

## EXAM of FOUNDATIONS OF COMPUTER SCIENCE

**Written Exam:** exercises on regular and context free languages (grammars, automata, regular expressions, the two pumping lemma). All the exercises contained in chapt.'s 1 and 2 of [S] and in chapt.'s 2-6 of [HU] are examples of what you may find in a written exam.

REMARK: both books contain more material than what we present in this course; so be careful when you choose your exercises therein.

### **Oral exam:**

- To pass the exam (with mark between 18 and 24), you will be required to know:
  - All definitions, examples and theorem statements;
  - The proofs of the following theorems:
    - From Sipser's book [S]:
      - ✓ 1. 1.39 (determ vs nondeterm),
      - ✓ 2. 1.45, 1.47, 1.49 (closures of reg.lang.'s),
      - 3. 1.55 (from reg.expr.'s to finite aut.),
      - 4. 1.70 (pumping lemma reg.lang.),
      - 5. 2.21 (from CFG to PDA),
      - 6. 3.21 (enumerators vs TM),
      - 7. 4.1, 4.2, 4.3, 4.4, 4.5 (decid. of membersh./emptin./equiv. in RL),
      - 8. 4.7, 4.8 (decid. of membership/emptiness in CFL),
      - 9. 5.9 (dec. of membership LBA),
      - 10. 4.22 (decidability vs R.E. and existence of non-RE lang's),
      - 11. 5.1 (halting prob.),
      - 12. 7.20 (NP = polytime verific.),
      - 13. 7.31 (pol.reduc. in P),
      - 14. 7.36 (pol.reduc. in NPC),
      - 15. 7.55 (HAM-PATH < U-HAM-PATH).
    - From Hopcroft&Ullman's book [UL]:
      - 16. Thm 9.1, 9.2 (reg.gramm. vs FA)
    - From Cormen&Leiserson&Rivest's book [CLR]:
      - 17. 34.10 (sat < 3cnfsat),
      - 18. 34.12 (clique < vertex cover),
      - 19. 34.14 (ham cycle < tsp),
      - 20. 35.1 (approx. vertex cover).
- To have a high mark (between 24 and 30), you will be further required to know the proofs of the following theorems:
  - From Sipser's book [S]:
    - 1. 1.60, 1.64 (from DFA to reg.expr.),
    - 2. 2.27 (from PDA to CFG),
    - 3. 2.34 (pumping lemma CFL),
    - 4. 3.13 (multitape vs single tape TM),
    - 5. 3.16 (nondet. vs det. TM),
    - 6. 4.11 (undec. of membership TM),

- 7. 7.8 (complexity of reduc. multitape to single tape),
    - 8. 7.11 (complexity of reduc. nondet to det),
    - 9. 8.25 (PATH is NL-complete).
  - From Hopcroft&Ullman's book [UL]:
    - 10. Thm 9.3 (0 gramm. to TM),
    - 11. Thm 9.5 (CSG in LBA).
  - From Cormen&Leiserson&Rivest's book [CLR]:
    - 12. 34.1 (polynomially related encodings),
    - 13. 34.11 (3cnfsat < clique),
    - 14. 35.2, 35.3 (approx. tsp with/without triangle eq.).
- To pass the exam *cum laude*, you will be asked one of the following proofs:
    - From Sipser's book [S]:
      - 1. 5.10 (undec. emptiness LBA),
      - 2. 5.13 (undec. all  $\Sigma^*$  for CFL),
      - 3. exercise 5.28 (Rice's theor.),
      - 4. 7.37 (Cook Levin),
      - 5. 7.46 (3cnfsat < HAM-PATH),
      - 6. 8.9 (TQBF is PSPACE-complete).
    - From Hopcroft&Ullman's book [UL]:
      - 7. Thm 9.4 (TM to 0 gramm.),
      - 8. Thm 9.6 (LBA to CSG).
    - From Cormen&Leiserson&Rivest's book [CLR]:
      - 9. 34.15 (3cnfsat < subset sum),
      - 10. 35.8 (PTAS for subset sum).