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Formula for derivatives

$$\frac{d}{dx}x^n = nx^{n-1}$$

$$\frac{d}{dx}(ax+b)^n = n(ax+b)^{n-1}a$$

$$\frac{d}{dx}\sin x = \cos x$$

$$\frac{d}{dx}\cos x = -\sin x$$

$$\frac{d}{dx}\tan x = \sec^2 x$$

$$\frac{d}{dx}\sec x = \sec x \tan x$$

$$\frac{d}{dx}\csc x = \csc x \cot x$$

$$\frac{d}{dx}\cot x = -\csc^2 x$$

$$\frac{d}{dx}e^x = e^x$$

$$\frac{d}{dx}e^x = ae^{ax}$$

$$\frac{d}{dx}\log_e x = \frac{1}{x}$$

$$\frac{d}{dx}\log_e (ax+b) = \frac{1}{ax+b}$$

Formulae for anti derivatives

$$\int x^n dx = \frac{x^{n+1}}{n+1}$$

$$\int (ax+b)^n dx = \frac{(ax+b)^{n+1}}{(n+1)a} + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\int \csc^2 x dx = -\cot x + C$$

$$\int \sec x \tan x dx = \sec x + C$$

$$\int \csc x \cot x dx = -\csc x + C$$

$$\int e^x dx = -\cot x + C$$

$$\int e^x dx = e^x + C$$

$$\int e^{ax} dx = \frac{e^{ax}}{a} + C$$

$$\int \frac{1}{ax+b} dx = \frac{\log_e(ax+b)}{a} + C$$

Formulae for substitution

$$x^{2} + a^{2} \implies x = a \tan \theta$$

 $a^{2} - x^{2} \implies x = a \sin \theta$
 $x^{2} - a^{2} \implies x = a \sec \theta$

Formulae for standard integrals

$$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{1}{x^2 - a^2} dx = \frac{1}{2a} \log_e (\frac{x - a}{x + a}) + C$$

$$\int \frac{1}{a^2 - x^2} dx = \frac{1}{2a} \log_e (\frac{a + x}{a - x}) + C$$

$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \log_e (x + \sqrt{x^2 + a^2}) + C$$

$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \log_e (x + \sqrt{x^2 - a^2}) + C$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} (\frac{x}{a}) + C$$

Concept of Integration

- · Indefinite integral is the collection of family of curves.
- Indefinite integral is the curve formed by composing the contact points of all possible tangents in a curve.
- The constant C is a family of possibilities.

$$\frac{d}{dx}[x^2, x^2 + 6, x^2 + 100, x^2 + \frac{12}{9087}, x^2 + \sqrt{31212} \times \frac{2617}{2893}] = 2x$$

$$\int 2x dx = x^2 + C$$

Integration of exponential function

Integral structure of function in base of euler's number

For a function f(x):

$$\frac{d}{dx}[e^{f(x)}] = e^{f(x)} \times \frac{d}{dx}f(x)$$
$$\int e^{f(x)} \cdot f'(x)dx = e^{f(x)} + C$$

• The integral of functions $e^{f(x)} \times f'(x)$ is given by:

$$\int e^{f(x)} \cdot f'(x) dx = e^{f(x)} + C$$

• If the function can be expressed as f'(x) forms only after operating with a constant in it should be added.

Integral structure of function in base of a constant a

For a function f(x) and a constant a:

$$\frac{d}{dx}[a^x] = a^x \cdot 1 \cdot \log_e(a)$$

$$\frac{d}{dx}[a^{f(x)}] = a^{f(x)} \cdot \frac{d}{dx}f(x)$$

$$\int a^{f(x)} \cdot f'(x) = a^{f(x)} \cdot \frac{1}{\log_e(a)} + C$$

The integral of functions $a^{f(x)\times f'(x)}$ is given by:

$$\int a^{f(x)} \cdot f'(x) = \frac{a^{f(x)}}{\log_e(a)} + C$$

If the function can be expressed as f'(x) forms only after operating with a constant in it should be added. - The **trigonometric** functions are related to each other.

- **Cosine** functions: \$\sin x , \cos x\$
- **Cosecant** functions: \$\csc x , \sec x\$
- **Cotangent** functions: \$\cot x , \tan x\$
 - The relation of antiderivative by parts is:

$$\int uvdx = u \int vdx - \int \left(\frac{du}{dx} \int vdx\right)dx$$

- The v and u functions are chosen by **ILLATEC** rule.
 - I = Inverse Circular
 - L = Logarithmic
 - A = Algaebraic
 - T = Trigonometric

- E = Exponential
- C = Constant
- The **antiderivative** of $\sec^3 x$ is:

$$\int \sec^3 x dx = \frac{1}{2} \left(\frac{d}{dx} \sec x + \int \sec x \right) + C$$

- The **antiderivative** of functions of the type $x^n f(x)$ is evaluated by:
 - f(x) is **easily** integrated.
 - expression can be evaluated using integration by parts rule.

$$\int x^n f(x) dx = x^n \int f(x)$$

$$\int x^n f(x) dx = \frac{d}{dx} x^n \int f(x) - \frac{d^2}{dx^2} x^n \int \int f(x) + \frac{d^3}{dx^3} \int \int \int f(x)$$

$$\int x^n f(x) dx = \int uv dx$$

• The **antiderivative** is calculated by **differentiation** of u and **integration** of v with **alternate** signs.

$$\int uvdx = \frac{d}{dx}u\int v - \frac{d^2}{dx^2}u\int \int v + \frac{d^3}{dx^3}u\int \int \int v$$

De -Dt rule for integration

• The integration of the function of form $e^{ax}\sin(bx)dx$ can be done in:

$$\int e^{ax} \sin bx dx = \frac{1}{a^2 + b^2} \left(\frac{d}{dx} e^{ax} \times \sin bx - e^{ax} \frac{d}{dx} \sin bx \right) + C$$