Computer Creativity

Interactions, Events, Variables and Math

UBC

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Announcements

- Test 2 is next week on Wednesday!

- Remember, all Bonus Tests need to be scheduled using PrairieTest!

- Additional References on Bezier Curves
  - Ref 1: Intro to Beziers
  - Ref 2: Documentation
  - Ref 3 (Advanced): Math of Bezier Curves)

Objectives

- You should be able to:

    - Define value, variable, and memory location

    - Create and use variables of different data types

    - recognize the naming rules and guidelines for variables.

    - List and compare the data types in processing.

    - Define and use the "color" type.

    - Creating and using constants.

    - Properly use math operators.
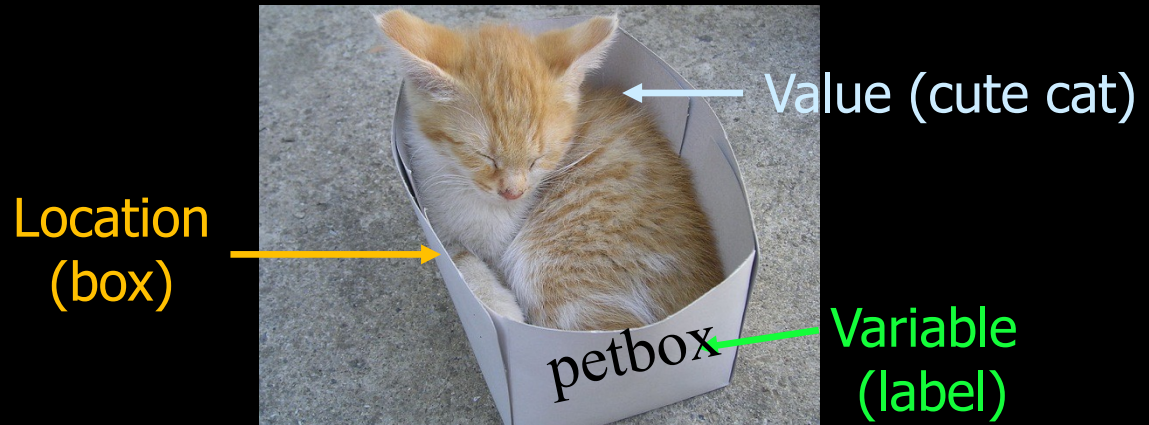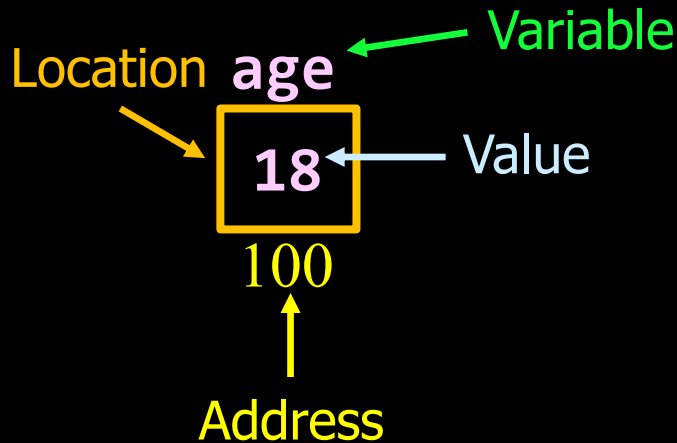
    - Evaluate math expressions.

Review on Variables

Values, Variables, and Locations

- A *value* is a data item that is manipulated by the computer.

- A *variable* is the name that the programmer uses to refer to a location in memory.

- A *location* has an address in memory and stores a value.

Variable → **age** (Location)

Location → **18** ← Value

100 (Address)

Value (cute cat)

Location (box)

Variable (label) → petbox

Values, Variables, and Locations

- Let's say we want to store a number that represents the age.
  - **Step #1**: *Declare* variable by giving it a ***NAME*** and a ***TYPE***.

    ```
    int age;    // age can only store integers
    ```
    - The computer allocates space for the variable in memory (at some memory address). Every time we give the name `age`, the computer knows what data item we mean.

  - **Step #2**: *Initialize* the variable to have a starting value. E.g.,
    ```
    age = 21;
    ```

  - **Step #3**: Value stored in a location can be changed throughout the program to whatever we want using *assignment* ("=" symbol).
    ```
    age = age + 3;
    ```

Memory

16   ~~???~~ ~~21~~ 24
20
24

Variable Name Lookup Table

Name	Location	Type
age	16	int

Variable Name

- A variable must have a **<u>NAME</u>** and a **<u>TYPE</u>**.

- Names (aka **identifiers**):
  - **are case sensitive** (*B* is not the same as *b*)
  - can be a sequence of characters that include only *letters*, *digits*, *underscores* (_), and *dollar signs* ($).
  - must start with a letter, an underscore (_), or a dollar sign ($).
    - cannot start with a digit.
  - can **not** be a reserved word.
    - E.g. cannot be called double, true, false, or null.
  - Naming guidelines
    - can be of any length, but reasonable (readable) length is preferred.
    - should start with a lower case letter.
    - if more than one word, remove the spaces and capitalize all words after the first one (e.g. my first car → `myFirstCar`)

Variable Type

- A variable must have a *name (identifier)* and a *<u>type</u>*. Each type has a valid range of values and uses a different amount of memory space.

	Type	Size in memory	Range
whole numbers	`byte`	8 bits	-2^7 to 2^7-1 (-128 to 127)
	`short`	2 bytes	-2^{15} to $2^{15}-1$ (-32768 to 32767)
	`int`	4 bytes	-2^{31} to $2^{31}-1$
	`long`	8 bytes	-2^{63} to $2^{63}-1$
real numbers	`float`	4 bytes	e.g. 17.345f
	`double`	8 bytes	e.g. 12452.212 (more accurate)
characters	`char`	2 bytes	e.g. 'a', '1'and '?'
boolean	`boolean`	1 byte	true or false

- *Note*: Unlike JavaScript, where you don't specify a type (i.e. just use `var`), in Java (and Processing) you must specify the variable type.

The String Type

- **Strings** are sequences of characters inside double quotes (i.e. text in double quotes).

- Example:

```
String personName = "Abdallah Mohamed";
personName = "John Smith";
```

  - The first statement creates (defines) a variable and initializes its value to "Abdallah Mohamed".
  - The second statement is assigns a new value to existing variable.

- The **concatenation operator** is used to combine two strings into a single string. The notation is a plus sign '**+**'.

```
String firstName = "Abdallah", lastName = "Mohamed";
String fullName = firstName + lastName;
```

The Color Type

- Processing introduces a new data type called **color** which stores color information. The value of a color variable can be set by the **color()** function.

```
color red = color(255,0,0);        // red in RGB mode
color navy = color(#443F76);       // navy in hex notation (RGB)

colorMode(HSB,360,100,100);

color green = color(128,100,100);// green in HSB mode
color blue = color(#0011FF);       // blue in hex notation (RGB)

background (navy);      // navy background

fill(red);
rect(10,10,40,40);      // red square

fill(green);
rect(50,50,40,40);      // green square

fill(blue);
ellipse(75,25,30,30); // green square
```

red uses RGB as it was defined before changing the color mode

blue uses RGB even though it was defined after setting the color mode because **blue** was defined using hex notation

Example 1

Declaring and Initializing Variables

```
// Declaring Variables
double a;       // Declare a to be a double variable
int x, y;       // Declare x and y as integer variables

// Assignment Statements
a = 7.1;        // Assign 7.1 to a;
x = 1 + 3;      // assign 4 to x;
y = x + 2;      // assign 6 to y;

// Declaring and Initializing in ONE Step
double a2 = 7.1;
int x2 = 1, y2 = 2;
```

Example 2

Using Variables

▫ Here are two more examples of two variables x and y

```
int x;                  // declare a variable
x = 5;                  // initialize a variable – what is assignment '='?
int y = 10;             // declare and initialize a variable
println(x);             // print value of x
x = 10;                 // overwrite old value
println("x " + x);    //what is the output?
```

```
int x = 10, y;          // y has no values yet
y = x;                  // y is 10 now
y = y + 1;              // = does not mean equal, it means assignment.
println("x + y = " + (x + y));   //notice the output
```

Constants

- Constants are similar to variables except that once initialized they cannot change.

- To create a constant, use the keyword **`final`** before your variable declaration.

```java
final double PI = 3.14159;
final int SIZE = 3;
```

- Naming Convention:
  - Capitalize all letters in constants
    - e.g. `MAX`, `PI`, `SIZE`
  - Use underscores for multiple words.
    - e.g. `MAX_VALUE`

Expressions

The Assignment Statement

- An ***assignment statement*** changes the value of a variable.

  - The variable on the left-hand side of the **=** is assigned the value from the right-hand side.

  - The value may be changed to a constant, to the result of an expression, or to be the same as another variable.

  - The values of any variables used in the expression are always their values before the start of the execution of the assignment.

- Example:

  ```
  int A, B;
  A = 5;
  B = 10;
  A = 10 + 6 / 2;
  B = A;
  A = 2*B + A - 5;
  ```

  Question: What are the values of A and B?

Expressions

- An ***expression*** is a sequence of operands and operators that yield a result. An expression contains:
  - ***operands*** - the data items being manipulated in the calculation
    - e.g. `5, "Hello, World", myDouble`
  - ***operators*** - the operations performed on the operands
    - e.g. `+, -, /, *, %` (modulus or remainder after integer division)

- An operator can be:
  - ***unary*** - applies to only one operand
    - e.g. `d = -3.5;` // "-" is a unary operator, 3.5 is the operand
  - ***binary*** - applies to two operands
    - e.g. `d = 3 * 5.0;` // "*" is binary operator, 3 and 5.0 are operands

- ***Integer Division:***
  - 5 / 2   if both operands are integers, the output is an integer 2
  - 5.0 / 2   if at least one operand is float, output is float 2.5

Division Operator

- What is the result of 25 / 4?

- How would you rewrite the expression if you wished the result to be a floating-point number?

- Are the following statements correct? If so, show the output.

```
println("25 / 4 is " + 25 / 4);
println("25 / 4.0 is " + 25 / 4.0);
println("3 * 2 / 4 is " + 3 * 2 / 4);
println("3.0 * 2 / 4 is " + 3.0 * 2 / 4);
```

The Remainder Operator (%)

- The % operator returns the remainder of two numbers.

- Examples:

Operation	Result
a) 14 % 6	2
b) -34 % 5	- 4 (matches numerator sign)
c) -34 % -5	- 4
d) 34 % -5	4
e) 5 % 1	0
f) 1 % 5	1
g) 3 % 0	runtime error. Can't divide by zero

Operator Precedence

- Each operator has its own priority similar to their priority in regular math expressions:

  1. Any expression in parentheses is evaluated first starting with the inner most nesting of parentheses.

  2. Unary + and unary - have the next highest priorities.

  3. Multiplication and division (*, /, %) are next.

  4. Addition and subtraction (+,-) are then evaluated.

The ++ and -- Operators

▫ It is very common to subtract 1 or add 1 from the current value of an integer variable.

▫ There are two operators which abbreviate these operations:
  ▫ ++   add one to the current integer variable
  ▫ --   subtract one from the current integer variable

▫ Example:

```
int j=0;

j++;        // j = 1;   Equivalent to j = j + 1;

j--;        // j = 0;   Equivalent to j = j - 1;
```

Augmented Assignment

- The operators +, -, *, /, and % can be combined with the assignment operator = to form augmented operators.

```
x += 5;    //Equivalent to   x = x + 5
x -= 5;    //Equivalent to   x = x - 5
x *= 5;    //Equivalent to   x = x * 5
x /= 5;    //Equivalent to   x = x / 5
x %= 5;    //Equivalent to   x = x % 5
```

Summary

- The pre-class materials covered the following:
  - *Variables and Data types*
    - *Primitive types:* `byte, short, int, long, float, double, char, boolean`
    - *New types:* `color`
    - `String` *type*
  - *Naming rules and guidelines (for variable and constants)*
  - *Math operators and expressions.*
    - *Binary operators:*   `+, -, *, /, %`
    - *Unary operators:*   `-3, x++, y--`
    - *Augmented assignment:* `-=, +=, /=, *=, %=`

Variable Scope

Variable Scope

- The **scope** of a variable is the part of the program where you can access or use the variable.

- **Local variables** are those defined in functions and can be only accessed inside this function.

- **Global variables** are those defined outside functions – all functions can access global variables.

Example 1

Variable Scope

This program increases the rectangle size every time a key is pressed.

```
int size = 10;

void setup(){
  size(200,200);
}

void draw(){
  int x = 100, y = 100;
  rectMode(CENTER);
  rect(x,y,size,size);
}

void keyPressed(){
  size += 5;
}
```

Global variable:
Declared outside all functions.
ALL functions can access `size`

Local variables:
Declared within a function.
Only this function can access `x` and `y`

`size` increases when a key is pressed, then draw uses the new value of `size`.

Variable Scope

Why does this code have a compile error?

A. We cannot have a variable called `size`

B. We need to specify a type for the variable y (i.e. `int y = 100`)

C. `draw()` and `keyPressed()` cannot access `x` or `y`.

D. The variable `size` must be defined as global variable.

E. Something else.

```
void setup(){
  int x = 10, y = 10;
  size(200,200);
}

void draw(){
  int size = 50;
  rect(x, y, size, size);
}

void keyPressed(){
    x += 20;
    y += 20;
}
```

Controlling Animations with Variables

Controlling Animations with Variables (1)

- Variables can be used to control many aspects of your animation.

- The key idea is to store some ***attributes*** of your sketch in global variables and update them:

  (a) every frame (e.g. x++ in the draw() method), *and/or*

  (b) whenever an event happens (e.g. x=0 whenever a key is pressed)

Controlling Animations with Variables (2)

- Example attributes include
  - Position
    - Use variables, e.g. x and y, to store the position.
  - Angle
    - Use a variable to store an angle. Use that variable to transform the shape coordinates using the rotate() function.
  - Scale
    - IDEA1: use a variable to store scale, and use it to transform coordinates
    - IDEA2: use variables to store scale and use it as a multiplicand to control the size of the shape/item.
  - Color
    - Use variables to store color components.
  - …etc

(a) updating attributes every frame

Example 2

Moving Square

- Here, we use a global variable x to control the x-position of the square. The variable is incremented in every frame.

- Question:
  - What happens if we declare and initialize x in
    - A) setup() ?
    - B) draw() ?

```
int x=0;

void setup(){

  size(200,200);

}

void draw(){

  background(100);

  rect(x, 75, 50, 50);

  x++;

}
```

Example 3

Revolving Wheel

- Previously, you created the design below.

- We can animate the angle of of the rotation using a variable dr that is updated in every frame.
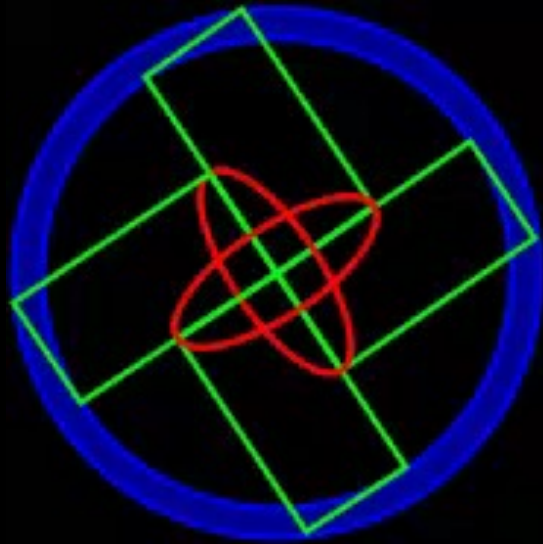
- You try it now!
  - *No need to submit anything yet to Canvas*

```
float dr = 0;
void setup(){
  size(300,300);  strokeWeight(2);
}
void draw(){
  background(0);
  translate(150,150);   // move origin to center
  // outer rings
  fill(0,0,150);stroke(0,0,255);ellipse(0,0,180,180);
  fill(0); stroke(0,0,255); ellipse(0,0,160,160);
  // green rectangles and red ellipses
  noFill();
  rotate(dr);
  stroke(0,255,0); rect(0,0,80,40);
  stroke(255,0,0); ellipse(0,0,80,30);
  rotate(PI/2);
  stroke(0,255,0); rect(0,0,80,40);
  stroke(255,0,0); ellipse(0,0,80,30);
  rotate(PI/2);
  stroke(0,255,0); rect(0,0,80,40);
  stroke(255,0,0); ellipse(0,0,80,30);
  rotate(PI/2);
  stroke(0,255,0); rect(0,0,80,40);
  stroke(255,0,0); ellipse(0,0,80,30);
  dr += 0.02;
}
```

Example 4

Moving Objects at Given Speed

- A good idea to show moving objects is to use two variables **x** and **y** for the location, and add to them a small displacement, **speedX** and **speedY**, every frame.

- In the example, the object moves to the right only.
  - *Q1*: **WHY?**
  - *Q2:* make the object move upwards only.
  - *Q3:* make the object move diagonally.

- We will see later how to change the speed in the runtime.

```
float x, y, diam = 16;
float speedX = 1, speedY = 0;

void setup(){
  size(200,200);
  x = 0;
  y = height/2;
}


void draw(){
  background(0);
  ellipse(x, y, diam, diam);
  x = x + speedX;
  y = y + speedY;
}
```

Example 5

Animating Size and Opacity

◻ Here, we control the circle using four variables.

  ◻ radius and opacity change at the end of each frame, causing the next frame to appear differently.
  ◻ location (x,y) is not changed.

◻ **Question**: modify the code so that the circle moves from the top-left corner to the bottom-right corner.

```
float radius = 10, opacity = 255;
float x = 75, y = 75;

void setup() {
  size(150, 150);
  noStroke();
}

void draw() {
  background(0);
  fill(255, opacity);
  ellipse(x, y, radius, radius);
  radius++;
  opacity--;
}
```

(b) updating attributes with events

Example 6

Controlling Speed with Mouse & Key Events

- This examples initially draws a rectangle in the middle of the sketch

- Clicking the mouse button will cause it to start moving left.

- Pressing a key on the keyboard will cause it to start moving right.

```
int x = 75, speedX = 0;
void setup(){
  size(400,200);
}
void draw(){
  background(100);
  rect(x, 75, 50, 50);
  x += speedX;
}
void keyPressed(){
  speedX = 2;
}
void mousePressed(){
  speedX = -2;
}
```

Example 7

Controlling Colors with Mouse & Key Events

- This examples initially draws a black circle on a white background.

- Clicking the mouse button brightens a circle.

- Pressing a key on the keyboard dims the background.
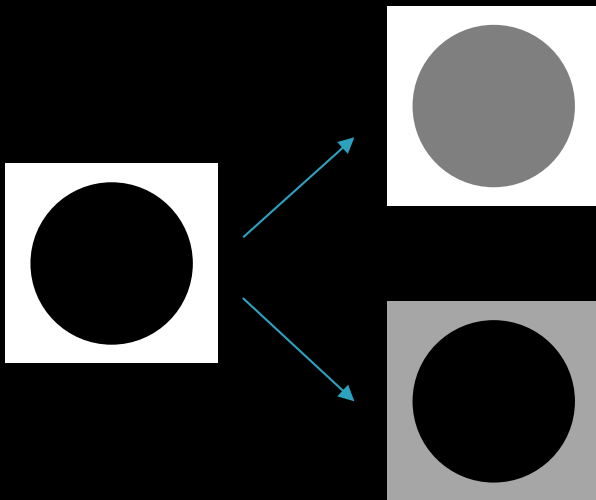
```
int background = 255, foreground = 0;

void setup() {
  size(100, 100);
}

void draw() {
  background(background);
  fill(foreground);
  ellipse(50,50,80,80);
}

void keyPressed() {
  background -= 10;
}

void mousePressed() {
  foreground += 10;
}
```

Example 7

Panning the Sketch with the Mouse

- When mouse is ***dragged***, x and y are updated with the relative mouse displacement.
  - i.e. the difference between current mouse location and the previous mouse location.
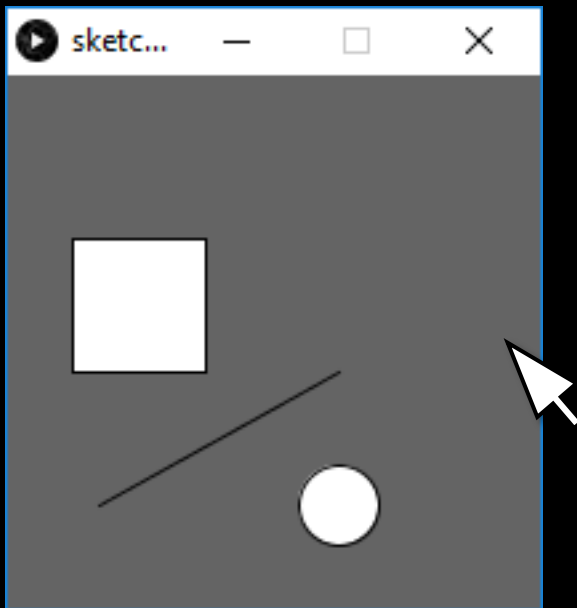
```
int x=0, y=0;

void setup(){
  size(200,200);
}
void draw(){
  background(100);
  translate(x,y);
  rect(0,0,50,50);
  ellipse(100,100,30,30);
  line(10,100,100,50);
}

void mouseDragged(){
  x += mouseX - pmouseX;
  y += mouseY - pmouseY;
}
```

Example 8 (Aside)

also Zooming…!

- ◘ This is the same code as before except that another variable is used to zoom in and out (scale the sketch).

- ◘ This variable is updated based on the mouse wheel rotation.
  - ◘ The **mouseWheel()** function:
    - ▪ This function is automatically called whenever the mouse wheel rotates.
    - ▪ The e.getCount() returns 1 or -1 every time the mouse wheel is rotated up or down.

```
int x=0, y=0;
float scl = 1.0;
void setup(){
  size(200,200);
}
void draw(){
  background(100);
  translate(x,y);
  scale(scl);
  rect(0,0,50,50);
  ellipse(100,100,30,30);
  line(10,100,100,50);
}
void mouseDragged(){
  x += mouseX - pmouseX;
  y += mouseY - pmouseY;
}
void mouseWheel(MouseEvent e){
  scl -= e.getCount()/10.0;
}
```

Example 9

Moving/Dragging Items

- In this example, we have 4 variables to store the location of the mouse.

- "moving" text is using the first two which are set whenever the mouse is moved

- "dragging" text is using the dragX and dragY which are set whenever the mouse is dragged.
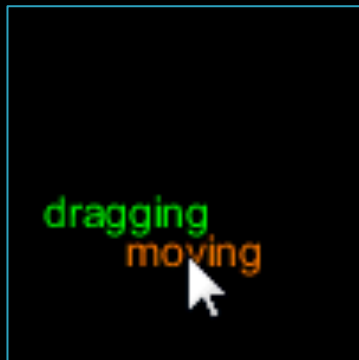

```
int moveX = 50, moveY = 50;
int dragX = 50, dragY = 50;
void setup() {
  size(100, 100);
  textAlign(CENTER);
}
void draw() {
  background(0);
  fill(255,125,0);
  text("moving", moveX, moveY);
  fill(0,255,0);
  text("dragging", dragX, dragY);
}
void mouseMoved() {  // Move the text "Moving"
  moveX = mouseX;
  moveY = mouseY;
}

void mouseDragged(){  // Move the text "Dragging"
  dragX = mouseX;
  dragY = mouseY;
}
```

Computer Creativity

Animations

Computer Creativity

Quick Tutorial on Animations

Key Idea 1: How to Animate "Things"

- A question is: *how to animate "Things" in your sketch?*
  - "Things" are basically the attributes of different items such as the color, location, transformation, size, etc.

- Here are the process you need to follow:
  (1) Identify which attributes you want to animate (e.g. size, color, location, etc.)
    - you may want to use the PDE's Tweak tool to help you identify the right attribute.
  (2) for each attribute you want to animate, create and initialize a global variable.
  (3) In `draw()`, use the global variables to represent the attributes.
  (4) Change the value of your global variables either:
    - in `draw()`
      - For continuous animation (e.g. falling rain drops).
    - in an event function (e.g. `keyPressed()`)
      - For interactive animations (e.g. controlling character position with keyboard)

Example 1

Animation Tutorial 1

- Let's say you have a white circle on a dark background.
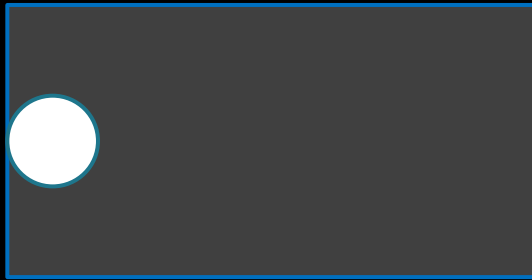
```
void setup() {
  size(600, 200);
}
void draw() {
  background(80);
  ellipse(25, 100, 50, 50);
}
```
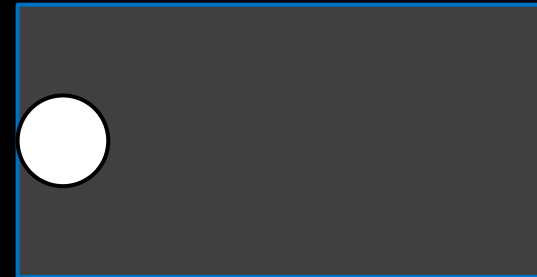
- And let's say we want two things to be animated:
  - The background to get lighter
  - The ball to move from left to right

Example 1

Animation Tutorial 1, cont'd

Step (1) Identify the attributes that we should change, i.e. the background color and the x-location of the ball.

```
void setup() {
   size(600, 200);
}
void draw() {
   background(80);
   ellipse(25,100,50,50);
}
```

Step (2) create two global variables, one for each attributes.

```
int c = 80, x = 25;
void setup() {
   size(600, 200);
}
void draw() {
   background(80);
   ellipse(25,100,50,50);
}
```

Step (3) use the variables for the attributes values

```
int c = 80, x = 25;
void setup() {
   size(600, 200);
}
void draw() {
   background(c);
   ellipse(x,100,50,50);
}
```

Step (4) Update your variables

```
int c = 80, x = 25;
void setup() {
   size(600, 200);
}
void draw() {
   background(c);
   ellipse(x,100,50,50);
   x = x + 2;
   c = c + 1;
}
```

45

Key Idea 2: Controlling Speed

- Let's have a look at the following code below. Obviously, the x's increment value controls the speed of the ball.
  - The speed is just another attribute in your sketch.

```
int x = 25;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + 1;
}
```
Slow movement

```
int x = 25;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + 3;
}
```
faster movement

```
int x = 25;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + 6;
}
```
fastest movement

- The following is the same code above after replacing the increment value with a speed variable

```
int x = 25, speedX = 1;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + speedX;
}
```
Slow movement

```
int x = 25, speedX = 3;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + speedX;
}
```
faster movement

```
int x = 25, speedX = 6;

void draw() {
  background(80);
  ellipse(x,100,50,50);
  x = x + speedX;
}
```
fastest movement

Key Idea 2: Controlling Object's Speed

- Now that we have the speed attribute stored in a variable, you can control it by updating its value either in draw() or other event functions.

```
float x = 25, speedX = 0;
void setup() {
  size(800, 200);
}
void draw() {
  background(80);
  ellipse(x,100,50,50);
  //update variables
  x = x + speedX;
  speedX += .4;
}
```

Ball gradually
increase its speed

```
float x = 25, speedX = 0;
void setup() {
  size(800, 200);
}
void draw() {
  background(80);
  ellipse(x,100,50,50);
  //update variables
  x = x + speedX;
  speedX = 0.01 * mouseX;
}
```

speedX is controlled
by mouseX

```
float x = 25, speedX = 0;
void setup() {
  size(800, 200);
}
void draw() {
  background(80);
  ellipse(x,100,50,50);
  //update variables
  x = x + speedX;
}
void mousePressed() {
  speedX = 3;
}
void mouseReleased() {
 speedX = 0;
}
```

Ball only moves when
mouse is clicked

Move Your Wheel!

- Create an animation where the speed and rotation of the wheel are controlled by `mouseX`.
  - When mouseX is 0, the wheel freezes.
  - The higher value mouseX is, the faster the wheel moves to the right while rotating.

- When any key is pressed, the wheel's location is reset (far left) and it stops rotation.

- *Idea*: Reuse the code of the wheel presented in last lecture's notes:
  - declare two variables: x and dr and initialize both to 0.
  - Use the two variables to *transform* your wheel.
  - Both variables should be updated every frame using mouseX.
  - Whenever a key is pressed, both variables should be set to 0.
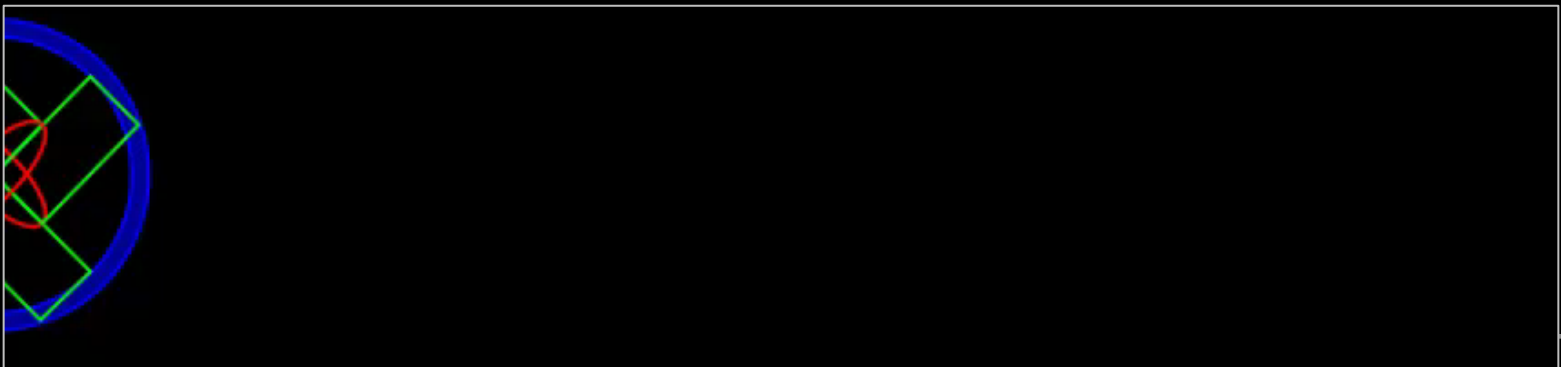
System Variables

System Variables

- We have seen some system variables, such as `mouseX` and `mouseY`, that hold useful values. Here is a longer list of commonly used system variables:

`mouseX`,`mouseY`	Mouse location
`width`,`height`	Sketch size (in pixels)
`displayWidth`, `displayHeight`	Entire screen size (in pixels)
`frameCount`	Number of frames displayed so far.
`frameRate`	the current frame rate.
`key`	The most recent key used on the keyboard. e.g. 'a', 'b', '!', ' ', ...
`keyCode`	The code of the most recent key used on the keyboard. *Useful for special keys, e.g.* UP, LEFT, SHIFT, ALT, ...
`keyPressed`	`true` or `false` based on whether a key is pressed.
`mouseButton`	LEFT, RIGHT, or CENTER, based on which mouse button is pressed
`mousePressed`	`true` or `false` based on whether mouse is pressed.

Example 1

System Variables to Control Animation

▫ This program draws a circle at the sketch center (determined by `width` & `height`) and writes some text on the top-left corner.

▫ The color and transparency are gradually changed using `framecount`.

▫ The program also ***reads the user's input*** using `key` and `keyPressed()`.

```
String msg = "You wrote: ";
void setup() {
  size(400, 200);
  colorMode(HSB);
  textSize(26);
  noStroke();
}
void draw() {
  background(0);
  fill(frameCount % 255 , 255, 255);    //color changes
  text(msg, 10 ,30);
  fill(255,255,255,frameCount);         //smooth appearance
  ellipse(width/2, height/2, 80, 80);   //center of sketch
}
void keyPressed() {
  msg += key;                           //read user's input
}
```

You wrote: abcd

Example 1

System Variables to Make Decisions

▫ You wrote code for the following program in a previous class using mouse-event methods. The same output can be produced using system variables (simpler code) .

▫ Create a program that draws a circle which follows the mouse (same location as the mouse)

▫ The circle should be:
  ▫ red with thick, yellow outline as long as the mouse is pressed.
  ▫ green with thin, white outline as long as the mouse is not pressed.
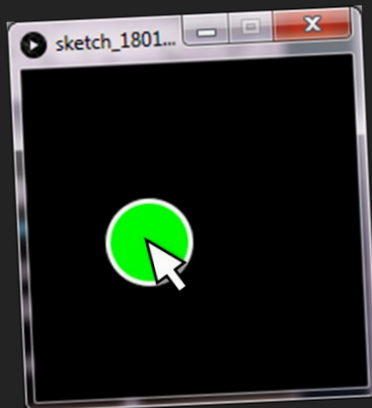
Mouse key is not pressed
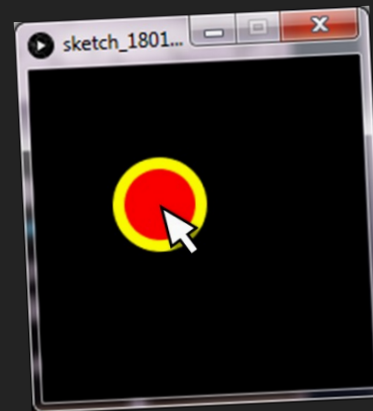
Mouse key is pressed

Example 1 (cont'd)

System Variables to Make Decisions, cont'd

```
void setup(){
  size(200,200);
  fill(0,255,0);
  stroke(255);
  strokeWeight(2);
}
void draw(){
  background(0);
  ellipse(mouseX,mouseY,40,40);
}
void mousePressed(){
  fill(255,0,0);
  stroke(255,255,0);
  strokeWeight(4);
}
void mouseReleased(){
  fill(0,255,0);
  stroke(255);
  strokeWeight(2);
}
```

➡

```
void setup() {
  size(200,200);
}
void draw() {
  background(0);
  if (mousePressed) {
    fill(255, 0, 0);
    stroke(255, 255, 0);
    strokeWeight(4);
  } else {
    fill(0, 255, 0);
    stroke(255);
    strokeWeight(2);
  }
  ellipse(mouseX, mouseY, 40, 40);
}
```

Simpler code.

Built-in Math Functions

Mathematical Functions

▫ You have used the math function abs() before to produce an absolute value of a given number. Here is a list of more functions that you can use in your computations.

Function	Example	Function	Example
`abs()`	`d = abs(-4);     // 4`	`max()`	`d = min(2,7);   // 7`
`round()`	`d = round(2.6); // 3`	`min()`	`d = min(2,7);   // 2`
`floor()`	`d = floor(2.9); // 2`	`sin()`	`d = sin(PI/6); // 0.5`
`ceil()`	`d = ceil(2.3);   // 3`	`cos()`	`d = cos(PI/3); // 0.5`
`pow()`	`d = pow(2,3);    // 8`	`tan()`	`d = tan(PI/4); // 1`
`sq()`	`d = sq(-3);       // 9`	`asin()`	`d = asin(0.5); // $\pi$/6`
`sqrt()`	`d = sqrt(9);      // 3`	`acos()`	`d = acos(0.5); // $\pi$/3`
`dist()`	`d=dist(0,0,3,4);// 5`	`atan()`	`d = atan(1.0); // $\pi$/4`

This one is particularly useful when developing games. We won't use it today, but just remember it for future lectures!

Angles in Processing

- Many Processing functions, e.g. trigonometric `sin()` & `cos()` and transformation's `rotate()` functions, take an angle argument *in radians*.
  - `sin(PI/6)` is `0.5`
  - `rotate(PI/4)` rotates the coordinates by 45 degrees.

- `degrees()` and `radians()` can be used to convert from degrees to radians and vise versa.
  - `degrees(PI/2)` is `90`.
  - `radians(90)` is `PI/2`

- *Note*: the inverse of the trigonometric functions, i.e. `asin()`, `acos()`, `atan()`, take any value from $-\infty$ to ∞ and output the corresponding angle in radians.
  - e.g. `asin(0.5)` is `PI/6` (i.e. $\pi/6$)

Example 2

Computing Motion Paths

```
float x=0, y=0;
void setup(){
    size(200,200);
    background(0);
    noStroke();
}
void draw(){
    translate(0,height/2);
    y = 30 * sin(x*4*PI/width);
    ellipse(x, y, 5, 5);
    x++;
}
```

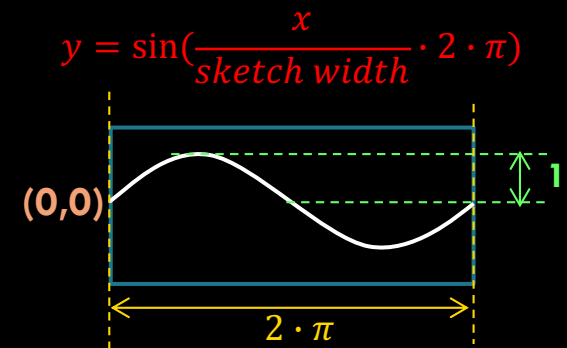This code moves a ball from left to right along a sinusoidal path.

The idea:

◘ 1) x is incremented by 1 after every frame, moving the ball from left to right.

◘ 2) for every x value, y is computed using the following expression which produces 2 full sinusoidal waves:

$$y = 30 \cdot \sin(\frac{x}{sketch\ width} \cdot 4 \cdot \pi)$$

◘ To make things easier, the coordinate is translated so that the origin (0,0) is at the middle of the left edge

$$y = \sin(\frac{x}{sketch\ width} \cdot 2 \cdot \pi)$$

(0,0)

$2 \cdot \pi$

1

$$y = 30 \cdot \sin(\frac{x}{sketch\ width} \cdot 4 \cdot \pi)$$

(0,0)

30

$2 \cdot \pi$

Example 3

Nice Idea for Games!

- The motion paths for different items in a game could be computed using the same idea presented in the previous example.

- The code shown is very similar to the previous slide, except that it moves 3 triangles (could be enemy ships in a side-scrolling game) along the same sinusoidal path.
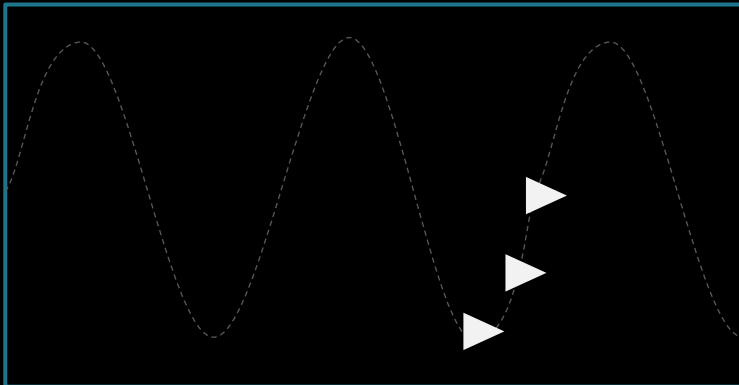
```
float x1=0,y1=0,x2=-20,y2=0,x3=-40,y3=0;
void setup(){
  size(400,200); noStroke(); fill(255);
}
void draw(){
  background(0);
  translate(0,height/2);
  //first spaceship
  y1 = 30 * sin(x1*6*PI/width);
  triangle(x1, y1-5, x1, y1+5, x1+10, y1);
  x1++;
  //second spaceship
  y2 = 30 * sin(x2*6*PI/width);
  triangle(x2, y2-5, x2, y2+5, x2+10, y2);
  x2++;
  //third spaceship
  y3 = 30 * sin(x3*6*PI/width);
  triangle(x3, y3-5, x3, y3+5, x3+10, y3);
  x3++;
}
```

Paths Defined by an Equation

▪ Do you understand this animation?
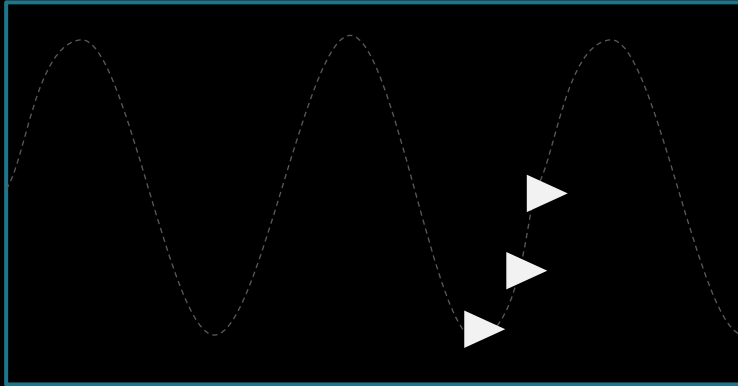
```
float x1=0,y1=0,x2=-20,y2=0,x3=-40,y3=0;
void setup(){
  size(400,200); noStroke(); fill(255);
}
void draw(){
  background(0);
  translate(0,height/2);
  //first spaceship
  y1 = 30 * sin(x1*6*PI/width);
  triangle(x1, y1-5, x1, y1+5, x1+10, y1);
  x1++;
  //second spaceship
  y2 = 30 * sin(x2*6*PI/width);
  triangle(x2, y2-5, x2, y2+5, x2+10, y2);
  x2++;
  //third spaceship
  y3 = 30 * sin(x3*6*PI/width);
  triangle(x3, y3-5, x3, y3+5, x3+10, y3);
  x3++;
}
```

▪ What if we want to have another group of ships going in the opposite direction or following a different path? How about you also add the player's own spaceship which is controlled by the mouse?
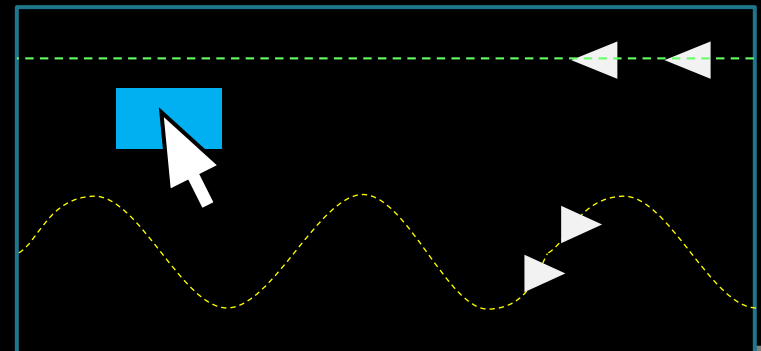
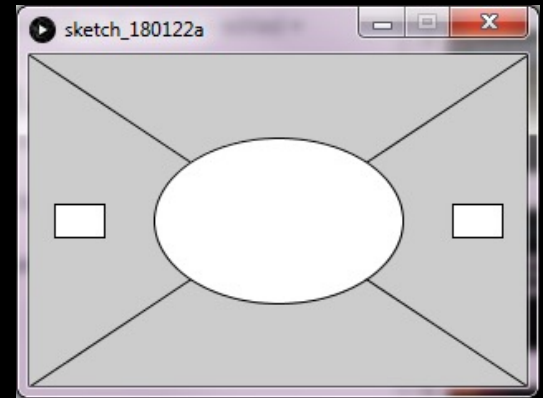# *Using System Variables* (based on the textbook)

- Write code to produce the following sketches so that the code for all three is EXACTLY the same except for the size() statement.

- That is, the shapes must resize themselves relative to the window size. No matter what you specify for size(), the result should look identical!

- *Hint*: use width and height to determine the shapes location and size.
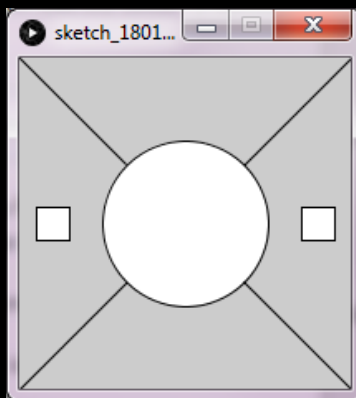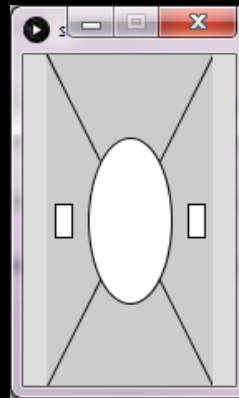
`size(200,200)`   `size(100,200)`   `size(300,200)`

Analogue Clock

- Write code to animate the seconds hand in a clock

$$\theta = \left(\text{second()} * \frac{PI}{30} \right) - \frac{PI}{2}$$

- How about we now add the minutes and the hours hands?

(0,0)

θ

r

(x,y)