

1. Review of Voting Methods so far

(a) Plurality Voting

Whoever gets the most votes wins

- winner might have much less than a majority
- can fail Condorcet

(b) Instant Runoff Voting (IRV) or Ranked Choice Voting (RCV)

- Winner is preferred by a majority
- if no majority, eliminate the candidate with the fewest 1st choice votes, and shift those votes to their next choice
- repeat until someone has a majority
 - can fail Condorcet, monotonicity

2. Borda Count

(a) Method:

Assign 1 point to last place,
2 pts to next-to-last place, etc.

Sum all the points
Winner has the most points

(b) example:

	# votes	3	4	2	1	1
4 pts	1st choice	A	B	C	C	D
3 pts	2nd choice	C	C	D	B	C
2 pts	3rd choice	B	D	B	A	B
1 pt	4th choice	D	A	A	D	A

Plurality: $A = 3$
 $B = 4$ ← plurality winner
 $C = 3$
 $D = 1$

$$A: 3(4) + 4(1) + 2(1) + 1(2) + 1(1) = 12 + 4 + 2 + 2 + 1 = 21$$

$$B: 3(2) + 4(4) + 2(2) + 1(3) + 1(2) = 6 + 16 + 4 + 3 + 2 = 31$$

$$C: 3(3) + 4(3) + 2(4) + 1(4) + 1(3) = 9 + 12 + 8 + 4 + 3 = 36$$

$$D: 3(1) + 4(2) + 2(3) + 1(1) + 1(4) = 3 + 8 + 6 + 1 + 4 = 22$$

C wins, with 36 points! (Note B was the plurality winner)

3. Copeland's Method

(a) Method:

Do all head-to-head matchups.

Assign 1 point to each winner

 $\frac{1}{2}$ pt to both candidates if there's a tie.

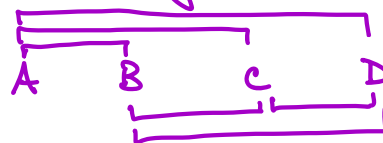
Sum all the points. Winner has the most points.

* guarantees winner is Condorcet winner, if one exists.

(b) example:

# votes	3	4	2	1	1
1st choice	A	B	C	C	D
2nd choice	C	C	D	B	C
3rd choice	B	D	B	A	B
4th choice	D	A	A	D	A

How many matches?

4 candidates
6 matchesA vs B

$A = 3$

$B = 4 + 2 + 1 + 1 = 8$

B wins

A vs C

$A = 3$

$C = 4 + 2 + 1 + 1 = 8$

C wins

A vs D

$A = 3 + 1 = 4$

$D = 4 + 2 + 1 = 7$

D wins

B vs D

$B = 3 + 4 + 1 = 8$

$D = 2 + 1 = 3$

B wins

B vs C

$B = 4$

$C = 3 + 2 + 1 + 1 = 7$

C wins

C vs D

$C = 3 + 4 + 2 + 1 = 10$

$D = 1$

C wins

Total points (= #wins)

$A = 0$

$B = 2$

$C = 3$

$D = 1$

← C wins under Copeland's method.