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# **Physics 111 - Class 9A PE & Energy Conservation**

**November 1, 2021**

Do not draw in/on this box!

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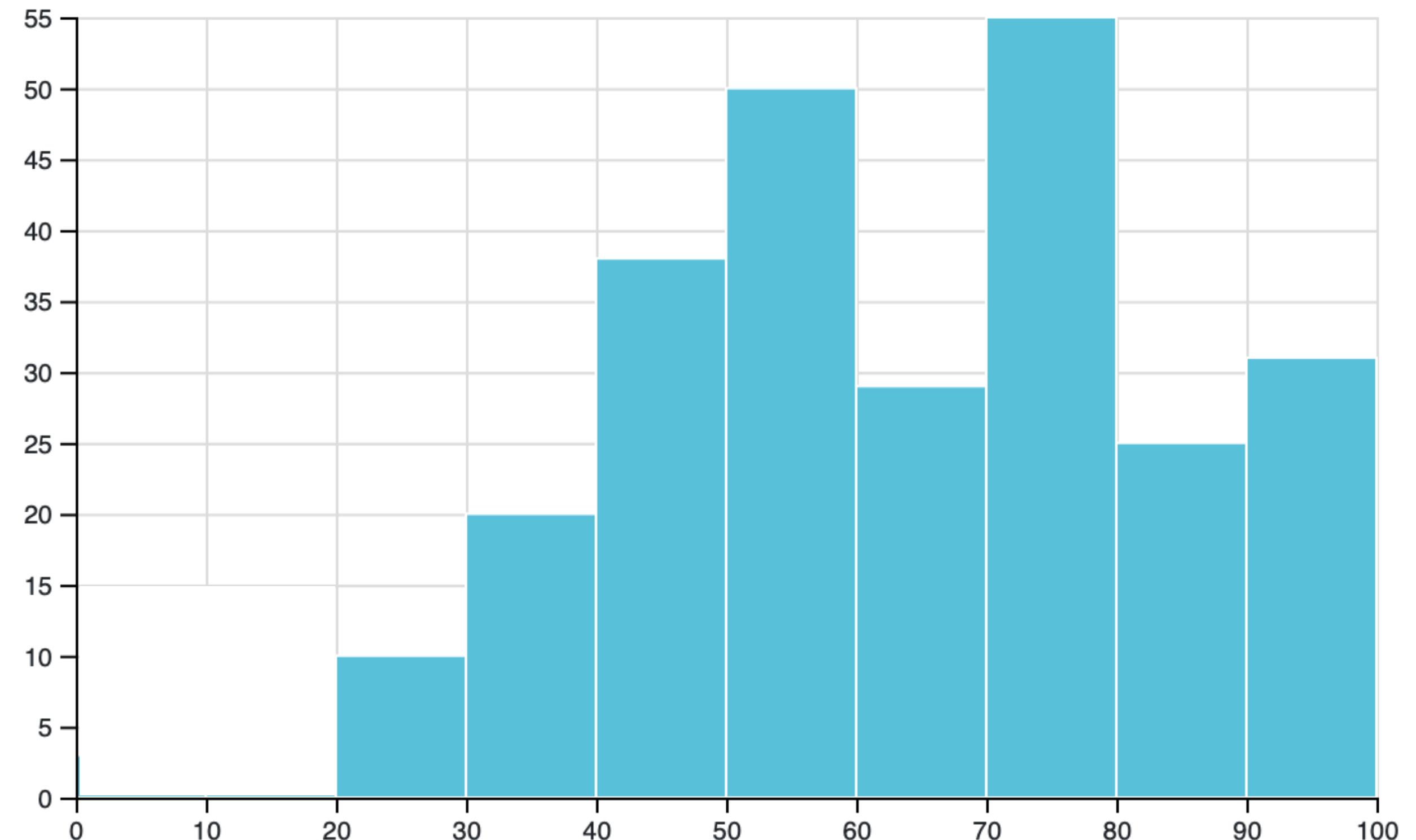
# Class Outline

- Logistics / Announcements
- Test 3 Reflection
- Chapter 8 Section Summary
- Clicker Questions (~~No time for CQs today!~~)
- Worked Problems

# Logistics/Announcements

- Lab this week: Lab 6
- HW8 due this week on Thursday at 6 PM
- Learning Log 8 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Bonus Test 3 available this week (Chapters 5 & 6)
- Test Window: Friday 6 PM - Sunday 6 PM

# Test 3 Reflection



Number of students

265

Mean score

62%

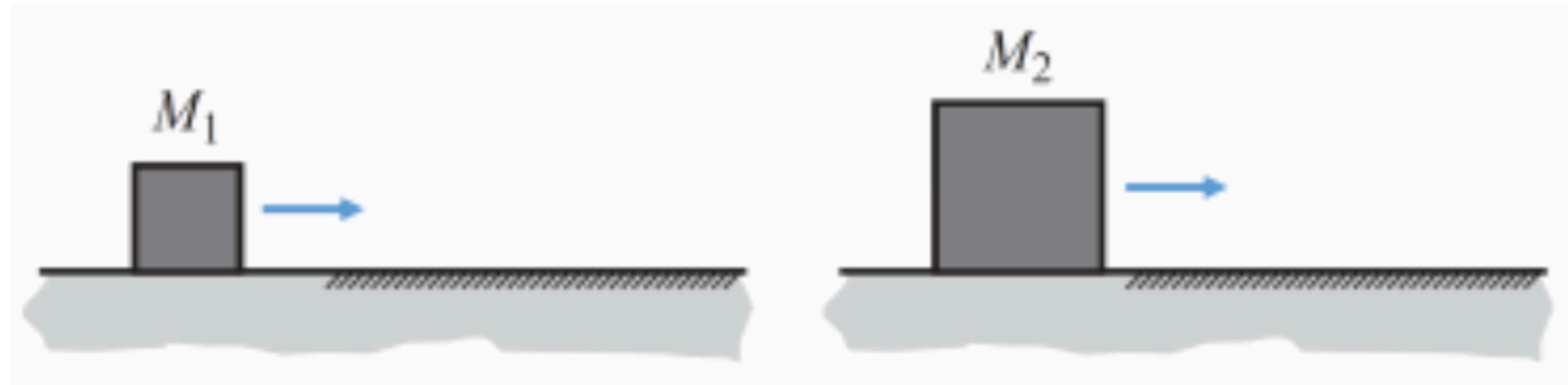
Standard deviation

21%

- Test 3 was pretty “fair”
- Several questions from previous homework assignments
- Time wasn’t a factor (on average)
- More conceptual questions than usual, because understanding Forces is very important
- A couple of misconceptions...

# Which Block stops first?

Two blocks,  $M_1 < M_2$ , having the same initial speed, move from a frictionless surface onto a surface having a coefficient of kinetic friction  $\mu_k$ .



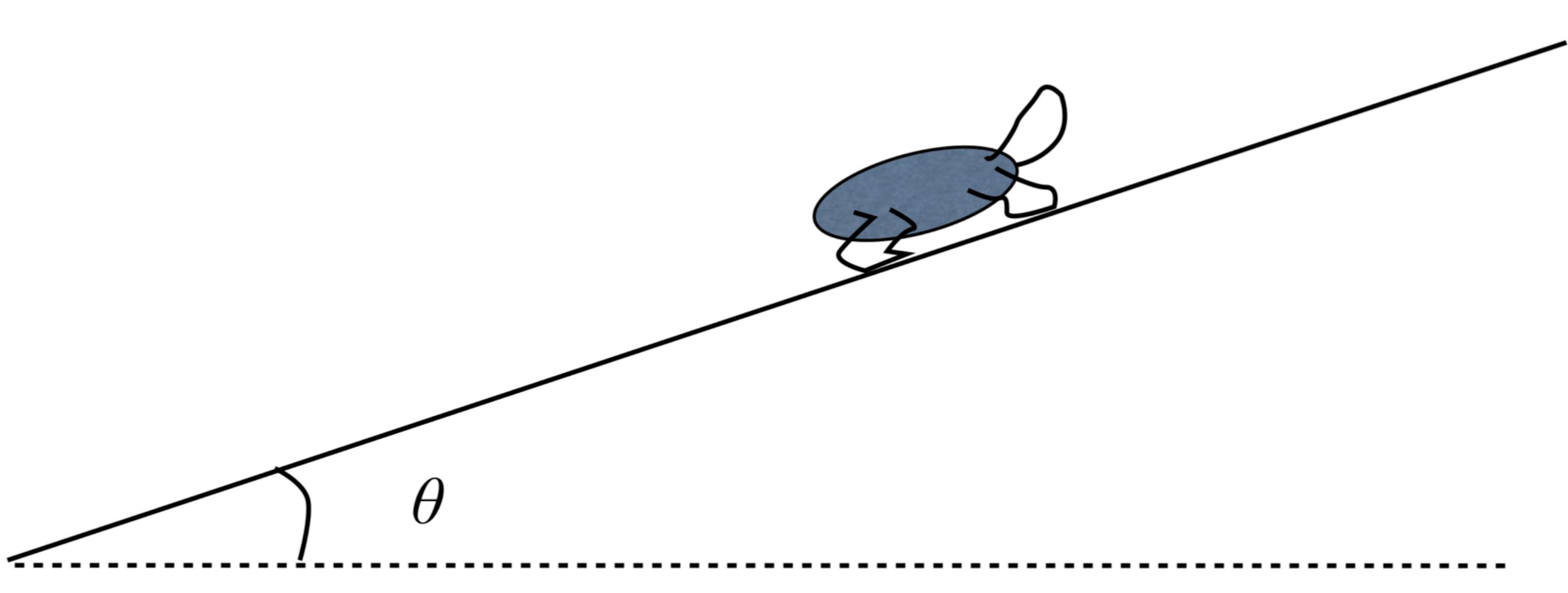
Which stops in a shorter distance?

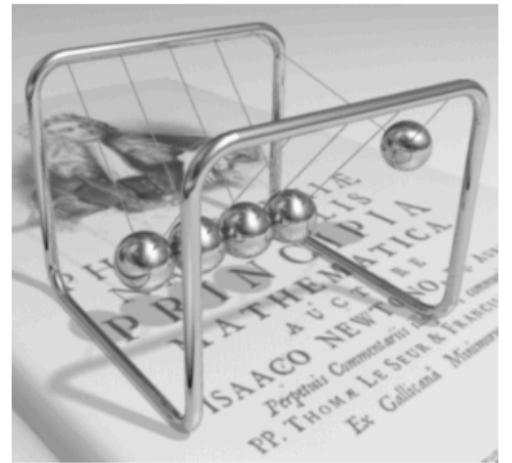
- (a)  $M_1$
- (b)  $M_2$
- (c) Cannot be determined without more information
- (d) Both stop in the same distance

# Turtle on a Log

A turtle lies on a log in the sun as shown in the figure below. The turtle has mass  $m$ , the log makes an angle  $\theta$  with respect to the horizontal and the coefficient of static friction between the turtle and the log is  $\mu_s$  (where  $\mu_s > \tan \theta$ ).

The magnitudes of the normal force,  $n$  and the frictional force  $f_s$  are:





## Physics 111

Search this book...

Unsyllabus

### ABOUT THIS COURSE

Course Syllabus (Official)

Course Schedule

Accommodations

How to do well in this course

### GETTING STARTED

Before the Term starts

After the first class

In the first week

Week 1 - Introductions!

### PART 1 - KINEMATICS

Week 2 - Chapter 2

Week 3 - Chapter 3

Week 4 - Chapter 4

### PART 2 - DYNAMICS

# Videos

Below are the assigned videos for this week. The videos are collapsible so once you're done with one, you can move to the next one. In the sidebar on the right, you can use the checklists to keep track of what's done.

## Required Videos

### 1. Introduction to Gravitational Potential Energy with Zero Line Examples

Introduction to Gravitational Potential Energy with Zero Line Examples

$PE_g = mgh$

m = mass of object

g = acceleration due to gravity

$[g_{Earth} = +9.81 \frac{m}{s^2}]$

$h = ?$

Watch on YouTube

zero line

- [Notes](#)
- [Direct link to Mr. P's page](#)

Required Videos  
Optional Videos

### Checklist of items

- Video 1
- Video 2
- Video 3
- Video 4
- Video 5
- Video 6
- Video 7
- Video 8
- Video 9
- Video 10

# Introduction

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Preface

▼ Mechanics

- ▶ 1 Units and Measurement
- ▶ 2 Vectors
- ▶ 3 Motion Along a Straight Line
- ▶ 4 Motion in Two and Three Dimensions
- ▶ 5 Newton's Laws of Motion
- ▶ 6 Applications of Newton's Laws
- ▶ 7 Work and Kinetic Energy
- ▶ 8 Potential Energy and Conservation of Energy

**Introduction**

Mon

8.1 Potential Energy of a System

8.2 Conservative and Non-Conservative Forces

8.3 Conservation of Energy

8.4 Potential Energy Diagrams and Stability

8.5 Sources of Energy

▶ Chapter Review

▶ 9 Linear Momentum and Collisions

▶ 10 Fixed-Axis Rotation

▶ 11 Angular Momentum

▶ 12 Static Equilibrium and Elasticity

▶ 13 Gravity

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≡ My highlights



**Figure 8.1** Shown here is part of a Ball Machine sculpture by George Rhoads. A ball in this contraption is lifted, rolls, falls, bounces, and collides with various objects, but throughout its travels, its kinetic energy changes in definite, predictable amounts, which depend on its position and the objects with which it interacts. (credit: modification of work by Roland Tanglao)

## Chapter Outline

[8.1 Potential Energy of a System](#)

[8.2 Conservative and Non-Conservative Forces](#)

[8.3 Conservation of Energy](#)

[8.4 Potential Energy Diagrams and Stability](#)

[8.5 Sources of Energy](#)

In George Rhoads' rolling ball sculpture, the principle of conservation of energy governs the changes in the ball's kinetic energy and relates them to changes and transfers for other types of energy associated with the ball's interactions. In this chapter, we introduce the important concept of potential energy. This will enable us to formulate

# Monday's Class

**8.1 Potential Energy of a System**

# Potential Energy

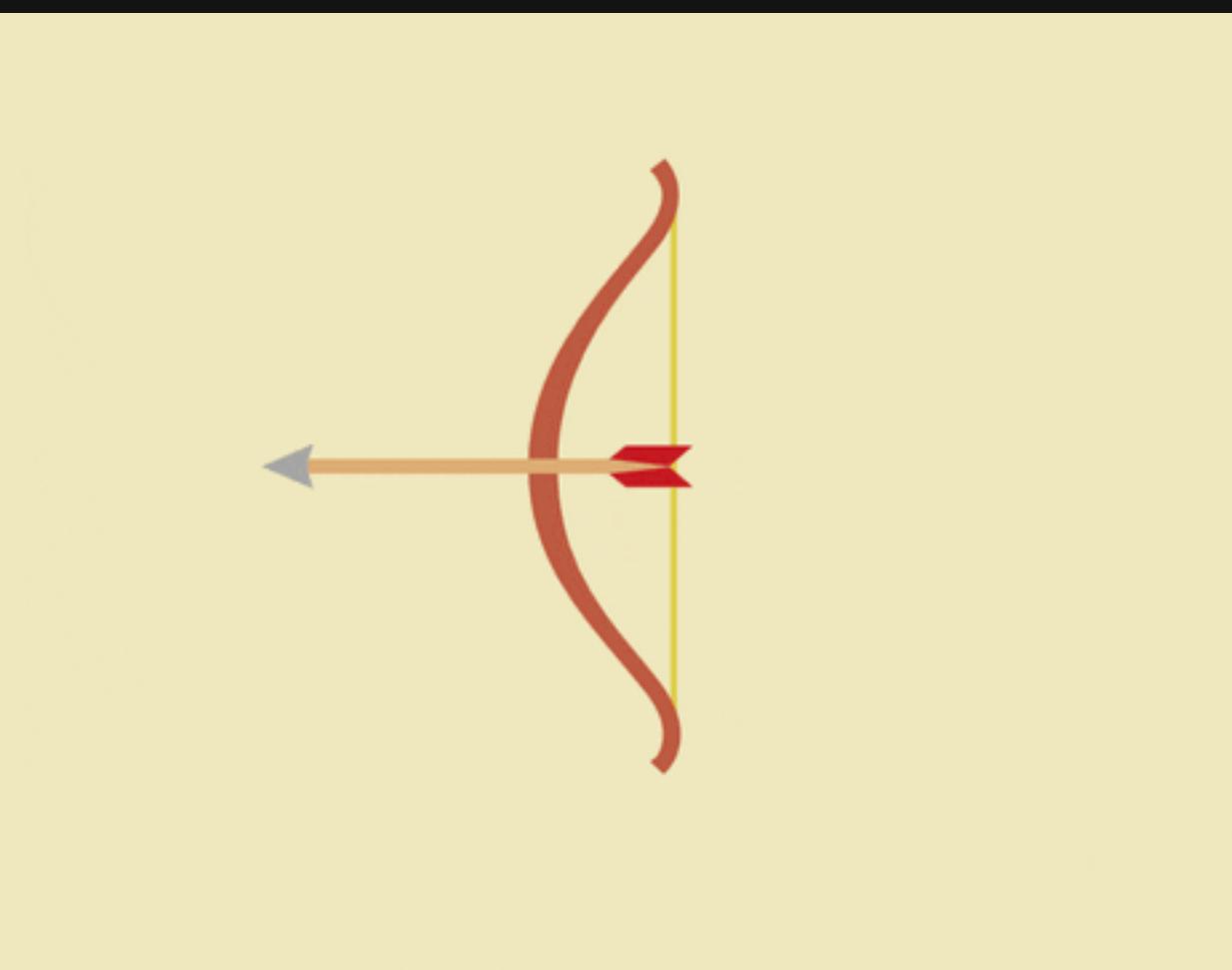
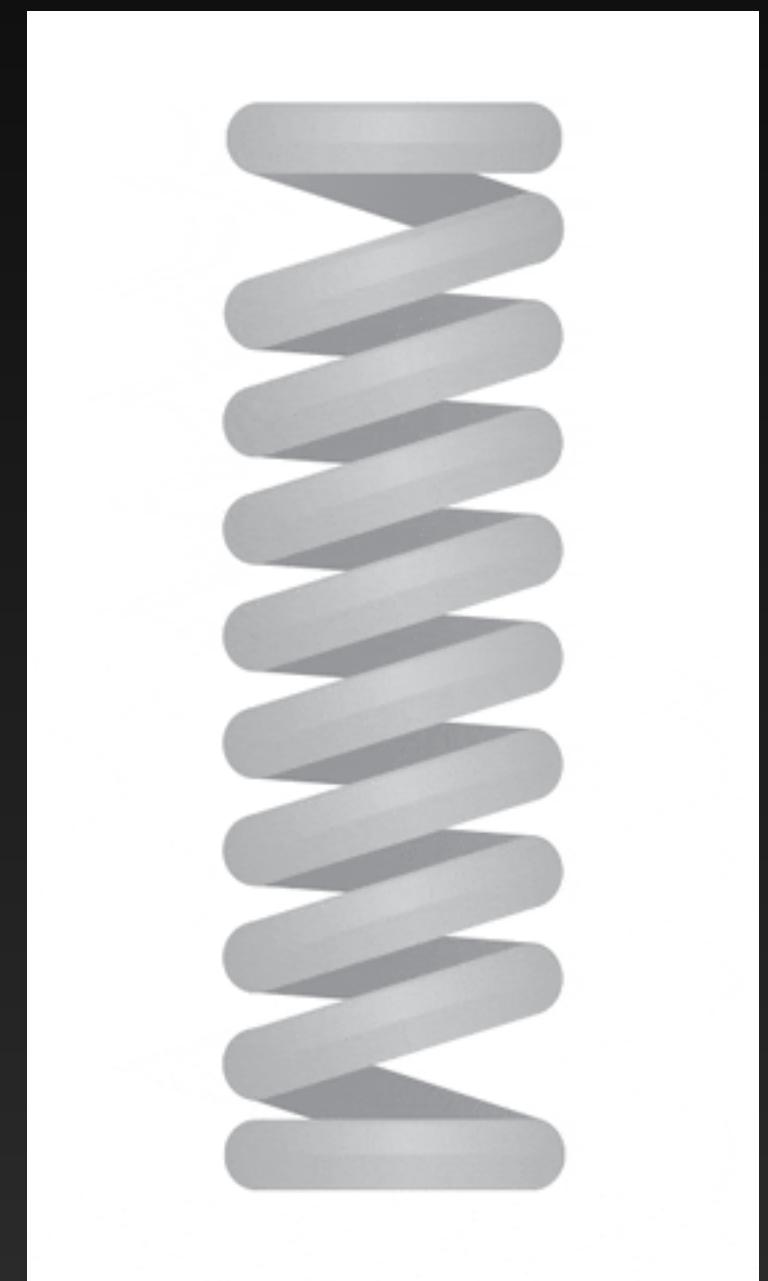
- Recall that “Kinetic Energy” was a characteristic of the object’s **mass** and **velocity**.
- “Potential Energy” is a different form of energy that’s characteristic of the object’s **position**.
- There are different forms of “Potential Energy”: Gravitational, Elastic/spring, Electrical, Nuclear...

# Examples of Potential Energy

## Gravitational Potential Energy



## Elastic Potential Energy



## Nuclear Potential Energy

# Definition of Potential Energy

Based on this scenario, we can define the difference of potential energy from point *A* to point *B* as the negative of the work done:

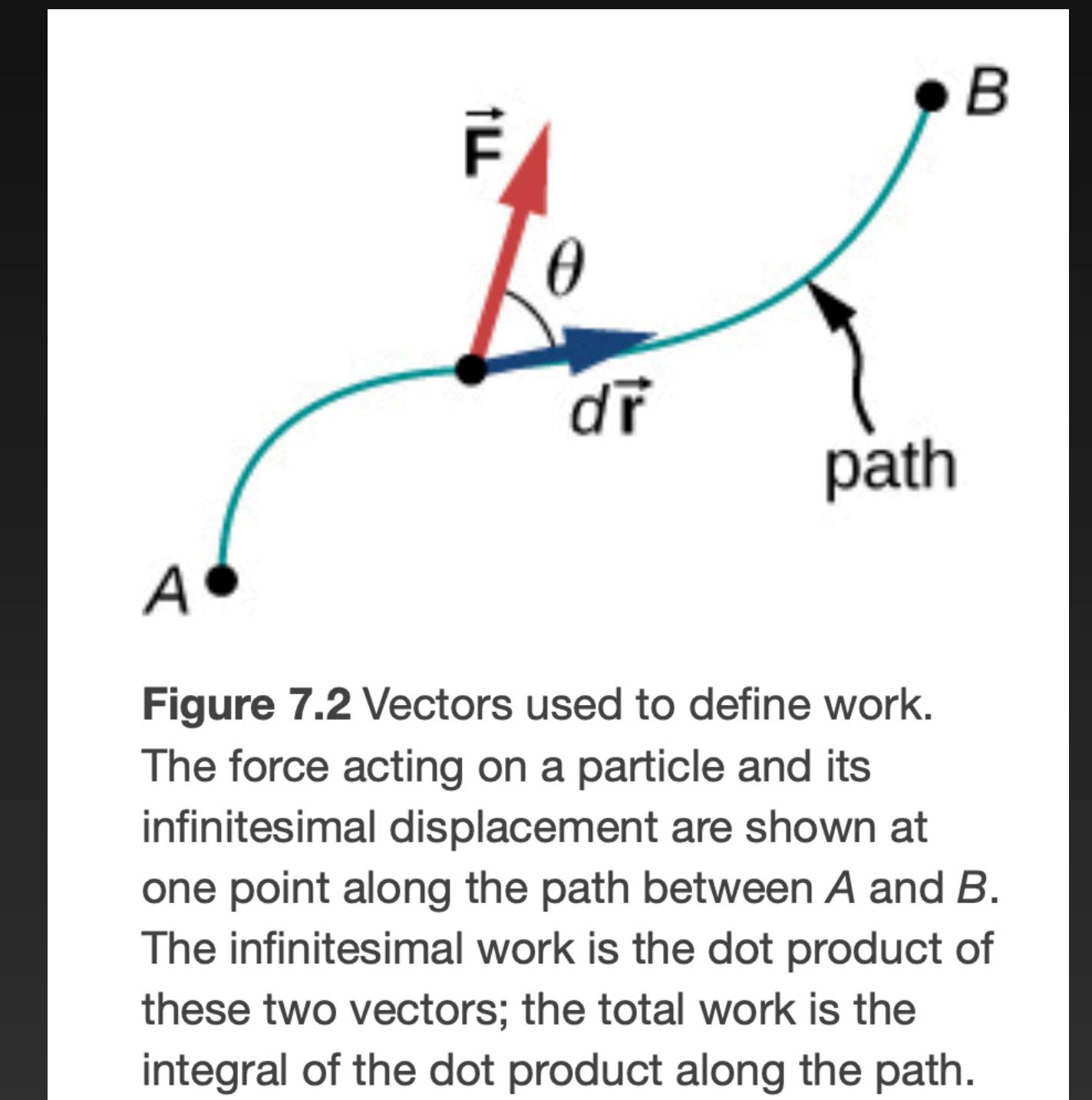
$$\Delta U_{AB} = U_B - U_A = -W_{AB}.$$

8.1

# Definition of Potential Energy from Work

Work is done whenever an applied (external) force causes displacement.

$$W = \int \vec{F} \cdot d\hat{\vec{r}}$$



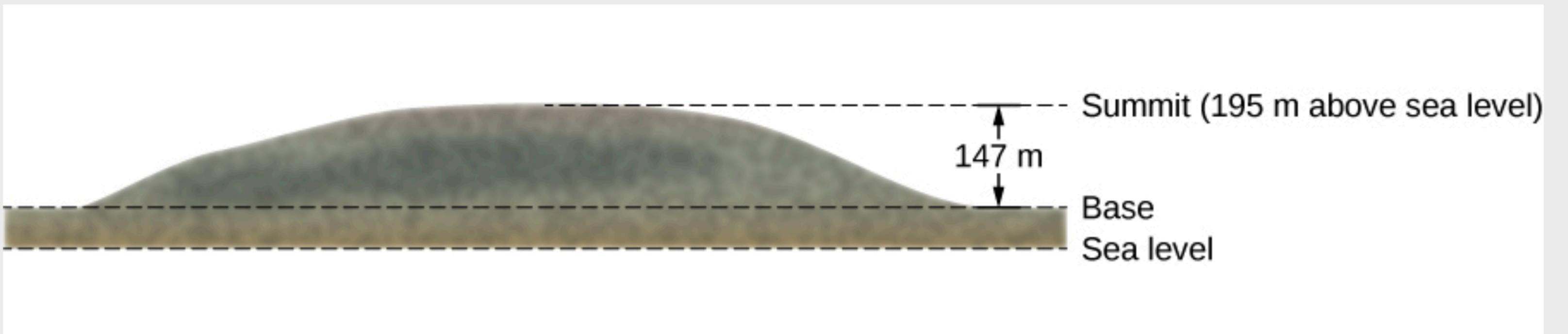
Change in Potential Energy is the negative of the work done...

$$\Delta U_{AB} = -W_{AB}$$

### EXAMPLE 8.2

#### Gravitational Potential Energy of a Hiker

The summit of Great Blue Hill in Milton, MA, is 147 m above its base and has an elevation above sea level of 195 m ([Figure 8.3](#)). (Its Native American name, *Massachusett*, was adopted by settlers for naming the Bay Colony and state near its location.) A 75-kg hiker ascends from the base to the summit. What is the gravitational potential energy of the hiker-Earth system with respect to zero gravitational potential energy at base height, when the hiker is (a) at the base of the hill, (b) at the summit, and (c) at sea level, afterward?

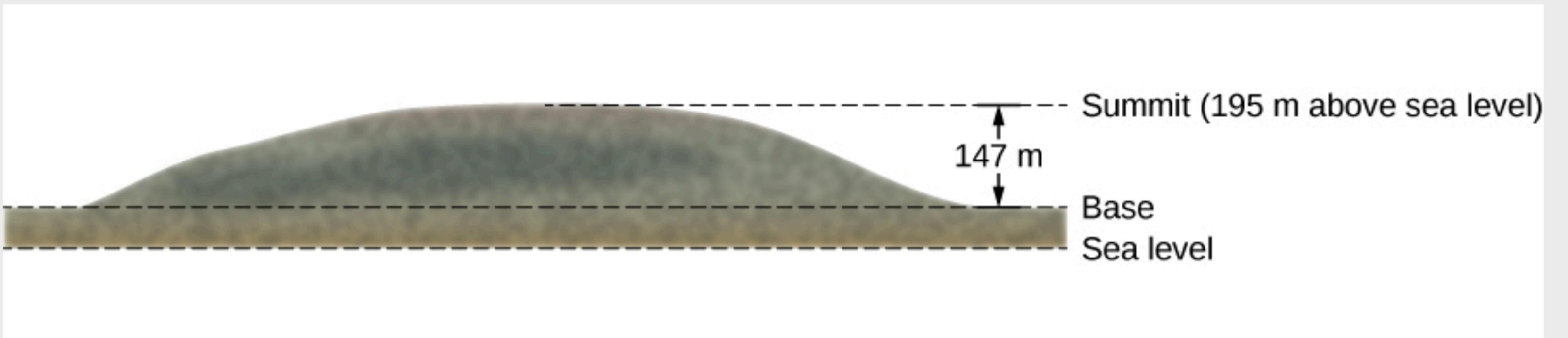


**Figure 8.3** Sketch of the profile of Great Blue Hill, Milton, MA. The altitudes of the three levels are indicated.

### EXAMPLE 8.2

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**Figure 8.3** Sketch of the profile of Great Blue Hill, Milton, MA. The altitudes of the three levels are indicated.

#### Strategy

First, we need to pick an origin for the  $y$ -axis and then determine the value of the constant that makes the potential energy zero at the height of the base. Then, we can determine the potential energies from [Equation 8.5](#), based on the relationship between the zero potential energy height and the height at which the hiker is located.



# Introduction to Gravitational Potential Energy with Zero Line Examples



Copy link

## Gravitational Potential Energy

$$PE_g \text{ [or } U_g]$$



$$PE_g = mgh$$

$m$  = mass of object

$g$  = acceleration due to gravity

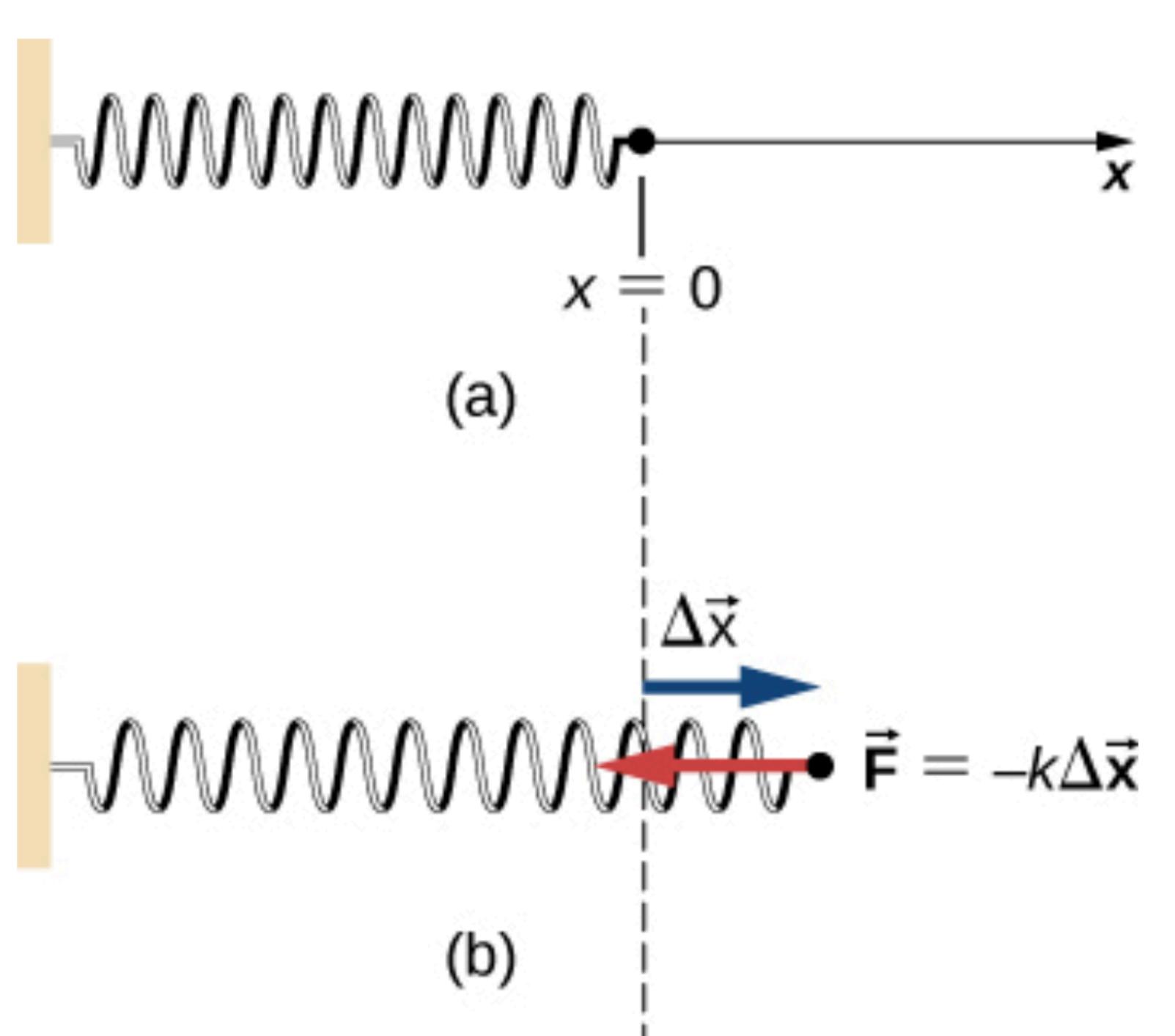
$$\left[ g_{\text{Earth}} = +9.81 \frac{\text{m}}{\text{s}^2} \right]$$

$h$  = Vertical height above  
the horizontal zero line

## EXAMPLE 7.5

### Work Done by a Spring Force

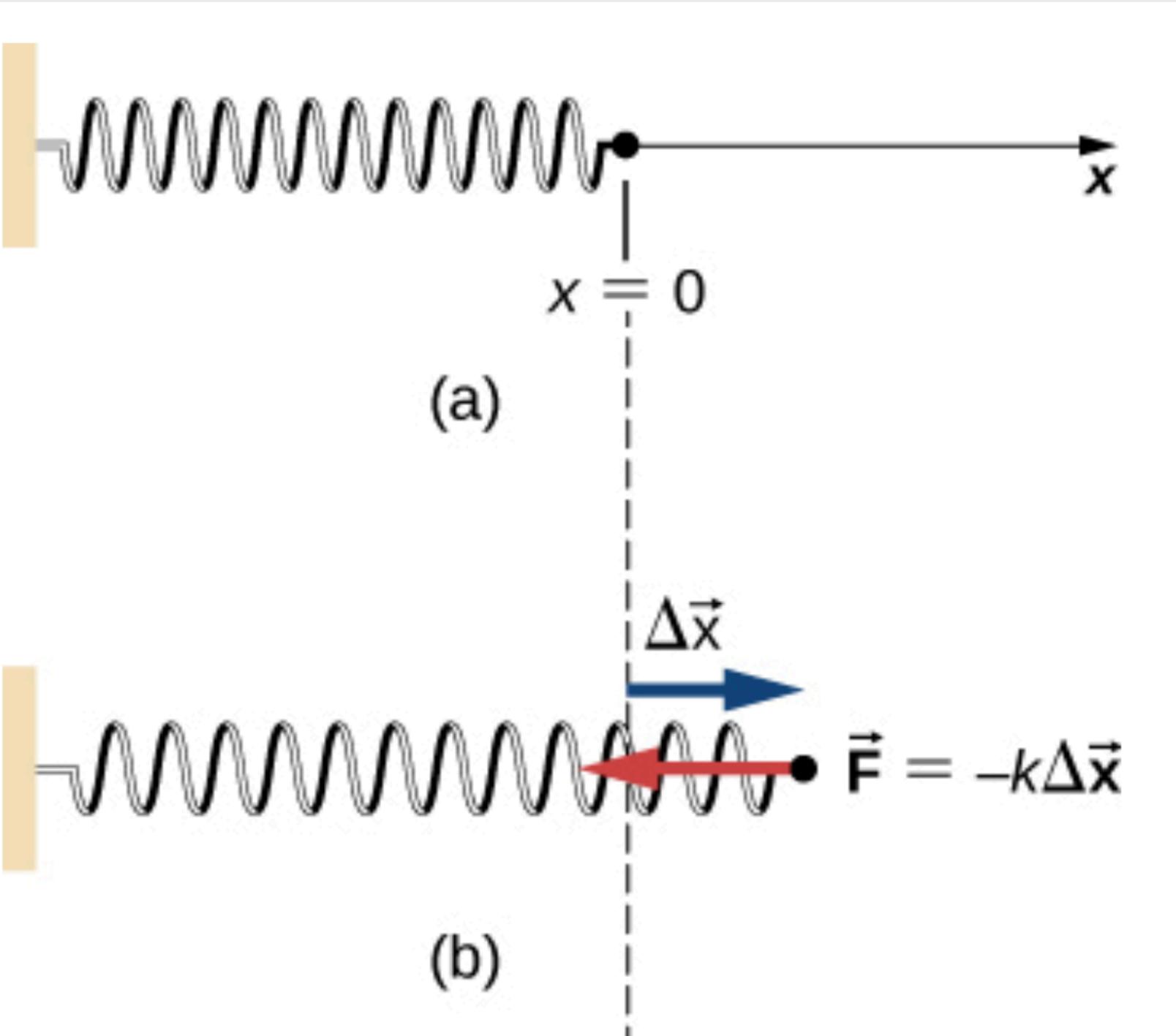
A perfectly elastic spring requires 0.54 J of work to stretch 6 cm from its equilibrium position, as in [Figure 7.7\(b\)](#). (a) What is its spring constant  $k$ ? (b) How much work is required to stretch it an additional 6 cm?



## EXAMPLE 7.5

### Work Done by a Spring Force

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#### Strategy

Work “required” means work done against the spring force, which is the negative of the work in [Equation 7.5](#), that is

$$W = \frac{1}{2}k(x_B^2 - x_A^2).$$

For part (a),  $x_A = 0$  and  $x_B = 6\text{cm}$ ; for part (b),  $x_B = 6\text{cm}$  and  $x_B = 12\text{cm}$ . In part (a), the work is given and you can solve for the spring constant; in part (b), you can use the value of  $k$ , from part (a), to solve for the work.

#### Solution

- a.  $W = 0.54\text{ J} = \frac{1}{2}k[(6\text{ cm})^2 - 0]$ , so  $k = 3\text{ N/cm}$ .
- b.  $W = \frac{1}{2}(3\text{ N/cm})[(12\text{ cm})^2 - (6\text{ cm})^2] = 1.62\text{ J}$ .

#### Significance

Since the work done by a spring force is independent of the path, you only needed to calculate the difference in the quantity  $\frac{1}{2}kx^2$  at the end points. Notice that the work required to stretch the spring from 0 to 12 cm is four times that required to stretch it from 0 to 6 cm, because that work depends on the square of the amount of stretch from equilibrium,  $\frac{1}{2}kx^2$ . In this circumstance, the work to stretch the spring from 0 to 12 cm is also equal to the work for a composite path from 0 to 6 cm followed by an additional stretch from 6 cm to 12 cm. Therefore,

# Elastic Potential Energy

## Elastic potential energy

In [Work](#), we saw that the work done by a perfectly elastic spring, in one dimension, depends only on the spring constant and the squares of the displacements from the unstretched position, as given in [Equation 7.5](#). This work involves only the properties of a Hooke's law interaction and not the properties of real springs and whatever objects are attached to them. Therefore, we can define the difference of elastic potential energy for a spring force as the negative of the work done by the spring force in this equation, before we consider systems that embody this type of force. Thus,

$$\Delta U = -W_{AB} = \frac{1}{2}k(x_B^2 - x_A^2),$$

8.6

### EXAMPLE 8.3

#### Spring Potential Energy

A system contains a perfectly elastic spring, with an unstretched length of 20 cm and a spring constant of 4 N/cm. (a) How much elastic potential energy does the spring contribute when its length is 23 cm? (b) How much more potential energy does it contribute if its length increases to 26 cm?

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#### Spring Potential Energy

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#### Strategy

When the spring is at its unstretched length, it contributes nothing to the potential energy of the system, so we can use [Equation 8.7](#) with the constant equal to zero. The value of  $x$  is the length minus the unstretched length. When the spring is expanded, the spring's displacement or difference between its relaxed length and stretched length should be used for the  $x$ -value in calculating the potential energy of the spring.

#### Solution

- a. The displacement of the spring is  $x = 23 \text{ cm} - 20 \text{ cm} = 3 \text{ cm}$ , so the contributed potential energy is  $U = \frac{1}{2}kx^2 = \frac{1}{2}(4 \text{ N/cm})(3 \text{ cm})^2 = 0.18 \text{ J}$ .
- b. When the spring's displacement is  $x = 26 \text{ cm} - 20 \text{ cm} = 6 \text{ cm}$ , the potential energy is  $U = \frac{1}{2}kx^2 = \frac{1}{2}(4 \text{ N/cm})(6 \text{ cm})^2 = 0.72 \text{ J}$ , which is a 0.54-J increase over the amount in part (a).

**EXAMPLE 8.3****Spring Potential Energy**

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**Significance**

Calculating the elastic potential energy and potential energy differences from [Equation 8.7](#) involves solving for the potential energies based on the given lengths of the spring. Since  $U$  depends on  $x^2$ , the potential energy for a compression (negative  $x$ ) is the same as for an extension of equal magnitude.

## EXAMPLE 8.1

### Basic Properties of Potential Energy

A particle moves along the  $x$ -axis under the action of a force given by  $F = -ax^2$ , where  $a = 3 \text{ N/m}^2$ . (a) What is the difference in its potential energy as it moves from  $x_A = 1 \text{ m}$  to  $x_B = 2 \text{ m}$ ? (b) What is the particle's potential energy at  $x = 1 \text{ m}$  with respect to a given 0.5 J of potential energy at  $x = 0$ ?

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**Solution**

- a. The work done by the given force as the particle moves from coordinate  $x$  to  $x + dx$  in one dimension is

$$dW = \vec{F} \cdot d\vec{r} = Fdx = -ax^2dx.$$

Substituting this expression into [Equation 8.1](#), we obtain

$$\Delta U = -W = \int_{x_1}^{x_2} ax^2dx = \frac{1}{3}(3 \text{ N/m}^2)x^3 \Big|_{1 \text{ m}}^{2 \text{ m}} = 7 \text{ J.}$$

- b. The indefinite integral for the potential energy function in part (a) is

$$U(x) = \frac{1}{3}ax^3 + \text{const.},$$

and we want the constant to be determined by

$$U(0) = 0.5 \text{ J.}$$

Thus, the potential energy with respect to zero at  $x = 0$  is just

$$U(x) = \frac{1}{3}ax^3 + 0.5 \text{ J.}$$

Therefore, the potential energy at  $x = 1 \text{ m}$  is

$$U(1 \text{ m}) = \frac{1}{3}(3 \text{ N/m}^2)(1 \text{ m})^3 + 0.5 \text{ J} = 1.5 \text{ J.}$$

# Key Equations

Difference of potential energy

$$\Delta U_{AB} = U_B - U_A = -W_{AB}$$

Potential energy with respect to zero of potential energy at  $\vec{r}_0$

$$\Delta U = U(\vec{r}) - U(\vec{r}_0)$$

Gravitational potential energy near Earth's surface

$$U(y) = mgy + \text{const.}$$

Potential energy for an ideal spring

$$U(x) = \frac{1}{2}kx^2 + \text{const.}$$

Work done by conservative force over a closed path

$$W_{\text{closed path}} = \int \vec{F}_{\text{cons}} \cdot d\vec{r} = 0$$

Condition for conservative force in two dimensions

$$\left( \frac{dF_x}{dy} \right) = \left( \frac{dF_y}{dx} \right)$$

Conservative force is the negative derivative of potential energy

$$F_l = -\frac{dU}{dl}$$

Conservation of energy with no non-conservative forces

$$0 = W_{nc,AB} = \Delta(K + U)_{AB} = \Delta E_{AB}.$$

**See you next class!**

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