

Two members are pin connected at B and are pin connected to the surface at A and C. If a force with magnitude F acts on the frame at the pin connection B such that its component acting along member AB is F_{AB} , directed from B to A, find the angle ϕ ($0^{\circ} \le \phi \le 45^{\circ}$) and the magnitude of the force component acting along member BC.

Using Cosine Law:

$$F_{BC} = \sqrt{F^2 + F_{AB}^2 - 2 \cdot F \cdot F_{AB} \cos(\theta)}$$

Using Sine Law:

$$\frac{F}{\sin(\phi + 45^{\circ})} = \frac{F_{BC}}{\sin(\theta)}$$
$$\Rightarrow \phi = \sin^{-1}\left(\frac{F\sin(\theta)}{F_{BC}}\right) - 45^{\circ}$$