

You can draw here

Physics 111 - Class 4A

2D and 3D Motion I

September 27, 2021

Do not draw in/on this box!

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Class Outline

- Logistics / Announcements
- Test 1 Reflection
- Introduction to Chapter 4
- Clicker Questions
- Activity: Worked Problem

Logistics/Announcements

- Lab this week: Lab 2
- HW4 due this week on Thursday at 6 PM
- Learning Log 4 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Bonus Test 1 available this week
- Test Window: Friday 6 PM - Sunday 6 PM



Physics 111

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Unsyllabus

ABOUT THIS COURSE

- Course Syllabus (Official)
- Course Schedule
- Accommodations
- How to do well in this course

GETTING STARTED

- Before the Term starts
- After the first class
- In the first week
- Week 1 - Introductions!

PART 1 - KINEMATICS

- Week 2 - Chapter 2
- Week 3 - Chapter 3

Week 4 - Chapter 4

Readings

Videos

Homework

Week 2 Classes

Bonus Test 01

Videos

Below are the assigned videos for this week. The videos are collapsible so once you're done with one, you can move to the next one. In the sidebar on the right, you can use the checklists to keep track of what's done.

Content Summary from Crash Course Physics

2D Motion

The video on uniform circular motion mentions forces - this we will cover in Chapter 5.

Uniform Circular Motion

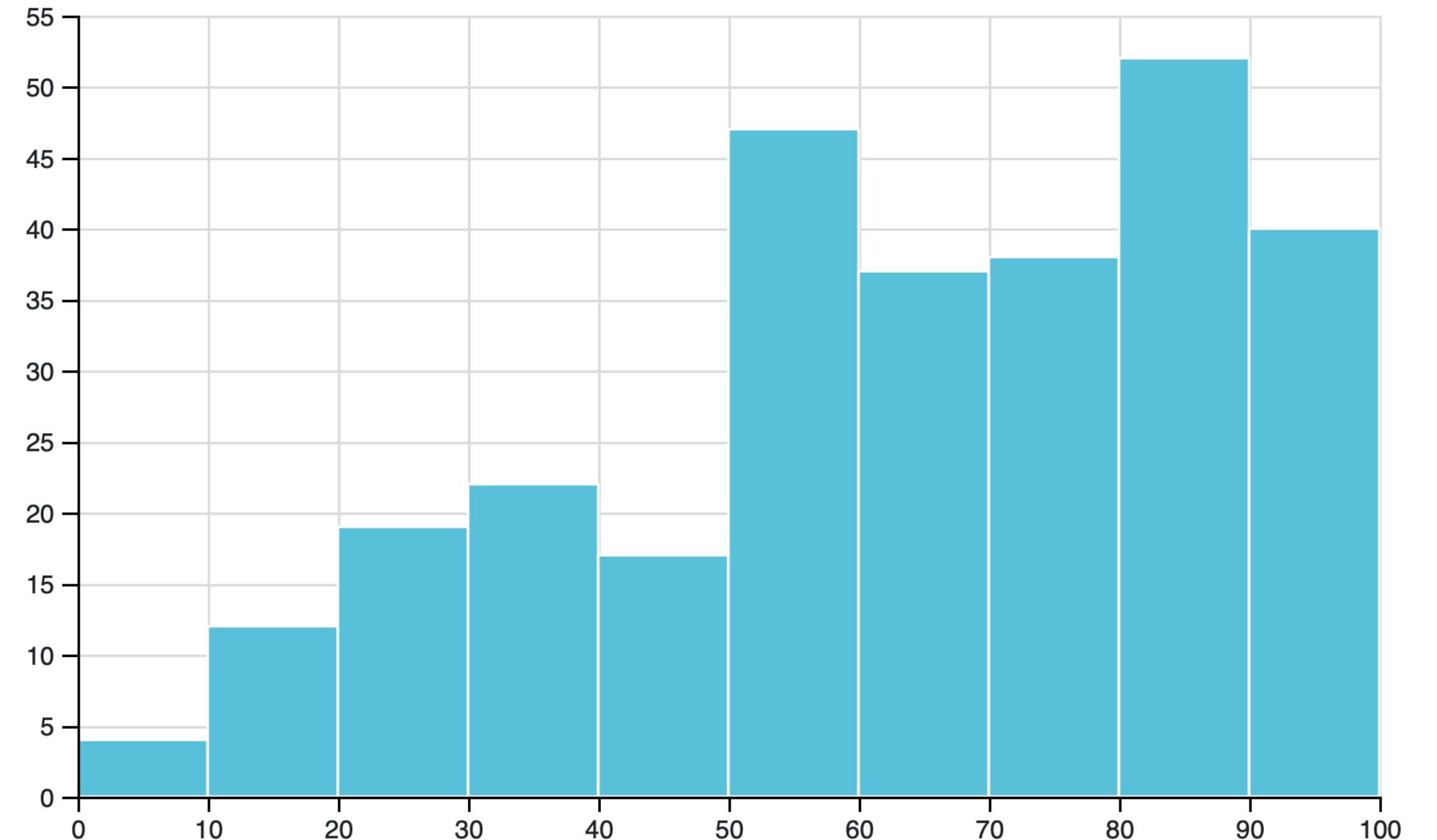
The video on uniform circular motion mentions forces - this we will cover in Chapter 5.

Checklist of items

- CrashCourse Physics I - 2D Motion
- CrashCourse Physics I - Uniform Circular Motion
- Video 1 - Introduction to Projectile Motion
- Video 4 - Nerd-A-Pult - An Introductory Projectile Motion Problem
- Video 7 - Understanding the Range Equation of Projectile Motion
- Video 12 - A Projectile Motion Problem using Unit Vectors
- Video 16 - Introduction to Relative Motion using a Quadcopter Drone

Test 1 Reflection

Tests and Bonus Tests 1: Score statistics



Number of students

288

Mean score

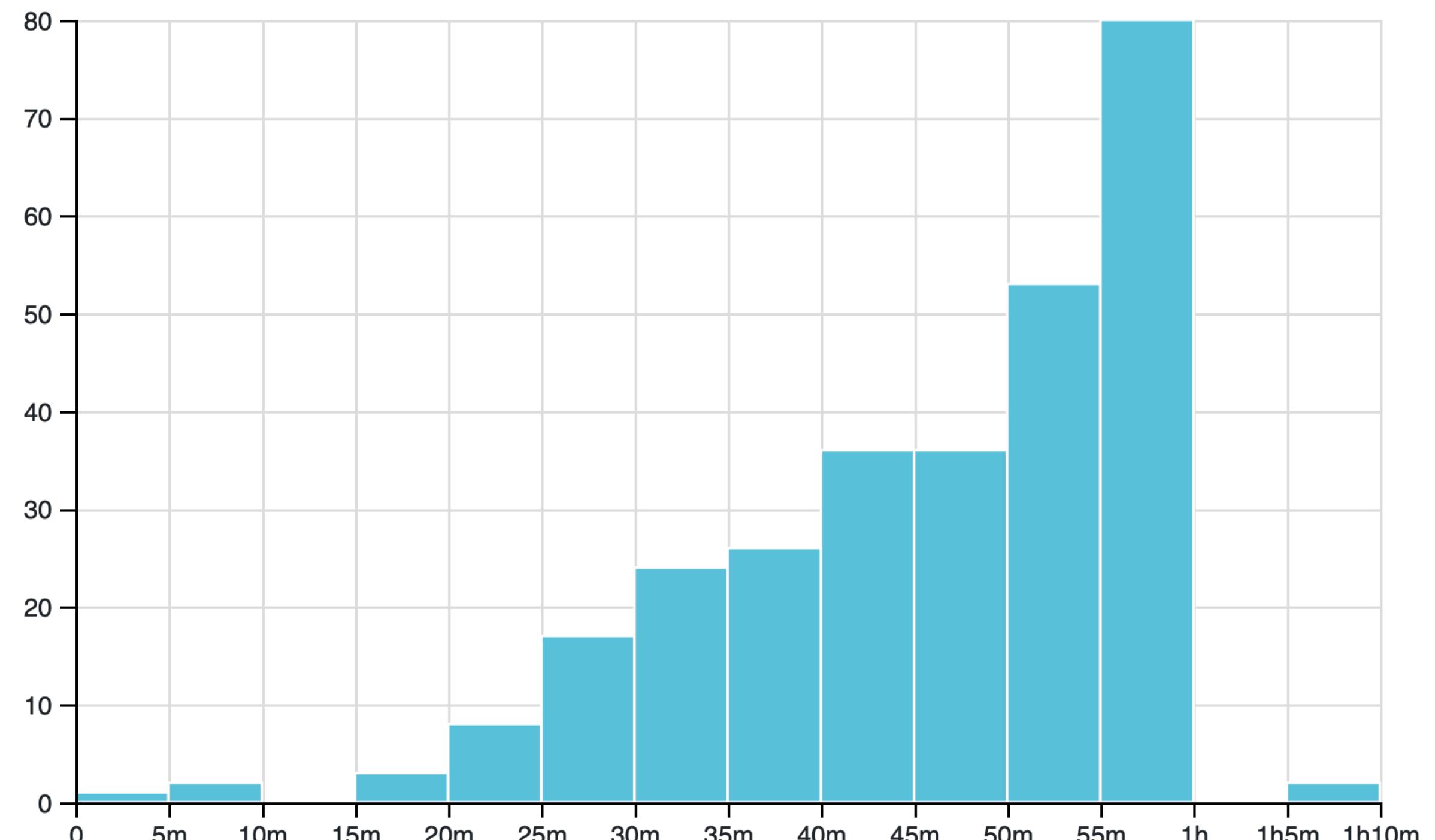
63%

Standard deviation

25%

Test 1 Reflection

Tests and Bonus Tests 1: Duration statistics



Mean duration

46m

Test 1 Reflection

Adjustment
(from Bonus
Test 1 onwards)

- Numeric answers will **increase in tolerance** from 1% to a much more generous 5%

Test 1 Reflection

Adjustment
(from Bonus
Test 1 onwards)

- Numeric answers will **increase in tolerance** from 1% to a much more generous 5%

Test 1

- Numeric answers will increase in tolerance from 1% to a much more generous 5%

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Figure 3.1 A JR Central L0 series five-car maglev (magnetic levitation) train undergoing a test run on the Yamanashi Test Track. The maglev train's motion can be described using kinematics, the subject of this chapter. (credit: modification of work by "Maryland GovPics"/Flickr)

Chapter Outline

[3.1 Position, Displacement, and Average Velocity](#)[3.2 Instantaneous Velocity and Speed](#)[3.3 Average and Instantaneous Acceleration](#)[3.4 Motion with Constant Acceleration](#)[3.5 Free Fall](#)[3.6 Finding Velocity and Displacement from Acceleration](#)

Our universe is full of objects in motion. From the stars, planets, and galaxies; to the motion of people and animals; down to the microscopic scale of atoms and molecules—everything in our universe is in motion. We can describe motion using the two disciplines of kinematics and dynamics. We study dynamics, which is concerned with the causes of motion, in [Newton's Laws of Motion](#); but, there is much to be learned about motion without referring to what causes it, and this is the study of kinematics. Kinematics involves describing motion through properties such

Conventions for Motion in 1D, 2D, 3D

$$x = x(t) \quad y = y(t) \quad z = z(t)$$

$$\vec{r} = x(t)\hat{i} + y(t)\hat{j} + z(t)\hat{k}$$

$$\vec{v} = \frac{d}{dt}\vec{r} = v_x(t)\hat{i} + v_y(t)\hat{j} + v_z(t)\hat{k}$$

$$\vec{a} = \frac{d^2}{dt^2}\vec{r} = a_x(t)\hat{i} + a_y(t)\hat{j} + a_z(t)\hat{k}$$

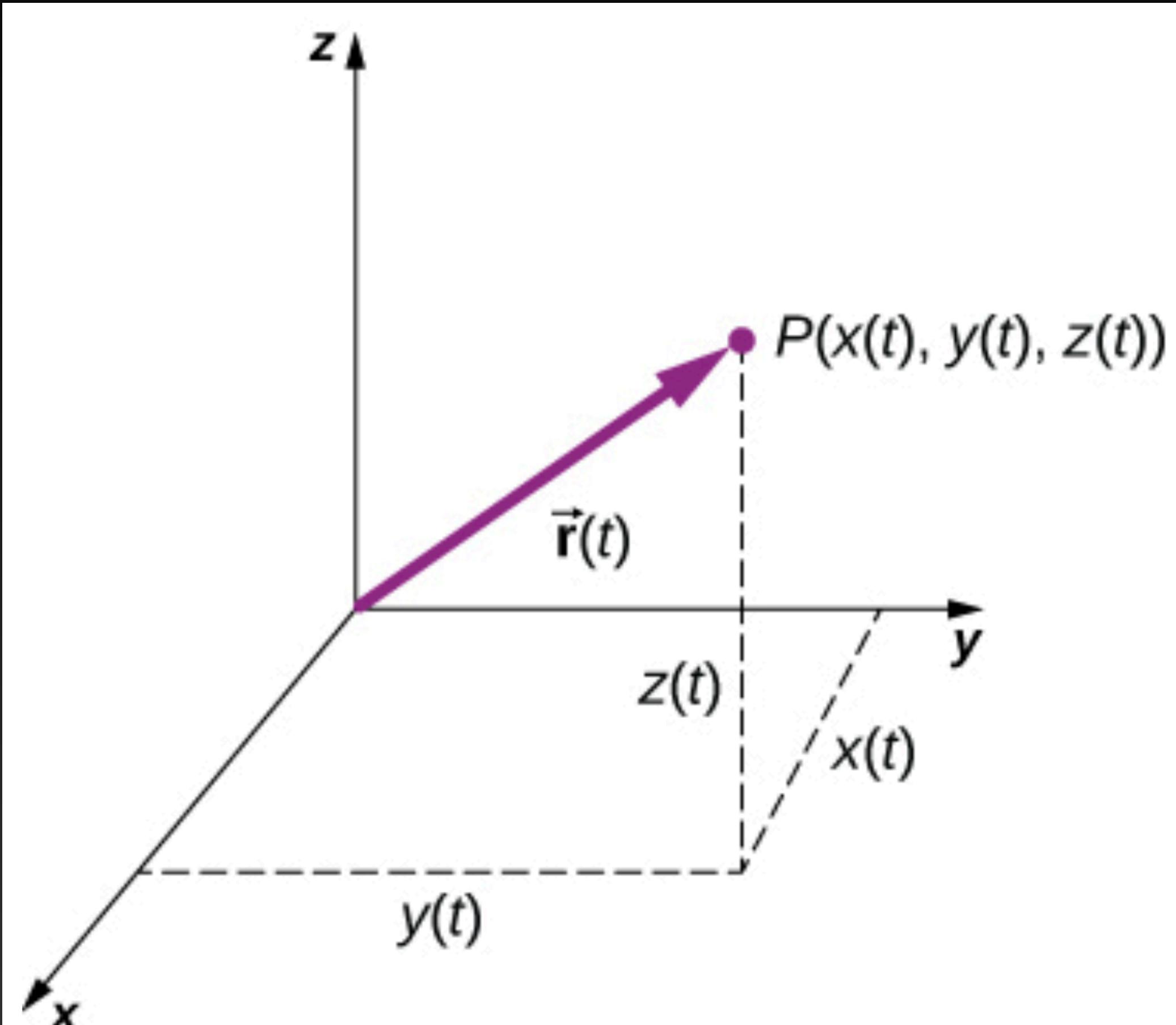


Figure 4.2 A three-dimensional coordinate system with a particle at position $P(x(t), y(t), z(t))$.

Projectile Motion

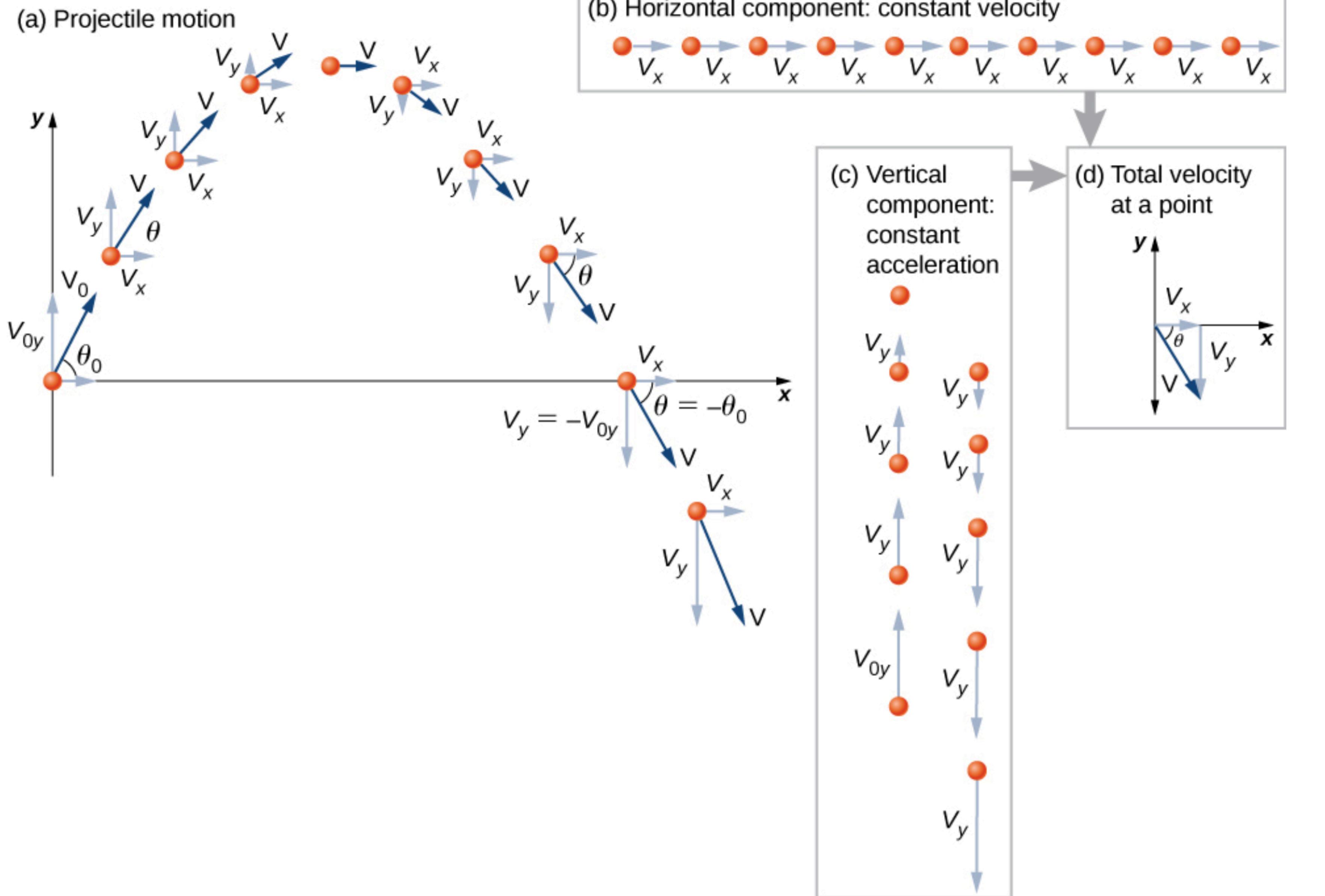


Figure 4.12 (a) We analyze two-dimensional projectile motion by breaking it into two independent one-dimensional motions along the vertical and horizontal axes. (b) The horizontal motion is simple, because $a_x = 0$ and v_x is a constant. (c) The velocity in the vertical direction begins to decrease as the object rises. At its highest point, the vertical velocity is zero. As the object falls toward Earth again, the vertical velocity increases again in magnitude but points in the opposite direction to the initial vertical velocity. (d) The x and y motions are recombined to give the total velocity at any given point on the trajectory.

Uniform Circular Motion

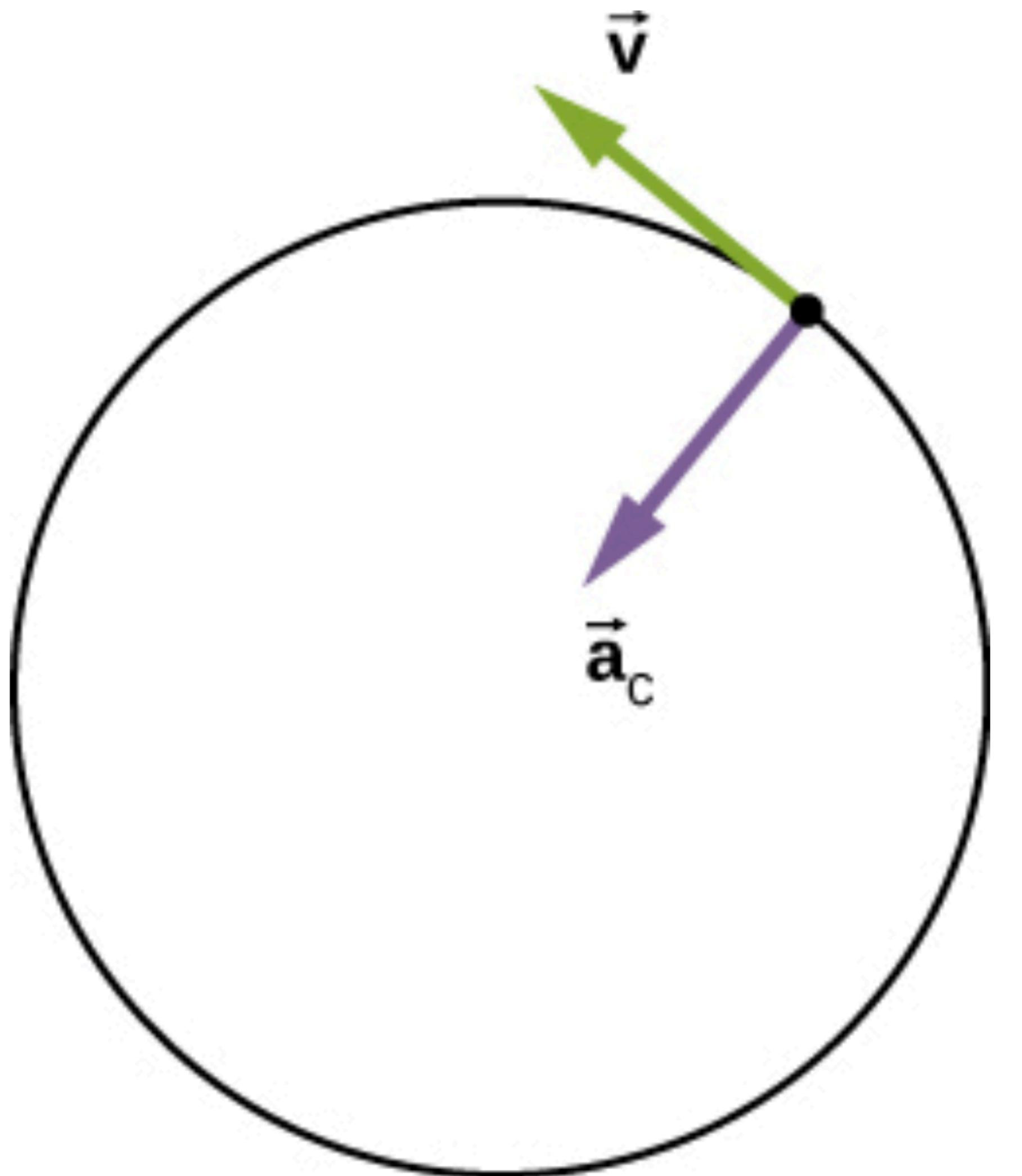


Figure 4.19 The centripetal acceleration vector points toward the center of the circular path of motion and is an acceleration in the radial direction. The velocity vector is also shown and is tangent to the circle.

Key Equations

Position vector

$$\vec{r}(t) = x(t)\hat{\mathbf{i}} + y(t)\hat{\mathbf{j}} + z(t)\hat{\mathbf{k}}$$

Displacement vector

$$\Delta\vec{r} = \vec{r}(t_2) - \vec{r}(t_1)$$

Velocity vector

$$\vec{v}(t) = \lim_{\Delta t \rightarrow 0} \frac{\vec{r}(t+\Delta t) - \vec{r}(t)}{\Delta t} = \frac{d\vec{r}}{dt}$$

Velocity in terms of components

$$\vec{v}(t) = v_x(t)\hat{\mathbf{i}} + v_y(t)\hat{\mathbf{j}} + v_z(t)\hat{\mathbf{k}}$$

Velocity components

$$v_x(t) = \frac{dx(t)}{dt} \quad v_y(t) = \frac{dy(t)}{dt} \quad v_z(t) = \frac{dz(t)}{dt}$$

Average velocity

$$\vec{v}_{\text{avg}} = \frac{\vec{r}(t_2) - \vec{r}(t_1)}{t_2 - t_1}$$

Instantaneous acceleration

$$\vec{a}(t) = \lim_{t \rightarrow 0} \frac{\vec{v}(t+\Delta t) - \vec{v}(t)}{\Delta t} = \frac{d\vec{v}(t)}{dt}$$

Instantaneous acceleration, component form

$$\vec{a}(t) = \frac{dv_x(t)}{dt}\hat{\mathbf{i}} + \frac{dv_y(t)}{dt}\hat{\mathbf{j}} + \frac{dv_z(t)}{dt}\hat{\mathbf{k}}$$

Instantaneous acceleration as second derivatives of position

$$\vec{a}(t) = \frac{d^2x(t)}{dt^2}\hat{\mathbf{i}} + \frac{d^2y(t)}{dt^2}\hat{\mathbf{j}} + \frac{d^2z(t)}{dt^2}\hat{\mathbf{k}}$$

Key Equations

Time of flight

$$T_{\text{tof}} = \frac{2(v_0 \sin \theta_0)}{g}$$

Trajectory

$$y = (\tan \theta_0)x - \left[\frac{g}{2(v_0 \cos \theta_0)^2} \right] x^2$$

Range

$$R = \frac{v_0^2 \sin 2\theta_0}{g}$$

Centripetal acceleration

$$a_C = \frac{v^2}{r}$$

Position vector, uniform circular motion

$$\vec{r}(t) = A \cos \omega t \hat{i} + A \sin \omega t \hat{j}$$

Velocity vector, uniform circular motion

$$\vec{v}(t) = \frac{d\vec{r}(t)}{dt} = -A\omega \sin \omega t \hat{i} + A\omega \cos \omega t \hat{j}$$

Acceleration vector, uniform circular motion

$$\vec{a}(t) = \frac{d\vec{v}(t)}{dt} = -A\omega^2 \cos \omega t \hat{i} - A\omega^2 \sin \omega t \hat{j}$$

Tangential acceleration

$$a_T = \frac{d|\vec{v}|}{dt}$$

Total acceleration

$$\vec{a} = \vec{a}_C + \vec{a}_T$$

Key Equations

Position vector in frame

S is the position
vector in frame S' plus the vector from the
origin of S to the origin of S'

$$\vec{r}_{PS} = \vec{r}_{PS'} + \vec{r}_{S'S}$$

Relative velocity equation connecting two
reference frames

$$\vec{v}_{PS} = \vec{v}_{PS'} + \vec{v}_{S'S}$$

Relative velocity equation connecting more
than two reference frames

$$\vec{v}_{PC} = \vec{v}_{PA} + \vec{v}_{AB} + \vec{v}_{BC}$$

Relative acceleration equation

$$\vec{a}_{PS} = \vec{a}_{PS'} + \vec{a}_{S'S}$$

Clicker Questions

CQ.4.1

Consider vectors \vec{A} , \vec{B} , and their resultant $\vec{R} = \vec{A} + \vec{B}$. How can you express its magnitude in terms of A_x , A_y , B_x , and B_y ?

- a) $|\vec{R}| = (A_x + B_x) + (A_y + B_y)$
- b) $|\vec{R}| = (A_x + B_x) - (A_y + B_y)$
- c) $|\vec{R}| = (A_x + B_x)^2 + (A_y + B_y)^2$
- d) $|\vec{R}| = \sqrt{(A_x + B_x)^2 + (A_y + B_y)^2}$

A

B

C

D

E

CQ.4.2

Consider vectors \vec{A} , \vec{B} , and their resultant \vec{R} . How can you express its direction as a counterclockwise angle from positive x in terms of A_x , A_y , B_x , and B_y ?

- a) $\theta = \sin^{-1} \left(\frac{A_y+B_y}{A_x+B_x} \right)$
- b) $\theta = \cos^{-1} \left(\frac{A_y+B_y}{A_x+B_x} \right)$
- c) $\theta = \tan^{-1} \left(\frac{A_x+B_x}{A_y+B_y} \right)$
- d) $\theta = \tan^{-1} \left(\frac{A_y+B_y}{A_x+B_x} \right)$

A

B

C

D

E

CQ.4.3

When will the x-component of a vector with angle θ be greater than its y-component?

- a) $0^\circ < \theta < 45^\circ$

The value of a vector's x-component is more than the value of its y-component when the angle is between 0° and 45° .

- b) $\theta = 45^\circ$

The value of x and y-component of the vector will be same at this angle.

- c) $45^\circ < \theta < 60^\circ$

Try to recall the variation of values of trigonometric identities with the increasing value of the angle.

- d) $60^\circ < \theta < 90^\circ$

Resolve the vector into its components and evaluate the expression for given values of the angle. The x-component will not be greater than the y-component.

A

B

C

D

E

Activity:

Worked Problem

EXAMPLE 4.6**WP 4.1****A Skier**

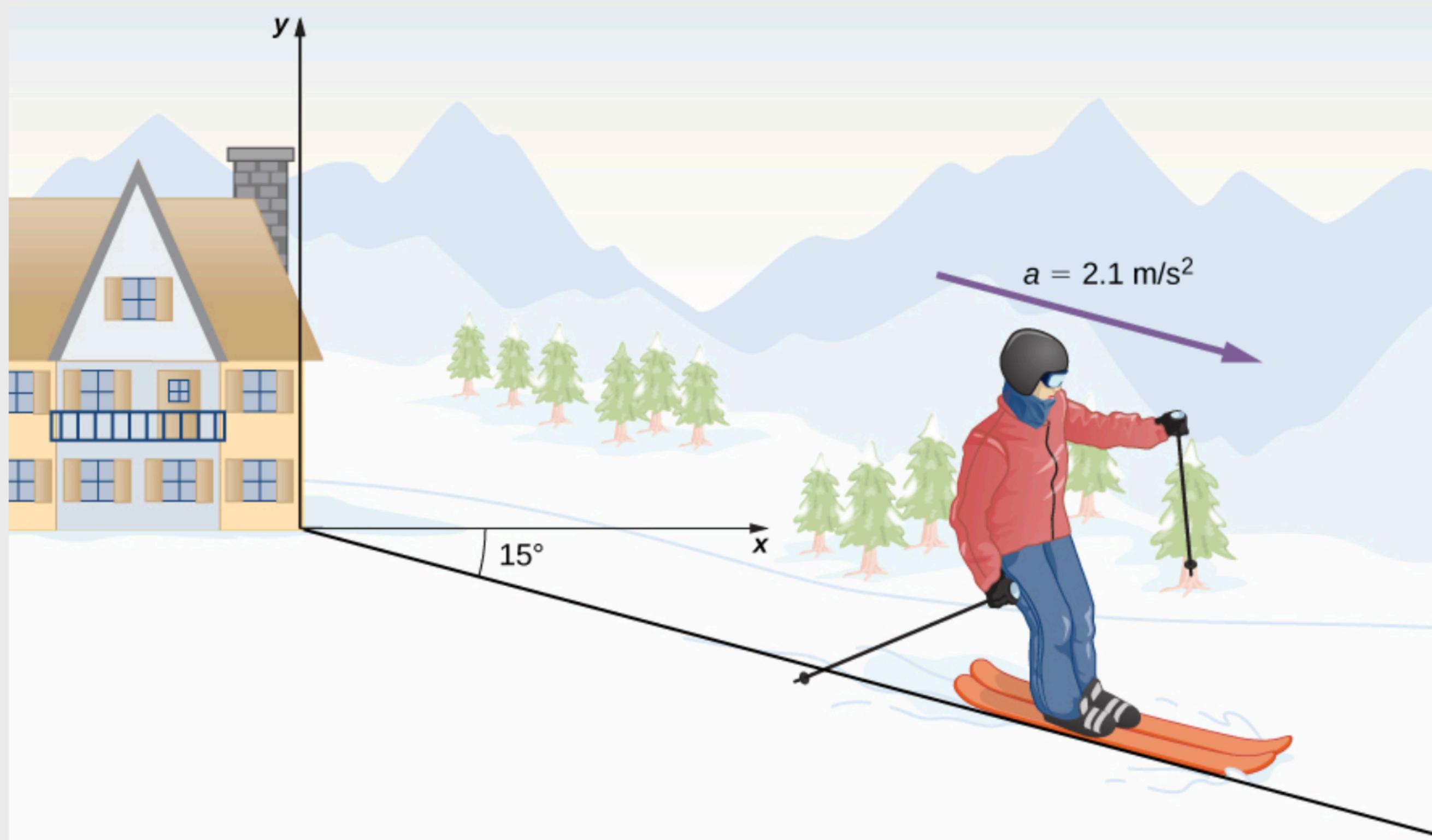
Figure 4.10 shows a skier moving with an acceleration of 2.1 m/s^2 down a slope of 15° at $t = 0$. With the origin of the coordinate system at the front of the lodge, her initial position and velocity are

$$\vec{r}(0) = (75.0\hat{\mathbf{i}} - 50.0\hat{\mathbf{j}}) \text{ m}$$

and

$$\vec{v}(0) = (4.1\hat{\mathbf{i}} - 1.1\hat{\mathbf{j}}) \text{ m/s.}$$

- (a) What are the x - and y -components of the skier's position and velocity as functions of time? (b) What are her position and velocity at $t = 10.0 \text{ s}$?



See you next class!

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