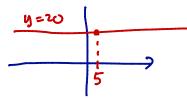
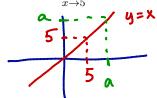
1. Let's use some concrete examples to figure out some rules.

(a)
$$\lim_{x\to 5} 20 = 20$$



(b)
$$\lim_{x \to 5} x = 5$$



(c)
$$\lim_{x\to 5} (x+20) = 5+20 = 25$$

5 70

(d)
$$\lim_{x \to \pi/2} x \sin(x) = \frac{\pi}{2} \cdot \operatorname{Sin}(\frac{\pi}{2})$$
$$= \frac{\pi}{2} \cdot 1 = \frac{\pi}{2}$$

(e)
$$\lim_{x \to \pi/2} \frac{100(x \sin(x))}{\sqrt{100 \text{ T}}} = \frac{100 \cdot \pi}{2}$$

= 50 T

The limit of a constant is constant.

$$|_{im} x = a$$

the limit of f(x)=X is evaluated by plugging in

$$\lim_{x\to a} \left[f(x) + g(x)\right] = \lim_{x\to a} f(x) + \lim_{x\to a} g(x)$$

$$\lim_{x\to a} f(x) + g(x) = \lim_{x\to a} f(x) + \lim_{x\to a} g(x)$$
The limit of a sum is the sum of limits.

The limit will pass through a sum.

$$\lim_{x \to a} \left[f(x) \cdot g(x) \right] = \left(\lim_{x \to a} f(x) \right) \left(\lim_{x \to a} g(x) \right)$$

The limit will pass through a product

$$\lim_{x\to a} \left[c f(x) \right] = c \cdot \left(\lim_{x\to a} f(x) \right)$$

A (multiplied) constant can be moved outside the limit.

2. ALL rules are formally listed in Theorem 2.5 in your textbook. The nutshell version of these rules

we can evaluate the limit of a function piece-by-piece provided the resulting number makes sense.

what bad thing could happen?

$$\frac{E \times \lim_{x \to 2} \frac{x^2 - 4}{x - 2} = \lim_{x \to 2} \frac{x^2 - 4}{\lim_{x \to 2} x - 2} = 0 \quad \text{whoh...}}{\lim_{x \to 2} x - 2}$$

What happens when the rules don't apply?

If we get a zero in the denominator, try some algebra.

3. lesson: factor and cancel

$$\lim_{t \to 2} \frac{t^2 - 4}{t - 2} = \lim_{t \to 2} \frac{(t + 2)(t - 2)}{t - 2} = \lim_{t \to 2} t + 2 = 2 + 2 = 4$$
go is bad.

Are you sure this is fair?

4. lesson: Get a common denominator.

$$\lim_{x\to 2} \frac{\frac{1}{4} - \frac{1}{2+x}}{\frac{1}{x-2}} = \lim_{X\to 2} \left(\frac{1}{x-2}\right) \left(\frac{1}{4} - \frac{1}{2+x}\right) = \lim_{X\to 2} \left(\frac{1}{x-2}\right) \left(\frac{2+x-4}{4(2+x)}\right) = *$$

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$$x = \lim_{x \to 2} \left(\frac{1}{x-2} \right) \left(\frac{x-2}{4(2+x)} \right) = \lim_{x \to 2} \frac{1}{4(2+x)} = \frac{1}{4(2+x)} = \frac{1}{16}$$

- -> How are the letters "a" and "h" different?
 - 5. lesson: Rationalize.

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$$\frac{\sqrt{a-\sqrt{a+h}}}{\ln h} = \lim_{h \to 0} \frac{a - (a+h)}{\ln a + \sqrt{a+h}} = \lim_{h \to 0} \frac{a - (a+h)}{\ln a + \sqrt{a+h}} = \lim_{h \to 0} \frac{-h}{\ln a + \sqrt{a+h}}$$
use $(c-d)(c+d)$

$$= c^2 - d^2$$