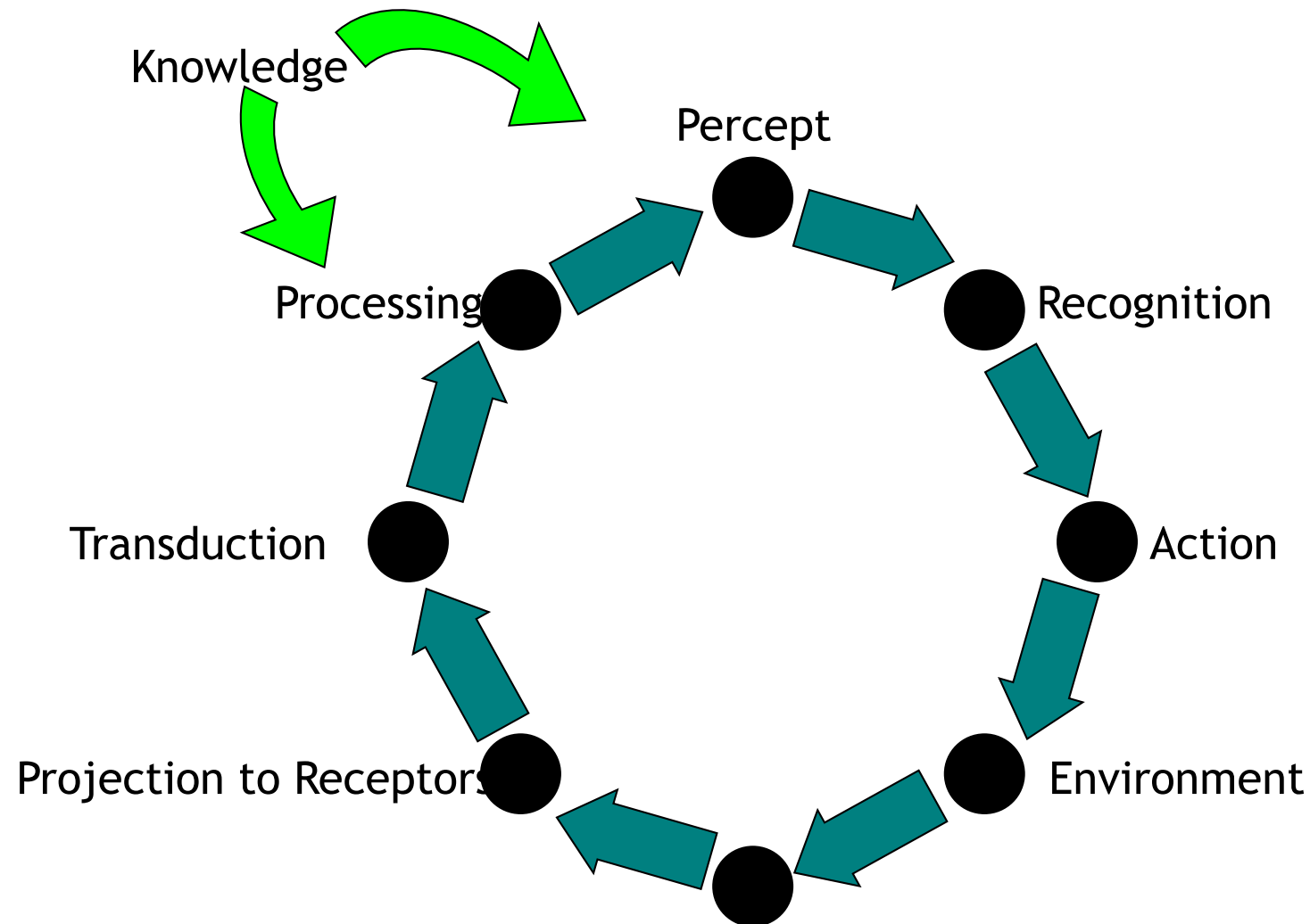


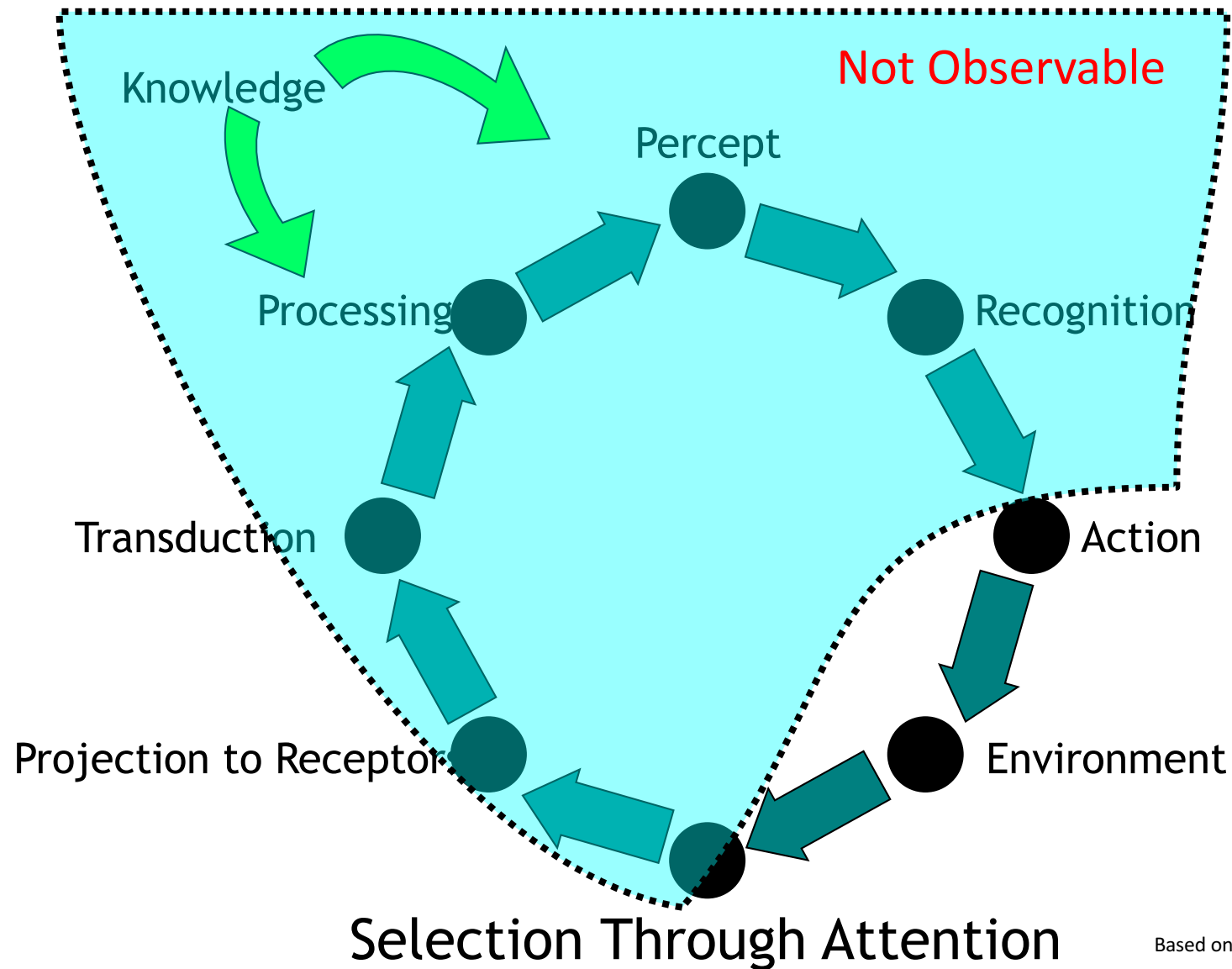
# Why is this hard?



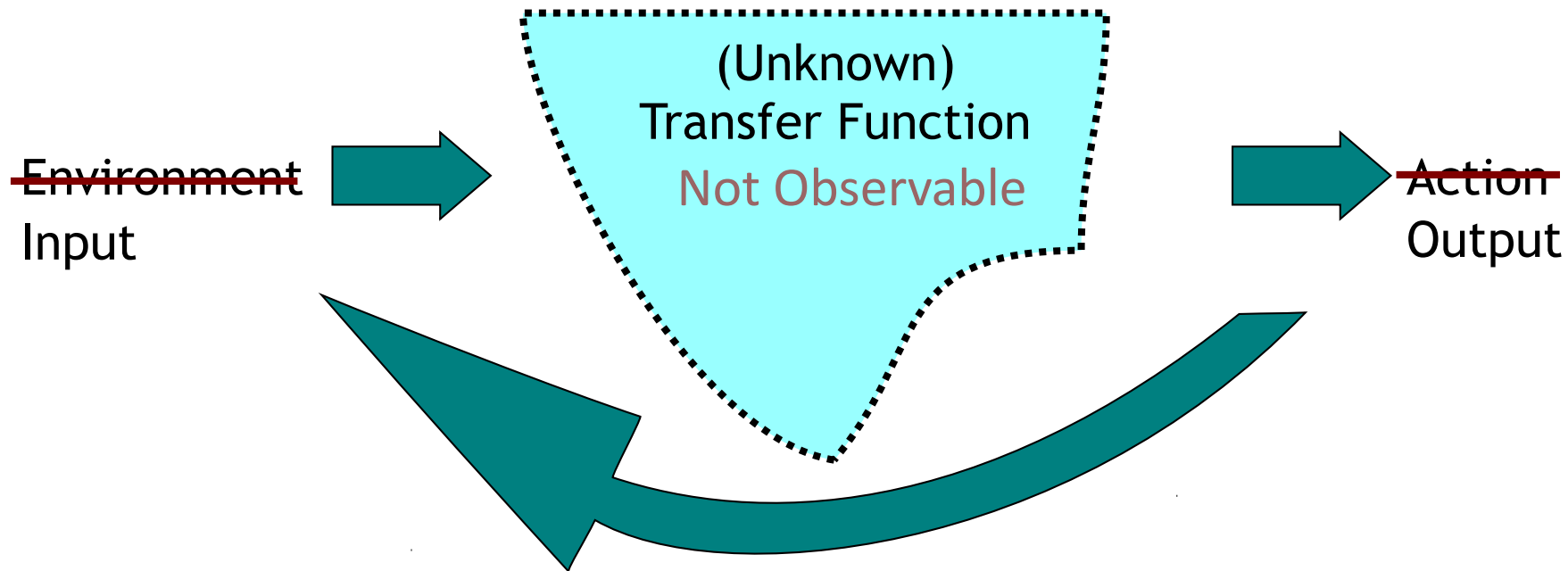
Selection Through Attention

Based on B. Goldstein 2002

# Why is this hard?



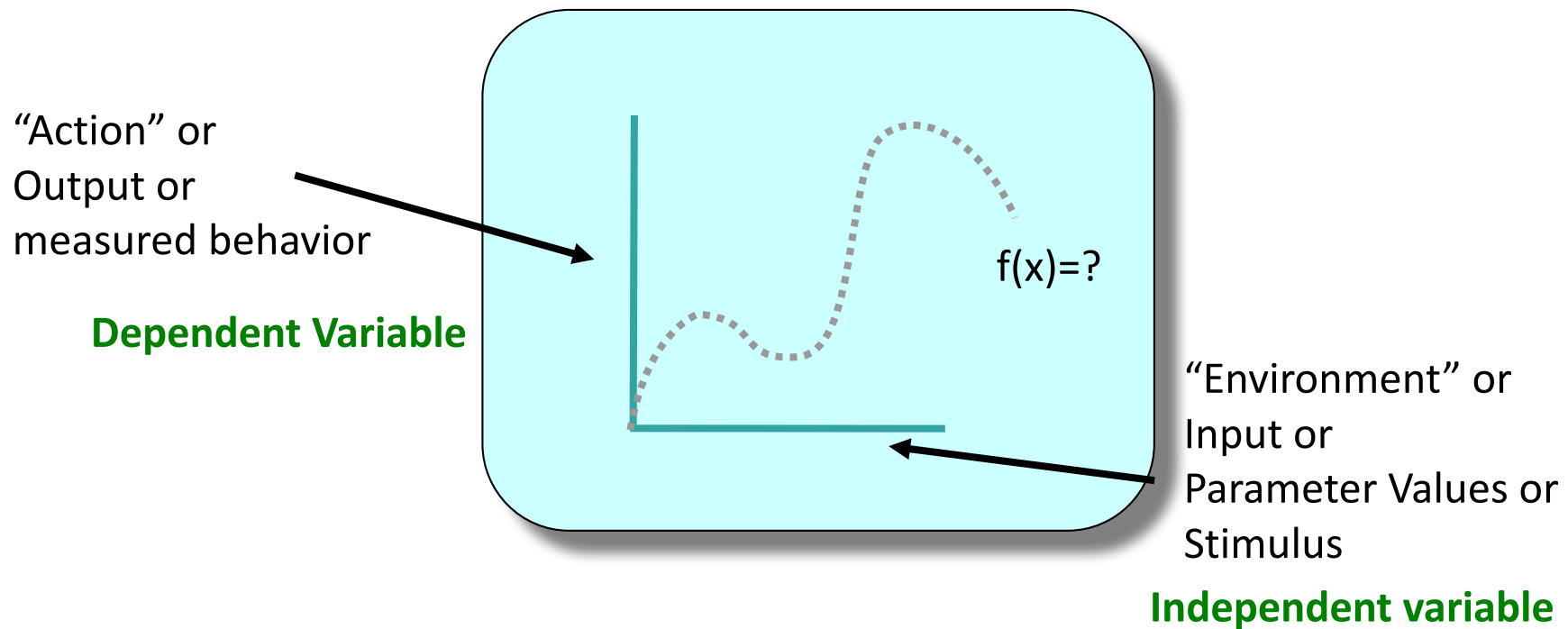
# The classic **black box**



Dynamically adaptable, non-linear system  
with feedback  
(and probably feed-forward...)

# A different (black) box

**Goal:** Estimate an unknown function



**Method: ??**

# Degree of Control To interfere or not?



- No control: Observational Research
  - examine things as they happen
  - often uses correlational analyses
  - Examples: Astronomy, Anthropology, Zoology, ...
- Complete control: Experimental or controlled research.
  - repeatedly and reliably produce a specific event in order to examine it
  - can talk about causation
  - Examples: Physics, Chemistry, Perceptual Psychology,...

# Degree of Control

## Type of experimental studies

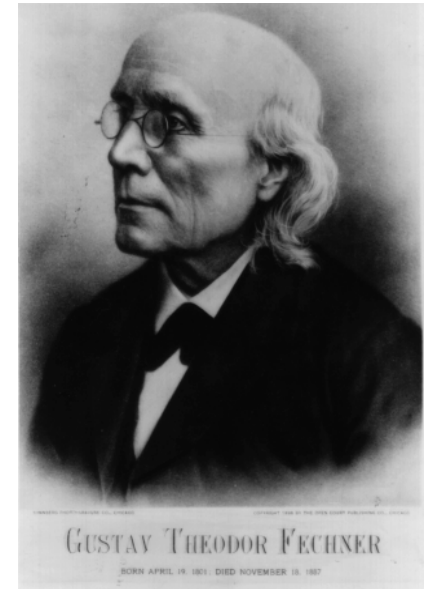


- Controlled experiment:
  - Examines more general questions (about the underlying parameters of the system and its influence on the participant)
  - Requires control over
    - what is shown (stimuli)
    - how and when the stimuli are shown (experimental procedure)
    - what the participants should do (task)

# Degree of Control

## Type of experimental studies

- An example of controlled experimental methodology in psychology is Psychophysics:
  - Set of experimental methodology invented by Gustav Fechner in 1860 (and since extended by lots of people).
  - Provides mathematical descriptions of the functional relationship between variations in the physical world and the resulting variations in the psychological (or perceptual) world.
  - Requires very fine control over
    - what is shown (stimuli)
    - how and when the stimuli are shown (experimental procedure)
    - what the participants should do (task)



# Degree of Control



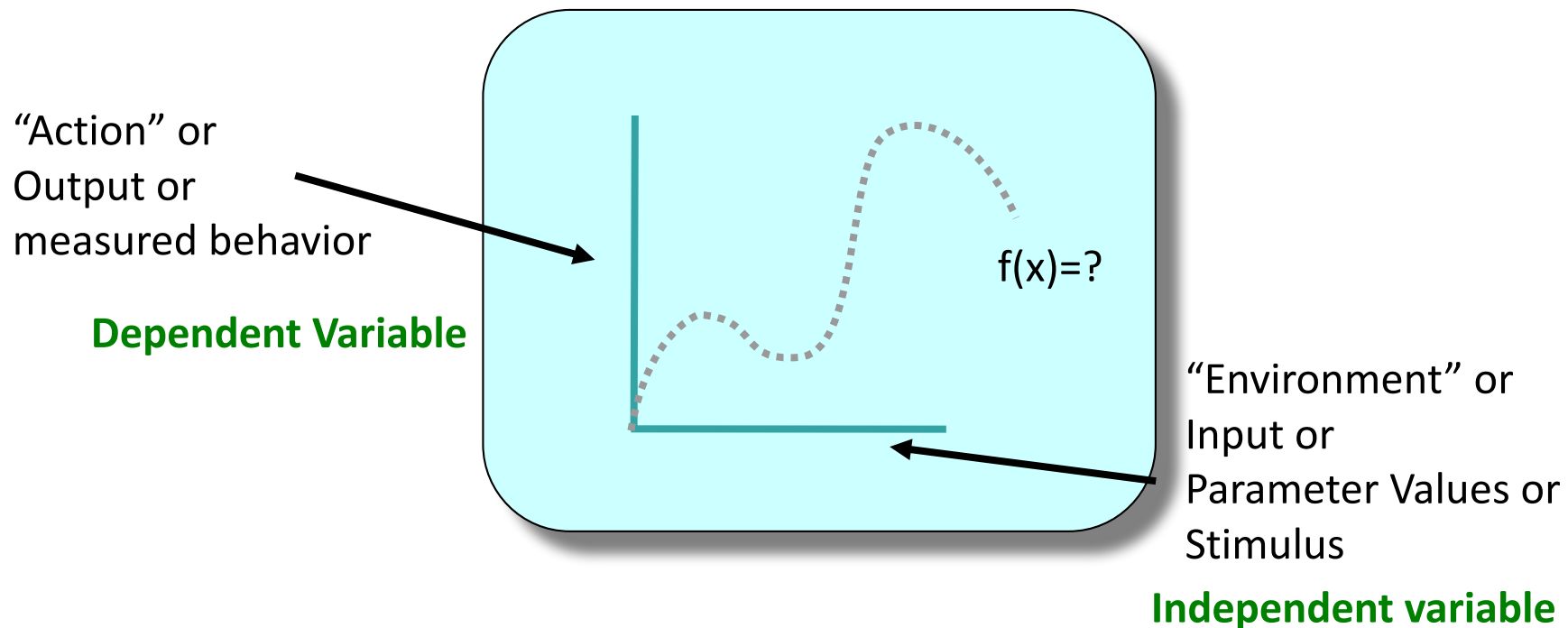
- Powerful experiments in psychology (such as those in psychophysics) can be thought of as “exploring the parameter space” of a technique, procedure, or algorithm in order to determine the function relationship between parameter values and perceptual effects (possibly, in order to optimize the technique, etc.)



- **WARNING:** The increased flexibility in answering questions that perceptual and psychophysical experiments offer comes at the cost of a need for increased vigilance, rigor, and expertise.

# Flashback: Why is this hard?

**Goal:** Estimate an unknown function



**Method:** Systematically sample the function

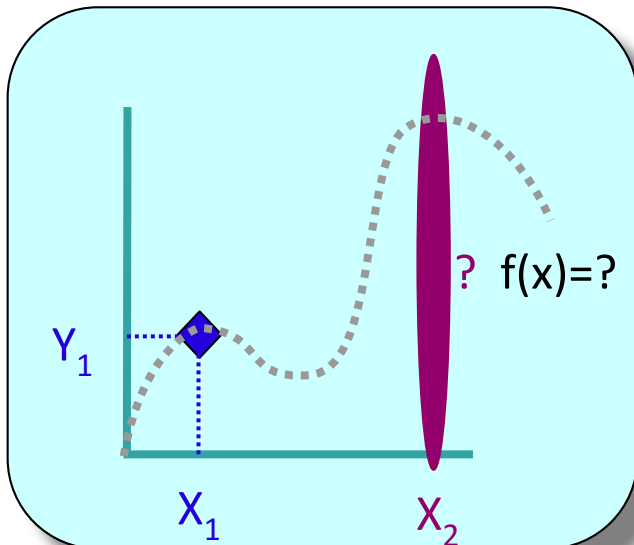
# Fundamental compromise

## Specificity

- You can only talk about what you measured



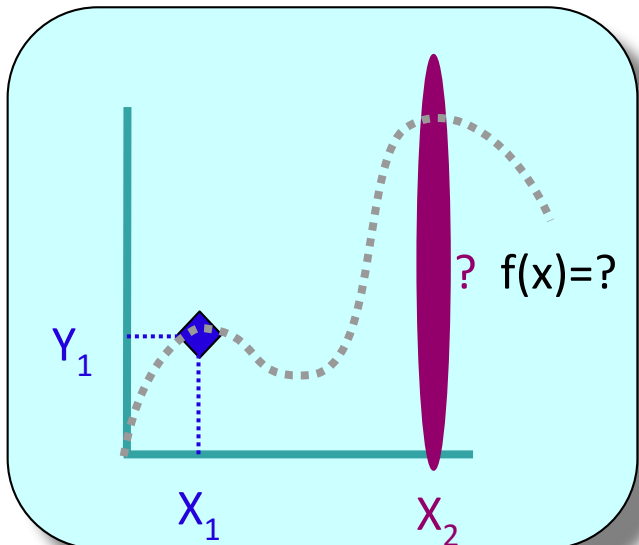
## Generality



# Fundamental compromise

## Specificity

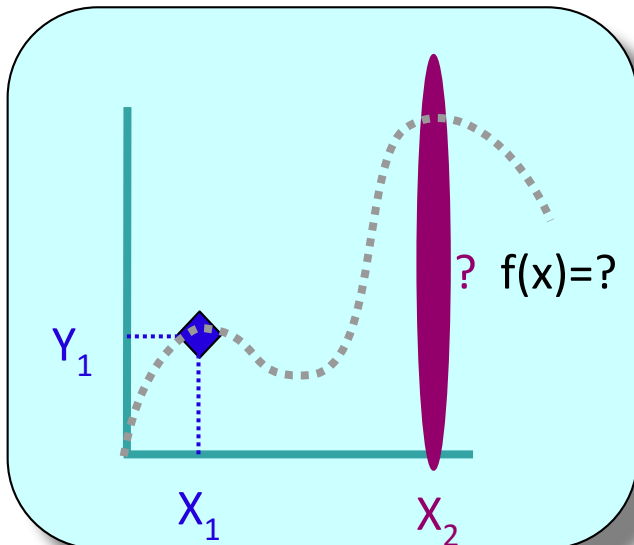
- You can only talk about what you measured



# Fundamental compromise

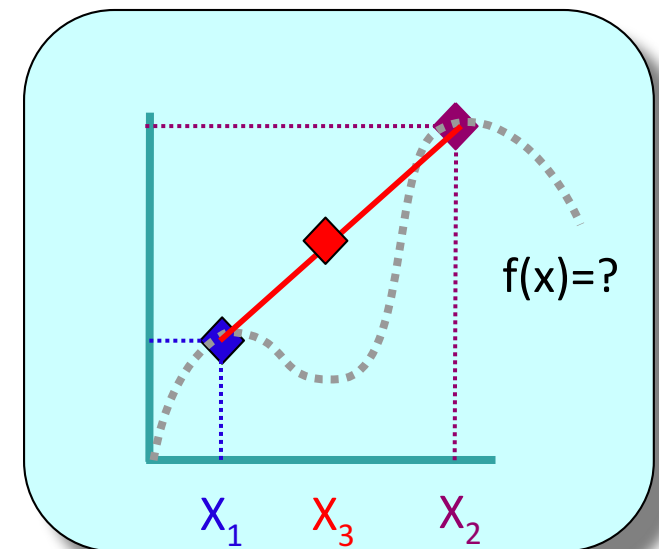
## Specificity

- You can only talk about what you measured



## Generality

- Make broad statements without measuring every point... **Interpolate!**

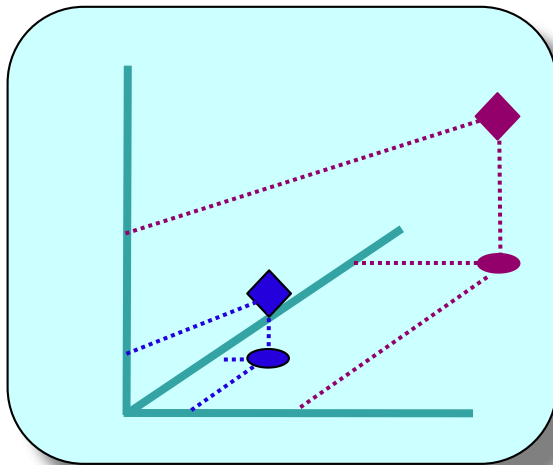


# Fundamental Compromise



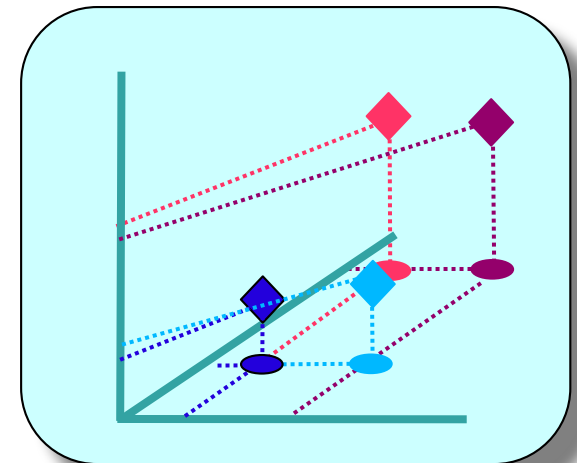
## Specificity

- You can only talk about what you measured
- If too much varies at once, you cannot say what **caused** any differences



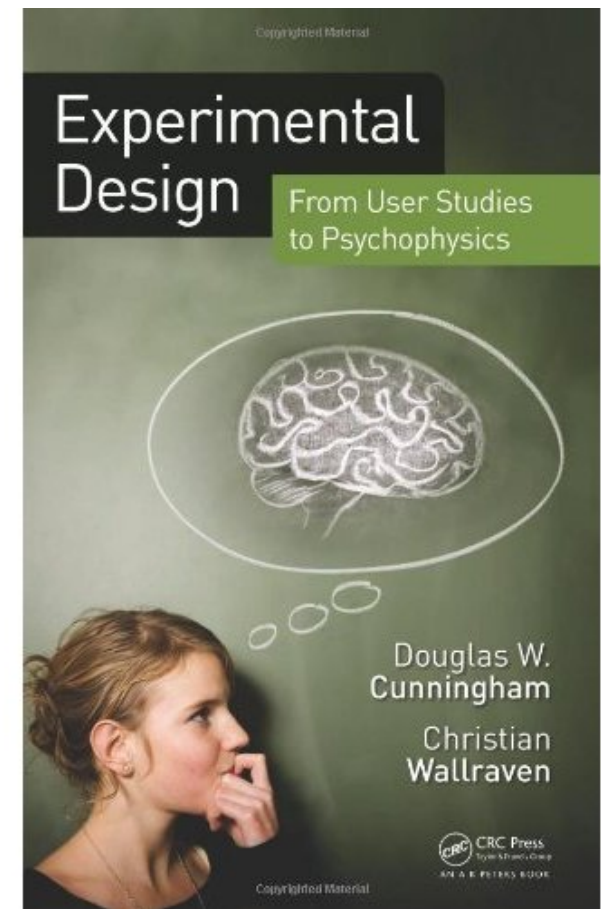
## Generality

- Make broad statements without measuring every point...**Interpolate!**
- Systematically vary dimensions



## 2: Philosophy of experiments – what is an experiment and **how can we model this mathematically?**

with material from  
Douglas Cunningham



# Some terms in Experimental Design

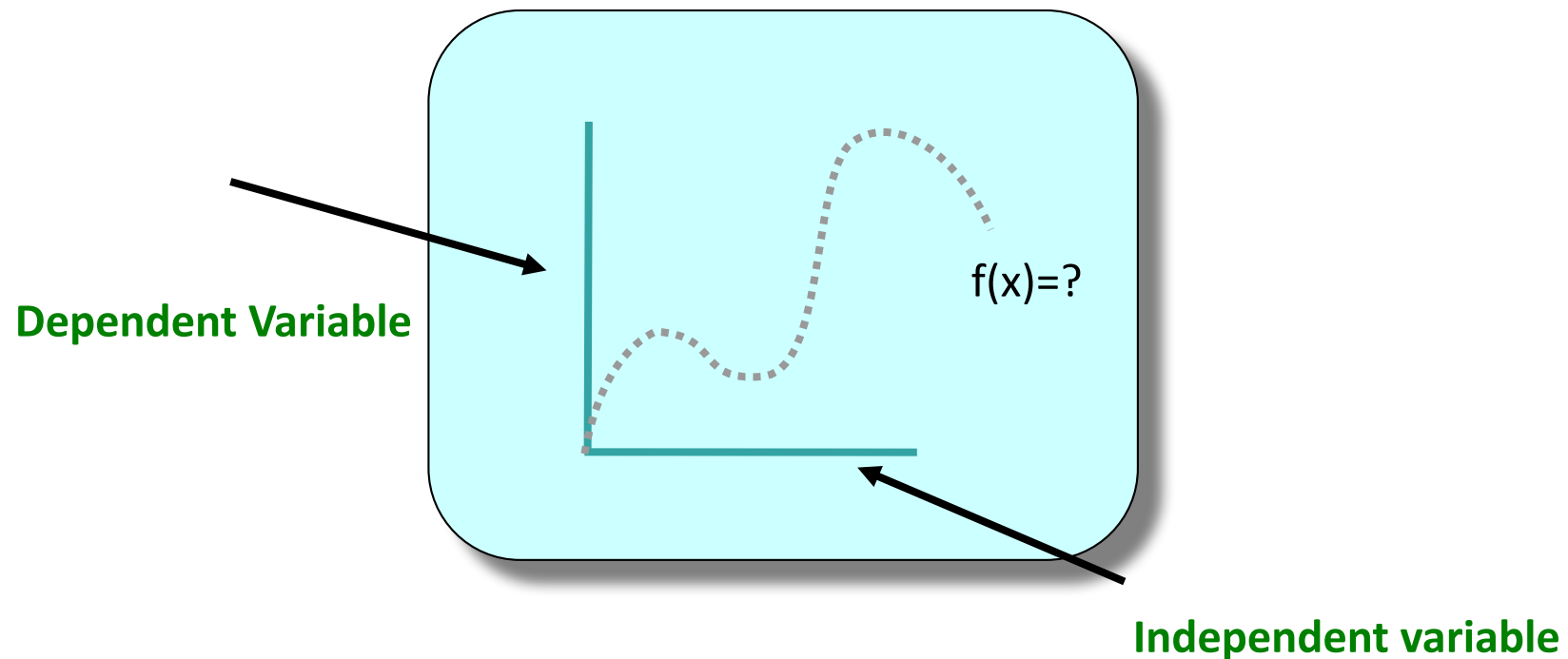


- Each dimension that we manipulate is called a **factor**.
- Each value that we used from a factor is called a **level**.
- Usually, all combinations of factors are used. Any given combination is called a **condition**.
- Each single execution of a condition is a **trial**.
- Since only an examination of what happens under all relevant conditions can answer our question conclusively, the full collection of trials that addresses the current research question is an **experiment**.



# What is Experimental Design?

**Goal:** Estimate an unknown function



**Method:** Systematically sample the function

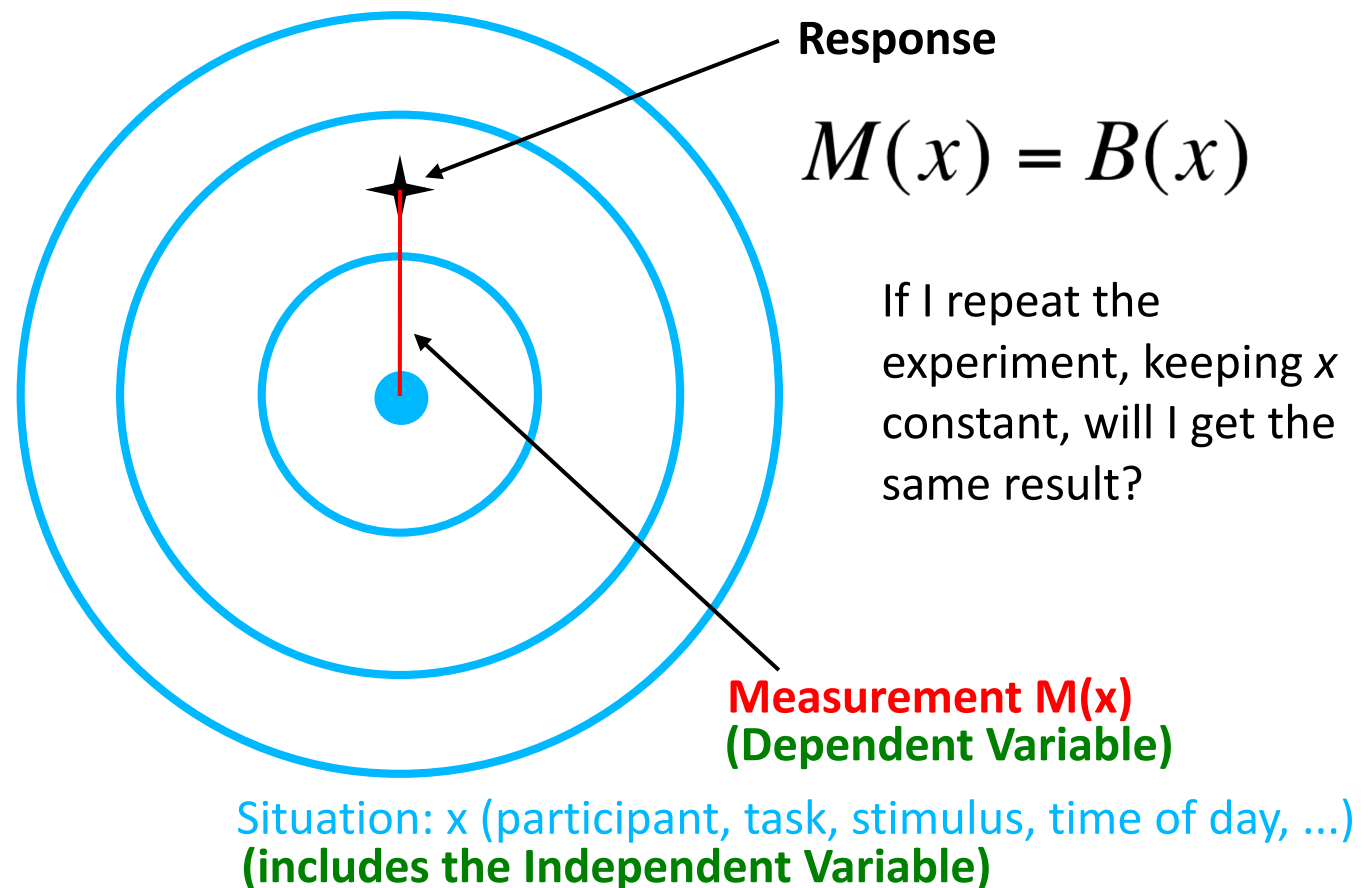
# Experiment I



- **Research Question:**
  - How accurately can people point to a target?
- **Methods:**
  - Stimulus: Blue bullseye target
  - Participants: One
  - Task: Point (once) as quickly and accurately as possible to the center
  - (total number of trials: 1)

# Experiment I

Let  $B(x)$  be the perception-action loop for pointing accuracy (for this situation)

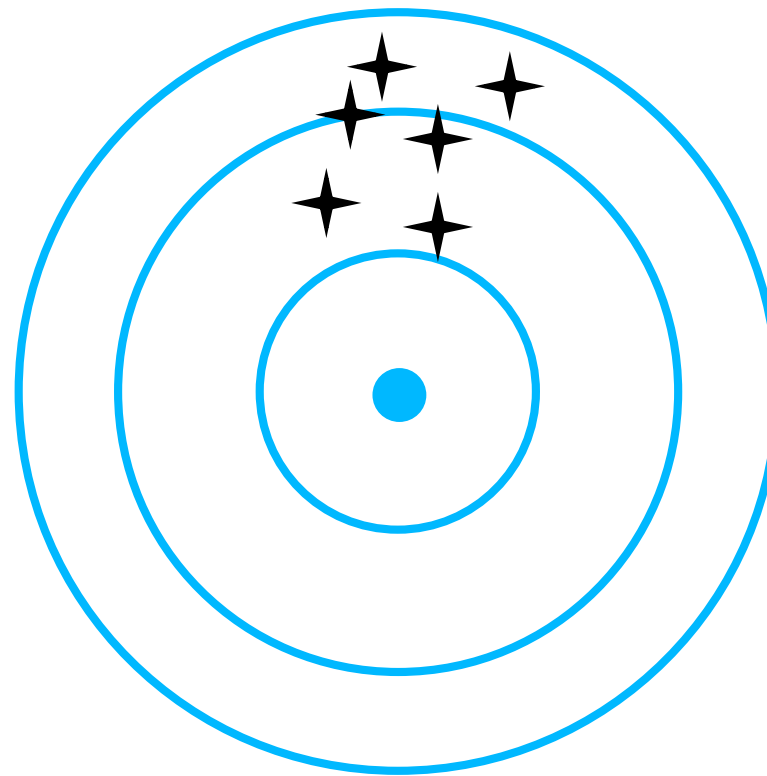


# Experiment Ib: Repeated Measures



- **Research Question:**
  - How accurately can people point to a target?
- **Methods:**
  - Stimulus: Blue bullseye target
  - Participants: One
  - Task: Point (n times) as quickly and accurately as possible to the center
  - (total number of trials:  $1 \times n$ )

# Experiment Ib: Repeated Measures



$$M(x) = B(x) + \varepsilon_w$$

Situation:  $x$  (participant, task, stimulus, time of day, ..)

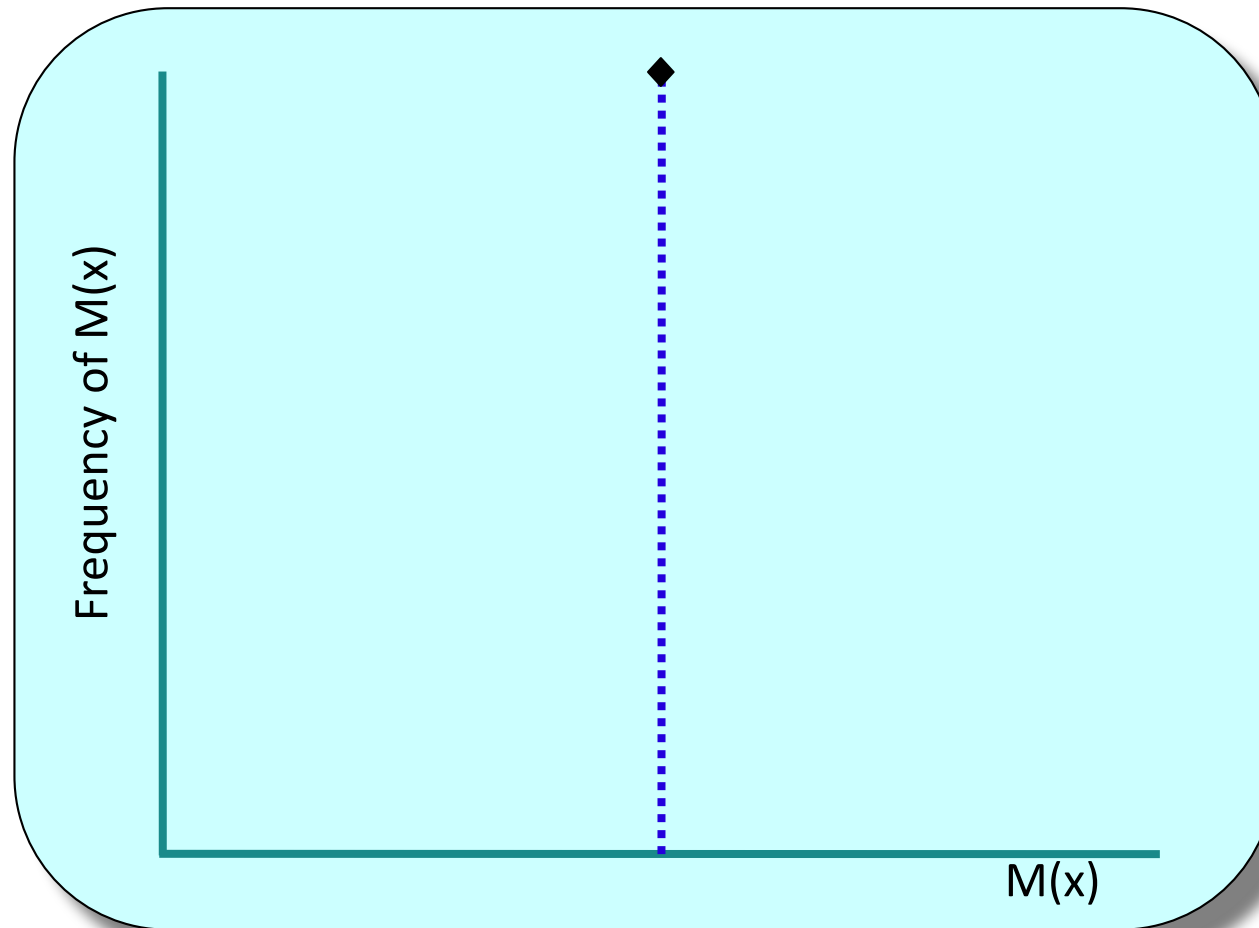
- People cannot exactly repeat any performance
- There is some inherent, unintentional variation/noise

# Experiment Ib: Repeated Measures



for  $\varepsilon_w = 0$ ,  $M(x) = B(x)$

$$M(x) = B(x) + \varepsilon_w$$



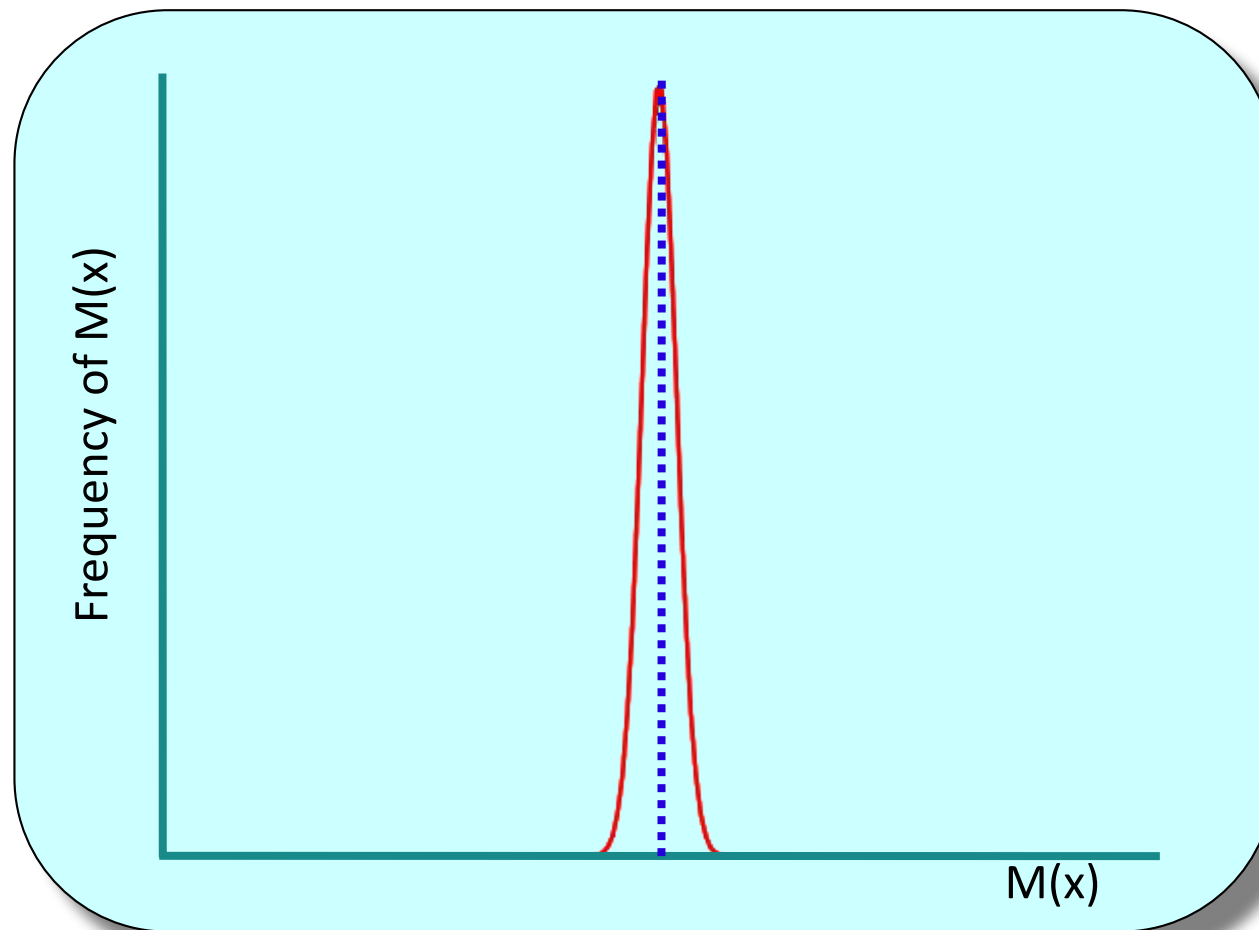
(note: Distributions have been rescaled)

# Experiment Ib: Repeated Measures



for small  $\varepsilon_w$  each measurement is close to  $B(x)$

$$M(x) = B(x) + \varepsilon_w$$



in this case, we do many trials and find that most of the time the measurements fall in a very small region around the “true” value of  $B(x)$

(note: Distributions have been rescaled)

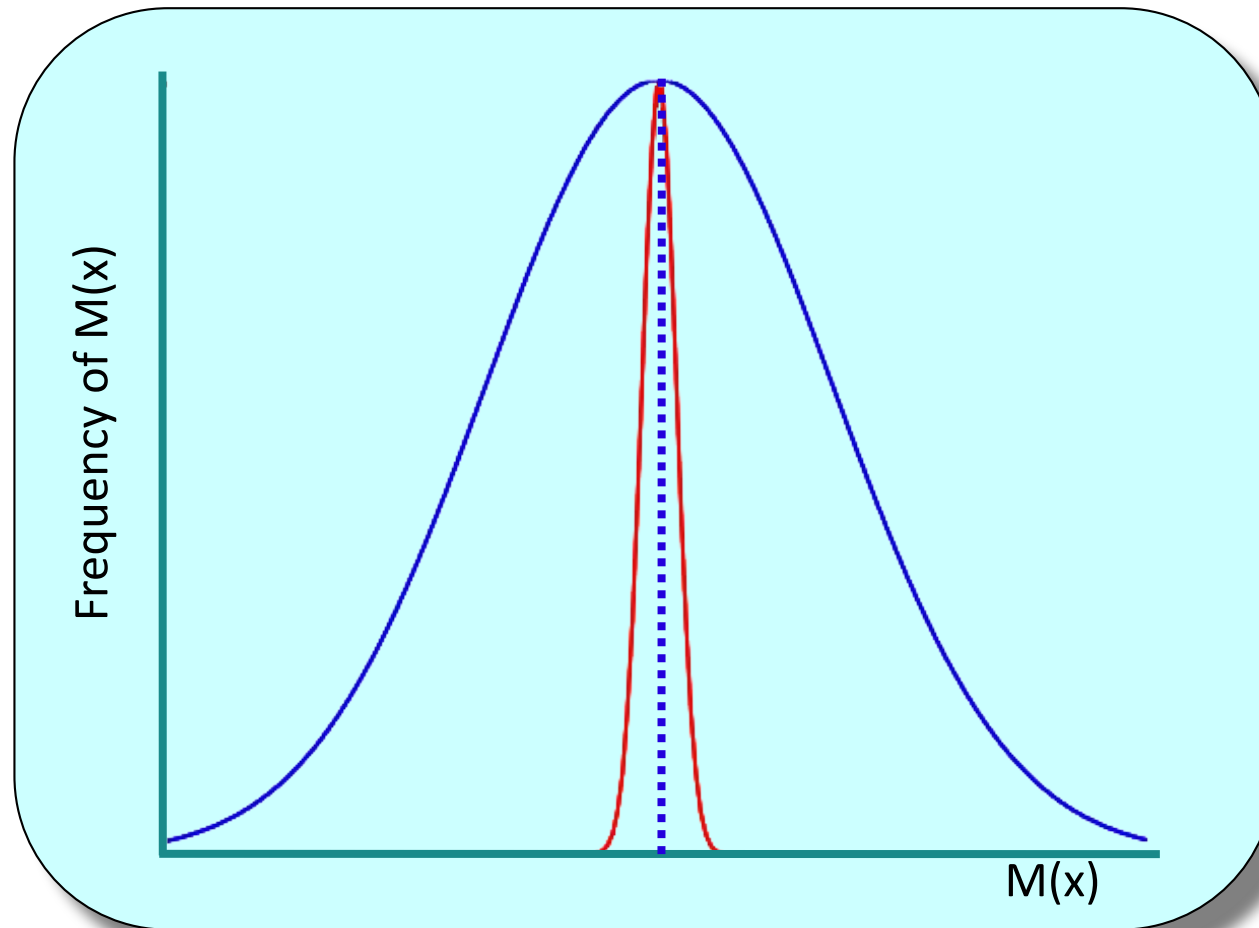
# Experiment Ib: Repeated Measures



for small  $\varepsilon_w$  each measurement is close to  $B(x)$

for large  $\varepsilon_w$  each measurement can be very far from  $B(x)$

$$M(x) = B(x) + \varepsilon_w$$



in this case, we do many trials and find that most of the time the measurements fall in a **large** region around the “true” value of  $B(x)$

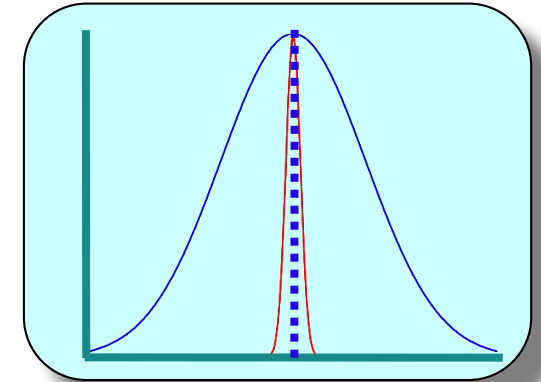
(note: Distributions have been rescaled)



# Experiment Ib: Repeated Measures



- The average approximates  $B(x)$
- $B(x)$  is constant
- $\epsilon_{wl}$  is different every time we measure  $M(x)$
- Bias from  $\epsilon_{wl}$  is sometimes positive, sometimes negative
- With enough trials, we can estimate the error, and factor it out



$$\text{trial 1: } m_1(x) = B(x) + \epsilon_{w1}$$

$$\text{trial 2: } m_2(x) = B(x) + \epsilon_{w2}$$

...

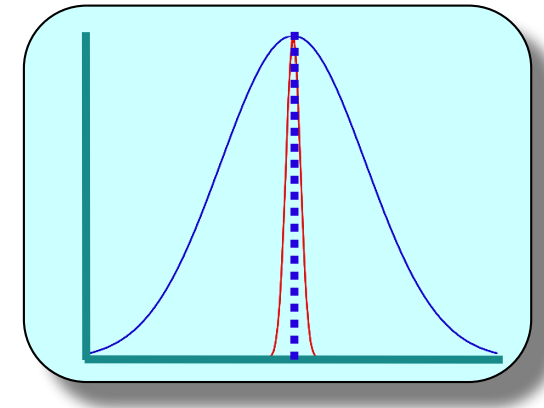
$$\text{trial n: } m_n(x) = B(x) + \epsilon_{wn}$$

$$\text{average: } \overline{M}(x) = \frac{\sum_{i=1}^n m_i}{n} = \frac{\sum_{i=1}^n B(x) + \epsilon_{wi}}{n} \approx B(x)$$

# Experiment Ib: Repeated Measures



- Anything that can reduce noise improves the approximation
- Increasing number of samples (trials) improves approximation
- How many repetitions?
  - There are equations for calculating this, based in part on
    - expected effect size
    - noise size
- Rule of thumb: More than 5 less than 20



# Experiment Ib: Repeated Measures

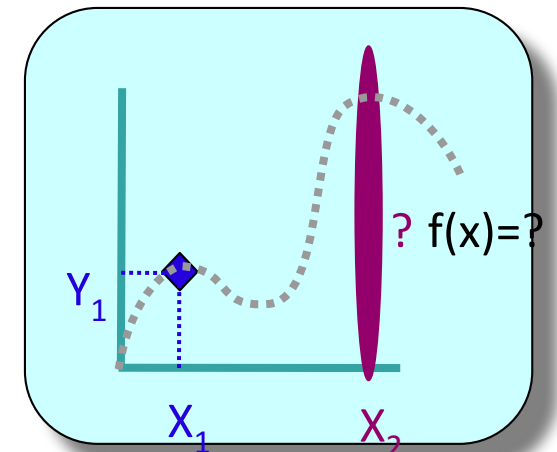


- **Research Question:**
  - How accurately can people point to a target?
- **Methods:**
  - Stimulus: Blue bullseye target
  - Participants: One
  - Task: Point (**5** times) as quickly and accurately as possible to the center
  - (total number of trials: 1 x **5**)

# Experiment Ib: Repeated Measures



- **Research Question:**
  - How accurately can people point to a target?
- **Methods:**
  - Stimulus: Blue bullseye target
  - Participants: **One**
  - Task: Point (**5** times) as quickly and accurately as possible to the center
  - (total number of trials: 1 x **5**)
- The results will be specific for this person
- $B(x)$  might be different for different people
- To generalize to the population, we need more people!



# Experiment 1c (Multiple Participants)

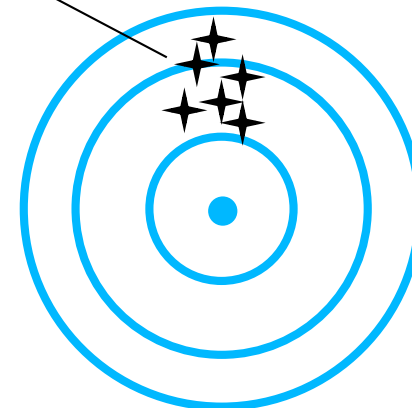


- **Research Question:**

- How accurately can people point to a target?

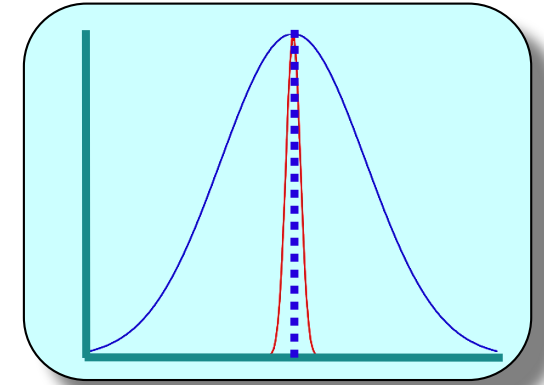
- **Methods:**

- Stimulus: Blue bullseye target
- Participants: Several ( $p$ )
- Task: Point (once each) as quickly and accurately as possible to the center
- (total number of trials: 1 per person)



# Experiment 1c (Multiple Participants)

- We can calculate the error as above



- Is measuring many people once really the same as measuring one person multiple times?
- Why are people different?
  - Fundamentally different action-perception loops?
  - Constant (population) action-perception loop with everyone having a minor variation of that (e.g., noise)?

# Experiment 1c (Multiple Participants)

- Per person, we assumed a constant effect  $B(x)$  plus internal noise  $\epsilon_w$  = within person noise
- We can likewise assume a globally constant effect  $B(x)$  and additional noise between people  $\epsilon_b$  = between person noise

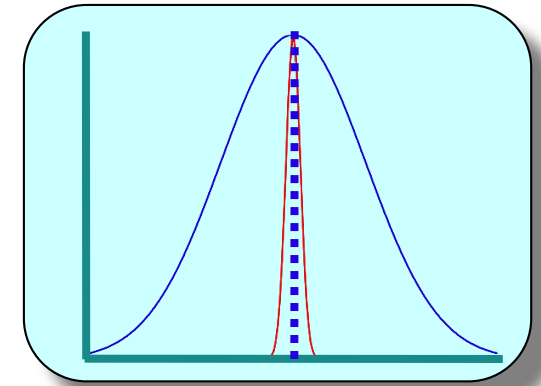
$$\overline{M}(x) = \frac{\sum_{i=1}^p m_i}{p} = \frac{\sum_{i=1}^p B(x) + \epsilon_{wi} + \epsilon_{bi}}{p}$$

- Might be wise to sample each of the two error functions separately! (n trials for each of p participants)

$$\overline{M}(x) = \frac{\sum_{i=1}^p \sum_{j=1}^n m_{ij}}{pn} = \frac{\sum_{i=1}^p \sum_{j=1}^n B(x) + \epsilon_{wj} + \epsilon_{bi}}{pn}$$

# How many samples??

- We are sampling unknown (noise) functions
- Multiple samples are needed per population
- How many participants?
- Again, there are equations for this
- As a rule of thumb,
  - for large effects, 10 is sufficient
  - for smaller effects, more
  - per Person (5+ repetitions per person)
- Two error terms, we need to sample both: Both Population and Person!





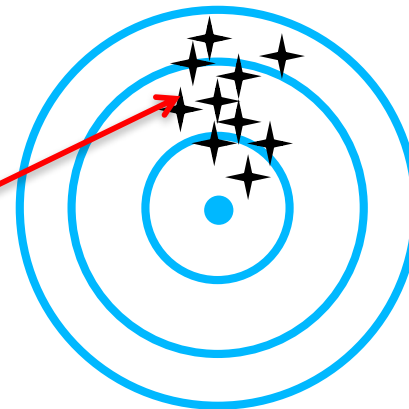
# Experiment Id

## Multiple Participants and Repetitions



- **Research Question:**
  - How accurately can people point to a target?
- **Methods:**
  - Stimulus: Blue bullseye target
  - Participants: 10
  - Task: Point (5 times) as quickly and accurately as possible to the center
  - (total number of trials:  $1 \times 5 = 5$  per person)

Each point is now the **AVERAGE** of the 5 trials per person!

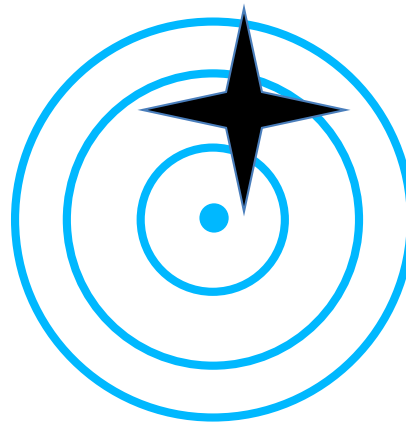
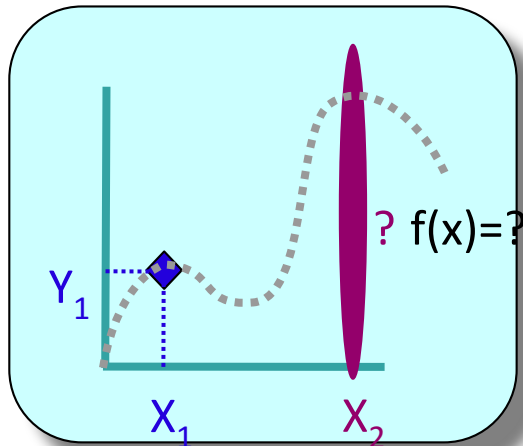


$$M(x) = B(x) + \varepsilon_w + \varepsilon_b$$

# Experiment Id

## Multiple Participants and Repetitions

- Why is performance so bad?



$$M(x) = B(x) + \varepsilon_w + \varepsilon_b$$

# Experiment II (Color)



- **Research Question:**
  - How do changes in color affect pointing?
- **Methods:**
  - Stimulus: Red and Blue bullseye targets
  - Participants: 10
  - Task: Point (5 times) as quickly and accurately as possible to the center
  - (total number of trials:  $2 \times 5 = 10$  per person)

# Experiment II (Color)

$$M(x) = B(x) + \varepsilon_w + \varepsilon_b$$

$$M(x + \Delta c) = B(x + \Delta c) + \varepsilon_w + \varepsilon_b$$

$$M(x + \Delta c) \approx B(x) + B(\Delta c) + \varepsilon_w + \varepsilon_b$$

Effect of color change

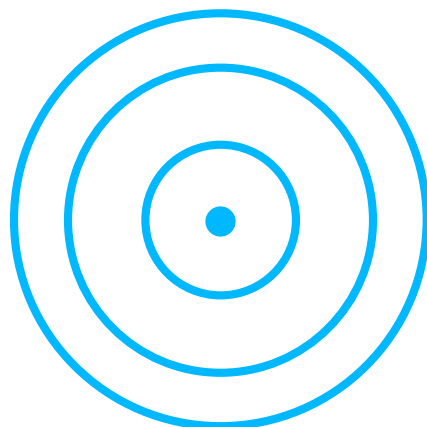
Change in stimulus color

$$M(x + \Delta c) - M(x) = \{B(x) + B(\Delta c) + \varepsilon_w + \varepsilon_b\} - \{B(x) + \varepsilon_w + \varepsilon_b\}$$

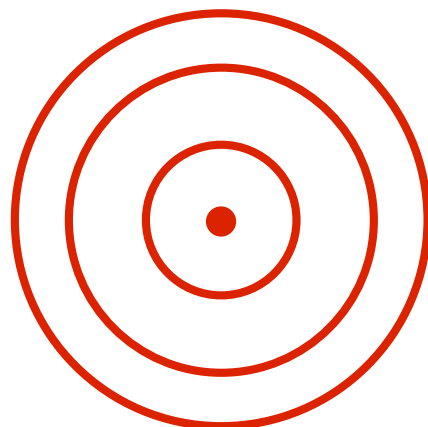
$$M(x + \Delta c) - M(x) = \{B(x) - B(x)\} + \{\varepsilon_w + \varepsilon_b - \varepsilon_w - \varepsilon_b\} + B(\Delta c)$$

$$M(x + \Delta c) - M(x) = B(\Delta c)$$

*The difference between conditions is the effect of changing color **from blue to red***



Situation:  $x$

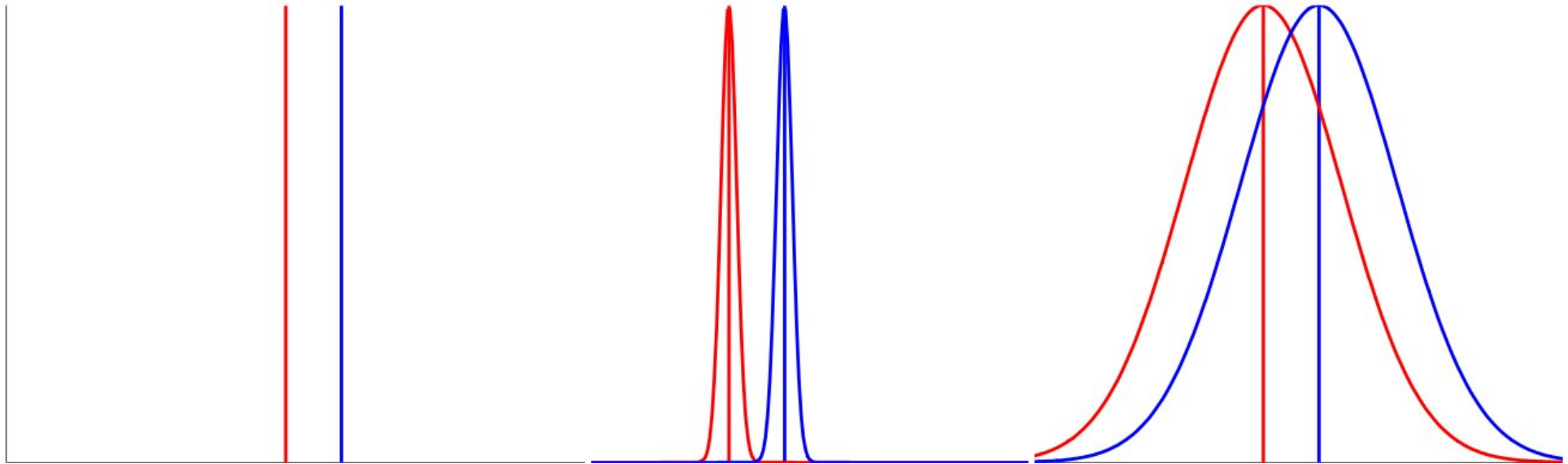


Situation:  $x + \Delta c$

specificity

Note that splitting the function  $B(x + \Delta c)$  into its component parts ( $B(x)$  and  $B(\Delta c)$ ) requires that the function  $B$  be homomorphic. Linear functions satisfy this property. Since we have assumed that the elements of  $x$  are independent of each other and can be modeled with as a linear, weighted sum,  $B$  is homomorphic.

# Experiment II (Color)



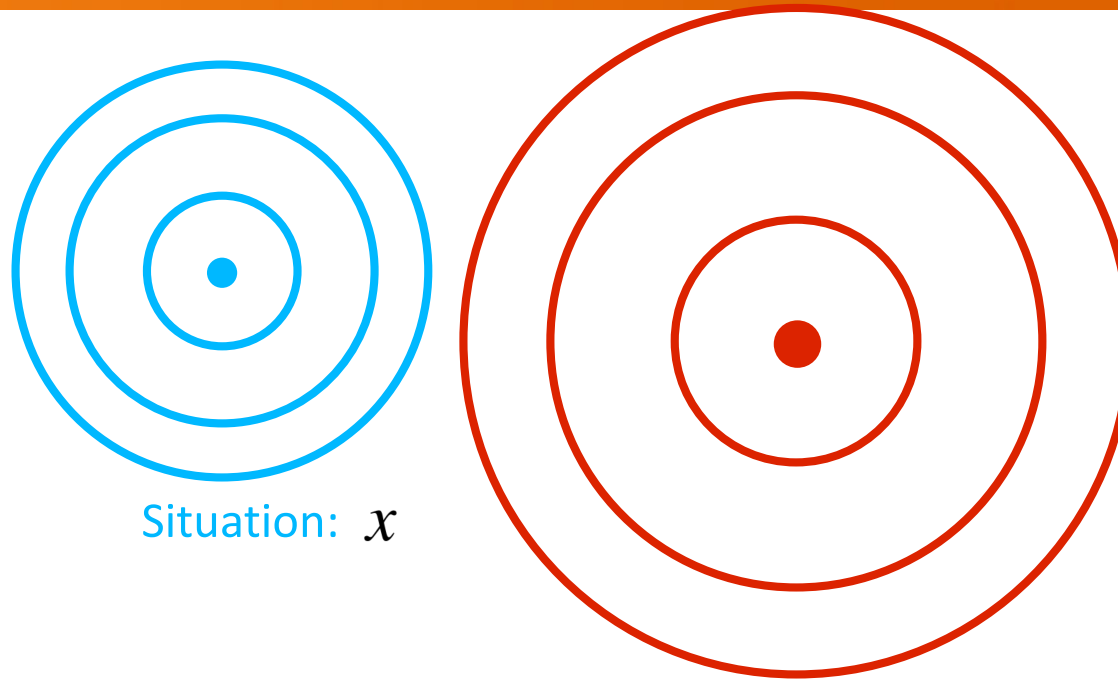
- Are the means *really* different?
- Noise may “swamp” effect!
  - Control noise
  - Identify and remove unwanted variance
  - Run (complicated) statistics

# Experiment III (Color and Size)



- **Research Question:**
  - How do changes in color and size affect pointing?
- **Methods:**
  - Stimulus: Large and small, Red and Blue bullseye targets
  - Participants: 10
  - Task: Point (5 times) as quickly and accurately as possible to the center
  - (total number of trials:  $2 \times 5 = 10$  per person)

# Experiment IIIa (Color and Size)



Situation:  $x$

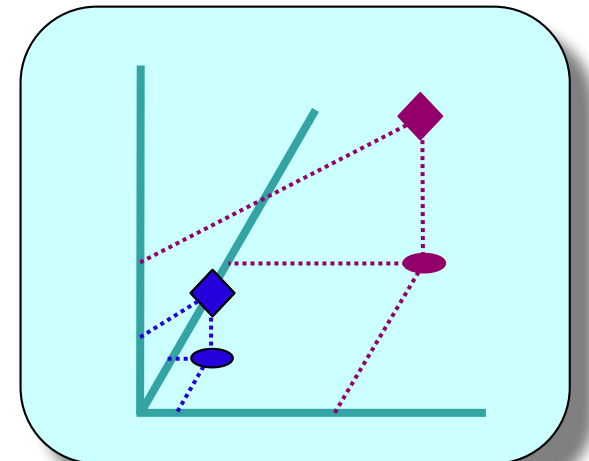
Situation:  $x + \Delta c + \Delta s$

$$M(x) = B(x) + \varepsilon_w + \varepsilon_b$$

$$M(x + \Delta c + \Delta s) = B(x) + B(\Delta c) + B(\Delta s) + \varepsilon_w + \varepsilon_b$$

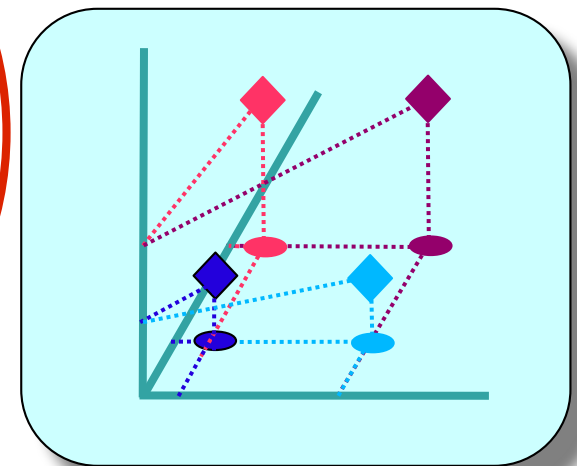
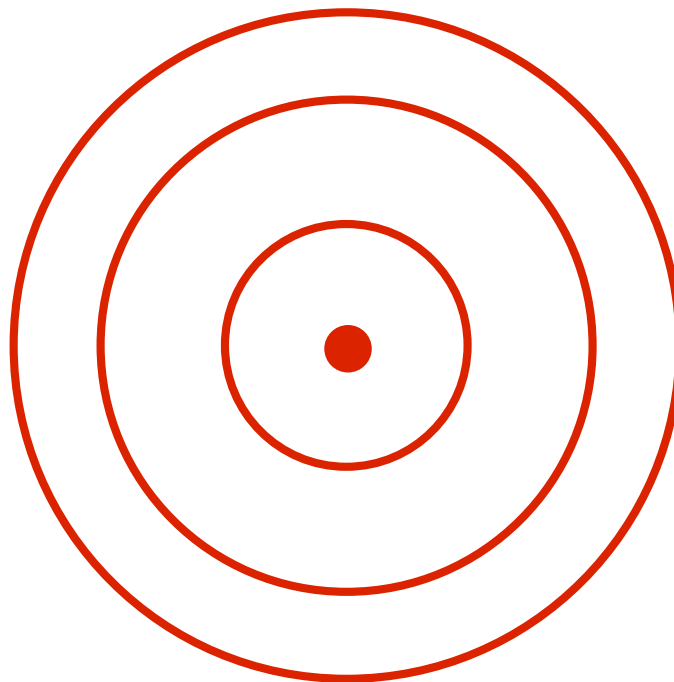
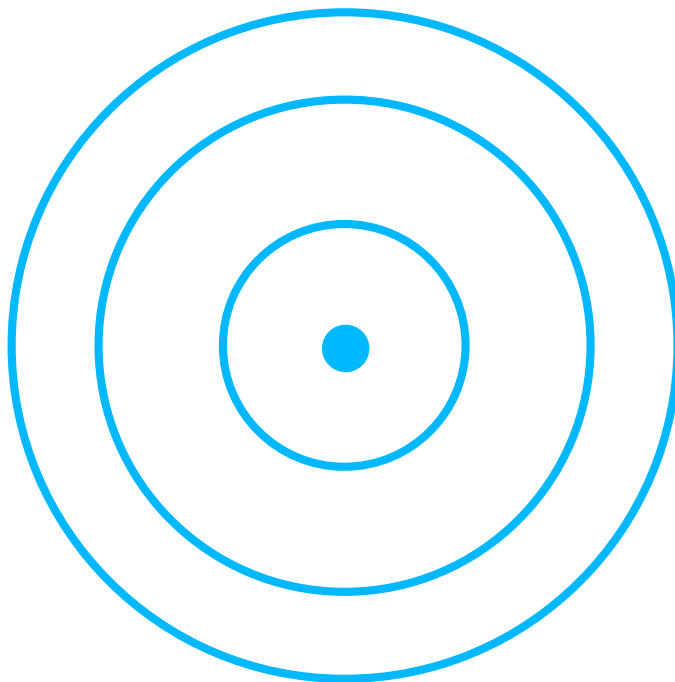
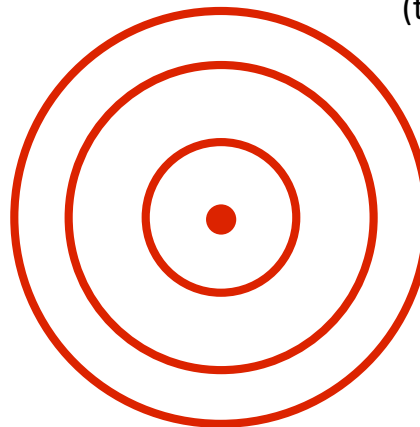
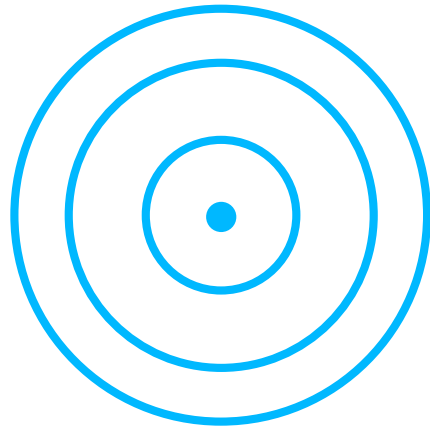
$$M(x + \Delta c + \Delta s) - M(x) = B(\Delta c) + B(\Delta s)$$

When changing two variables at the same time, you can no longer **conclusively** say what caused the difference between conditions



# Experiment IIIb (Color and Size)

(total number of trials:  $4 \times 5 = 20$  per person)



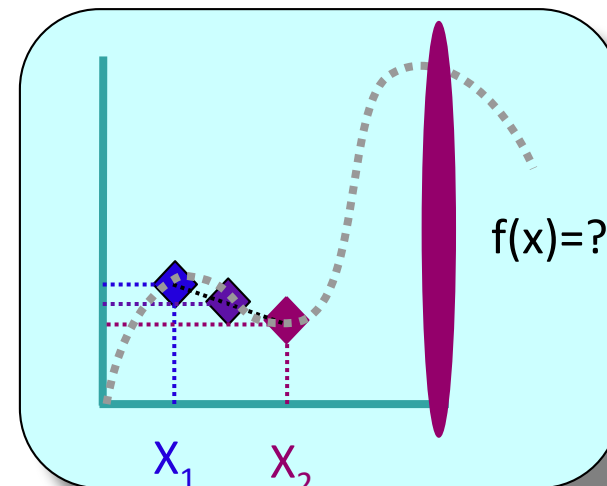
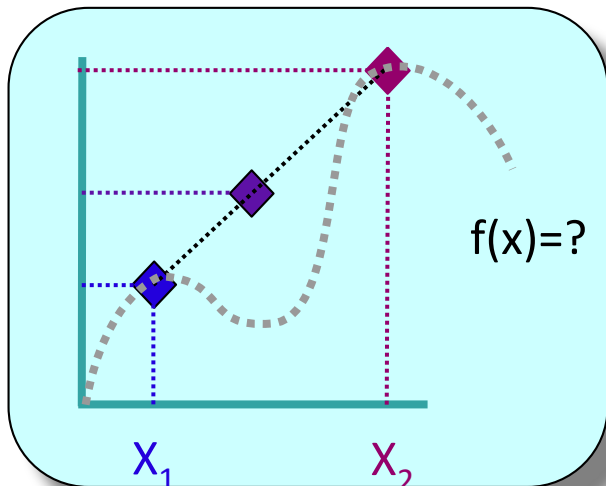
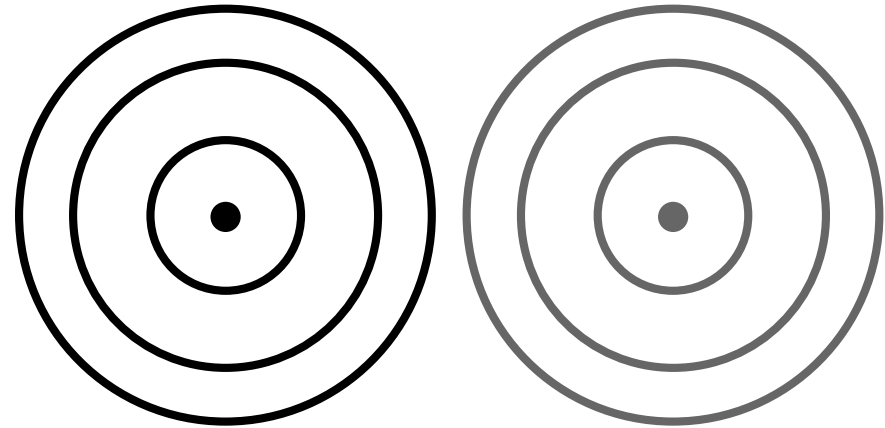
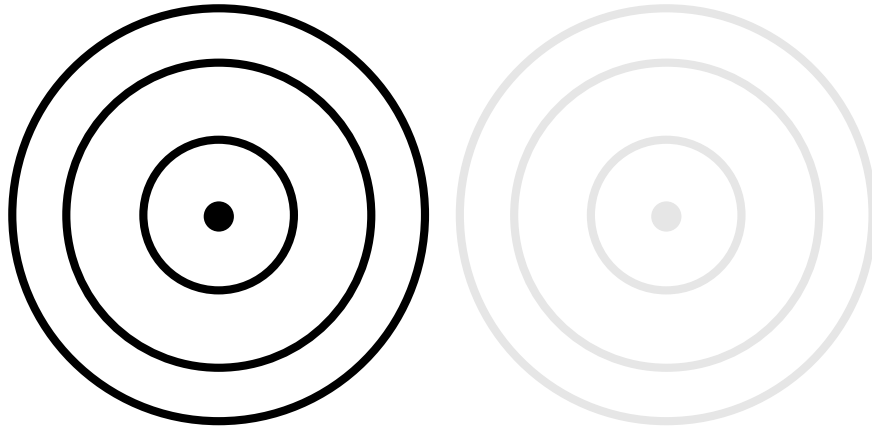


# Experiment IV (Contrast: Trial Order)

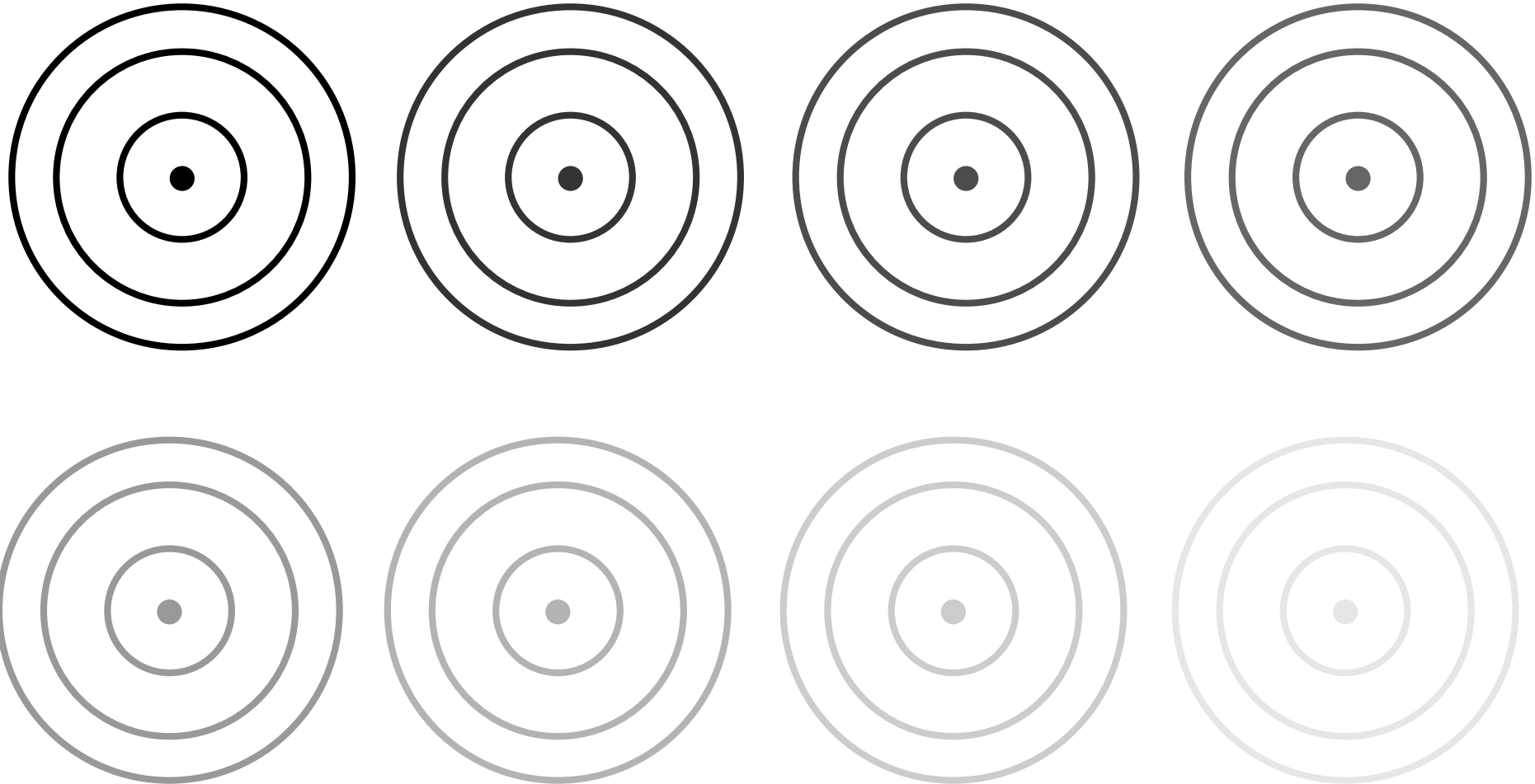


- **Research Question:**
  - How do changes in contrast affect pointing?
- **Methods:**
  - Stimulus: high and low contrast bullseye targets
  - Participants: 10
  - Task: Point (5 times) as quickly and accurately as possible to the center
  - (total number of trials:  $2 \times 5 = 10$  per person)

# Experiment IV (Contrast: Trial Order)



# Experiment IV (Contrast: Trial Order)



# Experiment IV (Contrast: Trial Order)

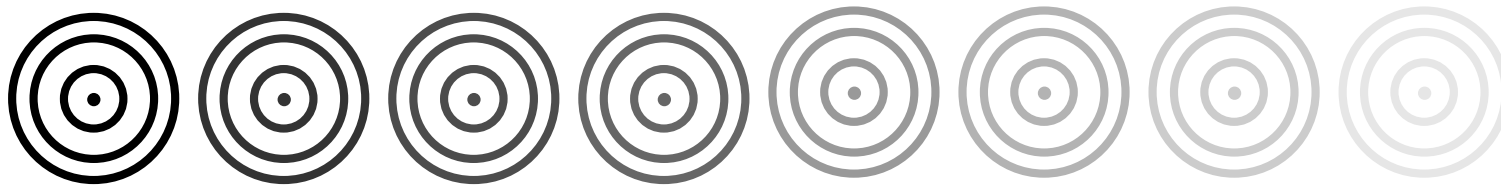


- **Research Question:**

- How do changes in contrast affect pointing?

- **Methods:**

- Stimulus: 8 bullseye targets, systematically varying contrast in equal steps
- Participants: 10
- Task: Point (5 times) as quickly and accurately as possible to the center
- (total number of trials:  $8 \times 5 = 40$  per person)



# Experiment IV (Contrast: Trial Order)



$$M(x) = B(x) + \varepsilon_w + \varepsilon_b$$

$$M(x - p) = B(x - a) + \varepsilon_w + \varepsilon_b$$

$$M(x - 2p) = B(x - b) + \varepsilon_w + \varepsilon_b$$

$$M(x - 3p) = B(x - c) + \varepsilon_w + \varepsilon_b$$

...

$$M(x - 7p) = B(x - g) + \varepsilon_w + \varepsilon_b$$

## Notes:

Measurements are in terms of a base condition  $x$  and multiples of 10% contrast change.

The underlying perception-action loop **does not** use this periodic representation.

# Experiment IV (Contrast: Trial Order)



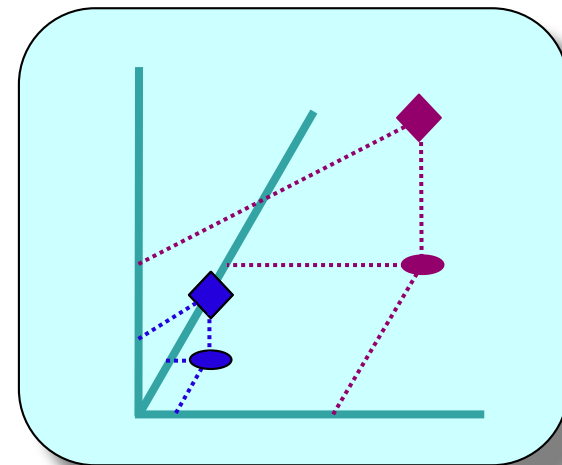
# Experiment IV (Contrast: Trial Order)



- Is trial 1 identical to trial 8?



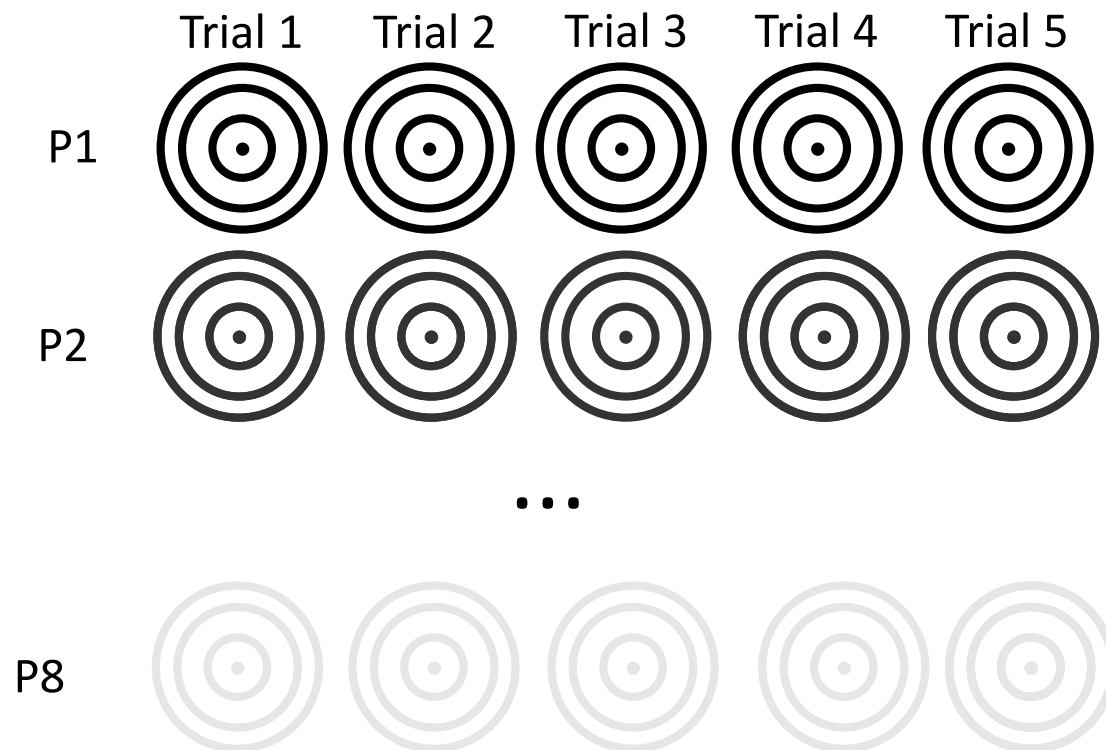
- Different contrasts
- Difference in practice!
- So, any difference between trial 1 and trial 8 might be due to
  - Contrast
  - order/practice effect



# Experiment IV (Contrast: Trial Order)

(total number of trials:  $1 \times 5 = 5$  per person)

- Solution 1: Eliminate order!
  - Everyone sees only one contrast
  - Each contrast is seen by one person
  - Between-participants design



- Difference between high and low might be due to
  - contrast
  - participant (P1 vs P8)
- So, multiple people per contrast.
- The higher  $\varepsilon_b$  is, the more participants one will need for **each** contrast condition
- 10 people for 8 groups= 80 people!



# Experiment IV (Contrast: Trial Order)



- Solution 2: Fully control for order
- We let everybody see every contrast, so we know that they act as their own control in terms of performance
- To explicitly check for order effects, we need to investigate how c1, c2, c3 may be different from c2, c3, c1 – for example
  - so we would need 10 people per possible order
- How many possible orders are there?
  - $n!$  for  $n$  conditions
  - 6 for 3 conditions
  - $8! = 40320$  for our 8 contrast levels  $\rightarrow >400000$  participants!

# Experiment IV (Contrast: Trial Order)



- Solution 3: Compromise by controlling only for some orders
- Maybe we are just interested to see, whether there IS an order effect, not WHICH order it has
- So, we don't test all possible orders ( $n!$ ), but only a subset ( $n$ ) of orders
- A popular selection is the latin square design, which for three conditions A,B,C looks like this
- We recruit 10 people per row, and compare their performance – if any row is different from the others, we know that there is an order effect and that we have to be careful!
  - 8 \* 10 participants total

	1	2	3
1	A	B	C
2	B	C	A
3	C	A	B

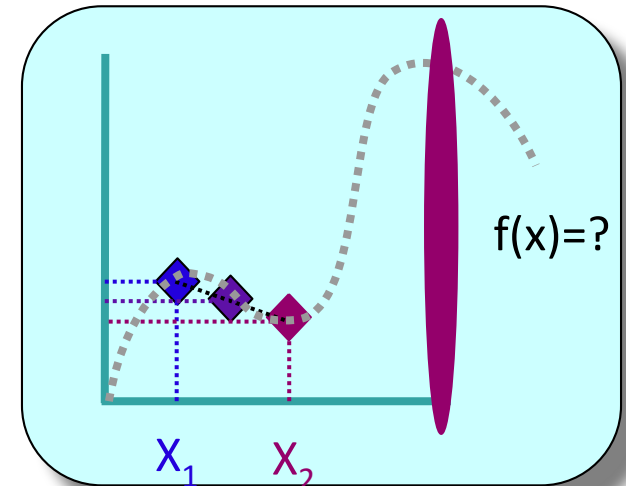
# Experiment IV (Contrast: Trial Order)



- Solution 4: Compromise by accepting some noise
- We let every participant see a different, random order and hope that order noise is washed out over many participants
- This is a good assumption if individual differences in performance are smaller than order effects (which is often the case)
- Again, more participants are needed than 8, but perhaps one may be able to spend fewer than 80 – let's say 40 participants

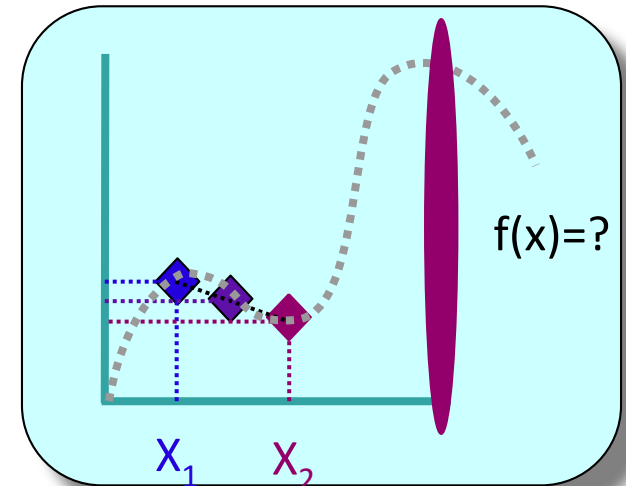
# Special Factors: Participants

- Why do people differ?
  - Natural talent
  - Expectations
  - Motivation
  - Fatigue
  - Physical differences (e.g., eye sight)
  - Experience
- What if we only used the authors?
  - Authors are not naive, can Bias
- What if we only used experts?
  - Experts/Novices have different skill levels, can Bias



# Special Factors: Participants

- Sampling a distribution!
- Participants should be representative
- If you want to understand people in general, use people in general
- Use naive participants, unless
  - sure knowledge cannot affect results
  - desired population consists solely of experts
- If you want to understand how a technique will affect surgery, use surgeons!



# What do you think?



- Going abroad, what are the differences that you have observed in other cultures?
  - ...

# People are WEIRD



- Arnett (2008) surveyed top journals in six sub-disciplines of psychology and found that
  - 68% of subjects were from the US
  - 96% from 'Western' industrialized nations (European, North American, Australian or Israeli) = 12% of the world's population
- You're 4000 times more likely to be studied by a psychologist if you're a university undergraduate at a Western university than a randomly selected individual

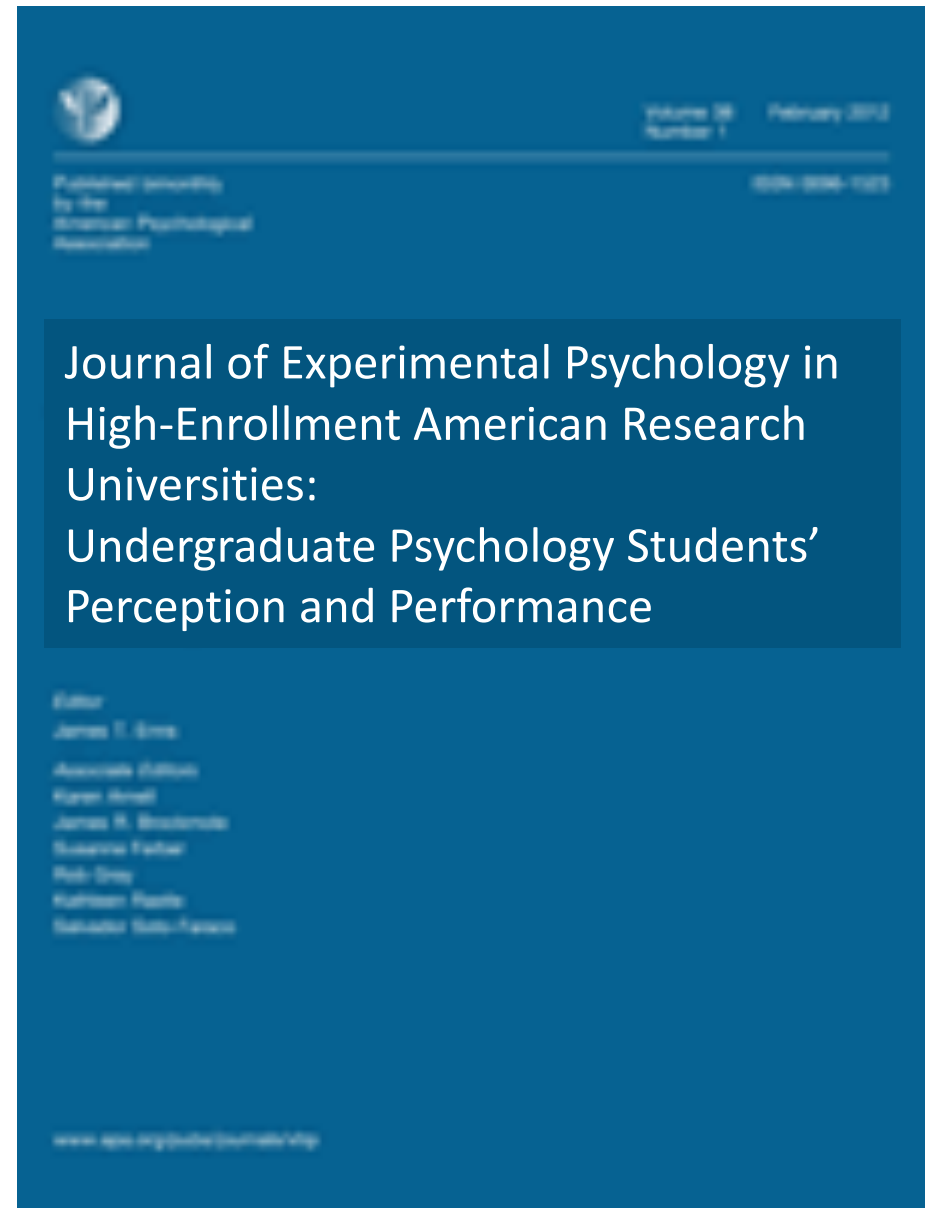
# People are WEIRD



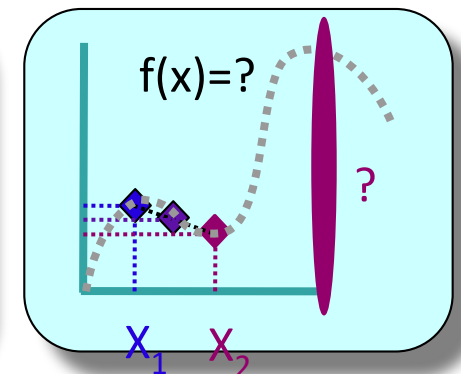
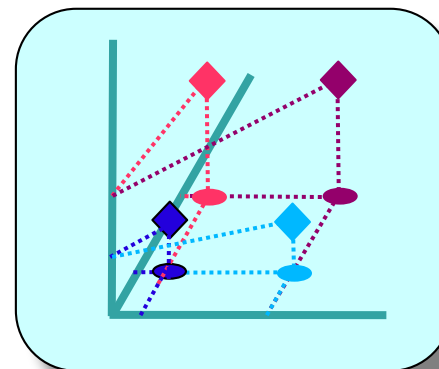
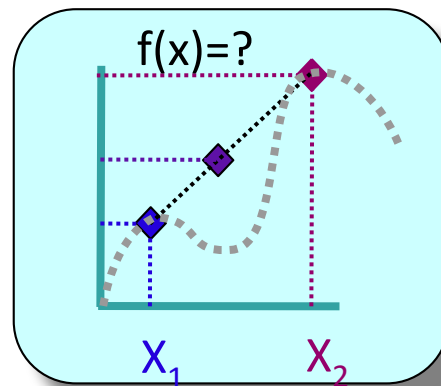
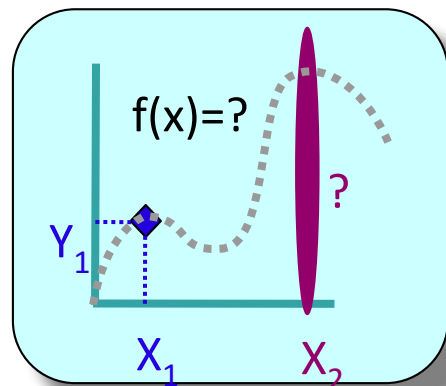
- The weirdest people in the world? Joseph Henrich, Steven J. Heine and Ara Norenzayan (2010). Behavioral and Brain Sciences, Volume 33, Issue 2-3, 2010; 61-83.
- Claim:
  - psychologists test people from Western, Educated, Industrialized, Rich, and Democratic (WEIRD) societies
  - this population shows considerable variation among visual perception, fairness, cooperation, spatial reasoning, categorization and inferential induction, moral reasoning, reasoning styles, self-concepts and related motivations, and the heritability of IQ
  - least representative population!
- Solution:
  - cross-cultural research agenda!
  - cautionary words in publications



# People are WEIRD



# Summary so far



# Summary so far



# Summary so far



- Try to remove variance through proper experimental design, and not through complex statistics
- The more complex your statistics become, the fewer the number of people that understand what you did or why becomes (i.e., you loose your audience)

# General summary



- Once we are clear about our research question, we need to go about trying to answer it. In general, that means:
  - Show something (stimuli)
  - somehow (stimulus presentation)
  - to someone (participants)
  - And ask them to do something (the task)
  - (and then analyze the results)