



UBC Engineering

Kate is climbing a ladder to clean the wall since she cannot reach the top on her own. She stops climbing just as the ladder is on the verge of slipping. If Kate is 4 ft and 11 in tall and weighs  $W_K$  lbs, and the ladder has a

uniform weight of  $W_L$  lbs, find the coefficient of friction between the ladder and the surface at  $A$  such that the ladder experiences impending slipping. Assume that there is no friction between the ladder and the wall at  $B$ .

Find the normal reactions at  $A$  and  $B$ .

Assume  $L = \text{length}$

$$\Sigma M_A = 0 \rightarrow (L \cos(\theta) - d_1) \cdot W_K + \frac{L \cos(\theta)}{2} \cdot W_L - L \sin(\theta) \cdot N_B = 0$$

$$\Rightarrow N_B = \frac{(L \cos(\theta) - d_1) \cdot W_K + \frac{L \cos(\theta)}{2} \cdot W_L}{L \sin(\theta)}$$

$$+ \uparrow \Sigma F_y = 0 \rightarrow N_A - W_K - W_L = 0$$

$$\Rightarrow N_A = W_K + W_L$$

Find the magnitude of the friction force applied on the ladder at  $A$  and the corresponding static coefficient of friction between the ladder and the floor.

$$+ \rightarrow \Sigma F_x = 0 \rightarrow N_B - F_A = 0$$

$$\Rightarrow F_A = N_B$$

Assuming impending slipping,  $F_A = \mu_s N_A$

$$\Rightarrow \mu_s = \frac{F_A}{N_A}$$