

SECTION 5.1: SEQUENCES

1. To know by the end of section 5.1:

- (a) what an infinite sequence is
- (b) how to read and use sequence notation
- (c) what it means to "Find a formula for the n th term", and how to find it
- (d) what it means for a sequence to converge or diverge
- (e) different limit techniques for determining if a sequence converges or diverges, including L'Hopital's rule
- (f) what $n!$ means
- (g) terms for describing a sequence: bounded, monotone, increasing, decreasing

2. For each sequence below, write the first 5 terms and graph them.

(a) $\left\{ \frac{n+2}{2n} \right\}_{n=1}^{\infty}$

(b) $a_n = 3 \left(\frac{-1}{2} \right)^{n-1}$ for $n \geq 1$

(c) $a_1 = 5$ and $a_n = 2a_{n-1} + 1$

3. Find a formula for 2 (c).

4. Definition: The symbol $n!$ or “n factorial” means

and $0! =$

5. Find the limit of each of the following sequences or show that it diverges.

(a) $\left\{ \pi + \frac{100}{n} \right\}$

(b) $a_n = \frac{3^n}{n!}$

(c) $\left\{ \frac{100n^2 + \sqrt{n}}{n - 3n^2} \right\}$

(d) $\left\{ \frac{n^2}{10^n} \right\}$

(e) $a_n = \left(1 + \frac{1}{n} \right)^n$

Now, go back to the examples in 2. Find the limit of each or show that it diverges.