
Contents

Calculation of wavelength	2
Excitation Energy	2
Definition	2
Excitation Potential	2
Definition	2
Ionization Energy	3
Ionization Potential	3
Limitation of Bohr's Atomic Model	3
De Broglie Hypothesis	4
Calculation of wavelength of an electron	4
Heisenberg's uncertainty Principle	5
Canonically conjugate variables	5
Statement	5
Mathematical Interpretation	5
Application of Heisenberg's Uncertainty Principle	6

Calculation of wavelength

- The **wavelength** of lyman series is calculated using:

$$\frac{1}{\lambda} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right)$$

- R is Rydberg *constant* .
- n is the value of orbit.

Excitation Energy

Definition

- The **excitation** energy is the amount of energy required to raise an electron from its ground state to the corresponding excited *state* .
- The *first* excited state's excitation energy is the amount of energy required to raise the electron from ground state $n = 1$ to the **first** excited state $n = 2$.

$$E = E_2 - E_1 = -3.4eV - (-13.6eV) = 10.2eV$$

Excitation Potential

Definition

- The **excitation** potential is the amount of potential difference required to accelerate the electron from the ground state to the *corresponding* excited state.
- The *first* excitation potential is the amount of potential difference required to accelerate the electron from the *ground* state to the *first excited* state.

$$\frac{E_2 - E_1}{e} = \frac{-3.4eV - (-13.6eV)}{e} = 10.2V$$

Ionization Energy

- **Ionization Energy** is the amount of energy required to move an electron from its **ground state** to **completely out** of the atom.

$$E = E_{\infty} - E_1 = 0 - (-13.6\text{eV}) = 13.6\text{eV}$$

Ionization Potential

- **Ionization Potential** is the amount of **potential difference** required to *accelerate* and electron from its *ground state* to *completely out of the atom*.

$$V = \frac{E_{\infty} - E_1}{e} = \frac{0 - (-13.6\text{eV})}{e} = 13.6\text{V}$$

Limitation of Bohr's Atomic Model

- **Bohr's atomic model** could not explain spectral lines of:
 - **multi** electron systems other than **hydrogen** and **hydrogen like** atoms.
- **Bohr's** atomic model doesnot clarify the **circular** structure of orbit of electron.
- **Zeeman Effect:**
 - **Zeeman Effect** is the splitting of spectral lines in **magnetic field**.
 - Bohr's model couldnot explain it.
- **Stark Effect:**
 - **Stark Effect** is the splitting of spectral lines in **electric field**.
 - Bohr's model couldnot explain it.
- Bohr's model couldnot explain the **wave like** character of **electron**.
- It doesnot explain the **relative splitting** of spectral lines.

De Broglie Hypothesis

- **Statement:** Luis Debroglie states that:
 - A moving particle has both **wave like** and **particle like** characters.
 - A moving particle is associated with **waves**.
- These waves are called:
 - Debroglie Waves
 - Matter Waves
- The **wavelength** λ of **matter waves** can be expressed as the same way for photon.

$$\lambda = \frac{h}{p}$$

Calculation of wavelength of an electron

- mass = m
- potential difference for acceleration = V
- velocity of electron = v
- momentum of electron = p
- charge of electron = e
- wavelength = λ

$$\begin{aligned}\lambda &= \frac{h}{p} \\ eV &= \frac{1}{2}mv^2 \\ v &= \sqrt{\frac{2eV}{m}} \\ \lambda &= \frac{h}{m\sqrt{\frac{2eV}{m}}} \\ \lambda &= \frac{h}{\sqrt{2meV}}\end{aligned}$$

-
- The equation for expressing wavelength of **electron** is:

$$\lambda = \frac{h}{\sqrt{2meV}}$$

Heisenberg's uncertainty Principle

Canonically conjugate variables

- **Canonically conjugate** variables are:
 - pair of *physical variables*
 - those which can *describe* the motion of a system.
- Examples of **cannonically** conjugate variables are:
 - **Momentum** and **Position**
 - **Energy** and **Time**
 - **Angular Momentum** and **Angular Position**

Statement

- **Heisenberg's** uncertainty principle states that:
 - The pair of *physical variables describing* the motion of an **atomic system** cannot be measured **precisely** and **simultaneously**.

Mathematical Interpretation

- The interpretation of **canonically paired** physical variables are:

$$\Delta x \Delta p \geq \frac{h}{2\pi}$$

$$\Delta E \Delta t \geq \frac{h}{2\pi}$$

$$\Delta \theta \Delta L \geq \frac{h}{2\pi}$$

Application of Heisenberg's Uncertainty Principle

- **Heisenberg's uncertainty** principle is used to prove that the **electron** cannot exist inside the **nucleus** .
- mass of electron = m
- planck's constant = h
- change in position = Δx
- Δx = magnitude of radius of nucleus
- $\Delta x = 10^{-14}m$
- change in momentum = Δp

$$\begin{aligned}\Delta x \Delta p &\geq \frac{h}{2\pi} \\ \Delta p &= \frac{h}{2\pi \Delta x} \\ \Delta v_x &= \frac{h}{2\pi \Delta x m} \\ \Delta v_x &= \frac{6.62 \times 10^{-34}}{2 \times 3.14 \times 9.1 \times 10^{-31} \times 10^{-14}} \\ \Delta v_x &= 1.16 \times 10^{10} m/s\end{aligned}$$

- This magnitude of velocity is *unattainable* .
- The speed limit in the universe is $3 \times 10^8 m/s$.