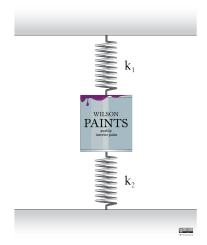
## 22-P-WE-TW-27



An engineer has developed a new contraption designed for shaking paint cans. A spring connects the top of the 20 kg can to the roof of the contraption and another spring connects the bottom of the can to the floor of the contraption. The system is initially at rest and the bottom spring is compressed by 0.3 m. If the bottom spring is cut, what is the maximum velocity of the paint can? (Take  $k_1 = 100 \text{ N/m}$  and  $k_2 = 100 \text{ N/m}$ . Also use  $g = 9.81 \text{ m/s}^2$  and ignore the effects of air resistance)

## **Solution:**

Equilibrium:

$$mg = k_1 x_1 - k_2 x_2$$
  
 $k_1 x_1 = mg + k_2 x_2$   
 $x_1 = \frac{mg + k_2 x_2}{k_1} = \frac{(20)(9.81) + (100)(-0.3)}{100} = 1.662 \text{ [m]}$ 

We will call this value  $x_{eq0} = 1.662$  m and will now only be analyzing spring 1.

The removal of spring 1 will cause the system to vibrate about a new equilibrium value  $x_{eq1}$ . So when the can is at  $x_{eq1}$  it will have its maximum kinetic energy

$$k_1 x_{eq1} = mg$$

$$x_{eq1} = \frac{mg}{k_1} = 1.962 \text{ [m]}$$

$$A = x_{eq0} - x_{eq1} = 1.962 - 1.662 = 0.3 \text{ [m]}$$

$$V_{s0} + V_{g0} + T_0 = T_1 + V_{s1} + V_{g1}$$

$$T_0 = V_{g1} = 0$$

$$T_{max} = \frac{1}{2} k_1 x_{eq0} - \frac{1}{2} k_1 x_{eq1}^2 + mgA$$

$$T_{max} = \frac{1}{2} (100)(1.662^2 - 1.962^2) + (20)(9.81)(0.3) = 4.5 \text{ [J]}$$

$$T_{max} = \frac{1}{2} mv^2$$

$$v = \sqrt{\frac{2T_{max}}{m}} = \sqrt{\frac{2(4.5)}{20}} = 0.671 \text{ [m/s]}$$