

Penguina is walking her three dogs, Alpaca, Bird, and Cat. If Penguina's hand is L ft away from the origin, find the position vectors of all the dogs relative to Penguina's hand.

Find Penguina's distance d_{Py} along the y axis from the origin.

$$L = \sqrt{d_{Py}^2 + h_P^2}$$

$$\Rightarrow d_{Py} = \sqrt{L^2 - h_P^2}$$

Find the position vectors of Penguina's dogs relative to her hand.

$$\overrightarrow{r}_{PA} = -d_{Ax}\widehat{i} + d_{Py}\widehat{j} + (h_A - h_P)\widehat{k}$$

$$\overrightarrow{r}_{PB} = d_{Bx}\widehat{i} + (d_{Py} - d_{By})\widehat{j} + (h_B - h_P)\widehat{k}$$

$$\vec{r}_{PC} = d_{Cx}\hat{i} + (d_{Py} + d_{Cy})\hat{j} + (h_C - h_P)\hat{k}$$

Find the distance of each dog from Penguina's hand.

$$d_{PA} = \sqrt{d_{Ax}^2 + d_{Py}^2 + (h_A - h_P)^2}$$

$$d_{PB} = \sqrt{d_{Bx}^2 + (d_{Py} - d_{By})^2 + (h_B - h_P)^2}$$

$$d_{PC} = \sqrt{d_{Cx}^2 + (d_{Py} + d_{Cy})^2 + (h_C - h_P)^2}$$