

# Week 5 Tutorial

Tutorial Section

Tutorial Time

Tutorial TA Name

# Tutorial Structure

- Introduction
- Question 1
- Problem Solving Framework
- Question 2
- Problem Solving Framework
- Q&A

## Question 1

3. When a cow swats a mosquito with its tail in mid-air,  
(a) compare the size of the forces that the tail and the mosquito feel from each other. /2

(b) compare the size of accelerations that the collision between the cow's tail and the mosquito produces for both the tail and the mosquito. /2

# Problem Solving Framework

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**Template for teaching and assessment of problem solving in introductory physics**

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# 1. Framing

Visual Representation

Assumptions and Simplifications

Relevant Concepts

Information Needed

Similar Problems

# 2. Planning

Solution Plan

Rough Estimate

# 3. Execution

Carry-out Plan for solving

- Work in algebra/symbols until the BITTER end
- Plug in numbers at the LAST step

# 4. Answer Checking

Compare to Estimate

Units Check

Limits Test

Getting (UnStuck)

1. Framing

2. Planning

3. Execution

4. Answer Checking

# 1. Framing

»» Visual representation: Draw free body diagrams to show the forces being applied on the cow and the mosquito.

⚠ Assumptions and simplifications: Only consider 1-D.

↔ Relevant concept: Newton's third law.

⌚ Information needed: Forces being applied on the cow and the mosquito by each other. How do their masses compare?

-Calculator icon Similar problems: Any problem that involves drawing free body diagrams.

## 2. Planning

- Rough estimate: Visualize the free body diagram. How do the mass of the mosquito and the cow's tail compare?  $F=ma$
- Solution plan: Determine how the two objects exert force on each other. Determine how different masses affect the acceleration.

# 3. Execution

- See solution on slide 10.

# 4. Answer Checking

Compare to estimates: Does this make sense based on your FBD?

Units: Not applicable

Limits: Not applicable

Getting (UnStuck)? ...

# Solution

3. When a cow swats a mosquito with its tail in mid-air,  
(a) compare the size of the forces that the tail and the mosquito feel from each other.

$$F_{tm} = F_{mt} \quad (1pt)$$

1/2

Newton's Third law. (1pt.)

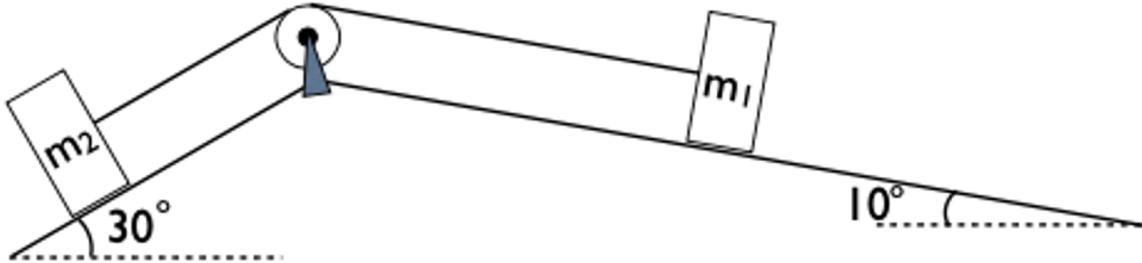
- (b) compare the size of accelerations that the collision between the cow's tail and the mosquito produces for both the tail and the mosquito.

1/2

$$m_m \ll m_t \quad \text{so} \quad m_t a_t = m_m a_m$$

The mosquito accelerates  
(1pt.) much more.  $\frac{a_m}{a_t} = \frac{m_t}{m_m} \gg 1$  (1pt.)

## Question 2



1. (a) Two masses  $m_1 = 10 \text{ kg}$  and  $m_2 = 1 \text{ kg}$  are connected by a light rope which passes over a light, low friction pulley between low friction slopes of  $30^\circ$  and  $10^\circ$  as shown in the figure. Approximating the masses of the rope and pulley to be negligible and the friction of both the slopes and the pulley to be negligible, find the acceleration (/2) of mass  $m_2$  up the slope. (Draw free body diagrams (/10), axes and acceleration vectors, and write Newton's second law equations in components independently (/10) for both masses.) /22

1. Framing

2. Planning

3. Execution

4. Answer Checking

# 1. Framing



Visual representation: Look at the diagram and draw relevant FBD's.



Assumptions and simplifications: Frictionless surface. Acceleration of  $m_1$  and  $m_2$  are due to each other.



Relevant concept: Newton's laws of motion.



Information needed: Acceleration of mass 1 and mass 2, FBD's, Newton's second law equations.



Similar problems: 1-D block on a slope, etc.

## 2. Planning

- Rough estimate: How do you expect the system to react?
- Solution plan: Draw FBD's for each mass. Substitute equations into FBD to determine acceleration of the system.

## 3. Execution

- See solution on next slide. Carry out the calculation, plug in the numbers at the last step.

# 4. Answer Checking

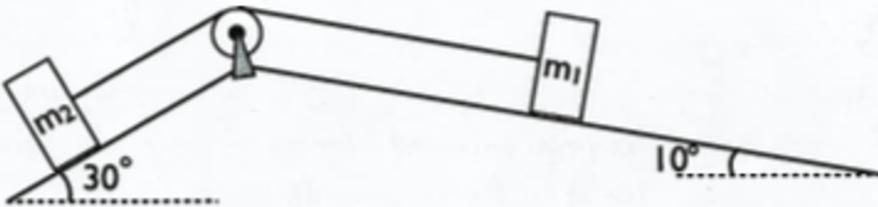
Compare to estimates: Is this what you expected?

Units: Check your units. Do they make sense?

Limits: Not applicable.

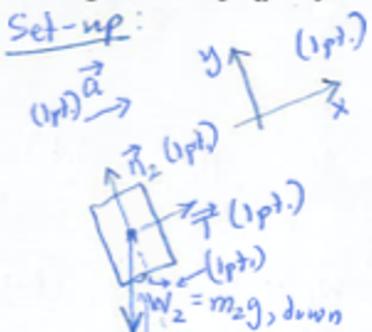
Getting (UnStuck)? ...

# Solution



1. (a) Two masses \$m\_1 = 10 \text{ kg}\$ and \$m\_2 = 1 \text{ kg}\$ are connected by a light rope which passes over a light, low friction pulley between low friction slopes of \$30^\circ\$ and \$10^\circ\$ as shown in the figure. Approximating the masses of the rope and pulley to be negligible and the friction of both the slopes and the pulley to be negligible, find the acceleration (/2) of mass \$m\_2\$ up the slope. (Draw free body diagrams (/10), axes and acceleration vectors, and write Newton's second law equations in components independently (/10) for both masses.)

Set-up:



$$T - m_2 g \sin 30^\circ = m_2 a \quad (1)$$

(1 pt.) (1 pt.)

$$n_2 - m_2 g \cos 30^\circ = 0$$

(1 pt.) (1 pt.)

(1 pt.) (1 pt.) /22

A free body diagram of mass \$m\_1\$ on the \$10^\circ\$ incline. The forces shown are the normal force \$n\_1\$ perpendicular to the incline, the weight \$W\_1 = m\_1 g\$ acting vertically downwards, and the tension \$T\$ in the rope acting parallel to the incline downwards. The angle of the incline is \$10^\circ\$.

$$m_1 g \sin 10^\circ - T = m_1 a \quad (2)$$

$$n_1 - m_1 g \cos 10^\circ = 0$$

(1 pt.) (1 pt.)

Solve:  
Adding equations (1) and (2)  
to eliminate \$T\$:

$$(m_1 \sin 10^\circ - m_2 \sin 30^\circ)g = (m_1 + m_2)a$$

$$a = g \left( \frac{m_1 \sin 10^\circ - m_2 \sin 30^\circ}{m_1 + m_2} \right)$$

$$= g \left( \frac{10 \text{ kg} \sin 10^\circ - 1 \text{ kg} \sin 30^\circ}{11 \text{ kg}} \right) = 0.11g$$

↑ 9.8 m/s<sup>2</sup> = 1.1 m/s<sup>2</sup>. (1 pt.)