

For solution consider $|F| = 20 \text{ N}$ for $\Delta t = 0.5 \text{ s}$
each mass $m = 3 \text{ kg}$. $b = 0.5 \text{ m}$

Magnitude of momentum gained from impulse:

$$\Delta p = F \cdot \Delta t = (20 \text{ N})(0.5 \text{ s}) = 10 \text{ kg m/s} = 10 \text{ N s}$$

We also know that $p = mv$

in this case, $\Delta p = 2m \Delta v$ since $v_i = 0$:

$$\Delta p = 2m v = F \cdot \Delta t$$

$$\Rightarrow v = \frac{\Delta p}{2m} = \frac{10 \text{ N s}}{2 \cdot 3 \text{ kg}} = 5/3 = \underline{\underline{1.667 \text{ m/s}}} \quad \underline{\underline{\text{linear velocity}}}$$

Now for angular velocity, use:

$$I_G \omega_1 + \sum \int_{t_1}^{t_2} \mathbf{p}_G dt = I_G \omega_2$$

Where I_G is the moment of inertia, p_G is the momentum, (about the centre of the dumbbell), and ω_1 and ω_2 are the initial and final angular velocities.

$$t_1 = 0, \quad t_2 = \Delta t = 0.5 \text{ s}; \quad \omega_1 = 0.$$

$$I_G = \sum m_i r_i^2 = m \cdot b^2 + m b^2 = 2mb^2$$

$$\Rightarrow \cancel{I_G(0)} + \Delta p \cdot \Delta t = I_G \omega_2$$

$$\omega_2 = \frac{\Delta p \cdot \Delta t}{I_G} = \frac{(10)(0.5)}{2(3)(0.5)^2} = 10/3 = \underline{\underline{3.333 \text{ rad/s}}} \quad \underline{\underline{\text{Angular velocity}}}$$