping from characters to integers
     stoi = { ch:i for i,ch in enumerate(chars) }
     itos = { i:ch for i,ch in enumerate(chars) }
     encode = lambda s: [stoi[c] for c in s] # Encoder: take a string, output a list_
     \rightarrow of integers
     decode = lambda 1: ''.join([itos[i] for i in 1]) # Decoder: take a list of
     →integers, output a string
     # Train and Test splits
                                                                                      ш
     data = torch.tensor(encode(text), dtype=torch.long)
     print(data.dtype)
     n = int(0.9*len(data)) # First 90% will be train, rest val
     train data = data[:n]
     val_data = data[n:]
```

torch.int64

```
[]: # Data loading
     def get_batch(split):
         # Generate a small batch of data of inputs x and targets y
         data = train_data if split == 'train' else val_data
         # Randomly select batch_size rows from data's row indices
         ix = torch.randint(0, data.shape[0]-block_size, (batch_size, ))
         # Select batch_size chuncks of text each of size block_size; stack them
         xb = torch.stack([data[i.item():i.item()+block_size] for i in ix])
         # Do the same for y, but make sure that this is shifted over by 1
         yb = torch.stack([data[i.item()+1:i.item()+block_size+1] for i in ix])
         # I.e. if you select xb (1, 2, 3, 4), yb should be (2, 3, 4, 5)
         xb, yb = xb.to(device), yb.to(device)
         # Each of xb, yb should be (batch_size, block_size)
         return xb, yb
[]:
[]: Otorch.no_grad()
     def estimate loss(model):
         out = {}
         # Put the model in eval mode here
         model.eval()
         for split in ['train', 'val']:
             losses = torch.zeros(eval_iters, device = device)
             for k in range(eval_iters):
                 # Get a batch of data
                 xb, yb = get_batch(split)
                 # Get the mean and loss
                 logits, loss = model(xb, yb)
                 # Get the loss for this batch
                 losses[k] = loss.item()
             # Insert the mean estimate for the loss, based on the slit you are in
             out[split] = loss.mean().item()
         # Put the model in train mode here
         model.train()
         return out
[]:
[]: class Head(nn.Module):
         This class represents one head of self-attention
         Note that since this is a Decoder, this is masked-self-attention
         There is no Encoder, so there is no cross-self-attention
```

```
def __init__(self, d_head):
       super().__init__()
       # Map each key, query, or value in to a d head dimensional model.
       # Each should be matcies from d_model to d_head
       self.W_K = nn.Linear(d_model, d_head)
       self.W_Q = nn.Linear(d_model, d_head)
       self.W_V = nn.Linear(d_model, d_head)
       self.d_head = d_head
       self.register_buffer('tril', torch.tril(torch.ones(block_size,_
→block size)))
       self.dropout = nn.Dropout(dropout)
   def forward(self, x):
       \# (B, T, d_model)
       # B = batch_size, T = block_size in the below
       B,T,d = x.shape
       # Get the key and query representations from the embedding x
       \# (B, T, d head)
       k = self.W K(x)
       # (B, T, d_head)
       q = self.W_Q(x)
       \# (B, T, d\_head)
       v = self.W V(x)
       \# Compute attention scores, and get the new representations for this
\hookrightarrow h.e.a.d.
       \# (B \ T, \ d\_head) \ @ (B, \ d\_head, \ T) = (B, \ T, \ T)
       # Multiply q by k and divide by the appropriate constant
       scores = torch.bmm(q, k.view(B, self.d_head, T))/torch.sqrt(torch.
→tensor(self.d_head))
       # (B, T, T)
       # Apply a mask to scores, making all scores above the diagonal -inf
       scores = scores.masked_fill(scores.tril()==0, torch.
→tensor(float('-inf')))
       # (B, T, T)
       # Apply softmax to the final dimension of scores
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       a = torch.nn.Softmax(dim=-1)(scores)
```

```
# Apply dropout
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             a = self.dropout(a)
              # Perform the weighted aggregation of the values
              # Using a and v, get the new representations
              \# (B, T, T) @ (B, T, d_{head}) \rightarrow (B, T, d_{head})
             out = torch.bmm(a, v)
              # For each token, return the weighted sum of the values
             return out
     class MultiHeadAttention(nn.Module):
         .....
         Multiple heads of self-attention in parallel
         You can have just sequential code below
          11 11 11
         def __init__(self, num_heads, d_head):
             super().__init__()
              self.heads = nn.ModuleList([Head(d_head) for _ in range(num_heads)])
              # This is to project back to the dimension of d_model. In this case, it_{\sqcup}
      → is just a learned linear map
              self.W_O = torch.nn.Linear(num_heads*d_head, d_model)
              self.dropout = nn.Dropout(dropout)
         def forward(self, x):
              # Concatenate the different representations per head along the last \Box
      \rightarrow dimension
              out = torch.cat([head(x) for head in self.heads], dim=-1)
              # Project the concatenation and apply dropout; this is the \mathbb{W}_{-}0 in
      → "Attention is all you need"
              out = self.dropout(self.W O(out))
              return out
[]: class FeedFoward(nn.Module):
         A simple linear layer followed by a non-linearity; this is applied at the 
      \hookrightarrow token level
         11 11 11
         def __init__(self, d_model):
             super().__init__()
              d_ff = 4 * d_model
              # Map each token via a linear map to d_ff, apply ReLU, map back to_
      \rightarrow d_model, and then apply dropout
```

```
# This can be done with nn.Sequential
self.ff = torch.nn.Sequential(
          torch.nn.Linear(d_model, d_ff),
          torch.nn.ReLU(),
          torch.nn.Linear(d_ff, d_model),
          torch.nn.Dropout(dropout)
)
def forward(self, x):
    return self.ff(x)
```

```
[]: class DecoderBlock(nn.Module):
         Transformer decoder block: communication followed by computation
         These are stacked on top of each other one after another
         def __init__(self, d_model, n_head):
             super().__init__()
             # Each head gets a smaller dimensional representation of the data
             # Assume each head gets a representation of dimension d_head and_
      \rightarrow d_{model} is divisible by n_{head}
             d_head = d_model // n_head
             self.sa = MultiHeadAttention(n_head, d_head)
             self.ff = FeedFoward(d_model)
             self.ln1 = nn.LayerNorm(d_model)
             self.ln2 = nn.LayerNorm(d_model)
         def forward(self, x):
             This is different from the originl transformer paper
             In the "Attention is all you need" paper, we had
             x = self.ln1(x + self.sa(x))
             x = self.ln2(x + self.ffwd(x))
             See Figure 1 here, and mimic that: https://arxiv.org/pdf/2002.04745.pdf
             x = x + self.sa(self.ln1(x))
             x = x + self.ff(self.ln2(x))
             return x
```

```
[]: class GPT(nn.Module):
    def __init__(self):
        super().__init__()
        # Each token directly reads off the logits for the next token from a
        →lookup table
```

```
# Token embeddings are from vocab_size to d_model
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                                                                                Ш
       self.token_embedding_table = torch.nn.Embedding(vocab_size, d_model)
       # Position embeddings are from block_size (T) to d_model
       self.position embedding table = torch.nn.Embedding(block size, d model)
       # This should be n_sequential applications of a DecoderBlock
       # This is the "Nx" piece in the paper
       self.blocks = torch.nn.Sequential(*[DecoderBlock(d model, n head) for ___
→in range(n_layer)])
        # Final layer norm
       self.ln = torch.nn.LayerNorm(d_model)
       self.ff = torch.nn.Linear(d_model, vocab_size)
   def forward(self, idx, targets=None):
       B, T = idx.shape
       # idx and targets are both (B,T) tensor of integers
       # (B, T, d_model)
       tok_emb = self.token_embedding_table(idx)
       \# (T, d_{model})
       pos_emb = self.position_embedding_table(idx)
       # Add positional encodings to encodings
       \# (B, T, d_{model})
       x = tok_emb + pos_emb
       # Mix up the token representations over and over via the blocks
       \# (B, T, d model)
       x = self.blocks(x)
       # Apply layer norm
       # (B, T, d_model)
       x = self.ln(x)
       # Apply the final linear map, to get to dimension vocab_size
       # (B,T,vocab_size)
       logits = self.ff(x)
       if targets is None:
           loss = None
       else:
           B, T, V = logits.shape
           logits = logits.view(B*T, V)
```

```
targets = targets.view(B*T)
           loss = F.cross_entropy(logits, targets)
       return logits, loss
   def generate(self, idx, max_new_tokens):
       idx is (B, T) array of indices in the current context
       This will generate B total paths in parrallel
       We will just geenrate 1 batch below
       n n n
       self.eval()
       for _ in range(max_new_tokens):
           # crop idx to the last block_size tokens
           # The model only has kowledge of the context of maximum size
\rightarrowblock_size
           # Get the newest (B, T) data; T = block_size
           idx_cond = idx[:, -block_size:]
           # Get the predictions
           # (B, T, vocab_size)
           logits, loss = self.forward(idx_cond)
           # Focus only on the last time step, get the logits
           # (B, vocab_size)
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\hookrightarrow
           logits = logits[:, -1, :]
           # Apply softmax to get probabilities
           # (B, vocab_size)
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           probs = nn.functional.softmax(logits)
           # Sample from the distribution proporttional to probs
```

```
# (B, 1)

idx_next = torch.multinomial(probs, 1)

# Append sampled index to the running sequence
# (B, T+1)

idx = torch.cat((idx, idx_next), 1)
self.train()
return idx
```

```
class EarlyStopping:
    def __init__(self, tolerance=5, min_delta=0):

        self.tolerance = tolerance
        self.min_delta = min_delta
        self.counter = 0
        self.early_stop = False

def __call__(self, train_loss, validation_loss):
    if (validation_loss - train_loss) / train_loss > self.min_delta:
        self.counter += 1
        if self.counter >= self.tolerance:
            self.early_stop = True
```

```
# Create a PyTorch optimizer
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optimizer = torch.optim.AdamW(model.parameters(), lr=learning_rate)
scheduler = torch.optim.lr_scheduler.StepLR(optimizer, 1, gamma=0.9)
early_stopping = EarlyStopping(tolerance=1, min_delta=0.2)
for iter in range(max_iters):
    # every once in a while evaluate the loss on train and val sets
                                                                                Ш
                                                                                Ш
 \hookrightarrow
                                                                                Ш
    if iter % eval_interval == 0 or iter == max_iters - 1:
        if iter:
          scheduler.step()
        losses = estimate_loss(model)
        print(f"step {iter}: train loss {losses['train']:.4f}, val loss⊔
early_stopping(losses['train'], losses['val'])
        if early_stopping.early_stop:
          print("We stop at epoch {}".format(iter))
          break
    # Sample a batch of data
                                                                                Ш
                                                                                ш
                                                                                Ш
    xb, yb = get_batch('train')
```

```
# Evaluate the loss
                                                                                     ш
                                                                                     ш
         logits, loss = model(xb, yb)
         optimizer.zero_grad(set_to_none=True)
         loss.backward()
         optimizer.step()
    5262
    step 0: train loss 4.2127, val loss 4.2041
    step 500: train loss 2.8627, val loss 2.8944
    step 1000: train loss 2.5296, val loss 2.5746
    step 1500: train loss 2.4317, val loss 2.4719
    step 2000: train loss 2.3744, val loss 2.4223
    step 2500: train loss 2.3610, val loss 2.3627
    step 3000: train loss 2.3321, val loss 2.3800
    step 3500: train loss 2.3021, val loss 2.3527
    step 4000: train loss 2.2858, val loss 2.3385
    step 4500: train loss 2.3163, val loss 2.3293
    step 4999: train loss 2.3008, val loss 2.3143
[]: # Start the model with a new line, generate up to 10000 tokens
     # This is technically doing generations in batches, but here we have a batch\sqcup
     ⇒size of 1 and 1 element to start in the batch
     # If you have a model that's very large, d model = 384, n head = 6, n layer = 1
     \hookrightarrow6, you'll get fairly decent results
     context = torch.zeros((1, 1), dtype=torch.long, device=device)
     print(decode(model.generate(context, max_new_tokens=100)[0].tolist()))
     open('fake hemingway.txt', 'w').write(decode(model.generate(context,
      →max_new_tokens=100)[0].tolist()))
    C:\Users\Alex\AppData\Local\Temp\ipykernel_9944\1457601639.py:73: UserWarning:
    Implicit dimension choice for softmax has been deprecated. Change the call to
    include dim=X as an argument.
      probs = nn.functional.softmax(logits)
    "exathenor til an het aseimed.
    He re therstinsherd ma fat tricor t ayovine s."; the sh outhe srg T
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[]: torch.save(model.state_dict(), 'gpt.pt')