## 21-R-WE-SS-35

A rocket (m=1  $\times$  10<sup>6</sup> kg) launches from the surface of Earth to an altitude of h = 100 km. Assuming that no mass is lost (a highly unrealistic assumption), how much work is done against gravity?

The force of gravity over large distances is given by  $F = \frac{GMm}{r^2}$ , where  $G = 6.67 \times 10^{-11} Nm^2/kg^2$ , M and m are the masses of Earth and the rocket, and r is the distance between the centers of the two objects.

The Earth has a radius of r = 6730 km and a mass of  $5.97 \times 10^{24}$  kg.

## Solution

Work is the integral of force over a distance. Knowing this it's pretty easy to find work done

$$F = \frac{GMm}{r^2}$$

$$W = \int_{r_1}^{r_2} F dx$$

$$= \left[ -\frac{GMm}{r} \right]_{6730 \times 10^3}^{(6730 + 100) \times 10^3}$$

$$= 8.66 \times 10^{11} \quad [\text{ J}]$$