



A rope is held in tension by the pipe OB and the hook at C . If \vec{F} has an x component of F_x , express the force \vec{F} as a cartesian vector, find its magnitude, and find the coordinate direction angles.

$$\text{Since } \frac{\vec{F}}{\|\vec{F}\|} = \hat{u}_{BC} = \frac{\vec{r}_{BC}}{\|\vec{r}_{BC}\|},$$

$$\Rightarrow \vec{F} = \frac{\|\vec{F}\|}{\|\vec{r}_{BC}\|} \cdot (d_2\hat{i} - d_3\hat{j} - d_4\hat{k})$$

$$F_x = \frac{||\vec{F}||}{||\vec{r}_{BC}||} \cdot d_2$$

$$F_y = \frac{||\vec{F}||}{||\vec{r}_{BC}||} \cdot (-d_3)$$

$$F_z = \frac{||\vec{F}||}{||\vec{r}_{BC}||} \cdot (-d_4)$$

$$\Rightarrow \frac{F_x}{d_2} = \frac{F_y}{-d_3} = \frac{F_z}{-d_4}$$

$$\vec{F} = F_x \hat{i} + \frac{-d_3}{d_2} \cdot F_x \hat{j} + \frac{-d_4}{d_2} \cdot F_x \hat{k}$$

$$||\vec{F}|| = F = \sqrt{F_x^2 + F_y^2 + F_z^2}$$

$$\alpha = \cos^{-1} \left(\frac{F_x}{F} \right)$$

$$\beta = \cos^{-1} \left(\frac{F_y}{F} \right)$$

$$\gamma = \cos^{-1} \left(\frac{F_z}{F} \right)$$