Name: Key

• There are 12 points possible on this proficiency, one point per problem. No partial credit will be given.

- You have one hour to complete this proficiency.
- · No aids (book, calculator, etc.) are permitted.
- · You do not need to simplify your expressions.
- Your final answers must start with $f'(x) = \frac{dy}{dx} = 0$, or similar.
- Draw a box around your final answer.
- 1. [12 points] Compute the derivatives of the following functions.

a.
$$f(x) = 4\sin^{-1}(3x^3)$$

$$f'(x) = \frac{4}{\sqrt{1-(3x^3)^2}} \cdot 9x^2$$

b.
$$f(x) = 3\sin(x)\cos(x)$$

$$f'(x) = 3(\cos x \cdot \cos x + \sin x (-\sin x))$$

c.
$$f(x) = \frac{\sqrt{x}}{5} - \frac{5}{\sqrt{x}} + \frac{\sqrt{3}}{4}$$

$$f'(x) = \frac{1}{5} \cdot \frac{1}{2\sqrt{x}} - 5 \cdot \frac{-1}{2\sqrt{x^2}}$$

$$\mathbf{d.} \ f(x) = \frac{\ln(x)}{\tan(x)}$$

$$f'(x) = \frac{\frac{1}{x} \cdot t_{anx} - L_{nx} \cdot sec^{2}x}{t_{an}^{2}x}$$

$$e. y = 3\csc(e^x)$$

$$\frac{dx}{dx} = -3\csc(e^x)\cot(e^x)\cdot e^x$$

f.
$$y = 6^x - \log_6(x)$$

$$\frac{dy}{dx} = 6^* Ln6 - \frac{1}{x Ln6}$$

g.
$$y = (x^{0.2} + \sec(x))^{-2/3}$$

$$\frac{dy}{dx} = -\frac{2}{3} \left(x^{0.2} + \sec x \right)^{-\frac{5}{3}} \cdot \left(0.2 x^{-0.8} + \sec x \tan x \right)$$

h.
$$f(x) = \frac{\cos(\pi/x)}{x^2}$$

$$f'(x) = \frac{-\sin(\frac{\pi}{x}) \cdot (-\pi x^{-2}) \cdot \chi^2 - \cos(\frac{\pi}{x}) \cdot 2x}{(\chi^2)^2}$$

i.
$$f(x) = \left(x^4 + \frac{1}{x} + e^5\right)^3$$

$$f(x) = 3(x^4 + \frac{1}{x} + e^5)^2 \cdot (4x^3 - x^{-2})$$

j.
$$f(x) = \ln\left(\frac{x^2 e^x}{12x}\right) = 2 \ln x + x - \ln 2 - \ln x$$

$$f'(x) = \frac{2}{x} + 1 - \frac{1}{x}$$

k.
$$f(x) = \frac{\sin(5)}{\sqrt[3]{\sin(x)}} = \sin(5) \cdot (\sin x)^{-\frac{1}{3}}$$

$$f'(x) = -\frac{1}{3} \sin(5) \cdot (\sin x)^{-\frac{4}{3}} \cdot (\cos x)$$

I. Find $\frac{dy}{dx}$ for the equation $e^x - e^y = 2\sin(xy)$. You must solve for $\frac{dy}{dx}$.

Find
$$\frac{dy}{dx}$$
 for the equation $e^{x} - e^{y} = 2\sin(xy)$. You must solve for $\frac{dy}{dx}$.

$$\frac{d}{dx} \left[e^{x} - e^{y} \right] = \frac{d}{dx} \left[2\sin(xy) \right] \Rightarrow e^{x} - e^{y} \cdot \frac{dy}{dx} = 2\cos(xy) \cdot \left(y + x \frac{dy}{dx} \right)$$

$$\Rightarrow e^{x} - 2\cos(xy) \cdot y = e^{y} \cdot \frac{dy}{dx} + 2\cos(xy) \cdot \frac{dy}{dx}$$

$$\Rightarrow e^{x} - 2\cos(xy) \cdot y = e^{y} \cdot \frac{dy}{dx} + 2\cos(xy) \cdot \frac{dy}{dx}$$

$$\Rightarrow e^{x} - 2\cos(xy) \cdot y = \frac{dy}{dx}$$

$$\Rightarrow e^{x} - 2\cos(xy) \cdot y = \frac{dy}{dx}$$