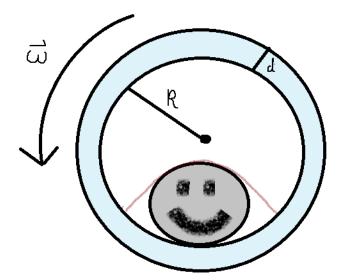
22-R-KM-TW-7



Julie is taking her pet rock, Rocko, for a walk. Rocko is safely fastened to the side of a spherical ball with inner radius R=5 cm and thickness d=0.5 cm. If Julie walks at a speed of 1.5 m/s, what is the angular velocity of her pet rock?

Solution:

$$\begin{split} r &= R+d = 5.5 \text{ cm} \\ \vec{v} &= \vec{\omega} \times \vec{r} \\ \vec{\omega} \perp \vec{r} \Rightarrow \omega &= \frac{v}{r} = \frac{v}{r} = \frac{1.5}{0.055} = 27.3 \text{ rad/s} \end{split}$$

What is the maximum speed her pet rock will experience at any point on its surface?

This will occur when the rock is at the top of the sphere. The bottom of the sphere can be treated as an IC.

$$|\vec{r}_{\rm ground \rightarrow rock}| = 2R + d = 10.5~{\rm cm}$$

$$v = \omega r = 2.86~{\rm m/s}$$