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### Expression for expansion of a constant raised to the power of x

$$a^x = 1 + \frac{x}{1!} \log_e a + \frac{x^2}{2!} (\log_e a)^2 + \dots + \frac{x^r}{r!} (\log_e a)^r + \dots \text{to } \infty$$

### Scope of application of expansion of constant raised to the power of x

All values of x

### Proof for the expansion of a constant raised to the power of x

•

$$a = e^k$$

•

$$k = \log_e(a)$$

•

$$a^x = (e^k)^x = e^{kx}$$

•

$$a^x = 1 + \frac{kx}{1!} + \frac{(kx)^2}{2!} + \dots + \frac{(kx)^r}{r!} + \dots \text{to } \infty$$

•

$$a^x = 1 + \frac{x}{1!} \log_e a + \frac{x^2}{2!} (\log_e a)^2 + \dots + \frac{x^r}{r!} (\log_e a)^r + \dots \text{to } \infty$$