- There are 12 points possible on this proficiency: one point per problem with no partial credit.
- You have 30 minutes to complete this proficiency.
- No aids (book, calculator, etc.) are permitted.
- You do **not** need to simplify your expressions.
- Your final answers should start with f'(x) = dy/dx = 0 something similar.
- 1. [12 points] Compute the derivatives of the following functions.

a.
$$f(x) = \frac{x^e}{5} + 7e^x + \sqrt{5} = \frac{1}{5} x^e + 7e^x + \sqrt{5}$$

$$f'(x) = \frac{e}{5} x^{e-1} + 7e^{x}$$

- · power rule
- · constents

b.
$$f(t) = \frac{t^3 - t^{\frac{3}{2}} + 1}{t} = t^2 - t^{\frac{1}{2}} + t^{-1}$$

- · algebra makes it easy

c.
$$f(x) = (x^4 - 2x) \tan(x)$$

$$f'(x) = (4x^3 - 2) \tan(x) + (x^4 - 2x) \sec^2(x)$$
 • product rule of trigfon.

- trigfen.

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PRACTICE

d.
$$f(x) = \frac{1 + e^{-3x}}{\cos(3x)}$$

$$f'(x) = [\cos(3x)][0 + -3e^{-3x}] - [1 + e^{-3x}][-3\sin(3x)]$$

$$[\cos(3x)]^{2}$$

· quotient rule w/ chain rule inside

e.
$$f(x) = \frac{1}{\sqrt{x}} + e^{\frac{1}{x}} + \sec(x) = \frac{-1/2}{x} + \frac{2x^{1}}{x} + \sec(x)$$

$$f'(x) = -\frac{1}{2}x^{-3/2} + (-2x^{-2})e^{2x^{-1}} + sec(x) + an(x)$$

f. $f(t) = \tan^{-1}(2t) + t \ln(at + b)$ where a and b are a fixed constants

$$f'(t) = 1 \cdot \ln(at+b) + t \cdot \left(\frac{1}{at+b}\right)$$
 (a)

$$f'(t) = \ln(at+b) + at$$

$$at+b$$

- · derivatives with parametus.
- · product rule w/ chain rule inside.
- · natural log.

g.
$$f(x) = (\sin x)(\ln(x^2 + 1))$$

$$f'(x) = \cos(x) \cdot \ln(x^2 + 1) + \sin(x) \cdot \left(\frac{2x}{x^2 + 1}\right)$$

h.
$$f(z) = \cot(z) + \sin^{-1}(\sqrt{z}) = \cot(z) + \operatorname{arcsin}(z^2)$$

$$f'(z) = -\csc^2(z) + \frac{1}{\sqrt{1 - (z'^2)^2}} (\frac{1}{2}z^{-1/2})$$

$$=-\csc^2(z)+\frac{1}{2\sqrt{z}\sqrt{1-z}}$$

i.
$$f(t) = \ln(\tan(1+t^2))$$

$$f'(t) = \frac{1}{\tan(1+t^2)} \cdot \left(\operatorname{Sec}^2(1+t^2) \right) (2t)$$

$$= \frac{2t \sec^2(1+t^2)}{\tan(1+t^2)}$$

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j.
$$f(x) = \sin^5(e^{-x} + x) = \left(\sin(e^{-x} + x) \right)$$

$$f'(x) = 5(\sin(e^{-x}+x))\cos(e^{-x}+x)\cdot(-1e^{-x}+1)$$

$$= 5(1-\bar{e}^{x})\cos(\bar{e}^{-x}+x)(\sin(\bar{e}^{-x}+x))$$

PRACTICE

· Chain rule inside chain rule

. chain rule w/

· chain rule uf trig fcn.

k.
$$f(x) = \frac{1}{4x^2} + \left(\frac{3-x}{2}\right)^2 = \frac{1}{4} x^{-2} + \left(\frac{3}{2} - \frac{1}{2} \times\right)^2$$

$$f'(x) = \frac{1}{4}(-2)x^3 + 2(\frac{3}{2} - \frac{1}{2}x)(-\frac{1}{2})$$

$$= \frac{-1}{2} \times 3 - \left(\frac{3}{2} - \frac{1}{2} \times\right)$$

the ability
to manage/
recognize
constants.
chain rule

I. Compute dy/dx if $e^y + x^2 = 1 - xy$. You must solve for dy/dx.

$$e^{y} \cdot dy + 2x = 0 - 1 \cdot y - x \cdot dy$$

$$\frac{dy}{dx}(e^{y}+x)=-2x-y$$

$$\frac{dy}{dx} = \frac{-2x - y}{e^y + x}$$

UAF Calculus I