

A curved rod with radius r resists a force  $\overrightarrow{F}$ . If the fixed connection at O can withstand a maximum moment magnitude of  $M_{max}$ , what is the largest magnitude F that can be applied before the connection breaks?

$$\overrightarrow{r}_{OA} = r(1 + \cos\theta)\hat{i} + r\sin\theta\hat{j}$$

$$\overrightarrow{F} = F(\cos\theta \, \hat{i} + \sin\theta \, \hat{j})$$

Assuming positive moments are counterclockwise:

$$M_O = r(1 + \cos \theta) \cdot F \sin \theta - r \sin \theta \cdot F \cos \theta$$
  
$$\Rightarrow M_O = r \cdot F \sin \theta$$

Since  $M_O \leq M_{max}$ ,

$$r \cdot F \sin \theta \le M_{max}$$

$$\Rightarrow F \le \frac{M_{max}}{r\sin\theta}$$