

## Problem E - Fire Emblem: Heroes

Maybe you've played the new phone game "Fire Emblem: Heroes"? It's a turn-based strategy game, where your characters are pitted in an arena (usually 4 vs 4) to defeat the opposing squad. Different characters have different skillsets, and one of the goals in the game is to assemble a squad of top-tier characters. The best tier of heroes is the **legendary** tier, and everyone knows that the best teams are chock full of **legendary** heroes.



In our simplified version of the game, the game consists of a series of  $N$  battles against the AI (which we always win, because we're so good at the game). After battle  $i$ , we summon 1 new champion, with probability  $p_i$  of being a **legendary** champion. Battles are always done in the order 1 through  $N$ . Our intention is to roll a team consisting of at least  $K$  **legendary** champions. After  $K$  legendary champions are rolled, we can stop the game.

There's a trick, though, that I haven't mentioned yet. Sometimes we get very unlucky with our rolls: for example, imagine playing ten battles in a row and receiving no **legendary** champions! This might have even been the best opportunities to receive **legendary** champions (i.e. the  $p_i$ 's associated with these battles was relatively high). Here's where our trick comes in: we DELETE THE GAME from our phone, and re-install! Now we can start over from the beginning, at no cost (note that this resets everything, so we don't get to keep the **legendary** champs that we've got so far). It is possible to restart the game after exhausting every battle in the game, if we didn't get  $K$  **legendary** champions.

What's the expected value of the number of battles required to get a team with  $K$  **legendary** heroes, assuming that we re-install whenever it's optimal to do so?

### Input Specification:

The problem begins with an integer  $T \leq 100$ , the number of testcases. Each testcase begins with two integers on their own line:  $1 \leq N \leq 420$ , the number of potential battles, and  $0 < K \leq N$ , the number of **legendary** heroes we're trying to summon. This is followed by a line containing  $N$  probabilities  $p_1$  through  $p_N$ , where  $p_i$  is the probability that we summon a **legendary** champion after battle  $i$ ;  $p_i \geq 0.01$  and will be given to 3 decimal places.

### Output Specification:

For each testcase, output a single number on its own line: the expected value of the number of battles required to obtain  $K$  **legendary** champions. It is guaranteed that this will never exceed  $10^6$  battles. A special judge will accept any answer with less than absolute or relative error of  $10^{-6}$ .

### Sample Input:

```
1
4 2
0.500 0.200 0.900 0.200
```

### Sample Output:

```
4.130434782
```