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## Calculation of wavelength

- The **wavelength** of lyman series is calculated using:

$$\frac{1}{\lambda} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right)$$

- $R$  is Rydberg *constant* .
- $n$  is the value of orbit.

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## Excitation Energy

### Definition

- The **excitation** energy is the amount of energy required to raise an electron from its ground state to the corresponding excited *state*.
- The *first* excited state's excitation energy is the amount of energy required to raise the electron from ground state  $n = 1$  to the **first** excited state  $n = 2$ .

$$E = E_2 - E_1 = -3.4\text{eV} - (-13.6\text{eV}) = 10.2\text{eV}$$

## Excitation Potential

### Definition

- The **excitation** potential is the amount of potential difference required to accelerate the electron from the ground state to the *corresponding* excited state.
- The *first* excitation potential is the amount of potential difference required to accelerate the electron from the *ground* state to the *first excited* state.

$$\frac{E_2 - E_1}{e} = \frac{-3.4\text{eV} - (-13.6\text{eV})}{e} = 10.2\text{V}$$

## Ionization Energy

- **Ionization Energy** is the amount of energy required to move an electron from its **ground state** to **completely out** of the atom.

$$E = E_{\infty} - E_1 = 0 - (-13.6\text{eV}) = 13.6\text{eV}$$

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## Ionization Potential

- **Ionization Potential** is the amount of **potential difference** required to *accelerate* and electron from its *ground state* to *completely out of the atom* .

$$V = \frac{E_{\infty} - E_1}{e} = \frac{0 - (-13.6eV)}{e} = 13.6V$$

## Limitation of Bohr's Atomic Model

- **Bohr's atomic model** could not explain spectral lines of:
  - **multi** electron systems other than **hydrogen** and **hydrogen like** atoms.
- **Bohr's** atomic model doesnot clarify the **circular** structure of orbit of electron.
- **Zeeman Effect:**
  - **Zeeman Effect** is the splitting of spectral lines in **magnetic field** .
  - Bohr's model couldnot explain it.
- **Stark Effect:**
  - **Stark Effect** is the splitting of spectral lines in **electric field** .
  - Bohr's model couldnot explain it.
- Bohr's model couldnot explain the **wave like** character of **electron** .
- It doesnot explain the **relative splitting** of spectral lines.

## De Broglie Hypothesis

- **Statement:** Luis Debroglie states that:
  - A moving particle has both **wave like** and **particle like** characters.
  - A moving particle is associated with **waves**.
- These waves are called:
  - Debroglie Waves
  - Matter Waves

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- The **wavelength**  $\lambda$  of **matter waves** can be expressed as the same way for photon.

$$\lambda = \frac{h}{p}$$

### Calculation of wavelength of an electron

- mass =  $m$
- potential difference for acceleration =  $V$
- velocity of electron =  $v$
- momentum of electron =  $p$
- charge of electron =  $e$
- wavelength =  $\lambda$

$$\begin{aligned}\lambda &= \frac{h}{p} \\ eV &= \frac{1}{2}mv^2 \\ v &= \sqrt{\frac{2eV}{m}} \\ \lambda &= \frac{h}{m\sqrt{\frac{2eV}{m}}} \\ \lambda &= \frac{h}{\sqrt{2meV}}\end{aligned}$$

- The equation for expressing wavelength of **electron** is:

$$\lambda = \frac{h}{\sqrt{2meV}}$$

## Heisenberg's uncertainty Principle

### Canonically conjugate variables

- **Canonically conjugate** variables are:
  - pair of *physical variables*
  - those which can *describe* the motion of a system.

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- Examples of **cannonically** conjugate variables are:
    - **Momentum** and **Position**
    - **Energy** and **Time**
    - **Angular Momentum** and **Angular Position**

### Statement

- **Heisenberg's** uncertainty principle states that:
  - The pair of *physical* variables *describing* the motion of an **atomic system** cannot be measured **precisely** and **simultaneously**.

### Mathematical Interpretation

- The interpretation of **canonically paired** physical variables are:

$$\Delta x \Delta p \geq \frac{h}{2\pi}$$

$$\Delta E \Delta t \geq \frac{h}{2\pi}$$

$$\Delta \theta \Delta L \geq \frac{h}{2\pi}$$

### Application of Heisenberg's Uncertainty Principle

- **Heisenberg's uncertainty** principle is used to prove that the **electron** cannot exist inside the **nucleus** .
- mass of electron =  $m$
- planck's constant =  $h$
- change in position =  $\Delta x$
- $\Delta x$  = magnitude of radius of nucleus
- $\Delta x = 10^{-14}m$

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- change in momentum =  $\Delta p$

$$\Delta x \Delta p \geq \frac{h}{2\pi}$$

$$\Delta p = \frac{h}{2\pi \Delta x}$$

$$\Delta v_x = \frac{h}{2\pi \Delta x m}$$

$$\Delta v_x = \frac{6.62 \times 10^{-34}}{2 \times 3.14 \times 9.1 \times 10^{-31} \times 10^{-14}}$$

$$\Delta v_x = 1.16 \times 10^{10} m/s$$

- This magnitude of velocity is *unattainable* .
- The speed limit in the universe is  $3 \times 10^8 m/s$ .