

Solution: 21-5-5.4-Mk-05

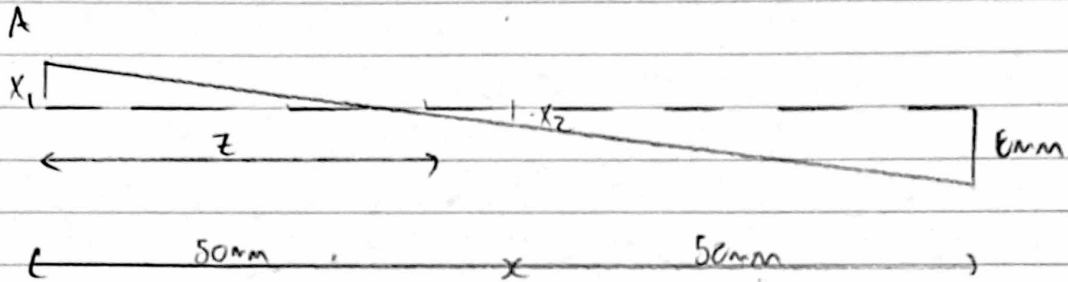
$$k_1 = 3 \text{ N/mm}$$

$$k_2 = 6 \text{ N/mm}$$

$$d_1 = 50 \text{ mm}$$

$$d_2 = 50 \text{ mm}$$

$$d_3 = 8 \text{ mm}$$



Using similar triangles:

$$\textcircled{1} \quad \frac{100-z}{80} = \frac{z}{x_1} = \frac{50-z}{x_2}$$

$$F = kx \rightarrow x = \frac{F}{k}$$

$$\textcircled{2} \quad x_1 = \frac{F}{k_1} \quad x_2 = \frac{2F}{k_2}$$

$$\textcircled{2} \rightarrow \textcircled{1} \quad \frac{2F}{k_1} = \frac{(50-z)k_2}{2F}$$

$$22k_1 = (50-z)k_2$$

$$\frac{22k_1}{k_2} = 50-z \rightarrow \frac{2k_1}{k_2} = \frac{50-z}{z}$$

$$\frac{zk_1}{k_2} = \frac{50-z}{z}$$

$$\frac{zk_1}{k_2} + 1 = \frac{50}{z}$$

$$z = \frac{50}{\frac{zk_1}{k_2} + 1} = z = \frac{50}{\frac{2(3)}{6} + 1} = 25 \text{ mm}$$

Find x_1

$$\frac{100-z}{E} = \frac{z}{x_1} \Rightarrow x_1 = \frac{(25 \text{ mm})(E_{\text{steel}})}{(100-25 \text{ mm})} = 2.6667 \text{ mm}$$

Find x_2

$$\frac{z}{x_1} = \frac{50-z}{x_2}$$

$$x_2 = \frac{(50-z)x_1}{z} = \frac{(50-25)(2.6667 \text{ mm})}{25} = 2.6667 \text{ mm}$$

$$F = k_1 \cdot x_1 = (3 \text{ N/mm})(2.6667) = 8 \text{ N}$$