

Two forces  $\overrightarrow{F_1}$  and  $\overrightarrow{F_2}$  have magnitudes of  $F_1$  and  $F_2$  respectively. If  $\overrightarrow{F_1}$  has coordinate angles of  $\alpha_1$ ,  $\beta_1$ , and  $\gamma_1$ , and  $\overrightarrow{F_2}$  has coordinate angles of  $\alpha_2$ ,  $\beta_2$ , and  $\gamma_2$ , express both forces as cartesian vectors.

$$\overrightarrow{F}_1 = F_1(\cos(\alpha_1)\hat{i} + \cos(\beta_1)\hat{j} + \cos(\gamma_1)\hat{k})$$

$$\overrightarrow{F_2} = F_2(\cos(\alpha_2)\hat{i} + \cos(\beta_2)\hat{j} + \cos(\gamma_2)\hat{k})$$

Find the magnitude and coordinate direction angles of the resultant force when adding both forces (disregard the rest of the system).

$$F_{Rx} = F_1 \cos(\alpha_1) + F_2 \cos(\alpha_2)$$

$$F_{Ry} = F_1 \cos(\beta_1) + F_2 \cos(\beta_2)$$

$$F_{Rz} = F_1 \cos(\gamma_1) + F_2 \cos(\gamma_2)$$

$$F_R = \sqrt{F_{Rx}^2 + F_{Ry}^2 + F_{Rz}^2}$$

$$\alpha_R = \cos\left(\frac{F_{Rx}}{F_R}\right)$$

$$\beta_R = \cos\left(\frac{F_{Ry}}{F_R}\right)$$

$$\gamma_R = \cos\left(\frac{F_{Rz}}{F_R}\right)$$