

Physics 111 - Class 7A

Force Applications

October 19, 2022

Class Outline

- Logistics / Announcements
- Mid-course Feedback Results
- Introduction to Chapter 6
- Clicker Questions
- Activity: Worked Problems

Logistics/Announcements

- Lab this week: Lab 4
- HW6 due this week on Thursday at 6 PM
- Learning Log 6 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Bonus Test 2 available this week (Chapters 3 & 4)
- Additional Student Hours from Tutorial TAs for more 1:1 help via Zoom

Changes moving forward...

- **Full worked solutions posted after class (Started in Week 5)**
- **Adjustment to Learning Logs**
 - Question 2 will not be required (though I still encourage you to do it)
- **Review HW problems in class**
 - In Tutorials, I will ask Ishanka and Siddharth to do a quick poll before every tutorial and spend 5 minutes with the strategy on one HW problem
 - In class, I will try to give some hints on one HW problem (may not happen every week)

Changes moving forward...

- **More opportunities for 1:1 help:** Three hours of additional time/week on Zoom
 - Siddharth (TA): Tuesdays 3:00 - 4:30 PM on Zoom
 - Ishanka (TA): Thursdays 2:00 - 3:30 on Zoom

Contact Us

Team Member	Pronounce as	Contact	Student Hours
Dr. Firas Moosvi (he/his/him); Instructor	Fur-az Moose-vee	Contact via Ed Discussion	Wednesdays and Fridays 3:30-4:00 PM and 5:00 - 5:30 in COM 201
Siddharth Perera	Pronunciation	Contact via Ed Discussion	Tuesdays 3:00 - 4:30 on Zoom
Ishanka Banerjee	Pronunciation	Contact via Ed Discussion	Thursdays 2:00 - 3:30 on Zoom
Skyler Alderson	Pronunciation	Contact via Ed Discussion	N/A

CQ.7.4

Two springs are attached to two hooks. Spring A has a greater force constant than spring B. Equal weights are suspended from both. Which of the following statements is true?

- a) Spring A will have more extension than spring B.
- b) Spring B will have more extension than spring A.
- c) Both springs will have same extension.
- d) Both springs are equally stiff.

A

B

C

D

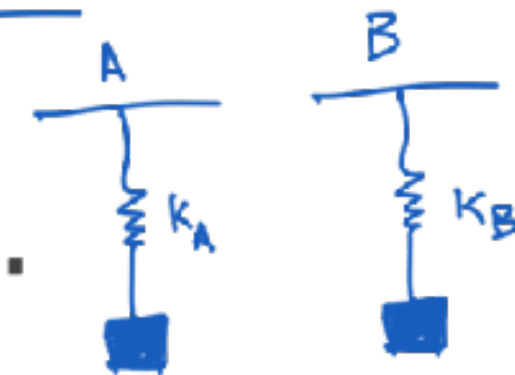
E

CQ.7.4

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- d) Both springs are equally stiff.

CQ 7.4



$k_A > k_B$, so From Hooke's Law:

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- c) Both springs will have same extension.

$$\vec{F}_r = -k\Delta x$$

In equilibrium, $\vec{F}_{NETy} = 0$

$$\vec{F}_g - \vec{F}_r = 0$$

$$mg + k\Delta x = 0$$

$$\Delta x = \frac{-mg}{k}$$

Inversely proportional relationship, so $\Delta x_B > \Delta x_A$ if $k_A > k_B$!

Detailed solution: The greater the force constant, the stiffer the spring. Therefore, spring B will have more extension than spring A.

A

B

C

D

E

Wednesday's Class

6.3 Centripetal Force

6.4 Drag force and Terminal Speed

Centripetal Motion

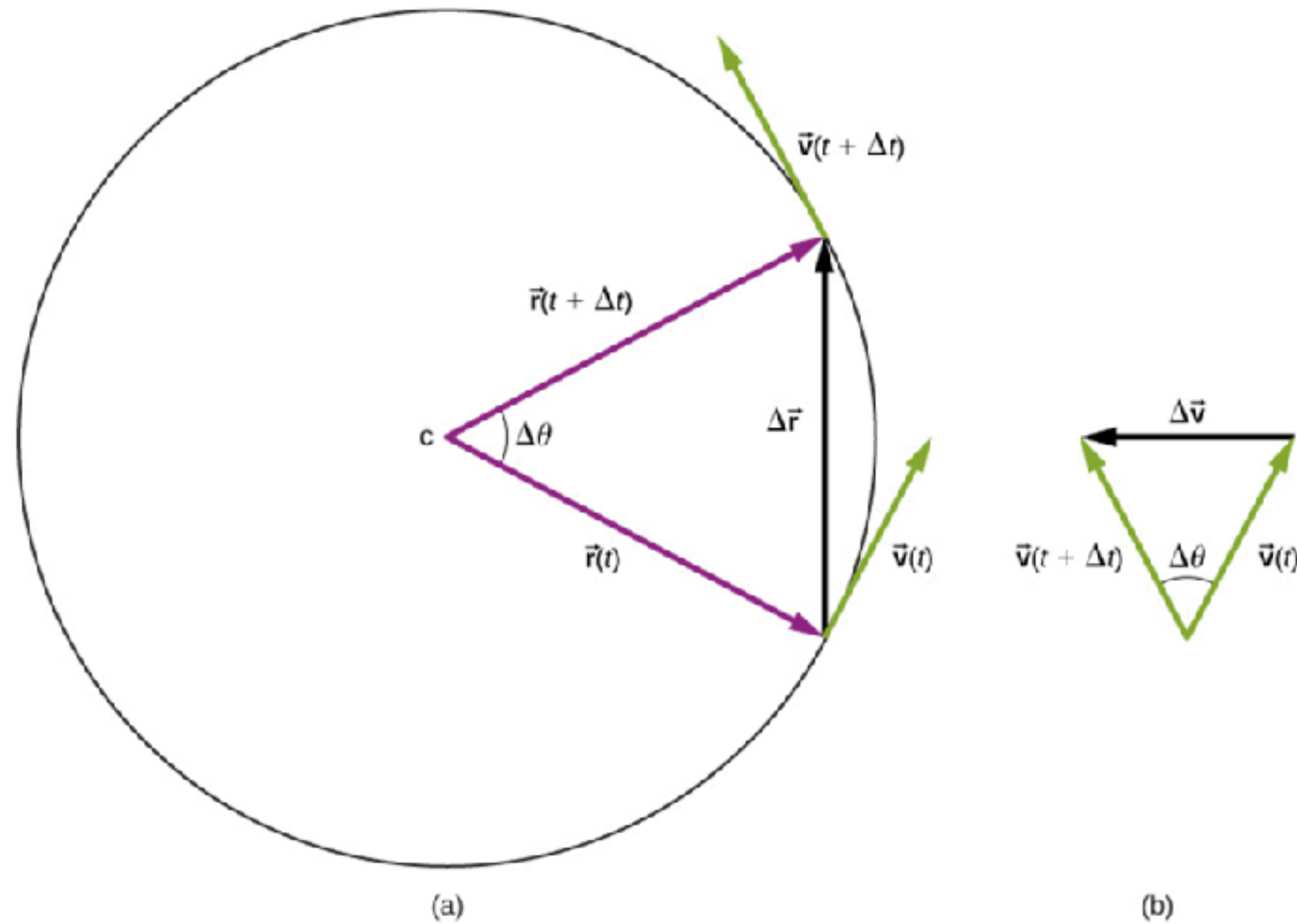


Figure 4.18 (a) A particle is moving in a circle at a constant speed, with position and velocity vectors at times t and $t + \Delta t$. (b) Velocity vectors forming a triangle. The two triangles in the figure are similar. The vector $\Delta \vec{v}$ points toward the center of the circle in the limit $\Delta t \rightarrow 0$.

We can find the magnitude of the acceleration from

$$a = \lim_{\Delta t \rightarrow 0} \left(\frac{\Delta v}{\Delta t} \right) = \frac{v}{r} \left(\lim_{\Delta t \rightarrow 0} \frac{\Delta r}{\Delta t} \right) = \frac{v^2}{r}.$$

The direction of the acceleration can also be found by noting that as Δt and therefore $\Delta \theta$ approach zero, the vector $\Delta \vec{v}$ approaches a direction perpendicular to \vec{v} . In the limit $\Delta t \rightarrow 0$, $\Delta \vec{v}$ is perpendicular to \vec{v} . Since \vec{v} is tangent to the circle, the acceleration $d\vec{v}/dt$ points toward the center of the circle. Summarizing, a particle moving in a circle at a constant speed has an acceleration with magnitude

$$a_c = \frac{v^2}{r}.$$

4.27

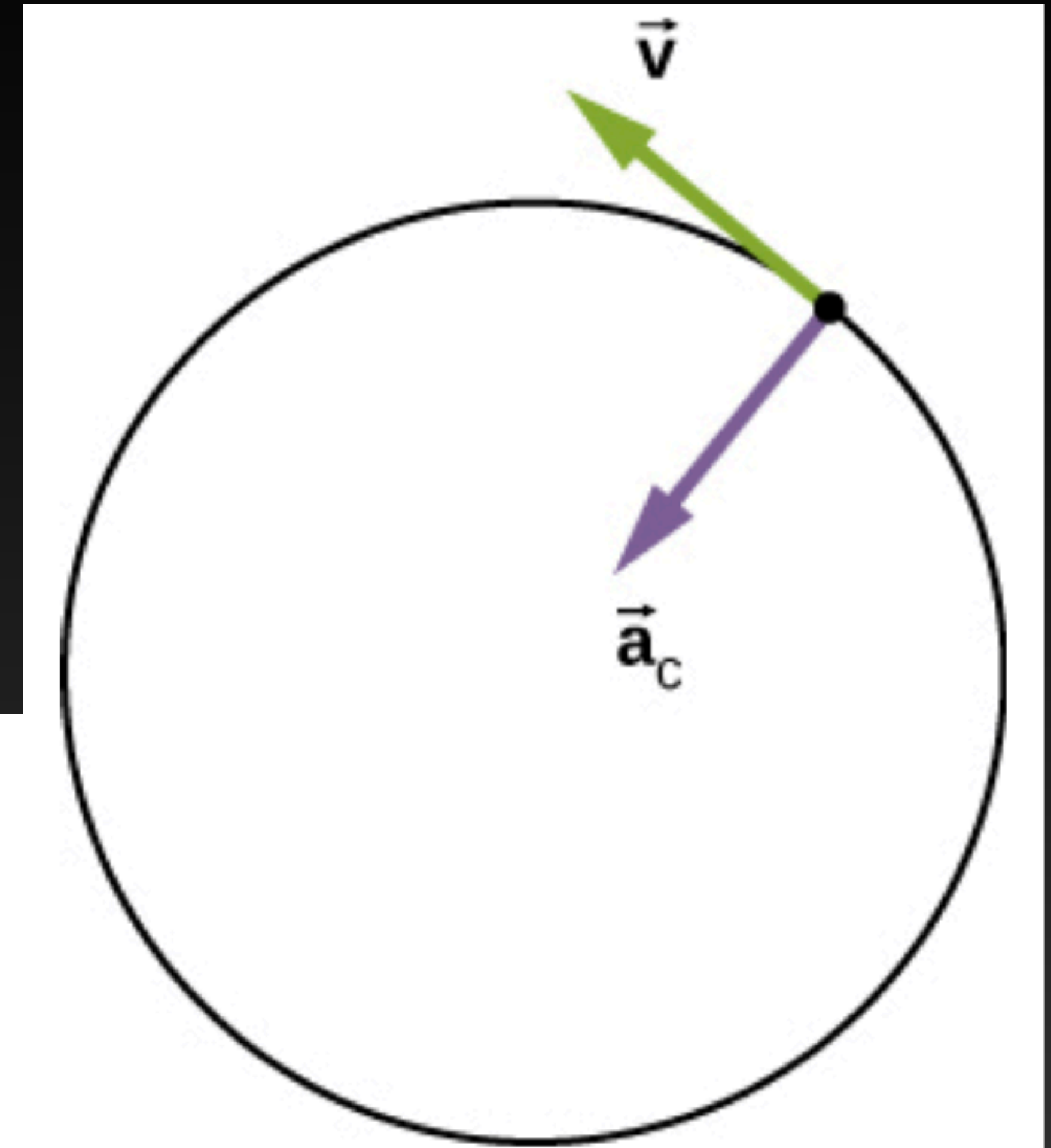


Figure 4.19 The centripetal acceleration vector points toward the center of the circular path of motion and is an acceleration in the radial direction. The velocity vector is also shown and is tangent to the circle.

Centripetal Motion

By substituting the expressions for centripetal acceleration a_c ($a_c = \frac{v^2}{r}$; $a_c = r\omega^2$), we get two expressions for the centripetal force F_c in terms of mass, velocity, angular velocity, and radius of curvature:

$$F_c = m\frac{v^2}{r}; \quad F_c = mr\omega^2.$$

6.3

arc of projectile motion





Drag Force

DRAG FORCE

Drag force F_D is proportional to the square of the speed of the object. Mathematically,

$$F_D = \frac{1}{2} C \rho A v^2,$$

where C is the drag coefficient, A is the area of the object facing the fluid, and ρ is the density of the fluid.

Drag Force

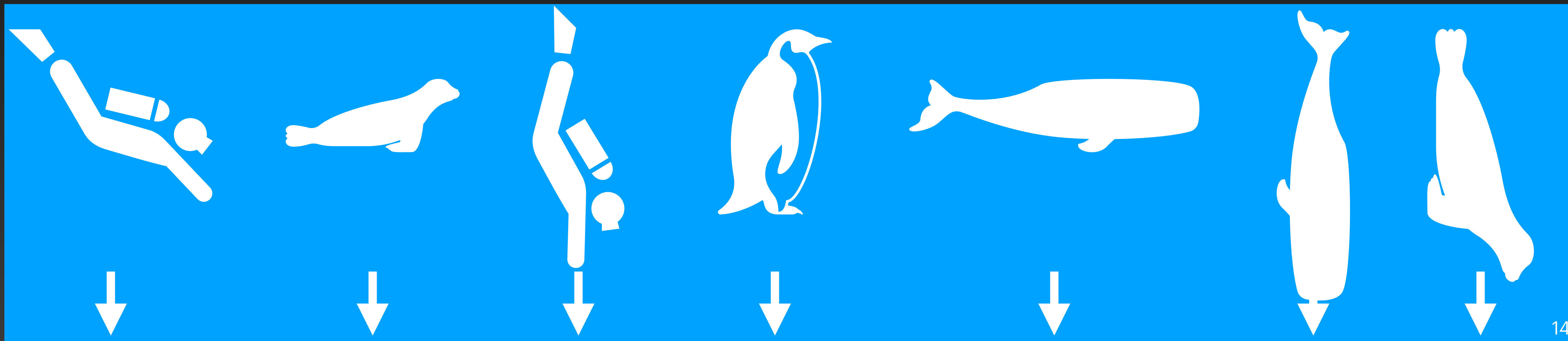
DRAG FORCE

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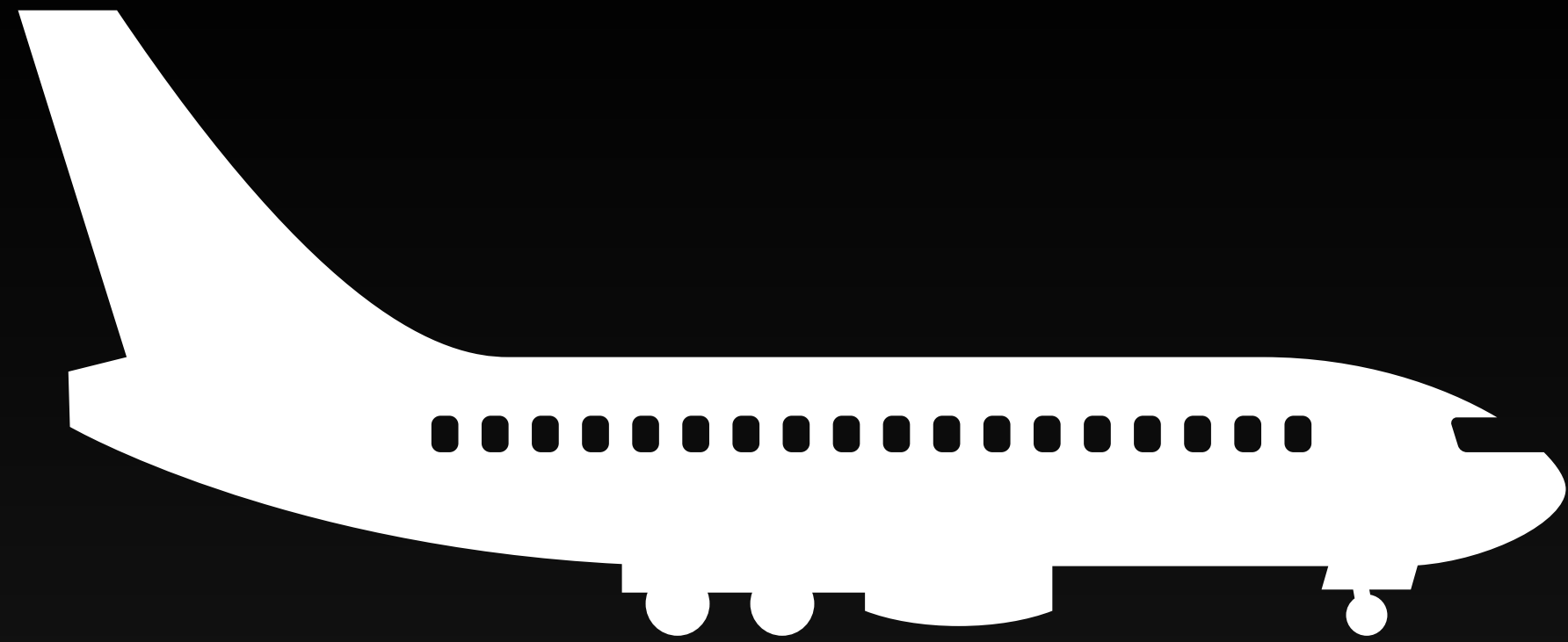
$$F_D = \frac{1}{2} C \rho A v^2,$$

where C is the drag coefficient, A is the area of the object facing the fluid, and ρ is the density of the fluid.

Rank the drag force on these specimens from highest (1) to lowest (7)

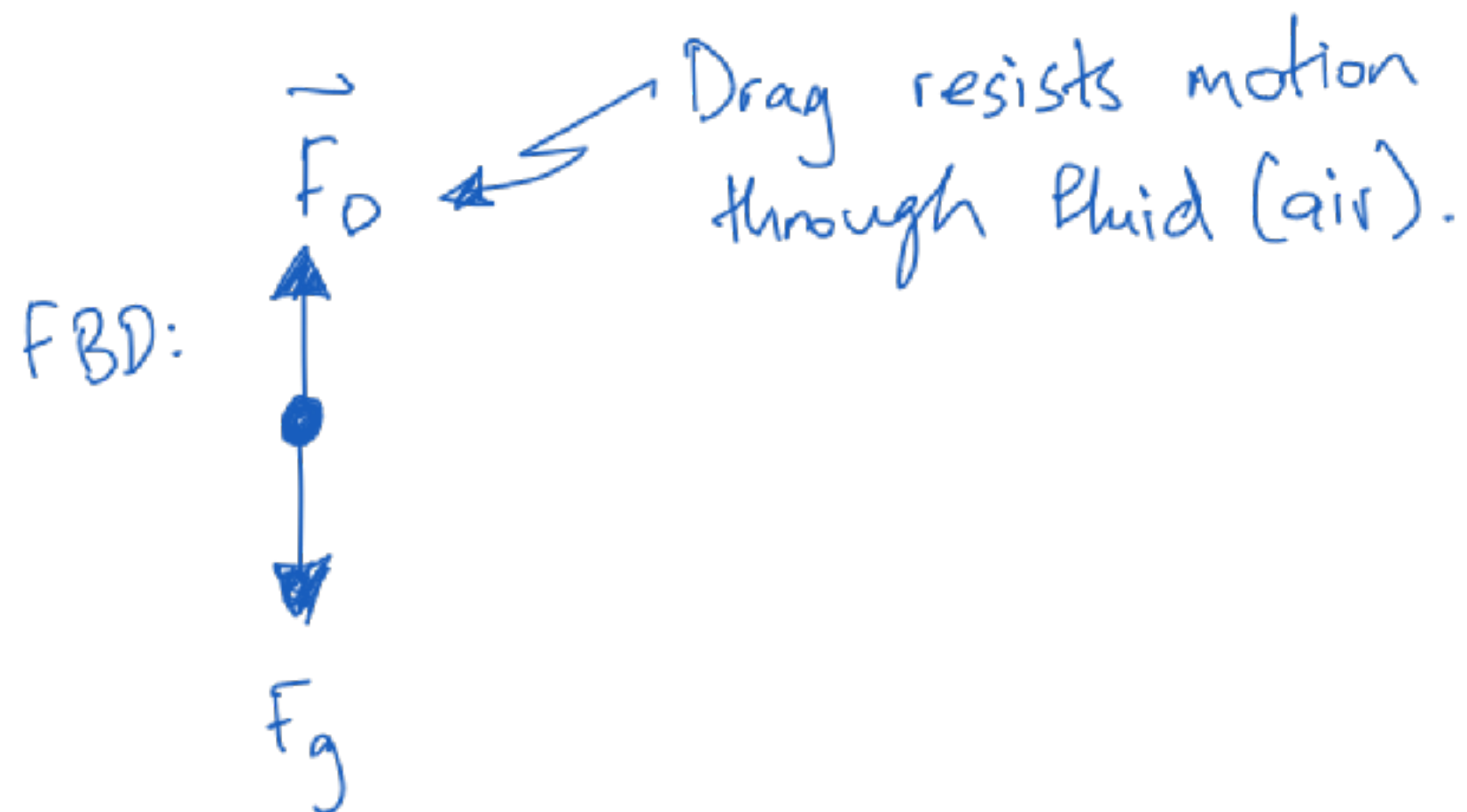


Terminal Velocity



Deriving Terminal Velocity

What is the maximum velocity of a skydiver who jumps out of a plane?



$$\vec{F}_{\text{net}} = 0 = \vec{F}_g - \vec{F}_D$$

\therefore the max velocity is achieved when $a=0$

$$\vec{F}_g = \vec{F}_D$$

$$mg = \frac{1}{2} C_f A v^2$$

$$v^2 = \frac{2mg}{C_f A}$$

Terminal Velocity

Parachute





Key Equations

Magnitude of static friction	$f_s \leq \mu_s N$
Magnitude of kinetic friction	$f_k = \mu_k N$
Centripetal force	$F_c = m \frac{v^2}{r}$ or $F_c = mr\omega^2$
Ideal angle of a banked curve	$\tan \theta = \frac{v^2}{rg}$
Drag force	$F_D = \frac{1}{2} C \rho A v^2$
Stokes' law	$F_s = 6\pi r \eta v$

Clicker Questions

CQ.7.6

Is an object in uniform circular motion accelerating? Why or why not?

- a) Yes, because the velocity is not constant.
- b) No, because the velocity is not constant.
- c) Yes, because the velocity is constant.
- d) No, because the velocity is constant.

A

B

C

D

E

CQ.7.6

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- b) No, because the velocity is not constant.
- c) Yes, because the velocity is constant.
- d) No, because the velocity is constant.

A

B

C

D

E

C Q 7.6

Remember that \vec{v} is a
vector quantity!



The direction of \vec{v}
is changing at every
point along the path;
so it must have
an acceleration!



CQ.7.7

An object is in uniform circular motion. Suppose the centripetal force was removed. In which direction would the object now travel?

- a) in the direction of the centripetal force
- b) in the direction opposite to the direction of the centripetal force
- c) in the direction of the tangential velocity
- d) in the direction opposite to the direction of the tangential velocity

A

B

C

D

E

CQ.7.7

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A

B

C

D

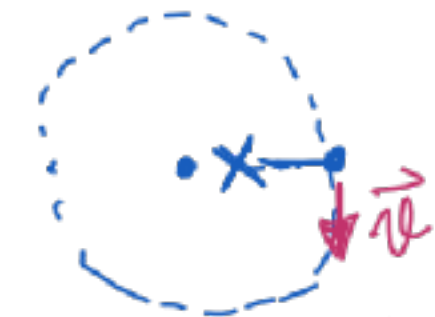
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CQ.7.7

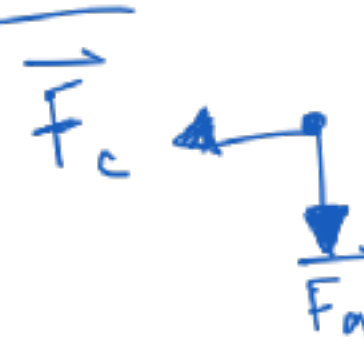
Remember Newt
1st Law!



Cut String



FBD:

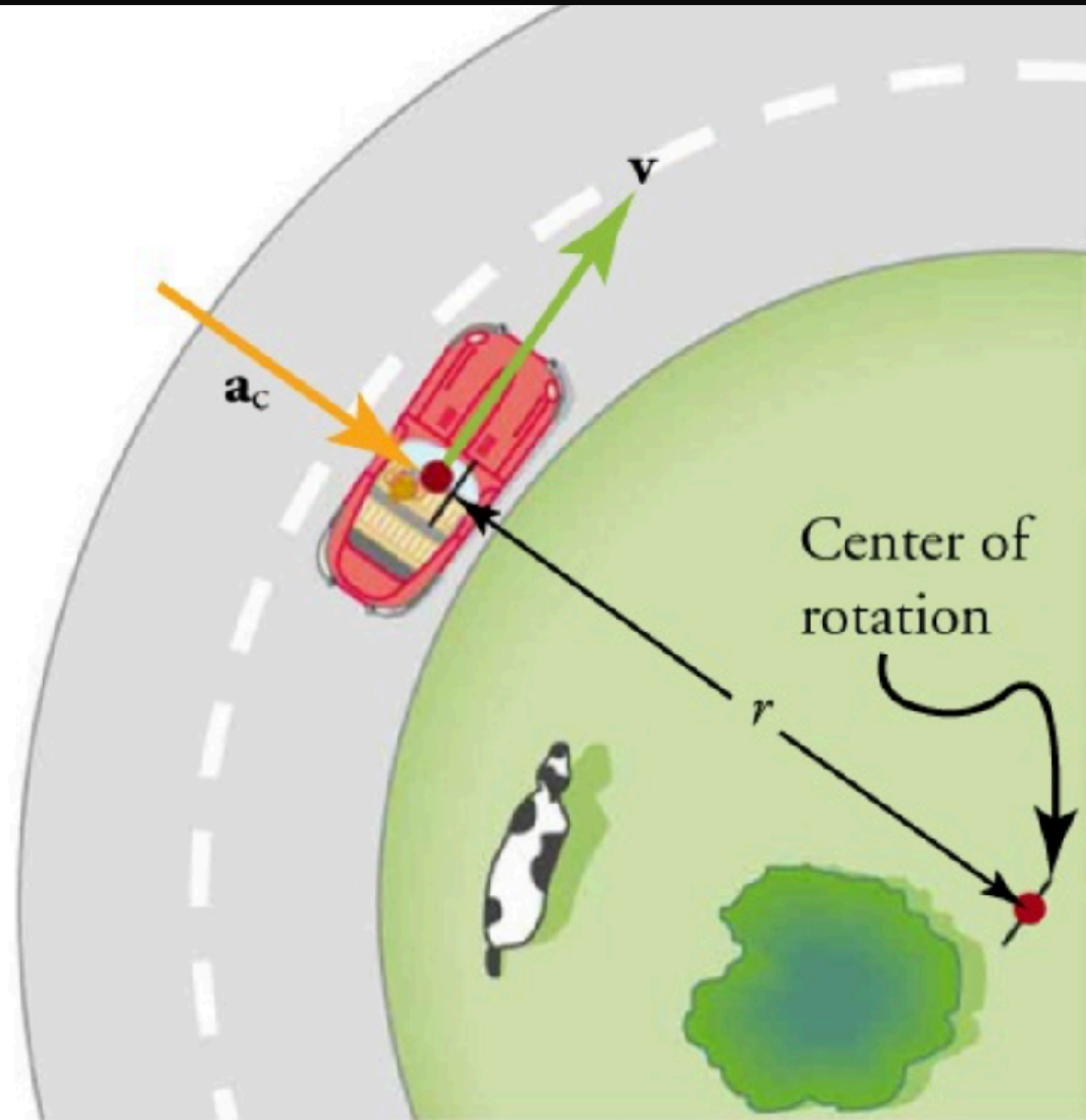


No more centripetal force! Object will continue travelling with the velocity as it had...

CQ.7.8

A car follows a curve of radius 500 m at a speed of 25.0 m/s (about 90 km/h). What is the magnitude of the car's centripetal acceleration? Compare the centripetal acceleration for this fairly gentle curve taken at highway speed with acceleration due to gravity g .

- a) The centripetal acceleration is 0.1 m/s and is 0.1 times the acceleration due to gravity.
- b) The centripetal acceleration is 1.25 m/s^2 and is 0.1 times the acceleration due to gravity.
- c) The centripetal acceleration is 0.1 m/s and is 0.01 times the acceleration due to gravity.
- d) The centripetal acceleration is 1.25 m/s^2 and is 0.01 times the acceleration due to gravity.



A

B

C

D

E

CQ.7.8

A car follows a curve of radius 500 m at a speed of 25.0 m/s (about 90 km/h). What is the magnitude of the car's centripetal acceleration? Compare the centripetal acceleration for this fairly gentle curve taken at highway speed with acceleration due to gravity g .

- a) The centripetal acceleration is 0.1 m/s and is 0.1 times the acceleration due to gravity.

The centripetal acceleration is $a_c = \frac{v^2}{r}$, where v is tangential velocity and r is the radius of curvature of the circular path. It is incorrect that the centripetal acceleration is $a_c = \frac{v}{r}$.

- ✓ b) The centripetal acceleration is 1.25 m/s² and is 0.1 times the acceleration due to gravity.

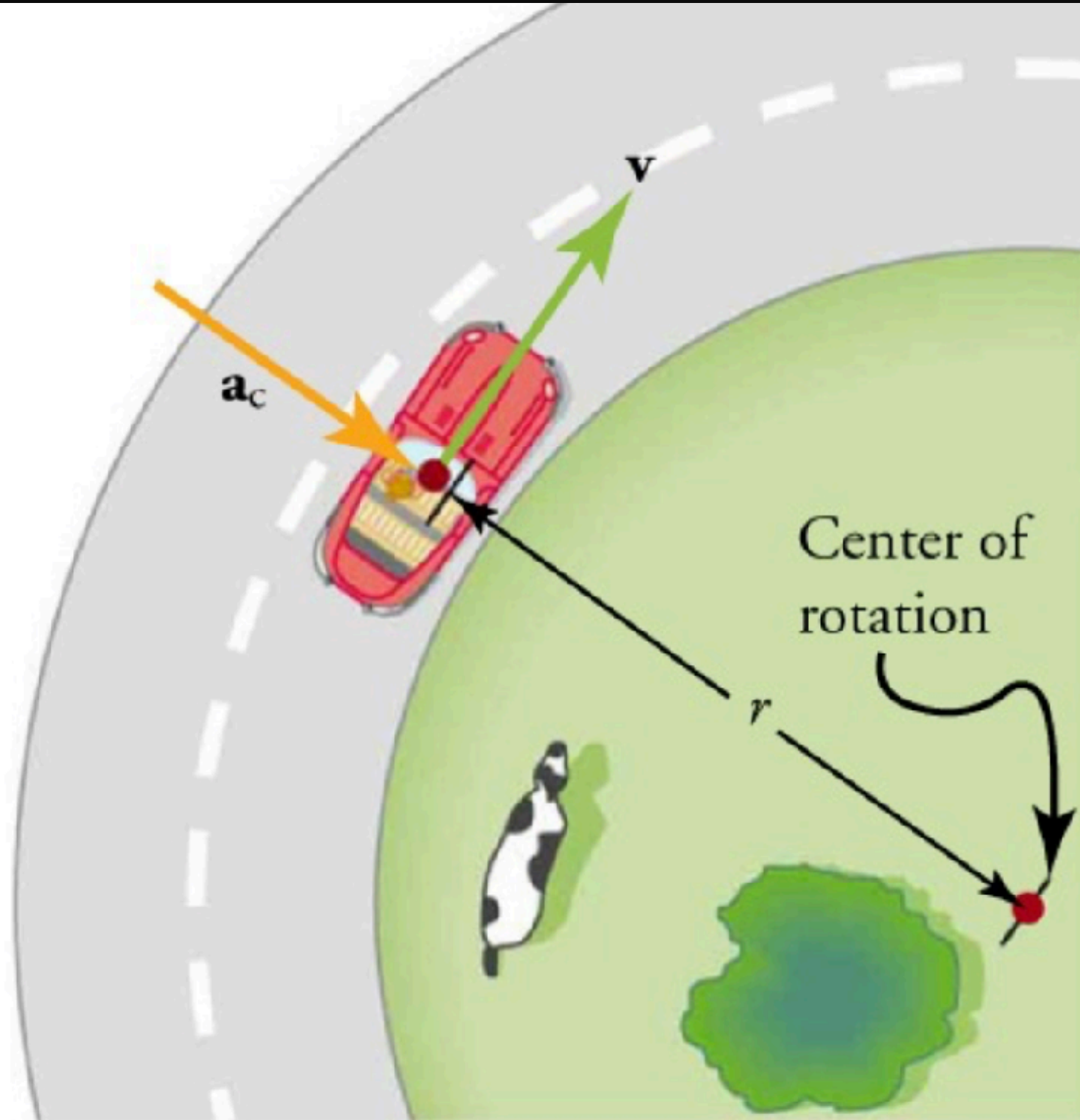
The centripetal acceleration can be obtained by using the relation $a_c = \frac{v^2}{r}$, where v is tangential velocity and r is the radius of curvature of the circular path. Also, the comparison is done by taking the ratio of centripetal acceleration to the acceleration due to gravity.

- c) The centripetal acceleration is 0.1 m/s and is 0.01 times the acceleration due to gravity.

It is incorrect that $a_c = \frac{v}{r}$. The centripetal acceleration is $a_c = \frac{v^2}{r}$, where v is tangential velocity and r is the radius of curvature of the circular path.

- d) The centripetal acceleration is 1.25 m/s² and is 0.01 times the acceleration due to gravity.

It is correct that the centripetal acceleration is $a_c = \frac{v^2}{r}$, but you have compared the centripetal acceleration with the acceleration due to gravity incorrectly. The comparison is done by taking the ratio of centripetal acceleration to the acceleration due to gravity.



A

B

C

D

E

CQ 7.6

$$F_c = \frac{m v^2}{R}$$

$$m a_r = \frac{m v^2}{R}$$

$$a_r = \frac{v^2}{R}$$

$$|a_r| = 1.25 \text{ m/s}^2 \approx 0.1g$$

CQ.7.9

A 50 kg bicyclist starts his ride down the road with an acceleration of 1m/s^2 in air with a density of 1.2 kg/m^3 . If his velocity at a given moment is 2m/s , how much force is he exerting? Assume the area of his body is 0.5m^2 .

Assume $C = 0.9$

- a) The bicyclist is exerting 1.1 N of force.
- b) The bicyclist is exerting 49 N of force.
- c) The bicyclist is exerting 50 N of force.
- d) The bicyclist is exerting 51 N of force.

A

B

C

D

E

CQ.7.9

A 50 kg bicyclist starts his ride down the road with an acceleration of 1m/s^2 in air with a density of 1.2 kg/m^3 . If his velocity at a given moment is 2m/s , how much force is he exerting? Assume the area of his body is 0.5m^2 .

CQ 7.9

$\vec{a} = 1\text{m/s}^2$

$\vec{v} = 2\text{m/s}$

$\rho_{\text{air}} = 1.2\text{ kg/m}^3$

$C = 0.9$

$A_{\text{Body}} = 0.5\text{m}^2$

air

\vec{F}_N

\vec{F}_D

\vec{F}_A

\vec{F}_g

Drag Force

$\vec{F}_{\text{NET}} = m \cdot \vec{a} = \vec{F}_A - \vec{F}_D$

$\vec{F}_A = m \cdot \vec{a} + \vec{F}_D$

$= m \cdot a + \frac{1}{2} C \rho A v^2$

$= (50\text{kg} \cdot 1\text{m/s}^2) + \frac{1}{2} \cdot 0.9 \cdot 1.2\text{ kg/m}^3 \cdot 0.5\text{m}^2 \cdot (2\text{m/s})^2$

$\vec{F}_A = 51.1\text{N} \sim 51\text{N}$

- a) The bicyclist is exerting 1.1 N of force.
- b) The bicyclist is exerting 49 N of force.
- c) The bicyclist is exerting 50 N of force.
- ✓ d) The bicyclist is exerting 51 N of force.

Detailed solution: The F_{NET} of the bicyclist is calculated as $ma = 50\text{ kg} \times 1\text{ m/s}^2 = 50\text{ N}$. Since $F_{\text{NET}} = F_{\text{CYC}} - F_D$ we can solve the equation to find F_{CYC} . The drag force can be calculated using the equation $F_D = \frac{1}{2} C \rho A v^2$ where $C = 0.9$, $\rho = 1.2\text{kg/m}^3$, $A = 0.5\text{m}^2$, and $v = 2\text{m/s}$. F_D is calculated to be 1.08 N , so F_{CYC} must be 51.08 N . Then, adjust for significant figures.

A

B

C

D

E

CQ.7.10

A 2.20 kg toy plane takes off with an acceleration of 3.30 m/s^2 . The engine supplies a force of 8.15 N. Determine the magnitude of drag force acting on the plane as it accelerates.

a) 7.26 N

b) 15.4 N

c) 0.89 N

d) 0.0 N

A

B

C

D

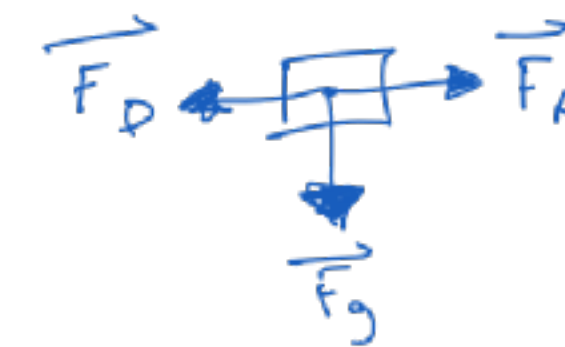
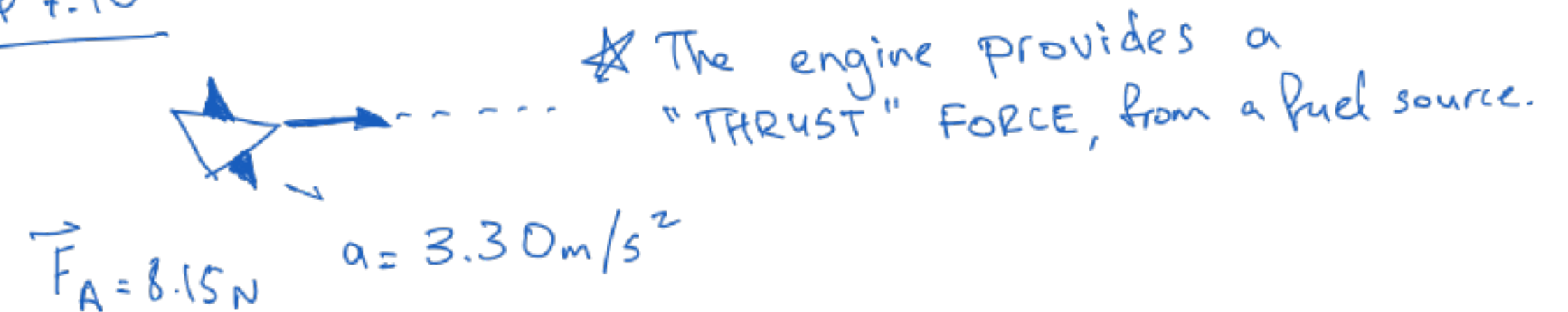
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CQ.7.10

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- a) 7.26 N
b) 15.4 N
✓ c) 0.89 N
d) 0.0 N

CQ 7.10



$$\vec{F}_{\text{NET}} = \vec{F}_A - \vec{F}_D = m \cdot \vec{a}$$

$$\vec{F}_D = \vec{F}_A - m \vec{a}$$
$$= 8.15 \text{ N} - (2.20 \text{ kg} \cdot 3.30 \text{ m/s}^2)$$

$$\boxed{\vec{F}_D = 0.89 \text{ N}}$$

Detailed solution: Without any drag force the airplane would accelerate at 3.7 m/s^2 . The drag force opposes a little bit of the force supplied by the motor. If you chose **15.4 N** you may have added a number that should have been subtracted. **7.26 N** is the net force acting on the plane. You'll need this to calculate the drag force.

A

B

C

D

E

Activity: Worked Problems

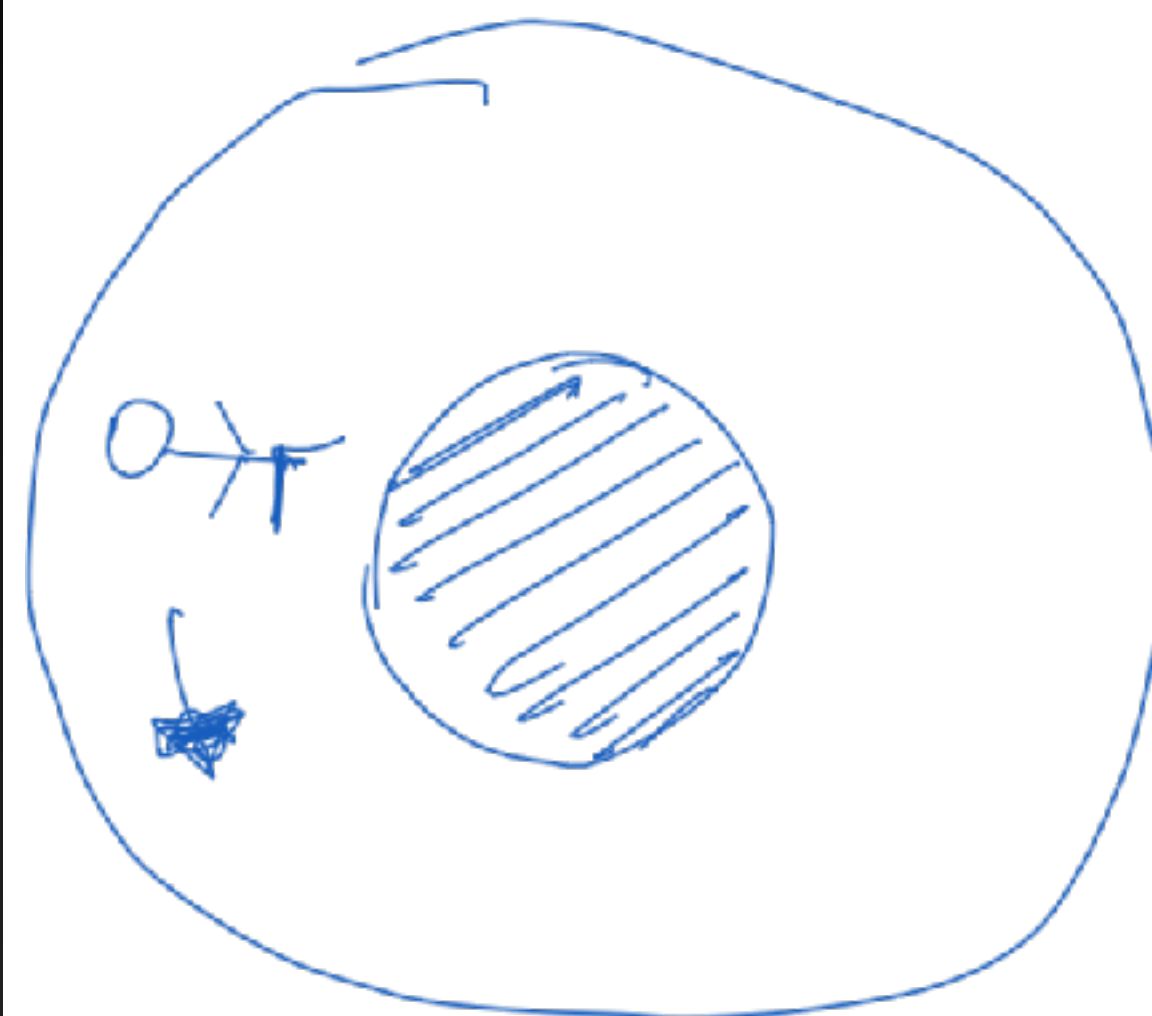
WP 7.3 - Rotor Ride: Friction & Centripetal Motion



WP 7.3 - Rotor Ride: Friction & Centripetal Motion



W 7.3



What friction force is required to keep the person stuck to the wall after the floor falls away?

F.B.D.



$$\underline{Y}: \vec{F}_{\text{NET}} = 0 = \vec{F}_g - \vec{F}_f$$

$$\underline{X}: \vec{F}_{\text{NET}} = m\vec{a} = \frac{m\omega^2}{R} = \vec{F}_N$$

Remember that:

$$\vec{F}_f = \mu_s \vec{F}_N$$

From here, you can solve any related problem!

See you next class!

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