## CSE 321 - Homework 1

Due date: 31/10/2022, 16:45

- 1. **20pts.** Sort the following functions in increasing order of asymptotic growth. Prove that  $T_i(n) \in O(T_i(n))$  for every  $T_i < T_j$  where  $1 \le i, j \le 8$  by using limit approach.
  - $T_1(n) = 3logn + 3$ •  $T_5(n) = (\frac{n}{6})^2$ •  $T_2(n) = 4log(logn)$ •  $T_6(n) = 3^n + n^2$ •  $T_6(n) = n^n + 1000n$ •  $T_4(n) = 2000n + 1$ •  $T_8(n) = 2^n + n^3$
- 2. **20pts.** For the following functions prove whether  $f(n) \in O(g(n))$ ,  $f(n) \in \Omega(g(n))$  or  $f(n) \in \theta(g(n))$  by using limit approach.
  - (a) f(n) = 99n and g(n) = n(b)  $f(n) = 2n^4 + n^2$  and  $g(n) = (log n)^6$ (c)  $f(n) = \sum_{x=1}^{n} x$  and g(n) = 4n + log n
  - (d)  $f(n) = 3^n \text{ and } g(n) = 5^{\sqrt{n}}$
- 3. **20 pts** Examine the following algorithm and answer the questions.

```
int myFunction (int nums[], int n)
{
    for (int i = 0; i < n; i++){
        int count = 1;
        for (int j = i + 1; j < n; j++)
            if (nums[j] == nums[i])
            count++;
        if (count > n / 2)
            return nums[i];
    }
return -1;
}
```

- (a) What does the algorithm do? Explain input/output variables.
- (b) What is the time complexity of the algorithm? Analyze the worst and best cases.

4. **20 pts** Examine the following algorithm and answer the questions.

```
int myFunction2 (int nums[], int n)
{
    int i, *map, max = 0;

    for (i = 0; i < n; i++)
        if (nums[i] > max)
            max = nums[i];

map = (int *) calloc (max + 1, sizeof (int));

    for (i = 0; i < n; i++)
        map[nums[i]]++;

    for (i = 0; i < n; i++)
        if (map[nums[i]] > n / 2)
        return nums[i];

return -1;
}
```

- (a) Whatdoesthealgorithmdo?Explaininput/outputvariables.
- (b) Whatisthetimecomplexityofthealgorithm? Analyze the worst and best cases.
- 5. **10pts.** Compare the algorithms in Question 3 and 4 in terms of time complexity and space used. Explain what makes them better.
- 6. **10pts.** Consider you are given 2 arrays as follows:  $A = [a_1, a_2, ..., a_n]$  and  $B = [b_1, b_2, ..., b_m]$  Describe an algorithm for each of the following problems. Write the pseudo-code of the algorithm and analyze the time complexity of the worst and best cases.
  - (a) Finding  $max\{a_i * b_j\}$  where  $1 \le i \le n$  and  $1 \le j \le m$ .
  - (b) Sorting all elements of A and B in descending order as a single array, e.g.  $\{a_3, b_1, b_7, ...\}$
  - (c) Adding an element to one of the arrays.
  - (d) Deleting an element from one of the arrays.