

You can draw here

Physics 111 - Class 4C

2D and 3D Motion III

October 1, 2021

Do not draw in/on this box!

You can draw here

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Class Outline

- Logistics / Announcements
- Clicker Questions
- Activity: Worked Problem

Logistics/Announcements

- Lab this week: Lab 2
- HW4 due this week on Thursday at 6 PM
- Learning Log 4 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Bonus Test 1 available this week
- Test Window: Friday 6 PM - Sunday 6 PM

Introduction

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- ▶ 2 Vectors
- ▶ 3 Motion Along a Straight Line
- ▼ 4 Motion in Two and Three Dimensions

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- 4.2 Acceleration Vector
- 4.3 Projectile Motion
- 4.4 Uniform Circular Motion
- 4.5 Relative Motion in One and Two Dimensions

▶ Chapter Review

- ▶ 5 Newton's Laws of Motion
- ▶ 6 Applications of Newton's Laws
- ▶ 7 Work and Kinetic Energy
- ▶ 8 Potential Energy and Conservation of Energy
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- ▶ 11 Angular Momentum
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Figure 1.1 This image might be showing any number of things. It might be a whirlpool in a tank of water or perhaps a collage of paint and shiny beads done for art class. Without knowing the size of the object in units we all recognize, such as meters or inches, it is difficult to know what we're looking at. In fact, this image shows the Whirlpool Galaxy (and its companion galaxy), which is about 60,000 light-years in diameter (about 6×10^{17} km across). (credit: modification of work by S. Beckwith (STScI) Hubble Heritage Team, (STScI/AURA), ESA, NASA)

Chapter Outline

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- [1.2 Units and Standards](#)
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Relative Motion



The positions of particle P relative to frames S and S' are \vec{r}_{PS} and $\vec{r}_{PS'}$, respectively.

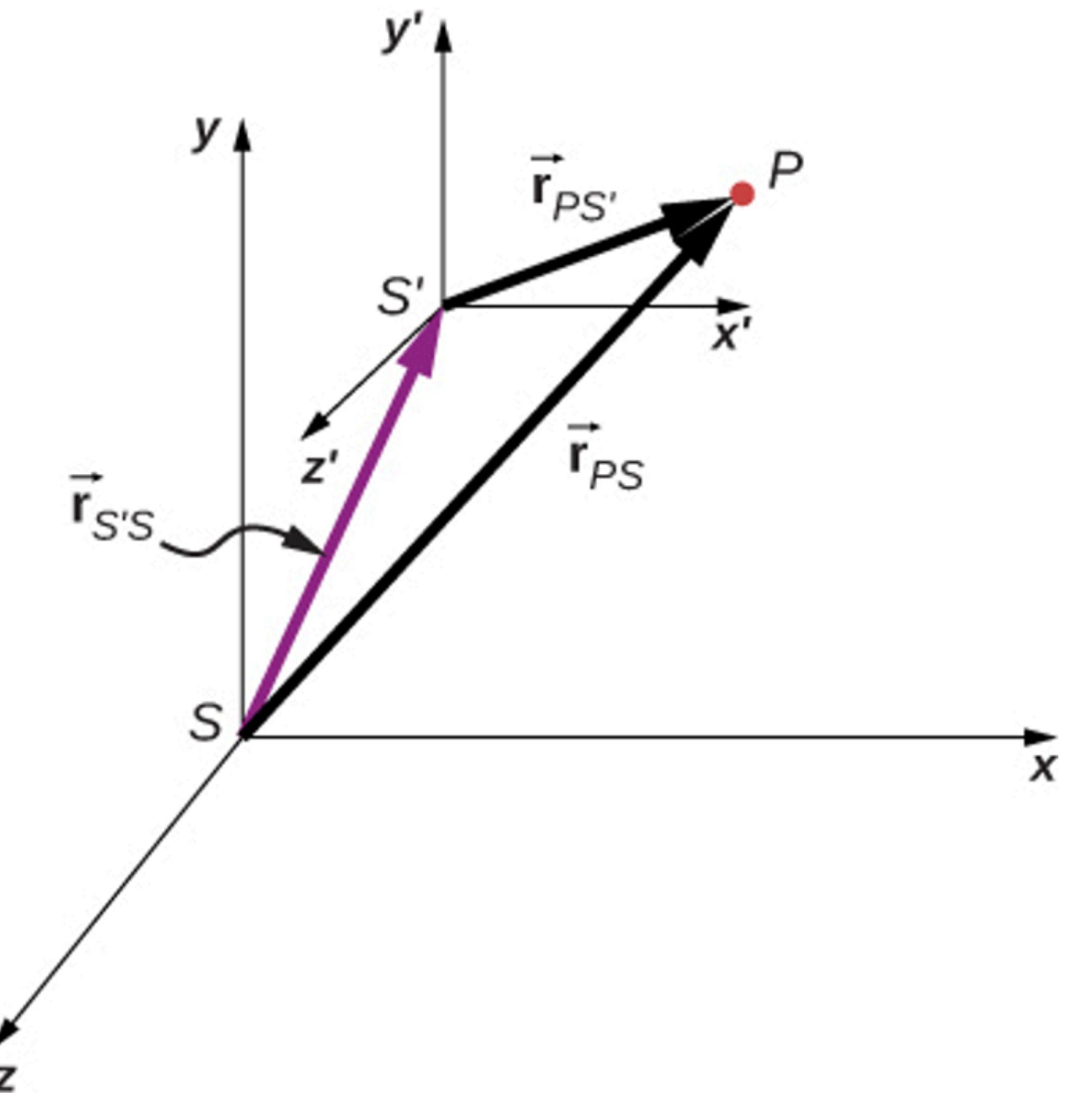


FIGURE 4.26

Relative Motion

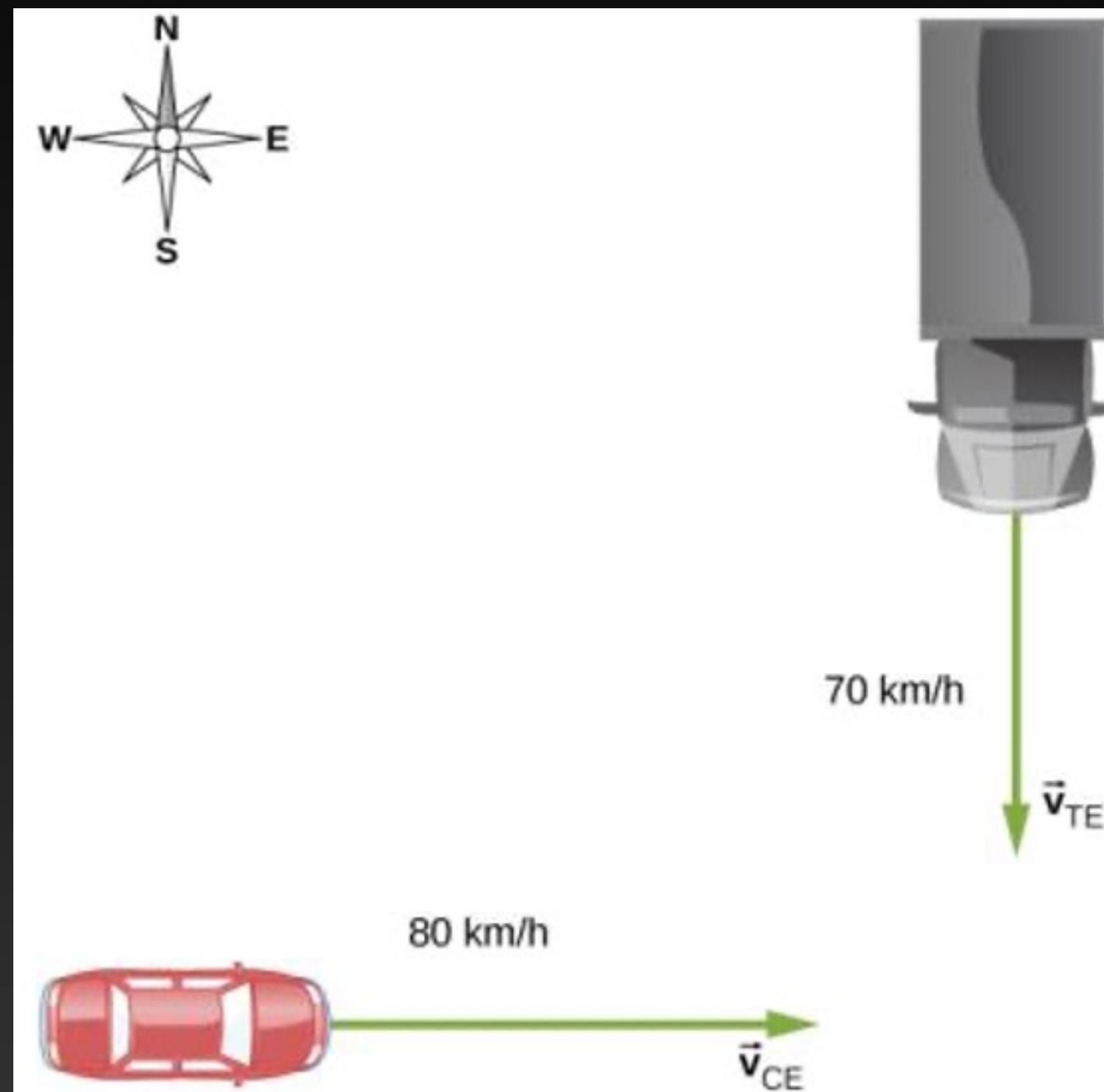
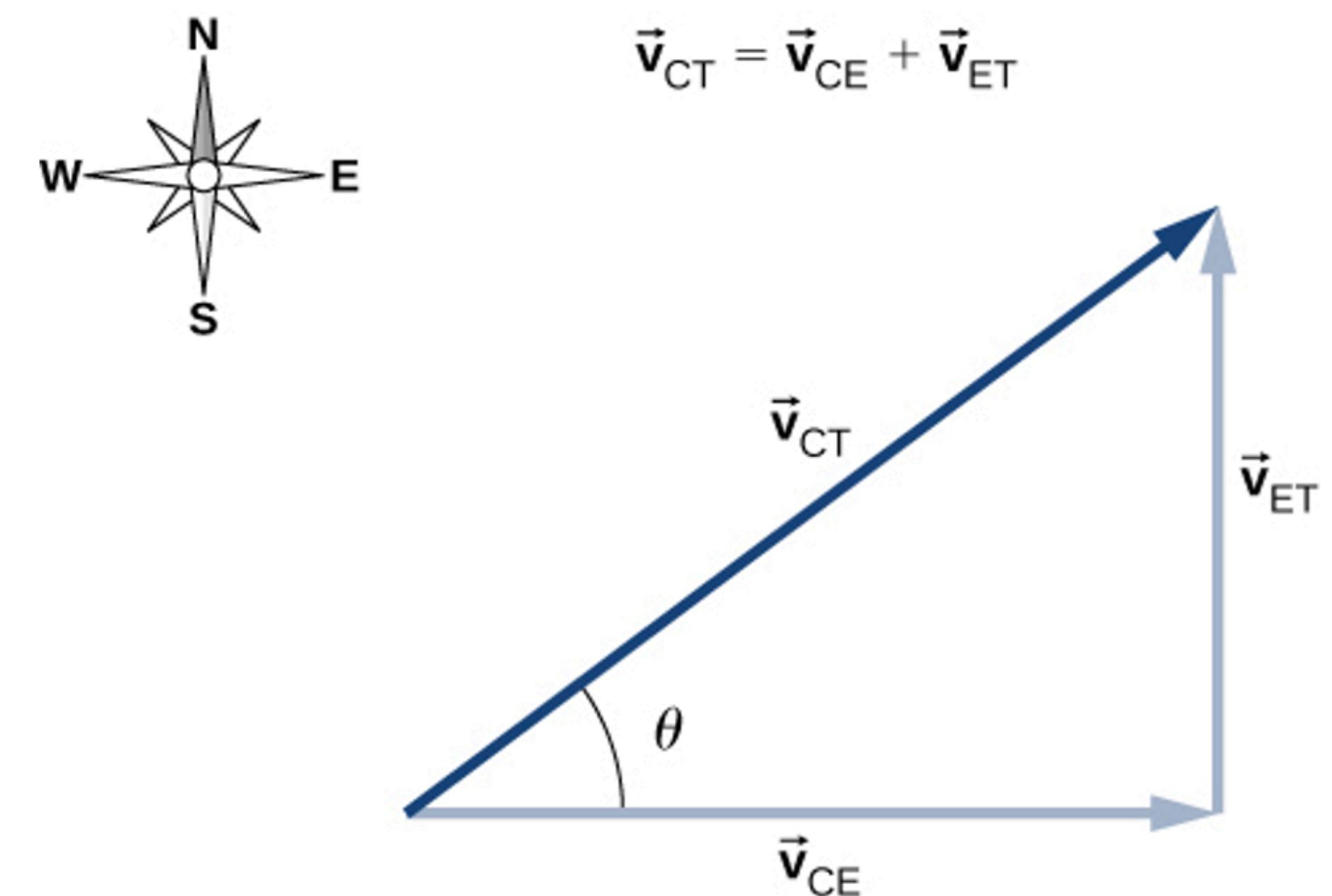


FIGURE 4.28



Vector diagram of the vector equation $\vec{v}_{CT} = \vec{v}_{CE} + \vec{v}_{ET}$.

Key Equations

Position vector

$$\vec{r}(t) = x(t)\hat{\mathbf{i}} + y(t)\hat{\mathbf{j}} + z(t)\hat{\mathbf{k}}$$

Displacement vector

$$\Delta\vec{r} = \vec{r}(t_2) - \vec{r}(t_1)$$

Velocity vector

$$\vec{v}(t) = \lim_{\Delta t \rightarrow 0} \frac{\vec{r}(t+\Delta t) - \vec{r}(t)}{\Delta t} = \frac{d\vec{r}}{dt}$$

Velocity in terms of components

$$\vec{v}(t) = v_x(t)\hat{\mathbf{i}} + v_y(t)\hat{\mathbf{j}} + v_z(t)\hat{\mathbf{k}}$$

Velocity components

$$v_x(t) = \frac{dx(t)}{dt} \quad v_y(t) = \frac{dy(t)}{dt} \quad v_z(t) = \frac{dz(t)}{dt}$$

Average velocity

$$\vec{v}_{\text{avg}} = \frac{\vec{r}(t_2) - \vec{r}(t_1)}{t_2 - t_1}$$

Instantaneous acceleration

$$\vec{a}(t) = \lim_{t \rightarrow 0} \frac{\vec{v}(t+\Delta t) - \vec{v}(t)}{\Delta t} = \frac{d\vec{v}(t)}{dt}$$

Instantaneous acceleration, component form

$$\vec{a}(t) = \frac{dv_x(t)}{dt}\hat{\mathbf{i}} + \frac{dv_y(t)}{dt}\hat{\mathbf{j}} + \frac{dv_z(t)}{dt}\hat{\mathbf{k}}$$

Instantaneous acceleration as second derivatives of position

$$\vec{a}(t) = \frac{d^2x(t)}{dt^2}\hat{\mathbf{i}} + \frac{d^2y(t)}{dt^2}\hat{\mathbf{j}} + \frac{d^2z(t)}{dt^2}\hat{\mathbf{k}}$$

Key Equations

Time of flight

$$T_{\text{tof}} = \frac{2(v_0 \sin \theta_0)}{g}$$

Trajectory

$$y = (\tan \theta_0)x - \left[\frac{g}{2(v_0 \cos \theta_0)^2} \right] x^2$$

Range

$$R = \frac{v_0^2 \sin 2\theta_0}{g}$$

Centripetal acceleration

$$a_C = \frac{v^2}{r}$$

Position vector, uniform circular motion

$$\vec{r}(t) = A \cos \omega t \hat{i} + A \sin \omega t \hat{j}$$

Velocity vector, uniform circular motion

$$\vec{v}(t) = \frac{d\vec{r}(t)}{dt} = -A\omega \sin \omega t \hat{i} + A\omega \cos \omega t \hat{j}$$

Acceleration vector, uniform circular motion

$$\vec{a}(t) = \frac{d\vec{v}(t)}{dt} = -A\omega^2 \cos \omega t \hat{i} - A\omega^2 \sin \omega t \hat{j}$$

Tangential acceleration

$$a_T = \frac{d|\vec{v}|}{dt}$$

Total acceleration

$$\vec{a} = \vec{a}_C + \vec{a}_T$$

Key Equations

Position vector in frame

S is the position
vector in frame S' plus the vector from the
origin of S to the origin of S'

$$\vec{r}_{PS} = \vec{r}_{PS'} + \vec{r}_{S'S}$$

Relative velocity equation connecting two
reference frames

$$\vec{v}_{PS} = \vec{v}_{PS'} + \vec{v}_{S'S}$$

Relative velocity equation connecting more
than two reference frames

$$\vec{v}_{PC} = \vec{v}_{PA} + \vec{v}_{AB} + \vec{v}_{BC}$$

Relative acceleration equation

$$\vec{a}_{PS} = \vec{a}_{PS'} + \vec{a}_{S'S}$$

Clicker Questions

CQ.4.9

 Multi-part question

Another airplane is flying in a jet stream that is blowing at 45.0 m/s in a direction 20° south of east (as in Exercise 7). Its direction of motion relative to the Earth is 45.0° south of west, while its direction of travel relative to the air is 5.00° south of west. What is the airplane's speed relative to the air mass?

- a) 45.0 m/s
- b) 29.6 m/s
- c) 63.5 m/s
- d) 53.2 m/s

A

B

C

D

E

CQ.4.9

 Multi-part question

Another airplane is flying in a jet stream that is blowing at 45.0 m/s in a direction 20° south of east (as in Exercise 7). Its direction of motion relative to the Earth is 45.0° south of west, while its direction of travel relative to the air is 5.00° south of west. What is the airplane's speed relative to the air mass?

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CQ.4.10

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Another airplane is flying in a jet stream that is blowing at 45.0 m/s in a direction 20° south of east (as in Exercise 7). Its direction of motion relative to the Earth is 45.0° south of west, while its direction of travel relative to the air is 5.00° south of west. What is the airplane's speed relative to the air mass?

What is the airplane's speed relative to the Earth?

- a) 108 m/s
- b) 106 m/s
- c) 18.5 m/s
- d) 29.6 m/s

A

B

C

D

E

CQ.4.10

 Multi-part question

Another airplane is flying in a jet stream that is blowing at 45.0 m/s in a direction 20° south of east (as in Exercise 7). Its direction of motion relative to the Earth is 45.0° south of west, while its direction of travel relative to the air is 5.00° south of west. What is the airplane's speed relative to the air mass?

What is the airplane's speed relative to the Earth?

- a) 108 m/s
- b) 106 m/s
- c) 18.5 m/s
- d) 29.6 m/s

A

B

C

D

E

CQ.4.11

A person attempts to cross a river in a straight line by navigating a boat at 15 m/s. If the river flows at 5.0 m/s from his left to right, what would be the magnitude of the boat's resultant velocity? In what direction would the boat go, relative to the straight line across it?

- a) The resultant velocity of the boat will be 10.0 m/s. The boat will go toward his right at an angle of 26.6° to a line drawn across the river.
- b) The resultant velocity of the boat will be 10.0 m/s. The boat will go toward his left at an angle of 26.6° to a line drawn across the river.
- c) The resultant velocity of the boat will be 15.8 m/s. The boat will go toward his right at an angle of 18.4° to a line drawn across the river.
- d) The resultant velocity of the boat will be 15.8 m/s. The boat will go toward his left at an angle of 18.4° to a line drawn across the river.

A

B

C

D

E

CQ.4.11

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- c) The resultant velocity of the boat will be 15.8 m/s. The boat will go toward his right at an angle of 18.4° to a line drawn across the river.
- d) The resultant velocity of the boat will be 15.8 m/s. The boat will go toward his left at an angle of 18.4° to a line drawn across the river.

Detailed solution: The resultant velocity of the boat will be 15.8 m/s. The boat will travel toward his right at an angle of 18.4° to a line drawn straight across the river.

A

B

C

D

E

CQ.4.8

 Multi-part question

A football player punts the ball at a 45.0° angle. Without an effect from the wind, the ball would travel 60.0 m horizontally.

When the ball is near its maximum height it experiences a brief gust of wind that reduces its horizontal velocity by 1.50 m/s. What distance does the ball travel horizontally?

- a) 69.6 m
- b) 57.4 m
- c) 60.0 m
- d) 57.8 m

A

B

C

D

E

CQ.4.8

 Multi-part question

A football player punts the ball at a 45.0° angle. Without an effect from the wind, the ball would travel 60.0 m horizontally.

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A

B

C

D

E

Activity:

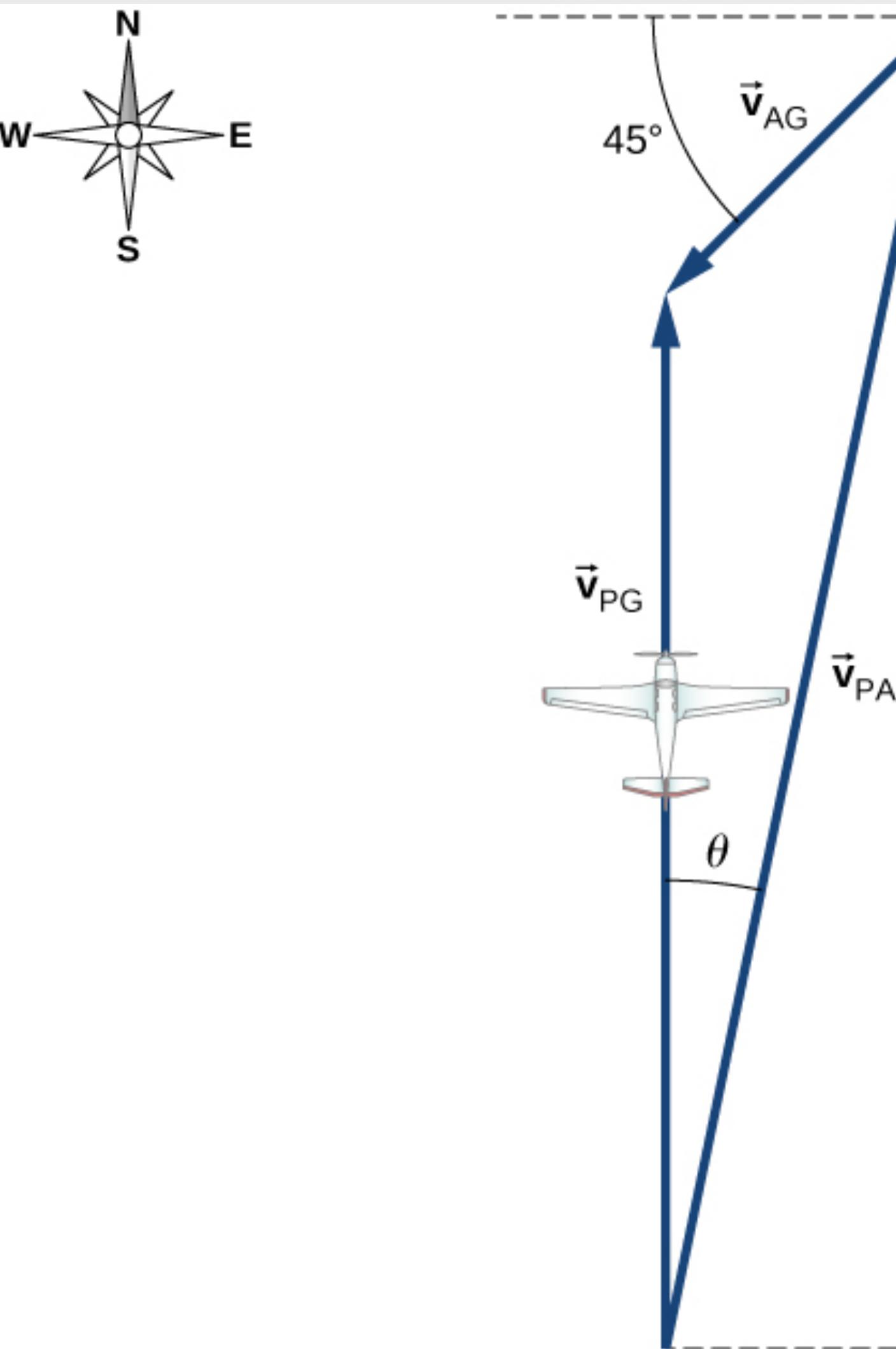
Worked Problem

EXAMPLE 4.14

WP 4.3

Flying a Plane in a Wind

A pilot must fly his plane due north to reach his destination. The plane can fly at 300 km/h in still air. A wind is blowing out of the northeast at 90 km/h. (a) What is the speed of the plane relative to the ground? (b) In what direction must the pilot head her plane to fly due north?

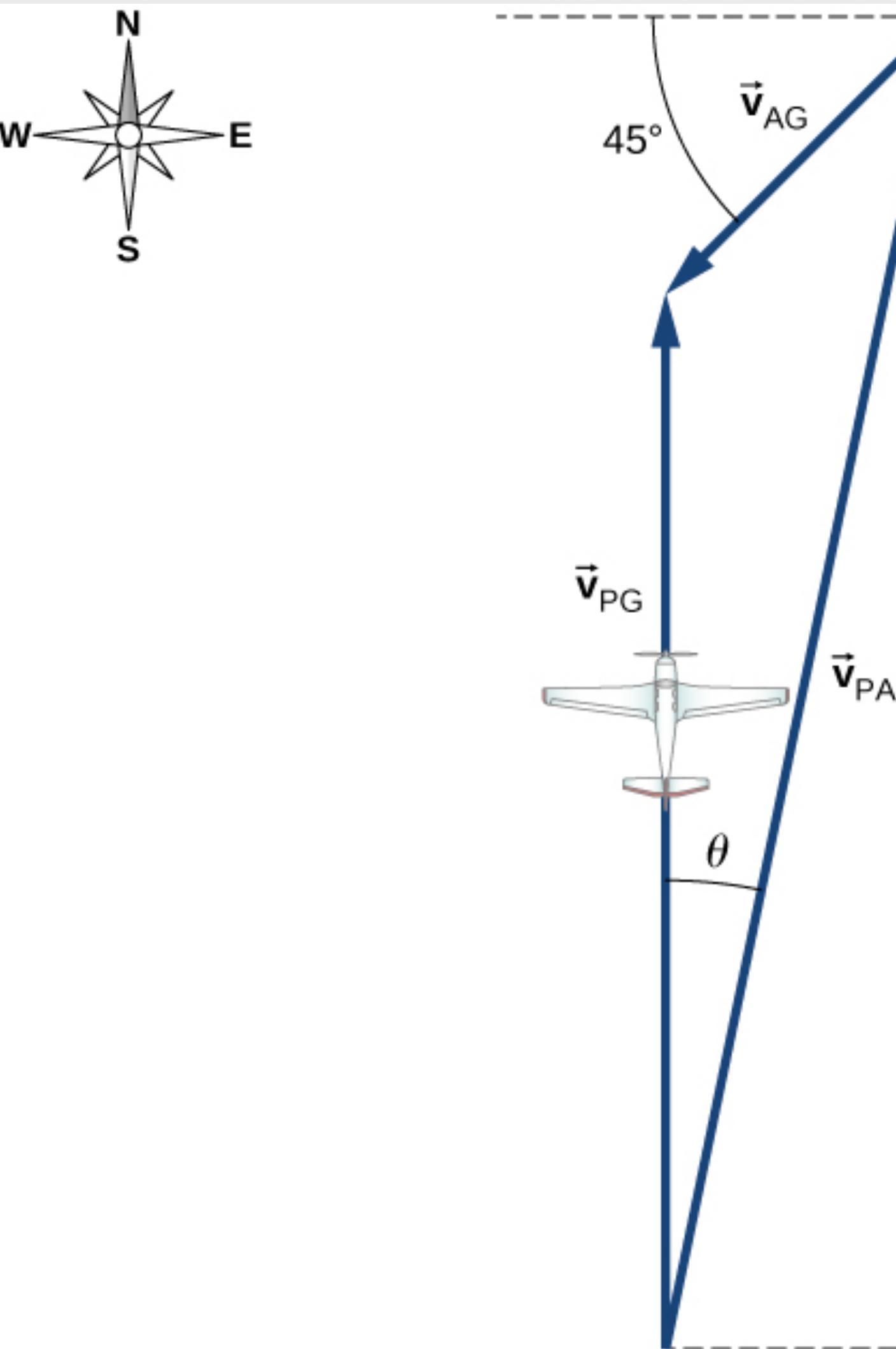


EXAMPLE 4.14

WP 4.2

Flying a Plane in a Wind

A pilot must fly his plane due north to reach his destination. The plane can fly at 300 km/h in still air. A wind is blowing out of the northeast at 90 km/h. (a) What is the speed of the plane relative to the ground? (b) In what direction must the pilot head her plane to fly due north?



(a) Known quantities:

$$|\vec{v}_{PA}| = 300 \text{ km/h}$$

$$|\vec{v}_{AG}| = 90 \text{ km/h}$$

Substituting into the equation of motion, we obtain $|\vec{v}_{PG}| = 230 \text{ km/h}$.

(b) The angle $\theta = \tan^{-1} \frac{63.64}{300} = 12^\circ$ east of north.

70 . The coordinate axes of the reference frame S' remain parallel to those of S , as S' moves away from S at a constant velocity $\vec{v}_{S'S} = (1.0\hat{i} + 2.0\hat{j} + 3.0\hat{k})t$ m/s. (a) If at time $t = 0$ the origins coincide, what is the position of origin O' in the S frame as a function of time? (b) How is particle position for $\vec{r}(t)$ and $\vec{r}'(t)$, as measured in S and S' , respectively, related? (c) What is the relationship between particle velocities $\vec{v}(t)$ and $\vec{v}'(t)$? (d) How are accelerations $\vec{a}(t)$ and $\vec{a}'(t)$ related?

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a. $\vec{r}_{S'S} = (1.0 \hat{i} + 2.0 \hat{j} + 3.0 \hat{k})t^2/2$ m = $\vec{a}_o t^2 / 2$,

b. $\vec{r}(t) = \vec{r}'(t) + \vec{r}_{S'S}$, $\vec{r}'(t) + (1.0 \hat{i} + 2.0 \hat{j} + 3.0 \hat{k})t^2/2$ m = $\vec{r}'(t) + \vec{a}_o t^2 / 2$,

c. $\vec{v}(t) = \vec{v}'(t) + \vec{v}_{S'S}$, d. $\vec{a}(t) = \vec{a}'(t) + (1.0 \hat{i} + 2.0 \hat{j} + 3.0 \hat{k})$ m/s² = $\vec{a}'(t) + \vec{a}_o$

See you next class!

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