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# Physics 111 - Class 8A

## Work & Kinetic Energy

October 25, 2021

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# Class Outline

- Logistics / Announcements
- Introduction to Chapter 7
- Clicker Questions
- Activity: Worked Problems

# Logistics/Announcements

- Lab this week: Lab 5
- HW7 due this week on Thursday at 6 PM
- Learning Log 7 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Test 3 on Friday this week (Chapters 5 & 6)

VIDEO 1
<input type="checkbox"/> Video 2
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## Physics 111

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Unsyllabus

### ABOUT THIS COURSE

Course Syllabus (Official)

Course Schedule

Accommodations

How to do well in this course

### GETTING STARTED

Before the Term starts

After the first class

In the first week

Week 1 - Introductions!

### PART 1 - KINEMATICS

Week 2 - Chapter 2

Week 3 - Chapter 3

Week 4 - Chapter 4

### PART 2 - DYNAMICS

## Work, Energy, and Power



Work, Energy, and Power: Crash Course Physics #9



# WORK, ENERGY, AND POWER



Watch on YouTube

## Required Videos

### 1. Introduction to Work with Examples



Introduction to Work with Examples

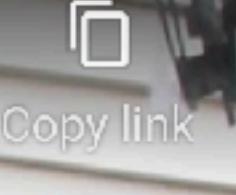


Table of contents



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My highlights

Preface

▼ Mechanics

- ▶ 1 Units and Measurement
- ▶ 2 Vectors
- ▶ 3 Motion Along a Straight Line
- ▶ 4 Motion in Two and Three Dimensions
- ▶ 5 Newton's Laws of Motion
- ▶ 6 Applications of Newton's Laws
- ▶ 7 Work and Kinetic Energy

**Introduction**

- 7.1 Work
- 7.2 Kinetic Energy
- 7.3 Work-Energy Theorem
- 7.4 Power

▶ Chapter Review

- ▶ 8 Potential Energy and Conservation of Energy
- ▶ 9 Linear Momentum and Collisions
- ▶ 10 Fixed-Axis Rotation
- ▶ 11 Angular Momentum
- ▶ 12 Static Equilibrium and Elasticity
- ▶ 13 Gravitation
- ▶ 14 Fluid Mechanics



**Figure 7.1** A sprinter exerts her maximum power with the greatest force in the short time her foot is in contact with the ground. This adds to her kinetic energy, preventing her from slowing down during the race. Pushing back hard on the track generates a reaction force that propels the sprinter forward to win at the finish. (credit: modification of work by Marie-Lan Nguyen)

## Chapter Outline

- [7.1 Work](#)
- [7.2 Kinetic Energy](#)
- [7.3 Work-Energy Theorem](#)
- [7.4 Power](#)

In this chapter, we discuss some basic physical concepts involved in every physical motion in the universe, going beyond the concepts of force and change in motion, which we discussed in [Motion in Two and Three Dimensions](#) and [Newton's Laws of Motion](#). These concepts are work, kinetic energy, and power. We explain how these quantities are

# Energy

- In the first part of the course, we talked about the motion of objects and systems (Kinematics) and “tools of the trade” like trigonometry, derivatives, integrals, and vector decomposition.
- In the second part of the course, we talked about how Forces affect the motion of objects and systems.
- In the last part of the course, we will talk about Energy; which is a very helpful accounting tool to help us understand what happens when Forces are applied to other objects.

# Monday's Class

7.1 Work

7.2 Kinetic Energy

# Definition of Energy

“Energy” is an abstract concept and you can think of it as an accounting system to help us understand the world.

A system has “energy” if it has the ability to do Work.

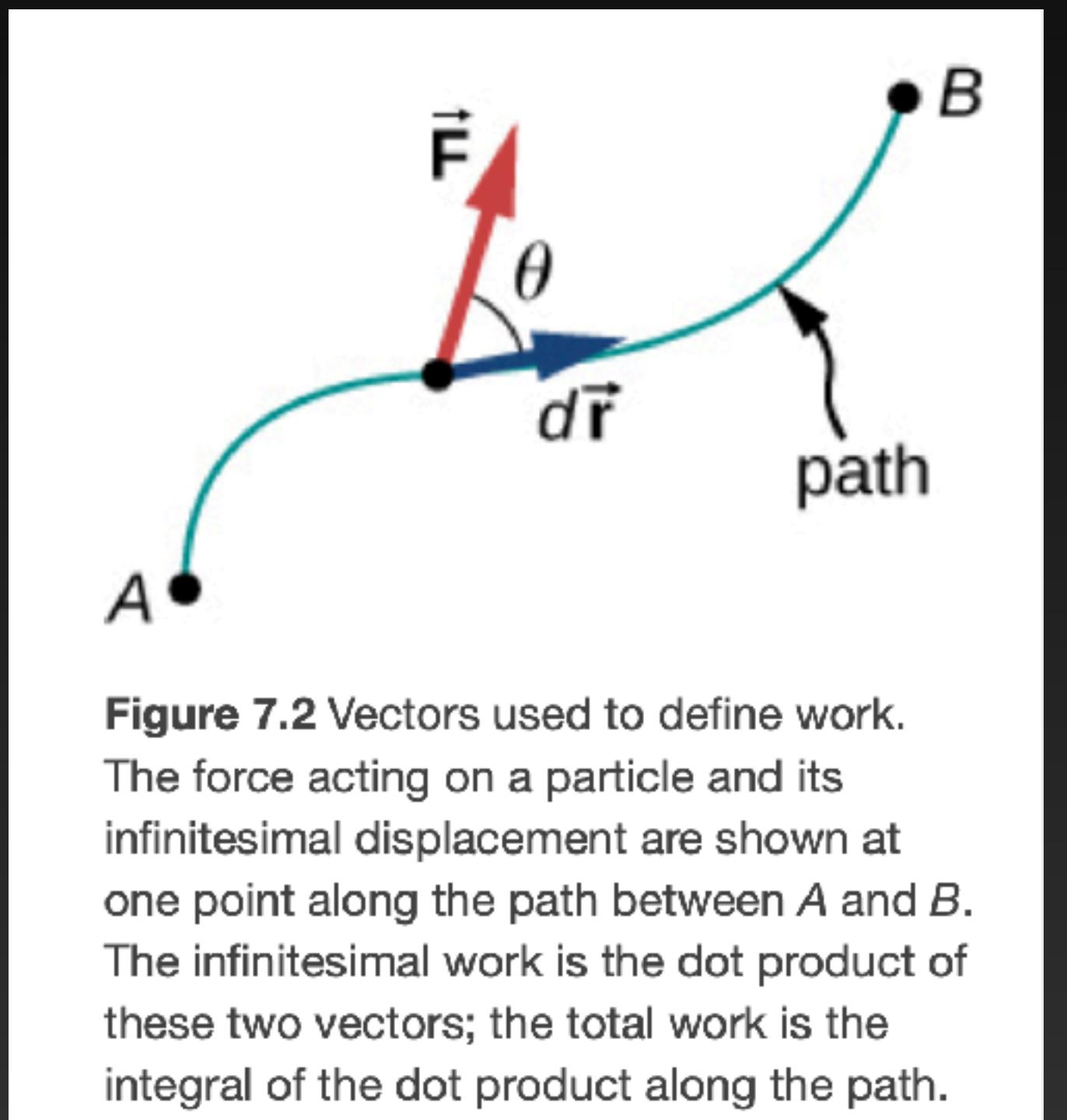
Energy is transferred (or transformed) when Work is done.

Energy is a “scalar” quantity (remember scalars can be positive or negative).

# Definition of Work

Work is done whenever an applied (external) force causes displacement.

$$W = \int \vec{F} \cdot d\hat{\vec{r}}$$



# Definition of Work

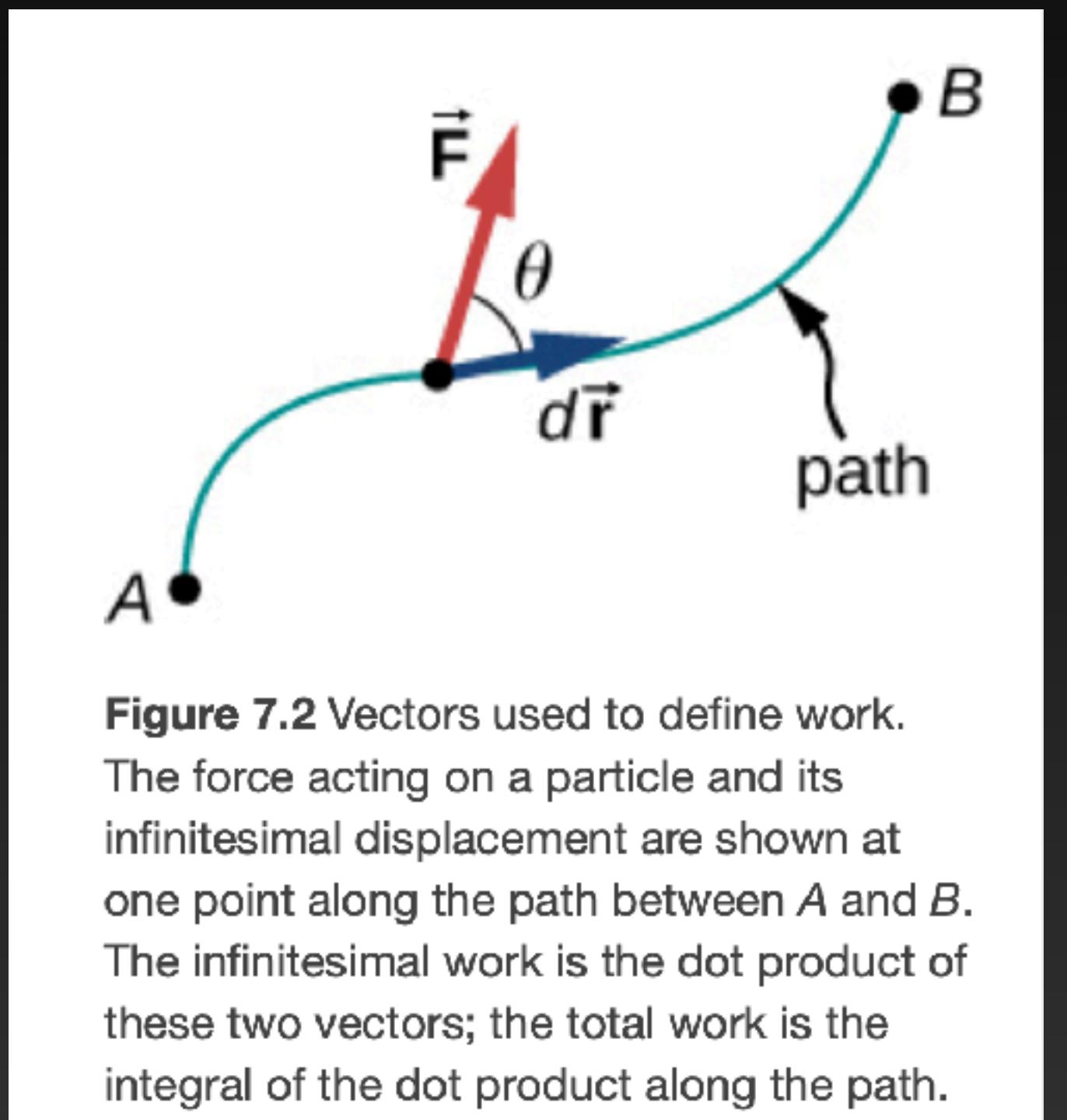
Work is done whenever an applied (external) force causes displacement.

$$W = \int \vec{F} \cdot d\hat{r}$$

When  $F$  is **constant**:

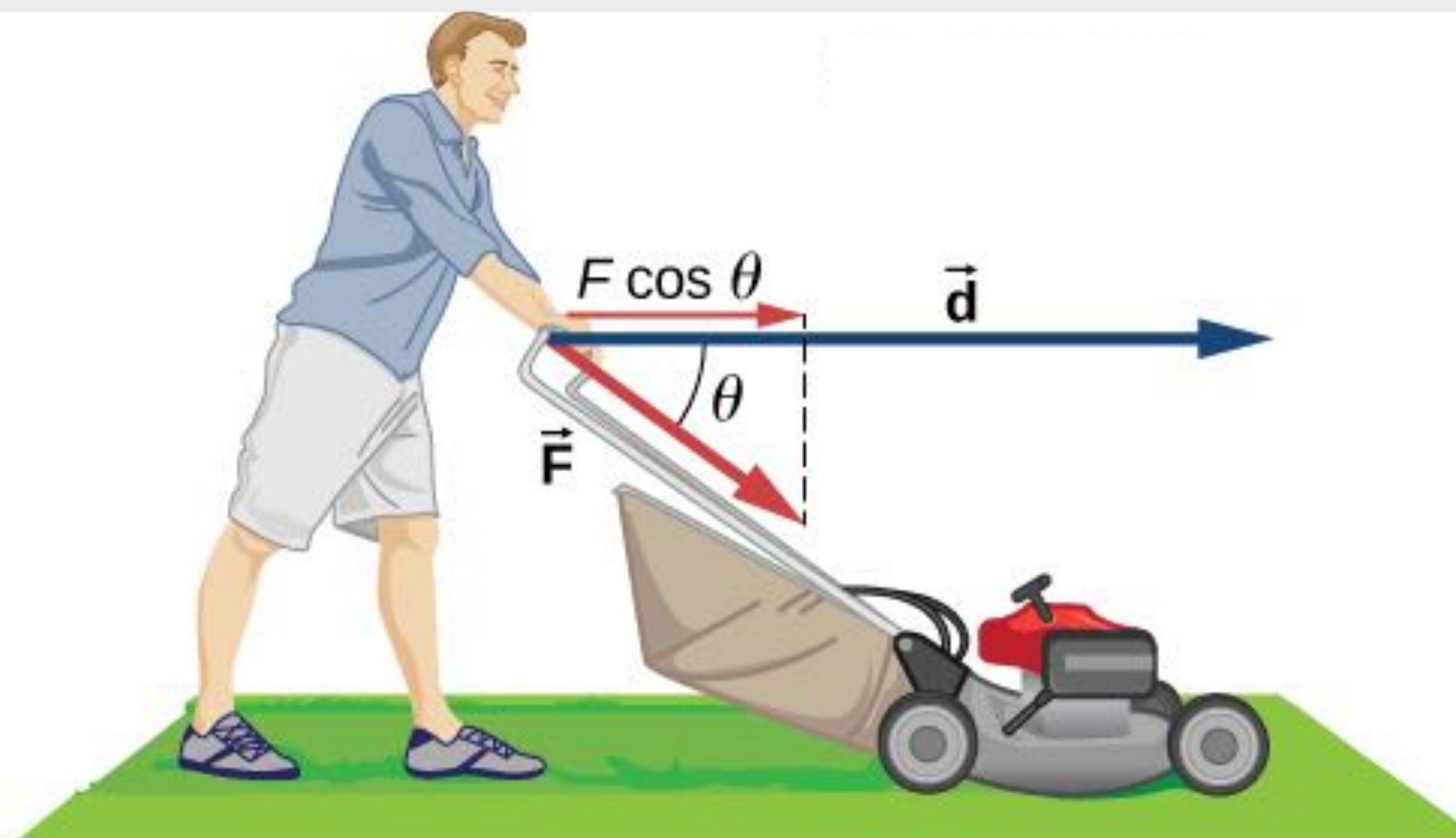
$$W = | \vec{F} | | \vec{d} | \cos(\theta)$$

No matter how complex the problem seems, this always holds true (when  $F$  is constant)!



**EXAMPLE 7.1****Calculating the Work You Do to Push a Lawn Mower**

How much work is done on the lawn mower by the person in [Figure 7.3\(a\)](#) if he exerts a constant force of 75.0 N at an angle  $35^\circ$  below the horizontal and pushes the mower 25.0 m on level ground?

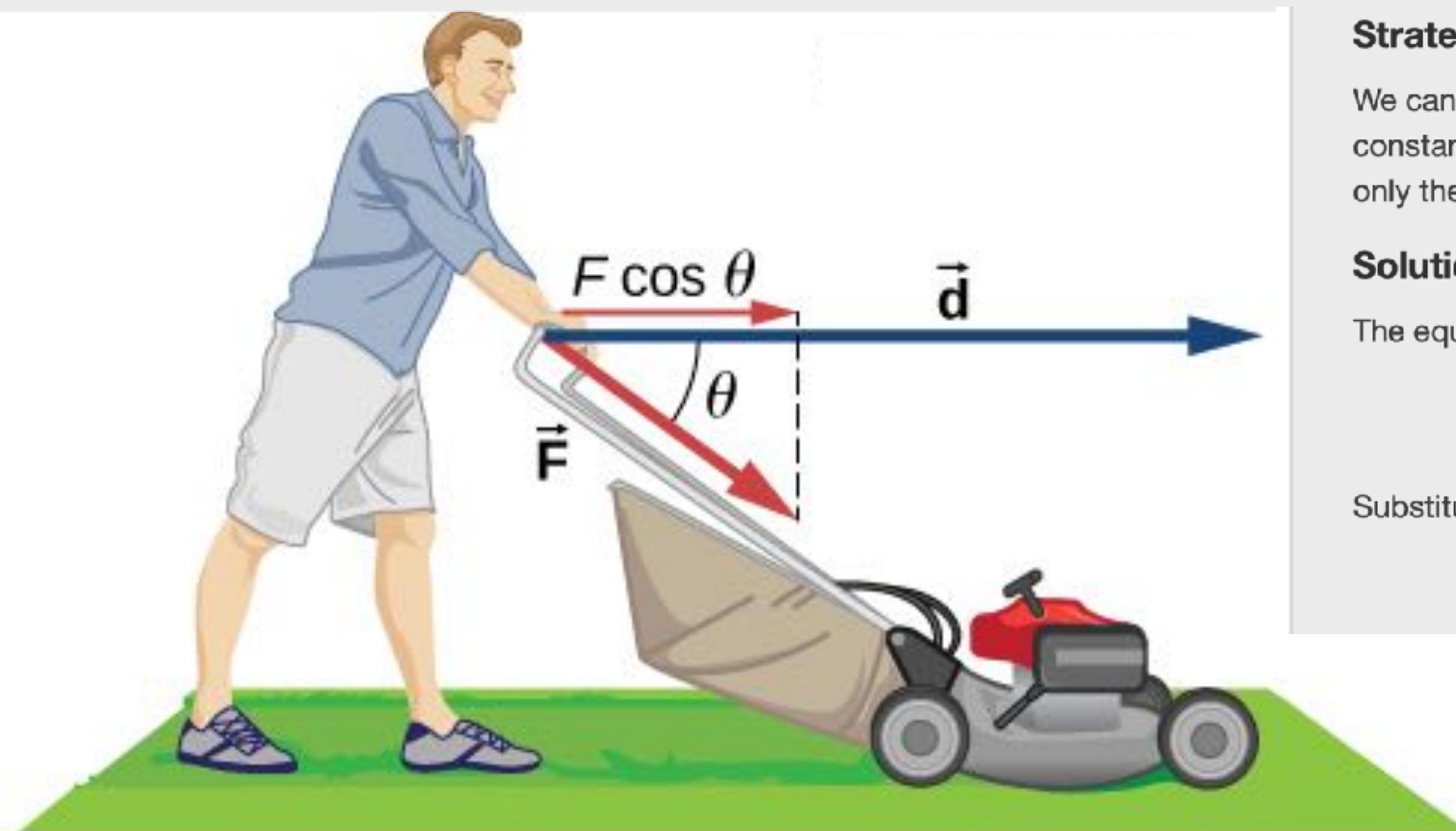


(a)

## EXAMPLE 7.1

### Calculating the Work You Do to Push a Lawn Mower

How much work is done on the lawn mower by the person in [Figure 7.3\(a\)](#) if he exerts a constant force of 75.0 N at an angle  $35^\circ$  below the horizontal and pushes the mower 25.0 m on level ground?



(a)

#### Strategy

We can solve this problem by substituting the given values into the definition of work done on an object by a constant force, stated in the equation  $W = Fd \cos \theta$ . The force, angle, and displacement are given, so that only the work  $W$  is unknown.

#### Solution

The equation for the work is

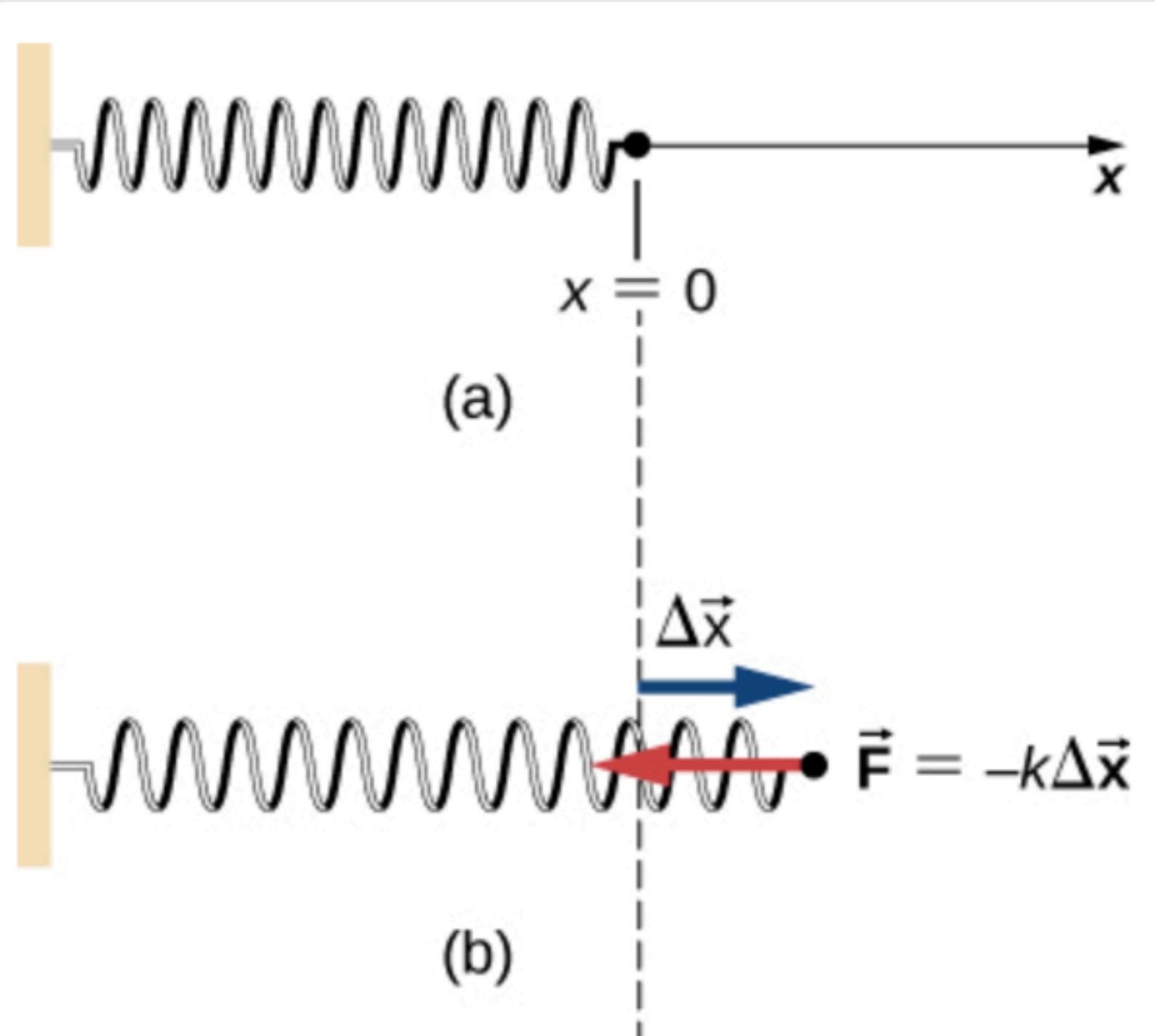
$$W = Fd \cos \theta.$$

Substituting the known values gives

$$W = (75.0 \text{ N})(25.0 \text{ m})\cos(35.0^\circ) = 1.54 \times 10^3 \text{ J}.$$

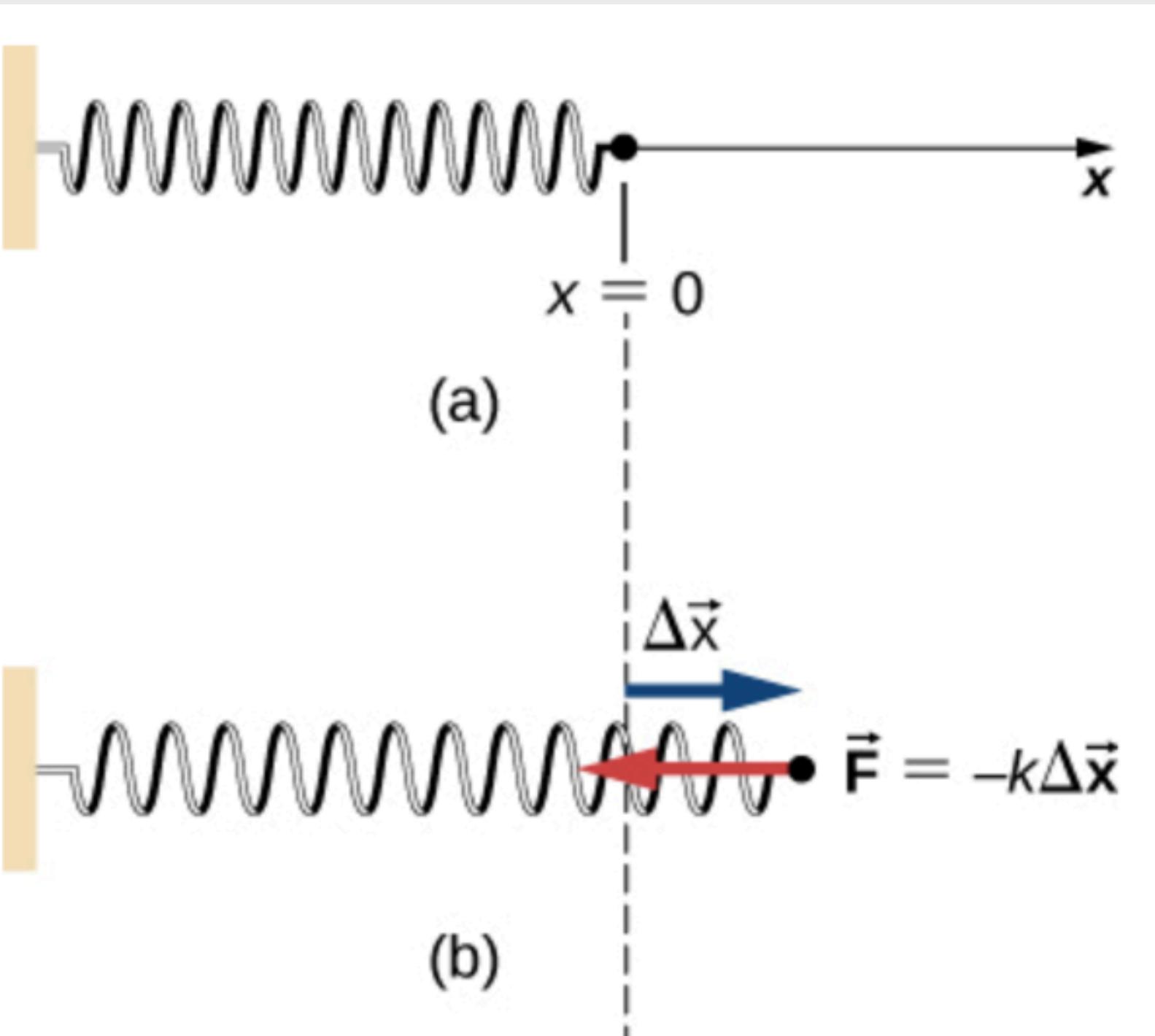
**EXAMPLE 7.5****Work Done by a Spring Force**

A perfectly elastic spring requires 0.54 J of work to stretch 6 cm from its equilibrium position, as in [Figure 7.7\(b\)](#). (a) What is its spring constant  $k$ ? (b) How much work is required to stretch it an additional 6 cm?



**EXAMPLE 7.5****Work Done by a Spring Force**

A perfectly elastic spring requires 0.54 J of work to stretch 6 cm from its equilibrium position, as in [Figure 7.7\(b\)](#). (a) What is its spring constant  $k$ ? (b) How much work is required to stretch it an additional 6 cm?

**Strategy**

Work “required” means work done against the spring force, which is the negative of the work in [Equation 7.5](#), that is

$$W = \frac{1}{2}k(x_B^2 - x_A^2).$$

For part (a),  $x_A = 0$  and  $x_B = 6\text{cm}$ ; for part (b),  $x_B = 6\text{cm}$  and  $x_B = 12\text{cm}$ . In part (a), the work is given and you can solve for the spring constant; in part (b), you can use the value of  $k$ , from part (a), to solve for the work.

**Solution**

- a.  $W = 0.54\text{ J} = \frac{1}{2}k[(6\text{ cm})^2 - 0]$ , so  $k = 3\text{ N/cm}$ .
- b.  $W = \frac{1}{2}(3\text{ N/cm})[(12\text{ cm})^2 - (6\text{ cm})^2] = 1.62\text{ J}$ .

**Significance**

Since the work done by a spring force is independent of the path, you only needed to calculate the difference in the quantity  $\frac{1}{2}kx^2$  at the end points. Notice that the work required to stretch the spring from 0 to 12 cm is four times that required to stretch it from 0 to 6 cm, because that work depends on the square of the amount of stretch from equilibrium,  $\frac{1}{2}kx^2$ . In this circumstance, the work to stretch the spring from 0 to 12 cm is also equal to the work for a composite path from 0 to 6 cm followed by an additional stretch from 6 cm to 12 cm. Therefore,

# Kinetic Energy

## KINETIC ENERGY

The kinetic energy of a particle is one-half the product of the particle's mass  $m$  and the square of its speed  $v$ :

$$K = \frac{1}{2}mv^2.$$

7.6

- Kinetic Energy is a scalar
- Since the mass is always  $> 0$ ,  $K$  is always  $\geq 0$
- Kinetic Energy is relative (to the reference frame)

# Friction

## EXAMPLE 7.7

### Kinetic Energy Relative to Different Frames

A 75.0-kg person walks down the central aisle of a subway car at a speed of 1.50 m/s relative to the car, whereas the train is moving at 15.0 m/s relative to the tracks. (a) What is the person's kinetic energy relative to the car? (b) What is the person's kinetic energy relative to the tracks? (c) What is the person's kinetic energy relative to a frame moving with the person?

### Strategy

Since speeds are given, we can use  $\frac{1}{2}mv^2$  to calculate the person's kinetic energy. However, in part (a), the person's speed is relative to the subway car (as given); in part (b), it is relative to the tracks; and in part (c), it is zero. If we denote the car frame by C, the track frame by T, and the person by P, the relative velocities in part (b) are related by  $\vec{v}_{PT} = \vec{v}_{PC} + \vec{v}_{CT}$ . We can assume that the central aisle and the tracks lie along the same line, but the direction the person is walking relative to the car isn't specified, so we will give an answer for each possibility,  $v_{PT} = v_{CT} \pm v_{PC}$ , as shown in [Figure 7.10](#).

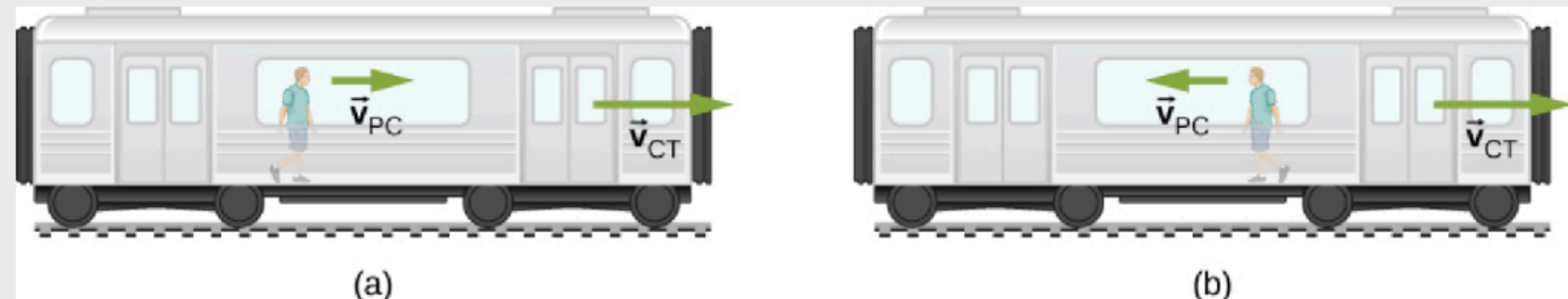


Figure 7.10 The possible motions of a person walking in a train are (a) toward the front of the car and (b) toward the back of the car.

### Solution

- $K = \frac{1}{2}(75.0 \text{ kg})(1.50 \text{ m/s})^2 = 84.4 \text{ J}$ .
- $v_{PT} = (15.0 \pm 1.50) \text{ m/s}$ . Therefore, the two possible values for kinetic energy relative to the car are

$$K = \frac{1}{2}(75.0 \text{ kg})(13.5 \text{ m/s})^2 = 6.83 \text{ kJ}$$

and

$$K = \frac{1}{2}(75.0 \text{ kg})(16.5 \text{ m/s})^2 = 10.2 \text{ kJ}.$$

- In a frame where  $v_P = 0$ ,  $K = 0$  as well.

### Significance

You can see that the kinetic energy of an object can have very different values, depending on the frame of reference. However, the kinetic energy of an object can never be negative, since it is the product of the mass and the square of the speed, both of which are always positive or zero.

# Key Equations

Work done by a force over an infinitesimal displacement

$$dW = \vec{F} \cdot d\vec{r} = |\vec{F}| |d\vec{r}| \cos \theta$$

Work done by a force acting along a path from  $A$  to  $B$

$$W_{AB} = \int_{\text{path } AB} \vec{F} \cdot d\vec{r}$$

Work done by a constant force of kinetic friction

$$W_{\text{fr}} = -f_k |l_{AB}|$$

Work done going from  $A$  to  $B$  by Earth's gravity, near its surface

$$W_{\text{grav},AB} = -mg (y_B - y_A)$$

Work done going from  $A$  to  $B$  by one-dimensional spring force

$$W_{\text{spring},AB} = -\left(\frac{1}{2}k\right)(x_B^2 - x_A^2)$$

Kinetic energy of a non-relativistic particle

$$K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

Work-energy theorem

$$W_{\text{net}} = K_B - K_A$$

Power as rate of doing work

$$P = \frac{dW}{dt}$$

Power as the dot product of force and velocity

$$P = \vec{F} \cdot \vec{v}$$

# Clicker Questions

# CQ.8.1

**While carrying a heavy box, a boy walks horizontally across a room at a constant speed. True or False: The boy is doing no work on the box.**

- a) True
- b) False

A

B

C

D

E

# CQ.8.2

If force and displacement are in opposite directions, will work be positive or negative?

a) positive

b) negative

A

B

C

D

E

# CQ.8.3

How much work is done when a weightlifter lifts a 200 N barbell from the floor to a height of 2 m?

- a) 0 J
- b) 100 J
- c) 200 J
- d) 400 J

A

B

C

D

E

# CQ.8.3

A friend slides a box along a flat floor to you, which you slow by applying a force at a  $30^\circ$  angle. Is the work you do to slow the box positive or negative? If you instead placed a book directly on top of the box as it passed you, what can you say about the work done by the book?

- a) positive; positive work done
- b) positive; negative work done
- c) negative work; positive work done
- d) negative work; no work done

A

B

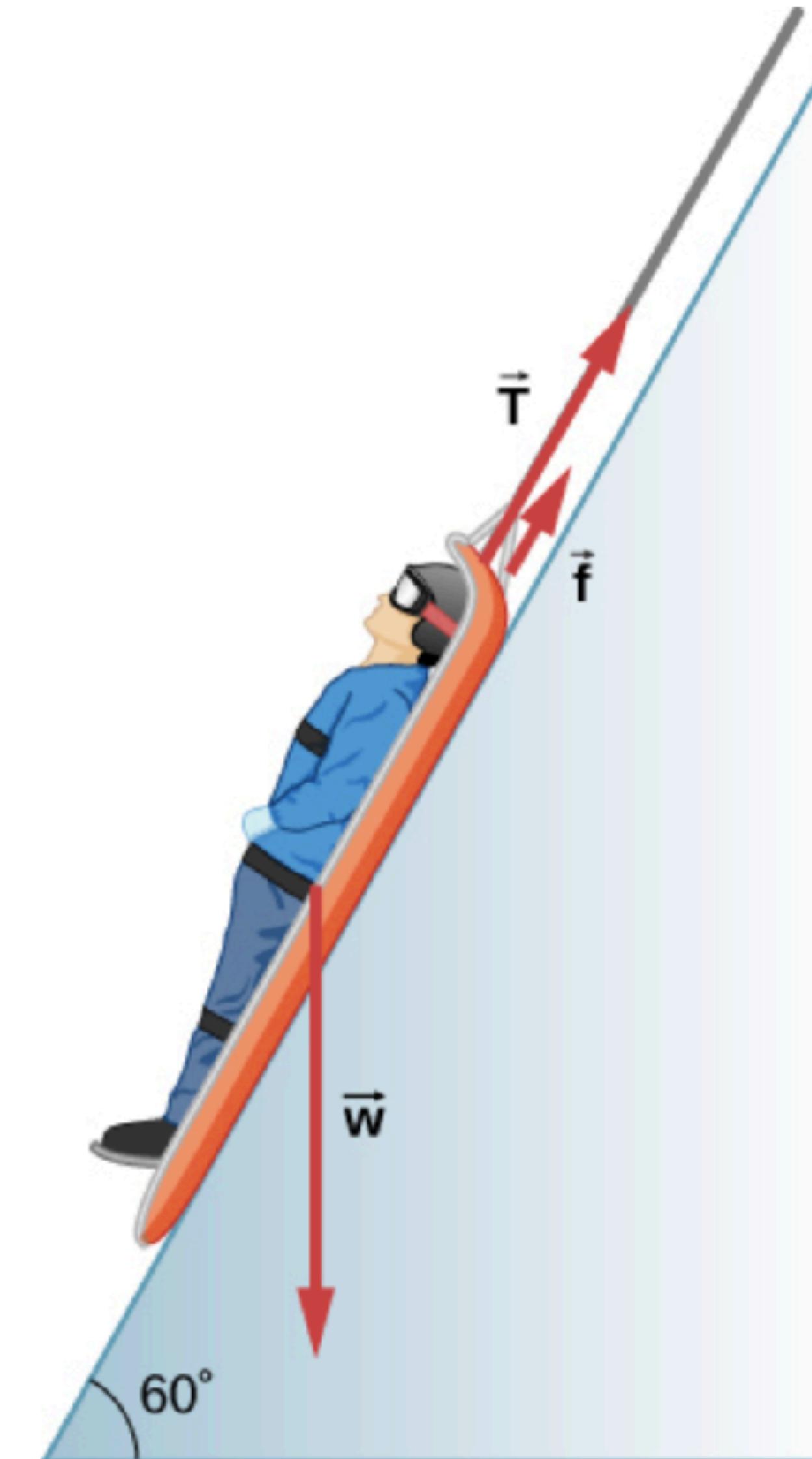
C

D

E

# Activity: Worked Problems

- 30 . Suppose the ski patrol lowers a rescue sled and victim, having a total mass of 90.0 kg, down a  $60.0^\circ$  slope at constant speed, as shown below. The coefficient of friction between the sled and the snow is 0.100. (a) How much work is done by friction as the sled moves 30.0 m along the hill? (b) How much work is done by the rope on the sled in this distance? (c) What is the work done by the gravitational force on the sled? (d) What is the total work done?



# WP 7.2

**36.** How much work does the force  $F(x) = (-2.0/x)$  N do on a particle as it moves from  $x = 2.0$  m to  $x = 5.0$  m?

**See you next class!**

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