

1. In earlier notes, we found seven possible coalitions with players P_1 , P_2 , and P_3 .
 - (a) List them again below.
 - (b) Suppose the system has a fourth player, P_4 . Determine how many coalitions in this case. Try to answer the question without actually listing all of them.
 - (c) What if there is a fifth player, P_5 ?
 - (d) Make a conjecture about how many coalitions are possible with n players, $P_1, P_2, P_3, \dots, P_n$. How would you argue that your count is correct?
 - (e) What does this suggest about the mechanics of calculating the Banzhaf Power Index for a weighted voting system with a lot of players?

2. What is the Banzhaf Power Index

(a) when there is a dictator

(b) for a dummy player

(c) if all players have an equal number of votes

(d) if player P_1 has double the number of votes as player P_2 ?