

# Advanced Microeconomics

Prof. Dr. Carsten Helm

## Lecture 15: Incentive contracts with moral hazard and limited liability

Essential reading:

- McMillan, John. Games, Strategies and Managers. Oxford University Press. 1992, chapter 8.
  - Patrick Bolton and Mathias Dewatripont. Contract Theory. MIT Press. 2005, chapter 4.
-

# The role of contracts

- We now extend the analysis by allowing parties to conclude contracts
- such contracts govern a wide variety of relationships
  - contracts for firms and workers that specify wages and other aspects of the employment relationship
  - contracts of homeowners with building contractors
  - contracts of firms with suppliers and customers
  - contracts of nations about trade (WTO) and security (NATO) issues

# The role of contracts

**Definition:** A **contract** is an agreement about behavior that is intended to be enforced.

- A contractual relationship consists of two phases:
  - Contracting phase, in which players set the terms of their contracts
    - Often this is simplified by assuming that one party can make a take-it-or-leave it offer
  - Implementation phase, in which contract is carried out and enforced

- Frederick Taylor (1856-1915)
  - “Hardly a competent worker can be found who does not devote a considerable amount of time to studying just how slowly he can work and still convince his employer that he is going at a good pace.”
- moral hazard due to
  - Asymmetric information and
  - divergences in the objective functions of the actors

# Moral hazard: some examples

- field sales employee
  - Employer wishes that field sales employee works hard
  - Employee wants to have more (and longer) breaks and monitoring is difficult
- Borrowed capital
  - If owners have limited liability in case of bankruptcy, a firm may invest in overly risky projects
  - the bank wishes a more conservative investment policy
- Car insurance
  - After purchasing a theft insurance, the owner is less careful
  - The insurance firm wants him to take more care
  - 30% of car accidents with fully comprehensive insurance end up in court due to alleged gross negligence of the insured

# Trade-offs in incentive schemes

- Sometimes the principal can reduce trade-offs through the selection of a suitable agent
  - Family businesses
- if there are conflicts of objectives, often incentives schemes are used
  - In the standard principal-agent model, incentive schemes will be modelled as **monetary rewards**
  - e.g., parcel carriers are paid per parcel
- Lemieux et al. (2009) report for the fraction of labor contracts with incentive components by the end of the 1990s
  - In the US 30% for craftsmen, 78% for sales workers, average of 45% across all jobs
  - In Europe ranging from 10 to 15% in some Mediterranean countries to more than 30% for Nordic countries

- **Principal-Agent model with moral hazard**

- Principal-agent: one party – the principal – hires another party – the agent – to work on a project on her behalf
- moral hazard: the agent's effort is not verifiable
  - hence parties can not write an externally enforced contract about this effort
  - standard assumption: only the outcome of the project is verifiable, which depends not only on effort but also on random events

- Model:
  - Risk neutral agent chooses effort  $e \in [0,1]$
  - Effort costs:  $0,5e^2$
  - alternative income (outside option):  $A$
  - Efforts of the agent produce output  $Q = e + u$
  - $u$  is a random variable with expected value  $E[u] = 0$
  - $e$  and  $u$  cannot be observed by the principal, only  $Q$
  - Stage 1: risk-neutral principal offers the agent a linear incentive contract with payment  $p = s + rQ$
  - Stage 2: Agent decides on acceptance
  - Stage 3: Agent chooses effort; output and payments result
- Note: because contract is agreed to ex-ante, there is no strategic move after the agent has chosen his non-observable effort
  - Hence this is a simple dynamic game that can be solved by backwards induction for subgame perfect equilibrium

## Linear incentive contracts with risk neutral actors

- Solving the game through backward induction
- agent's expected net return on effort :
- The agent's objective function is thus:
  - $r$  represents strength of the incentive contract
    - $r = 0$ : the agent makes no effort
    - $r = 1$ : the agent bears full responsibility for his activity
  - expected net income of the agent (as  $e = r$ ):

## Linear incentive contracts with risk neutral actors

- Solving the game through backward induction
- agent's expected net return on effort :

$$s + r \cdot \underbrace{E(Q|e)}_{e+E(u)=e} - 0,5e^2$$

- The agent's objective function is thus:

$$\max_e s + re - \frac{e^2}{2} \quad \Rightarrow \text{FOC: } r - e = 0 \text{ or } e = r$$

- $r$  represents strength of the incentive contract
  - $r = 0$ : the agent makes no effort
  - $r = 1$ : the agent bears full responsibility for his activity
- expected net income of the agent (as  $e = r$ ):  $\pi = s + 0.5r^2$

## Linear incentive contracts with risk neutral actors

- participation constraint of the agent:  $\pi = s + 0.5r^2 \geq A$
- principal maximises  $\Pi =$ 
  - principal keeps  $s$  as small as possible. Why?
    - i.e. the participation condition binds:
- by substitution, the maximisation problem simplifies to
- In the optimal incentive contract, the agent thus receives the entire output

## Linear incentive contracts with risk neutral actors

- participation constraint of the agent:  $\pi = s + 0.5r^2 \geq A$
- principal maximises  $\Pi = E(Q) - [s + rE(Q)]$ :

$$\max_{r,s} r - (s + r^2) \quad \text{s.t. } s + 0.5r^2 \geq A$$

- principal keeps  $s$  as small as possible. Why?
  - i.e. the participation condition binds:  $s = A - 0.5r^2$
- by substitution, the maximisation problem simplifies to

$$\begin{aligned} & \max_r r - A - 0.5r^2 \\ \Rightarrow \text{FOC: } & r^* = 1, \quad s^* = A - 0.5, \quad e^* = 1 \end{aligned}$$

- If  $s^* < 0$  this is called „franchise contract“: agent pays a fixed fee and in return gets all of the realized benefits

## Pareto-efficient solution

- Without the moral hazard problem, the principal can set the desired effort level  $e$  and wage  $w$
- Profit maximisation of the principal:
- the participation condition binds. Why?
- That is, in this example, the solution is Pareto-efficient despite the moral hazard problem. Why?

## Pareto-efficient solution

- Without the moral hazard problem, the principal can set the desired effort level  $e$  and wage  $w$
- Profit maximisation of the principal:

$$\max_{e,w} e - w \quad \text{s.t.} \quad w - 0.5e^2 \geq A$$

- the participation condition binds. Why?

$$w = A + 0.5e^2 \Rightarrow \begin{aligned} & \max_e e - A - 0.5e^2 \\ & \text{FOC: } e^* = 1, w^* = A + 0.5 \end{aligned}$$

- That is, in this example, the solution is Pareto-efficient despite the moral hazard problem. Why?

# Pareto-efficient solution

- Note: Even in the situation without a moral hazard problem, the principal must give incentives to the agent:

- The incentive structure is trivial:  $w = \begin{cases} 0 & e < 1 \\ w^* & e \geq 1 \end{cases}$

## Bonus contract versus linear incentive contracts

- Above we have considered a linear incentive contract with payment  $p = s + rQ$ 
  - Fixed payment  $s$  plus bonus  $r$  per unit of output
- In practice, incentive contracts often provide that a bonus  $\beta$  is paid if a target  $Q^*$  is met, yielding wage payment

$$w = \begin{cases} \alpha & Q < Q^* \\ \alpha + \beta & Q \geq Q^* \end{cases}$$

- This bonus contract can be designed such that it is equivalent to linear incentive contract (i.e., provides same incentives)
  - Note: If the random variable  $u$  is equally distributed over the interval  $[a, b]$ , the bonus contract that is equivalent above linear incentive contract has

$$\alpha = s + (Q - b)r \quad \text{and} \quad \beta = (b - a)r$$

# Non-monetary incentive schemes

- In the real world, often non-monetary incentives are used
  - Promotion (due to a good evaluation)
  - Layoff (due to a bad evaluation)
  - „Perks“, e.g. bigger office, business car etc. (due to a good evaluation)
- Also such non-monetary incentives can be evaluated monetarily
  - 2 examples on next slide

# Non-monetary incentive schemes

- Tombola
  - In the 1940s a company reduced days of absence by conducting a daily tombola
  - Winners got goods that were difficult to obtain during the war
  - Workers had to be present
- Bonus points in a car company
  - One bonus point for each day being present
  - Points could be converted into prizes (e.g. plane tickets to a popular vacation destination)
  - Points were given not to the workers, but to their spouses
  - The involvement of spouses into the control of the workers turned out to be very effective
- Reference: R.G. Ehrenberg and Robert S. Smith, 1988, Modern Labor Economics, Scott Foresman and Company, Glenview Illinois, p.417

# Moral hazard and Pareto efficiency

---

- The encouraging result that incentive contracts may solve the moral hazard problem and lead to efficient solution was based on some implicit assumptions
- One of them is that the agent has unlimited liability
  - Example 1: investment bankers often get high boni if their investments are profitable
    - but they are held responsible for losses to a much smaller extent
    - Hence they have an incentive to take risks that are too high
  - General problem behind example: „gains are privatized, losses are socialized“
    - Reflects limited liability for losses

## Linear incentive contracts with payment constrained agents

- Agents can often make no – or only limited – payments to the principal
  - e.g. because their assets are limited
- we therefore add a payment restriction to the model:  $s \geq 0$
- Problem of the principal:

## Linear incentive contracts with payment constrained agents

- Agents can often make no – or only limited – payments to the principal
  - e.g. because their assets are limited
- we therefore add a payment restriction to the model:  $s \geq 0$
- Problem of the principal:

$$\max_{r,s} e - (s + re) \quad \text{s.t.}$$

$$e = \arg \max_{\tilde{e}} s + r\tilde{e} - \frac{\tilde{e}^2}{2} \quad (\text{IC: incentive constraint})$$

$$s + re - \frac{e^2}{2} \geq 0 \quad (\text{PC: participation constraint})$$

$$s \geq 0 \quad (\text{LL: payment constraint})$$

## Linear incentive contracts with payment constrained actors

- Analysis of the incentive constraint:

$$\max_e s + re - \frac{e^2}{2} \quad \Rightarrow \text{FOC:}$$

- Substitution into the participation and payment constraint:

$$s + re - 0.5e^2 = \quad (\text{PC})$$

$$s \geq 0 \quad (\text{LL})$$

- assuming PC binds. Then  $s =$   $\Rightarrow$  Violation of (LL)
- $\Rightarrow$  PC does not bind
- $\Rightarrow$  LL binds
  - otherwise the principal could reduce  $s$  and thus increase his profits

## Linear incentive contracts with payment constrained actors

- Analysis of the incentive constraint:

$$\max_e s + re - \frac{e^2}{2} \quad \Rightarrow \text{FOC: } r - e = 0 \quad \text{or} \quad e = r$$

- Substitution into the participation and payment constraint:

$$s + re - 0.5e^2 = s + 0.5r^2 \geq 0 \quad (\text{PC})$$

$$s \geq 0 \quad (\text{LL})$$

- assuming PC binds. Then  $s = -0.5r^2 < 0 \Rightarrow$  Violation of (LL)
  - ⇒ PC does not bind
  - ⇒ LL binds
    - otherwise the principal could reduce  $s$  and thus increase his profits

## Linear incentive contracts with payment constrained actors

- from (IC) and (LL) it follows:  $e = r$  and  $s = 0$
- Substitution into problem of principal,  $\max_{r,s,e} e - (s + re)$ , results in
- the incentive parameter is thus only half as high as in the efficient solution without moral hazard ( $r^* = 1$ )

## Linear incentive contracts with payment constrained actors

- from (IC) and (LL) it follows:  $e = r$  and  $s = 0$
- Substitution into problem of principal,  $\max_{r,s,e} e - (s + re)$ , results in

$$\max_r r - r^2 \quad \text{BeO: } 1 - 2r = 0 \quad \Rightarrow \quad r^{**} = 0,5$$

- the incentive parameter is thus only half as high as in the solution without limited liability ( $r^* = 1$ )

# Linear incentive contracts with payment constrained actors

- Intuition:

- Without wealth constraint, the principal sets
  - $r = 1$  to set optimal effort incentives
  - appropriates the profits from the P-A relationship through a negative fixum  $s$
- With wealth constraint, this is no longer possible and the principal faces a trade-off:
  - Appropriation of profits requires reduction of  $r$
  - However, this reduces the incentives of the agent
- the principal balances these effects and sets  $r = 0,5$ 
  - the agent therefore receives a rent
  - i.e. his participation condition does not bind

# Linear incentive contracts with payment constrained actors

- Intuition:
  - Without wealth constraint, the principal sets
    - $r = 1$  to set optimal effort incentives
    - appropriates the profits from the P-A relationship through a negative fixum  $s$
  - With wealth constraint, this is no longer possible and the principal faces a trade-off:
    - Appropriation of profits requires reduction of  $r$
    - However, this reduces the incentives of the agent
  - the principal balances these effects and sets  $r = 0,5$ 
    - the agent therefore receives a rent

$$s + re - 0.5e^2 = 0.5r^2 = 1/8 > 0$$

- i.e. his participation condition does not bind

## Linear incentive contracts with payment constrained actors

- Example: Waitresses at the Oktoberfest receive
  - no fixed salary
  - 9% of the revenue they collect
  - they are usually only employed during the Oktoberfest, which lasts 18 days
    - due to the short duration of the contract, a good incentive structure is particularly important
- Source: Ray Rees (Royal Economic Society Newsletter, Issue 142, 2008)