

SECTION 3.4 CHAIN RULE (DAY 2)  
SECTION 3.5 INTRO

1. Evaluate the derivatives.

(a)  $H(x) = \sqrt[3]{\frac{4-2x}{5}}$

(b)  $y = e^{\sec \theta}$

(c)  $f(x) = \frac{8}{x^2 + \sin(x)}$

(d)  $x(t) = \frac{1}{\sqrt{2}} \tan\left(\frac{\pi}{6} - x\right)$

(e)  $y = \frac{xe^{-\pi x^2/10}}{100}$

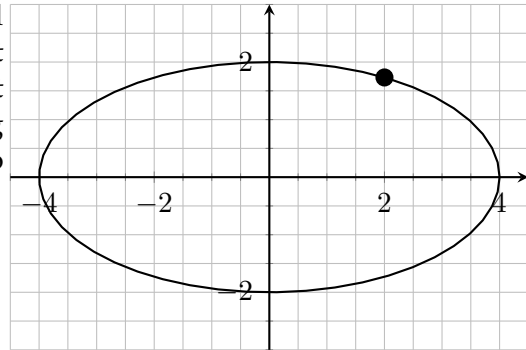
(f)  $y = \frac{e^2 - x}{5 + \cos(5x)}$

(g)  $F(x) = (2re^{rx} + n)^p$  (Assume  $r$ ,  $n$ , and  $p$  are fixed constants.)

2. (a) Complete the **rule**:  $\frac{d}{dx}(b^x) = \underline{\hspace{2cm}}$   
 (b) Determine the derivative of  $f(x) = 2^x - x^3$

3. Consider the curve  $x^2 + 4y^2 = 16$ .

- (a) Think of  $y$  as being some function of  $x$ , and differentiate everything in sight with respect to  $x$ . Your answer should be an equation that contains  $x$ ,  $y$ , and  $y'$ . Because we are thinking of  $y = g(x)$ ,  $\frac{d}{dx}(y) = \frac{dy}{dx}$  (or  $y'$ ). You need to use the chain rule to determine  $\frac{d}{dx}(y^2)$ .



Your first step:

$$\frac{d}{dx}(x^2 + 4y^2) = \frac{d}{dx}(16) \implies$$

- (b) Solve your previous step for  $y'$ .
- (c) Determine the slope of the tangent line at the point  $(2, \sqrt{3})$  by substituting  $x = 2$ ,  $y = \sqrt{3}$  into your equation for  $y'$ . Draw the tangent line at the point indicated on the graph. Is your computation plausible?

Write the equation of the tangent line at  $(1, \sqrt{3})$ :  $\underline{\hspace{2cm}}$