

You can draw here

GET READY: Go here and make sure you see the “Are you Ready” Sli.do Q
Canvas -> Course Content -> Lecture (under Week 4 - Chapter 4)

Physics 111 - Lecture 4

October 1, 2020

Do not draw in/on this box!

You can draw here

You can draw here

Reminders/Announcements

- Bonus Test 1 starts today from 6PM - Saturday at 6 PM
 - (might be slightly delayed)
- For questions about grading Test 1, contact Tutorial TA on Piazza (be patient)
- Homework05 and Homework06 has been released if you want to work on it in advance
- Will post a Piazza message about some feedback I've received - up for discussion

Reminders/Announcements

Homework (due Wed 6 pm)

Test/Bonus Test (Thurs 6pm - Sat 6pm)

Learning Log (Fri 6pm)

Week 1

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Week 2

HW01 - Intro to Mastering
Physics
(not for marks)

Test 0
(not for marks)

Learning Log 1
(yes for marks!)

Week 3

HW02 - Chapter 2
HW03 - Chapter 3

Test 1
(on Chapters 2 & 3)

Learning Log 2

Week 4
(this week!)

HW04 - Chapter 4

Bonus Test 1

Learning Log 3

Week 5

Summary of comments from Homework 4 (Chapter 4)

Taking a step back this week... 😕

- Relative motion: annoying but okay.
- Circular motion is straight forward.
- ω and α : angular velocity and angular acceleration
- Getting lost in formulas...
- What **IS** angular velocity?
- Direction of pendulum acceleration (!!?)

Students Completed



79 / 321

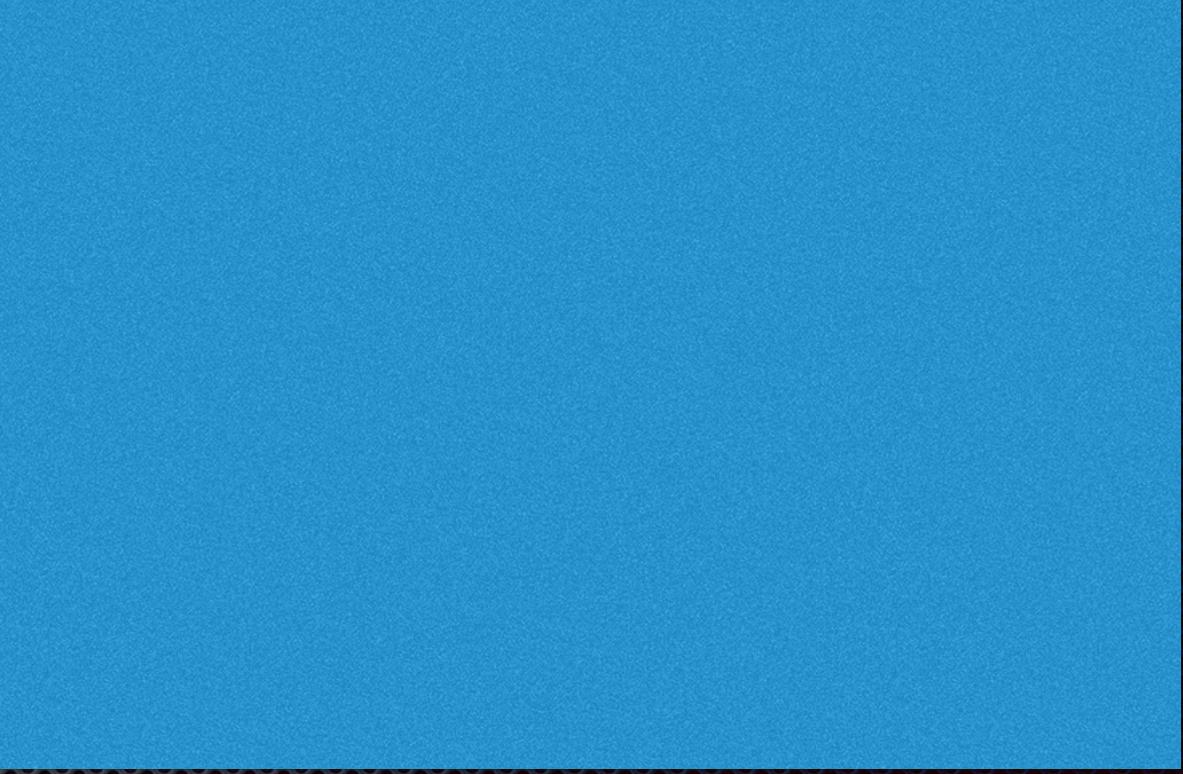
Summary of comments from Homework 4 (Chapter 4)

- Relative motion: annoying but okay.
- Circular motion is straight forward
- ω and α : angular velocity and angular acceleration
- Getting lost in formulas
- What **IS** angular velocity?
- Direction of pendulum acceleration (!!?)

“Quote of the week” QOTW

“The tilted axis questions had me sweating; I would say that I found those the most confusing.”

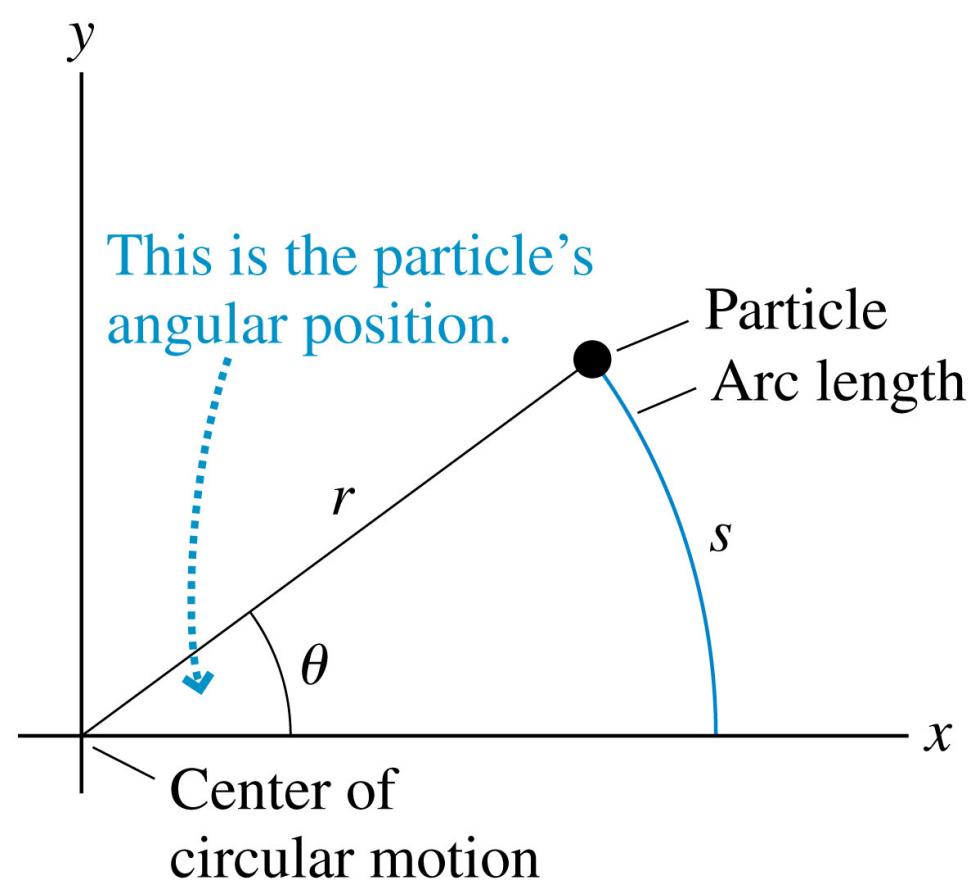
Why do we need angular velocity?



Why do we need angular velocity?

Angular Position

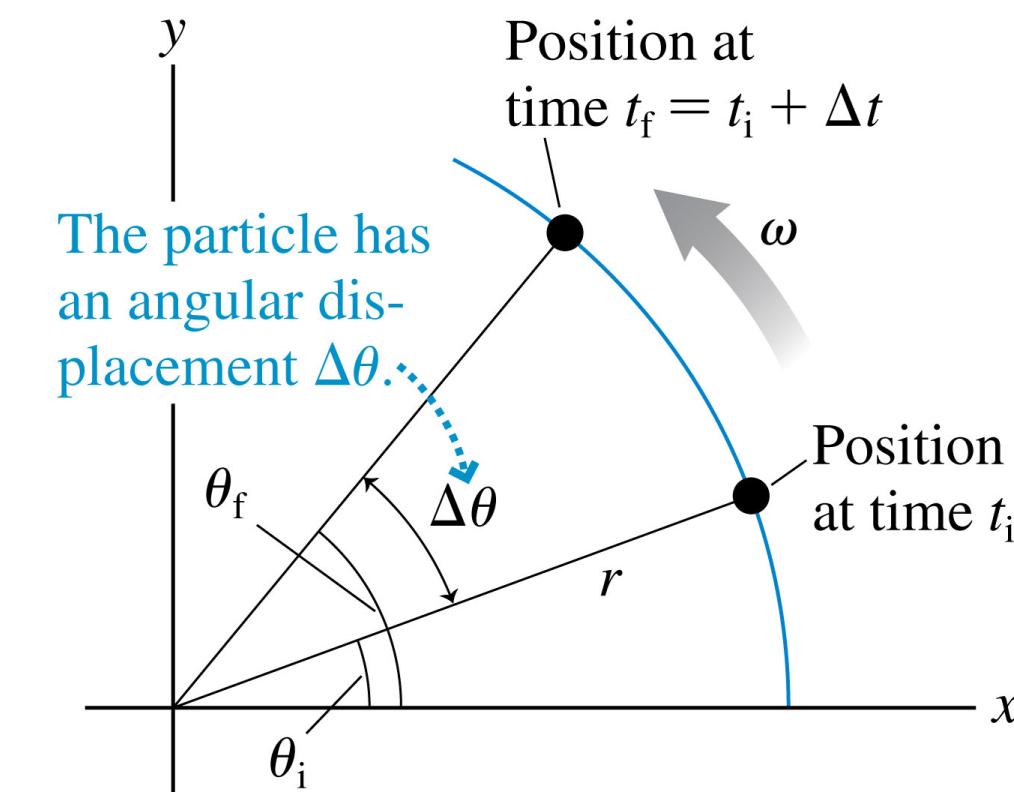
- Consider a particle at a distance r from the origin, at an angle θ from the positive x -axis.
- The angle may be measured in degrees, revolutions (rev) or **radians** (rad), that are related by:
$$1 \text{ rev} = 360^\circ = 2\pi \text{ rad}$$
- If the angle is measured in radians, then there is a simple relation between θ and the **arc length** s that the particle travels along the edge of a circle of radius r :
$$s = r\theta \quad (\text{with } \theta \text{ in rad})$$



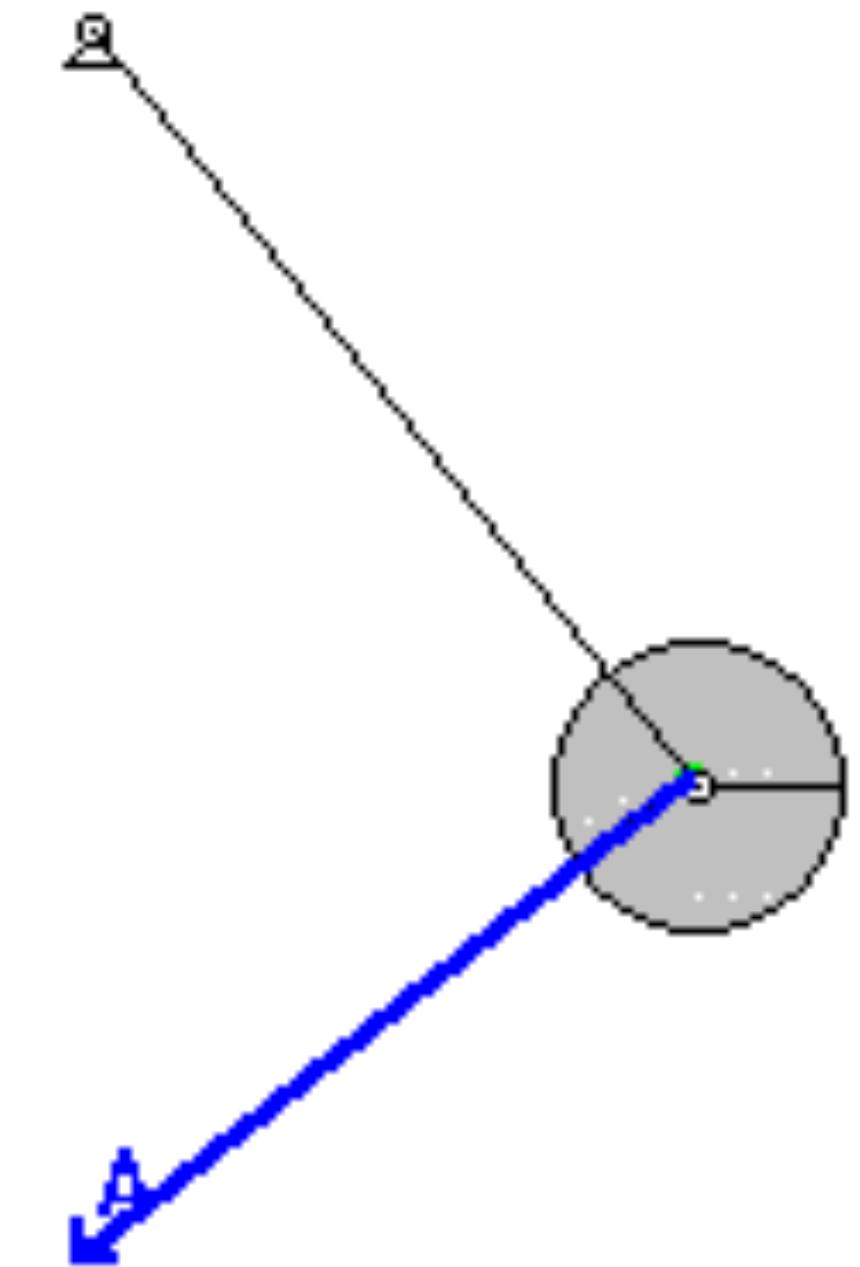
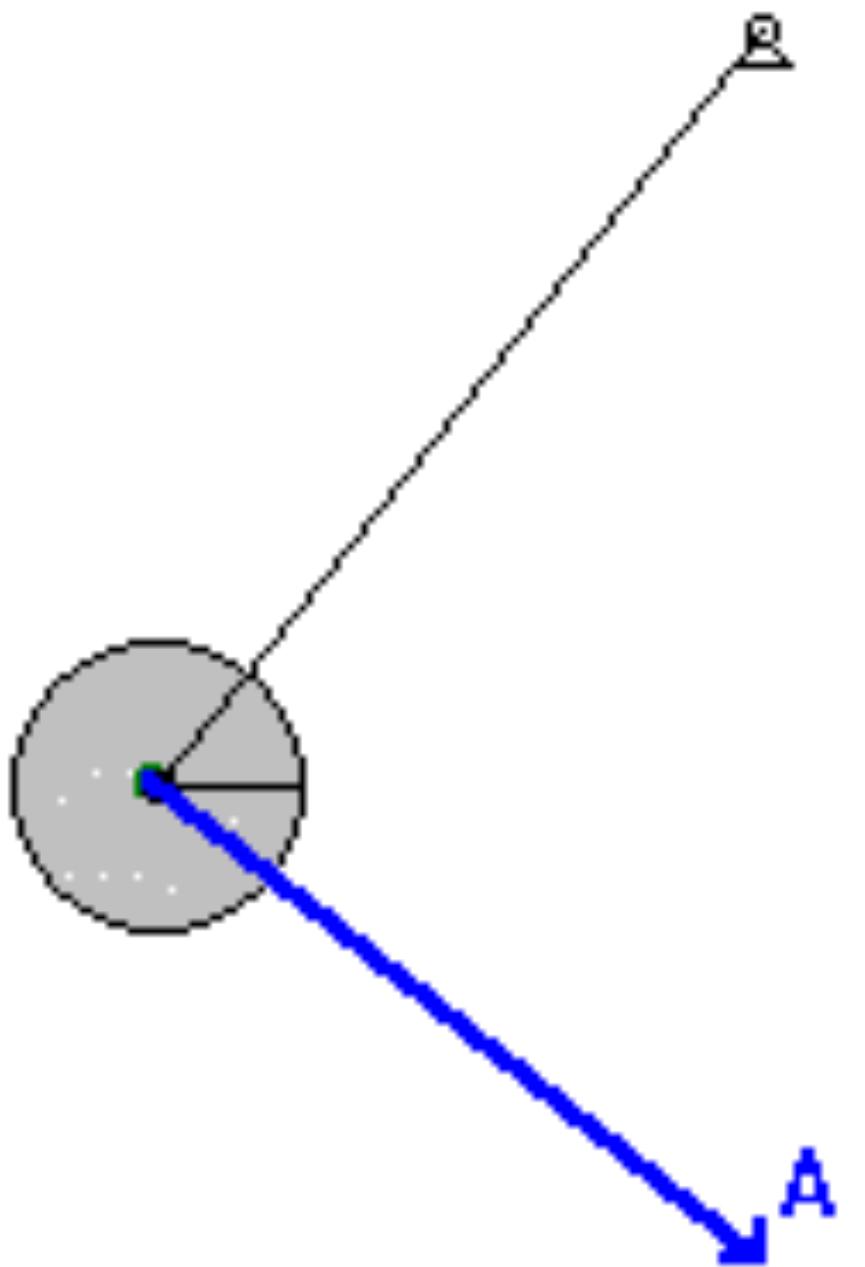
Angular Velocity

- A particle on a circular path moves through an **angular displacement** $\Delta\theta = \theta_f - \theta_i$ in a time interval $\Delta t = t_f - t_i$.
- In analogy with linear motion, we define
average angular velocity $\equiv \frac{\Delta\theta}{\Delta t}$
- As the time interval Δt becomes very small, we arrive at the definition of instantaneous **angular velocity**:

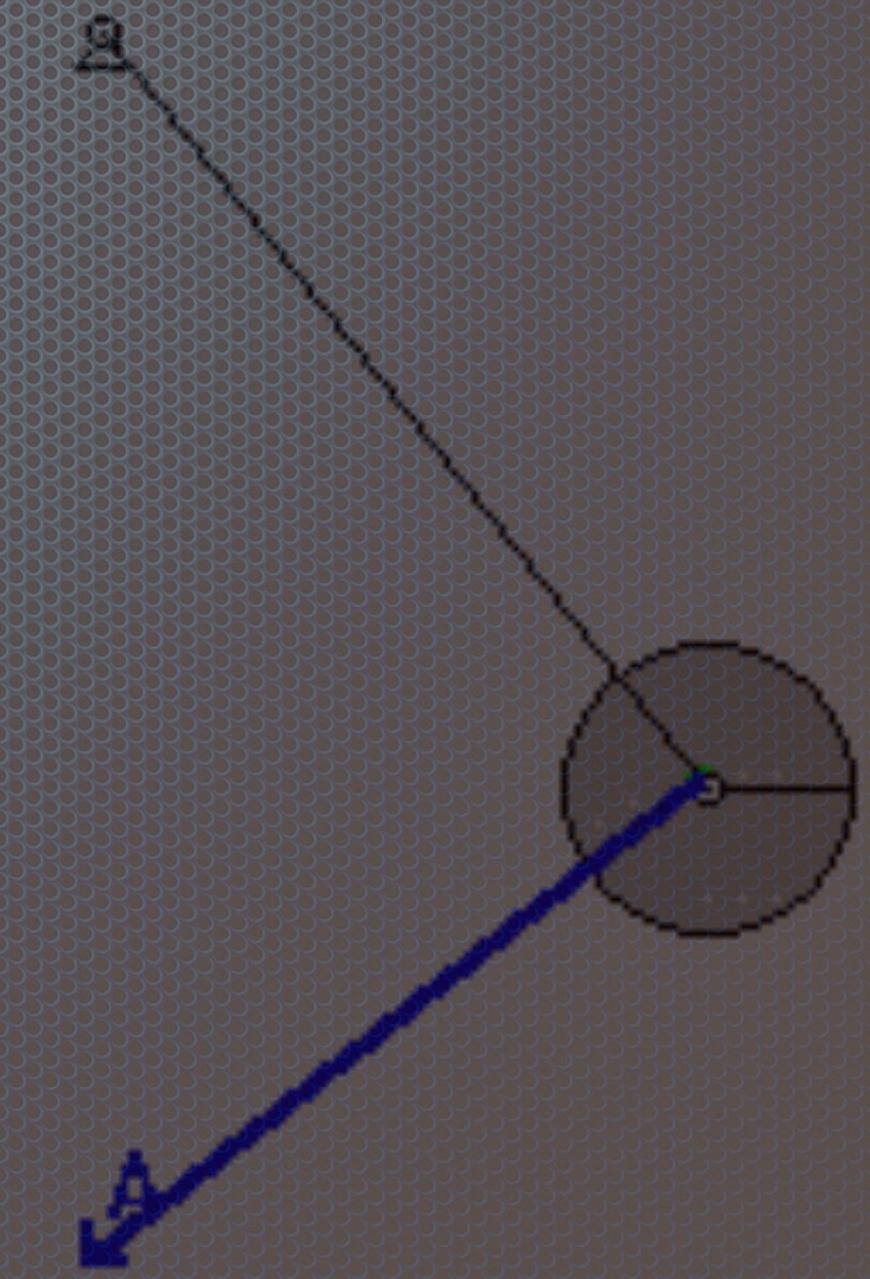
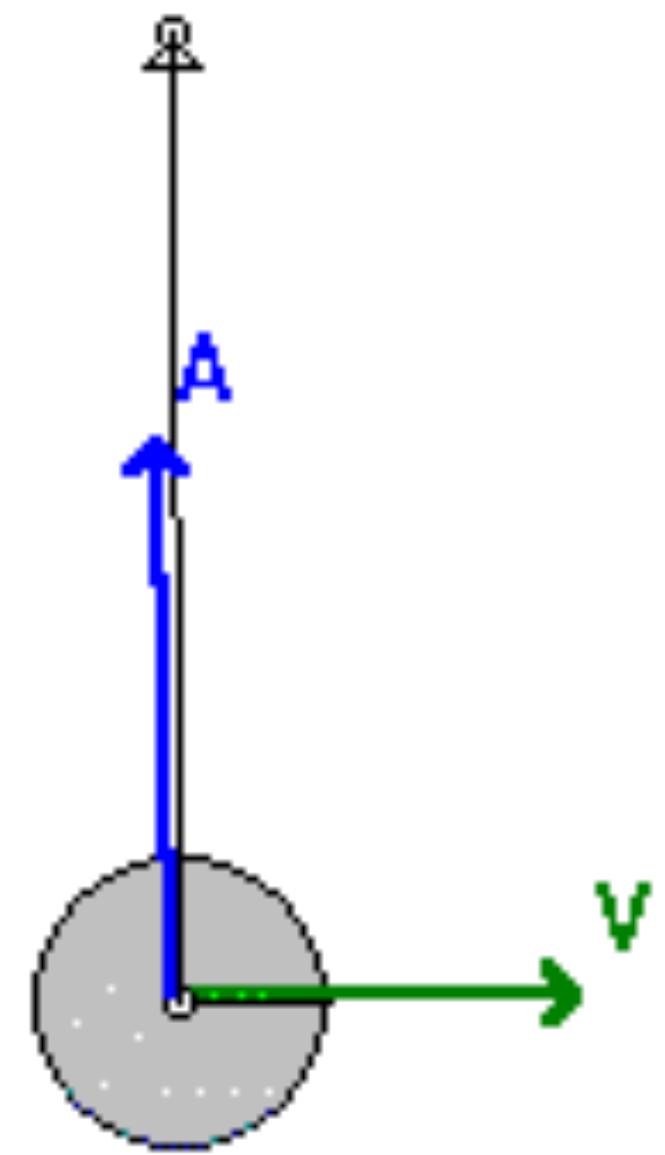
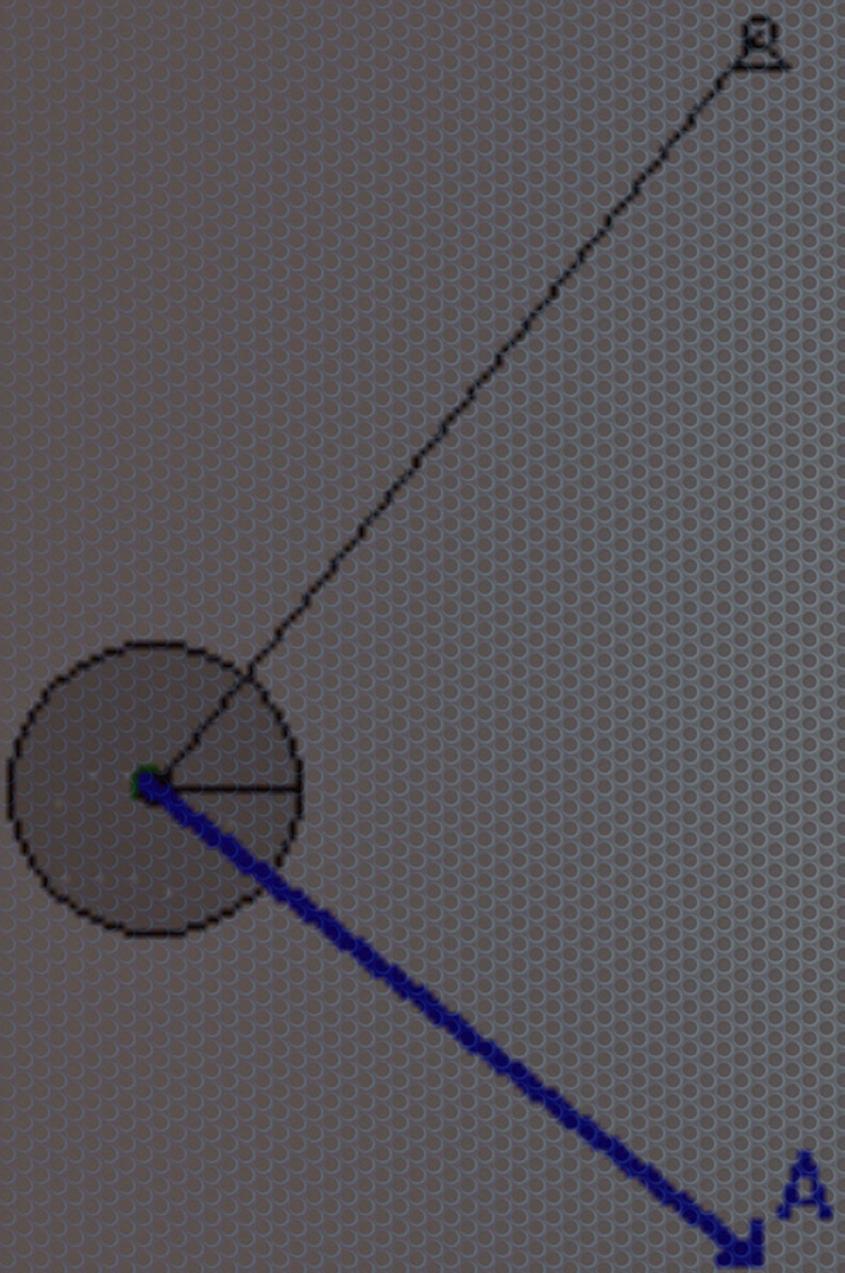
$$\omega \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta\theta}{\Delta t} = \frac{d\theta}{dt} \quad (\text{angular velocity})$$



Direction of Pendulum Acceleration



Direction of Pendulum Acceleration

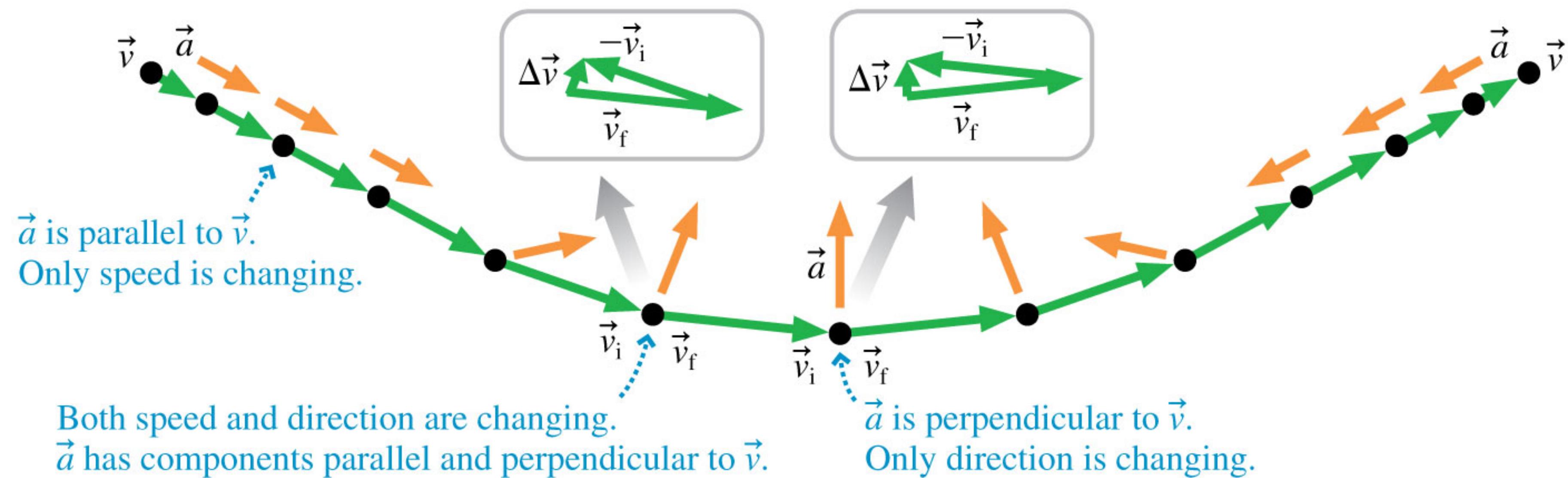


Direction of Pendulum Acceleration

EXAMPLE 4.2 | Through the valley

VISUALIZE FIGURE 4.4 is the motion diagram. Where the particle moves along a *straight line*, it speeds up if \vec{a} and \vec{v} point in the same direction and slows down if \vec{a} and \vec{v} point in opposite

directions. This important idea was the basis for the one-dimensional kinematics we developed in Chapter 2. When the direction of \vec{v} changes, as it does when the ball goes through the valley, we need to use vector subtraction to find the direction of $\Delta\vec{v}$ and thus of \vec{a} . The procedure is shown at two points in the motion diagram.



Chapter 4

Clicker Questions

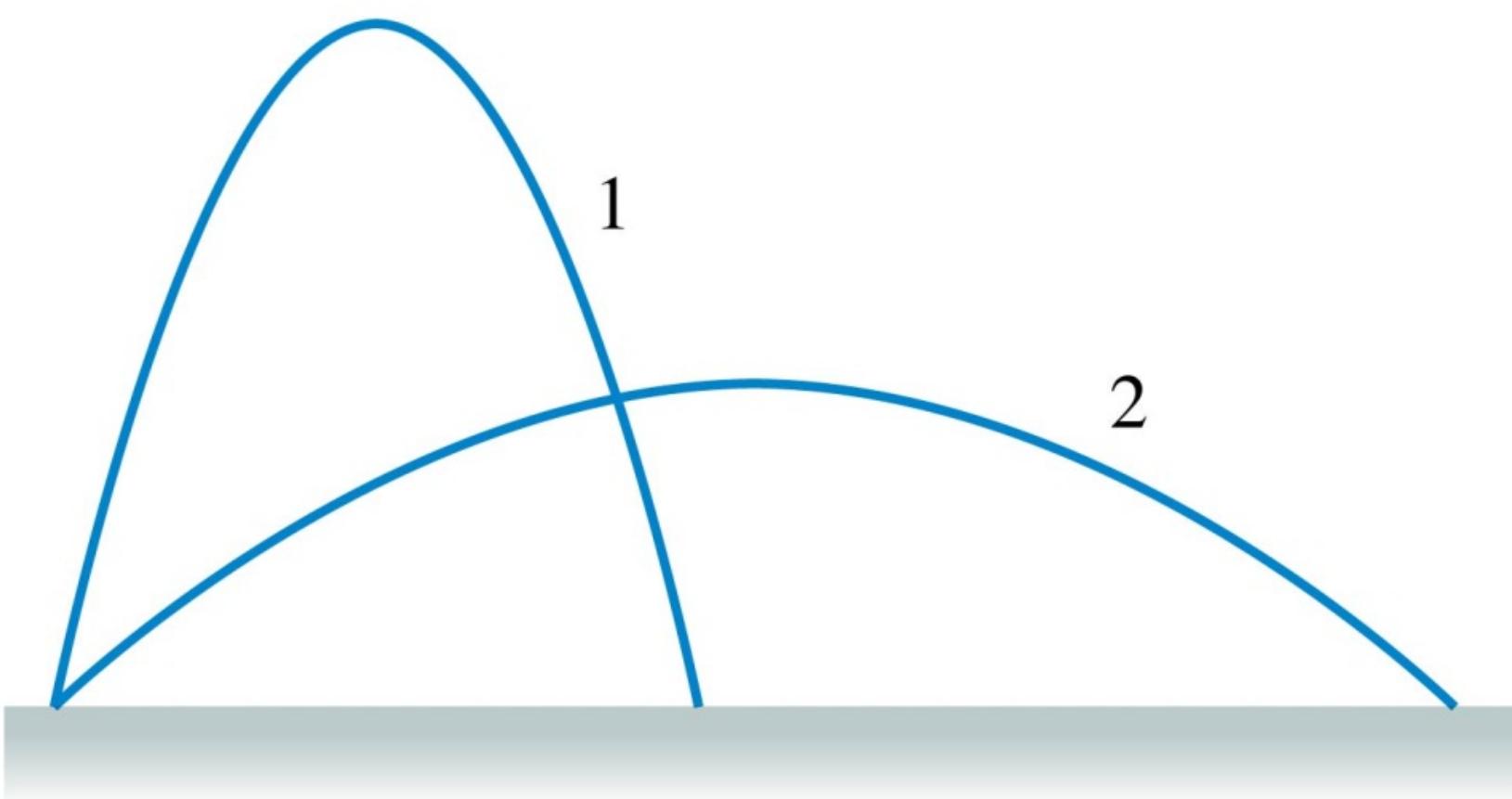
L4.Q1 - QuickCheck 4.4

Projectiles 1 and 2 are launched over level ground with the same speed but at different angles.

Which hits the ground first?

Ignore air resistance.

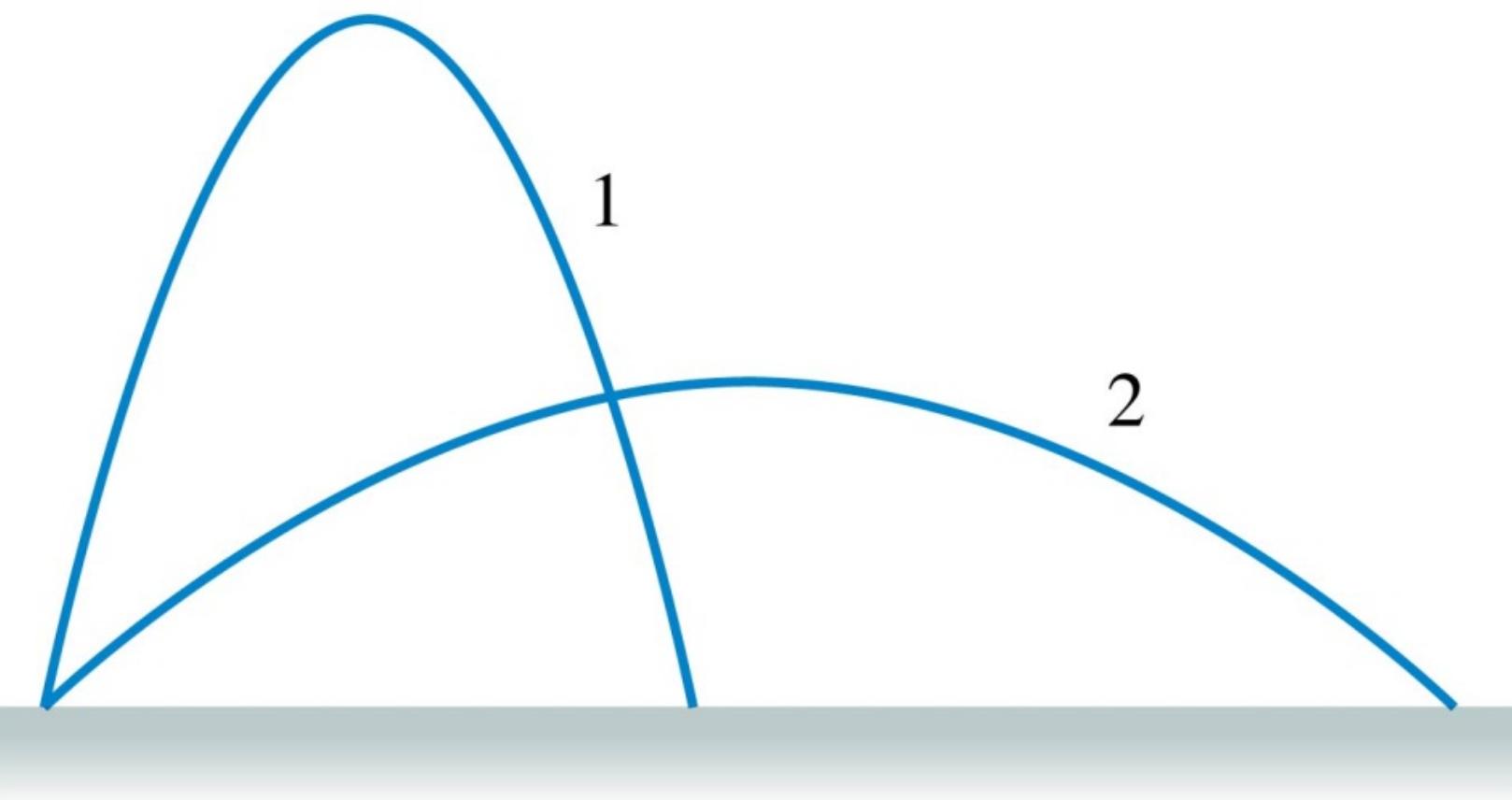
- A. Projectile 1 hits first.
- B. Projectile 2 hits first.
- C. They hit at the same time.
- D. There's not enough information to tell.



L4.Q1 - QuickCheck 4.4

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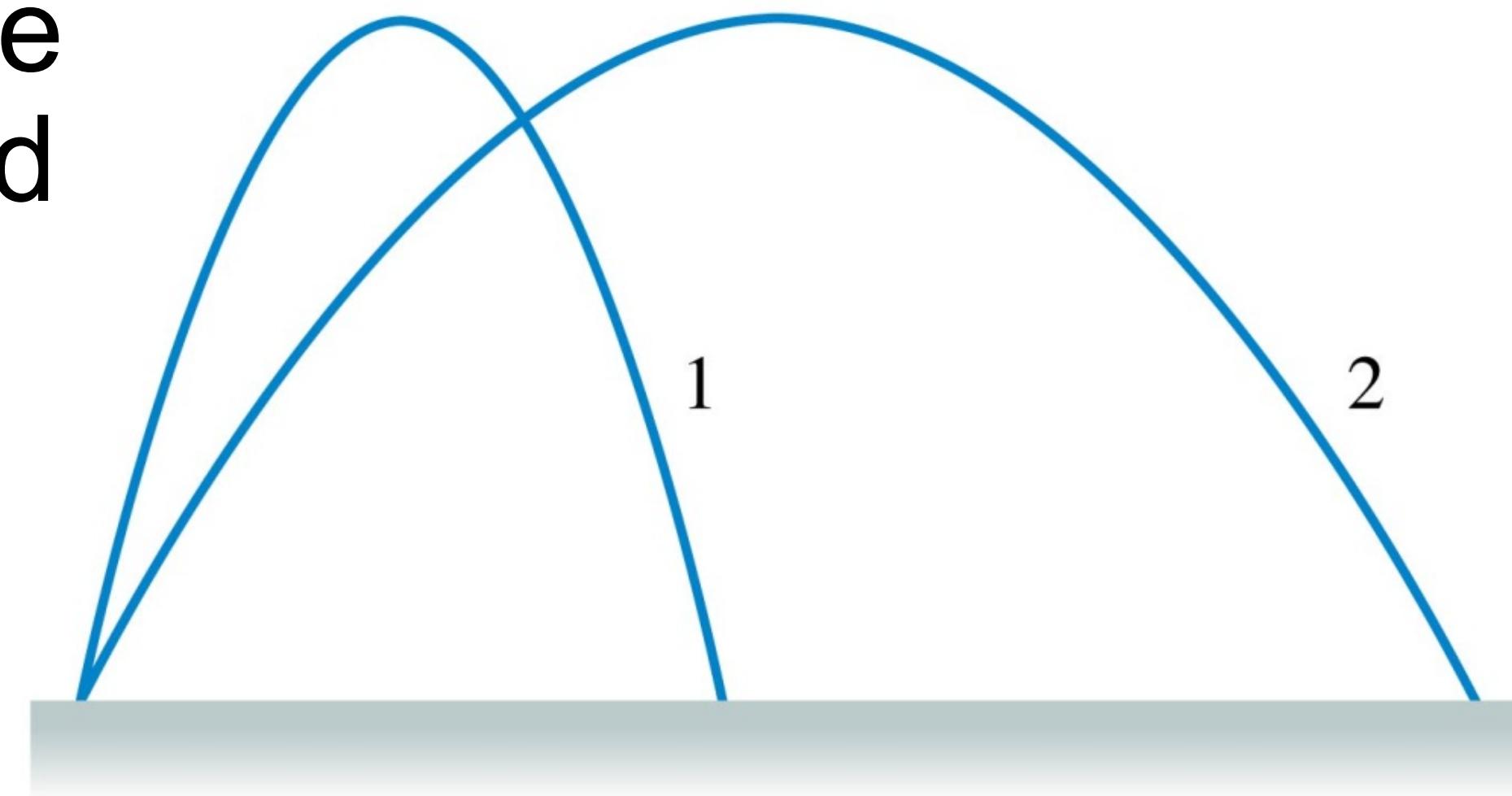
- A. Projectile 1 hits first.
- B. Projectile 2 hits first.
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- D. There's not enough information to tell.



L4.Q2 - QuickCheck 4.5

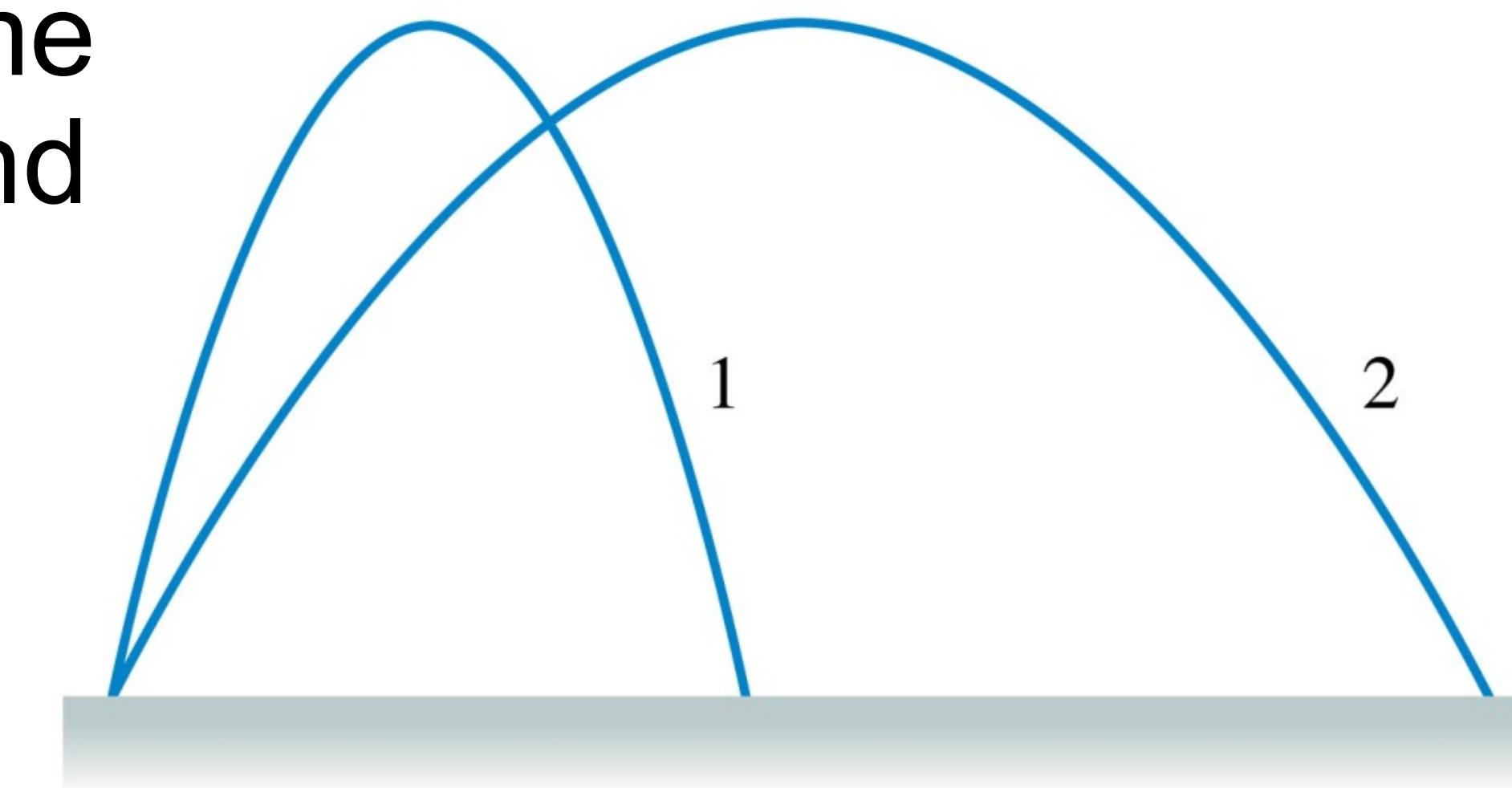
Projectiles 1 and 2 are launched over level ground with different speeds. Both reach the same height. Which hits the ground first? Ignore air resistance.

- A. Projectile 1 hits first.
- B. Projectile 2 hits first.
- C. They hit at the same time.
- D. There's not enough information to tell.



L4.Q2 - QuickCheck 4.5

Projectiles 1 and 2 are launched over level ground with different speeds. Both reach the same height. Which hits the ground first? Ignore air resistance.

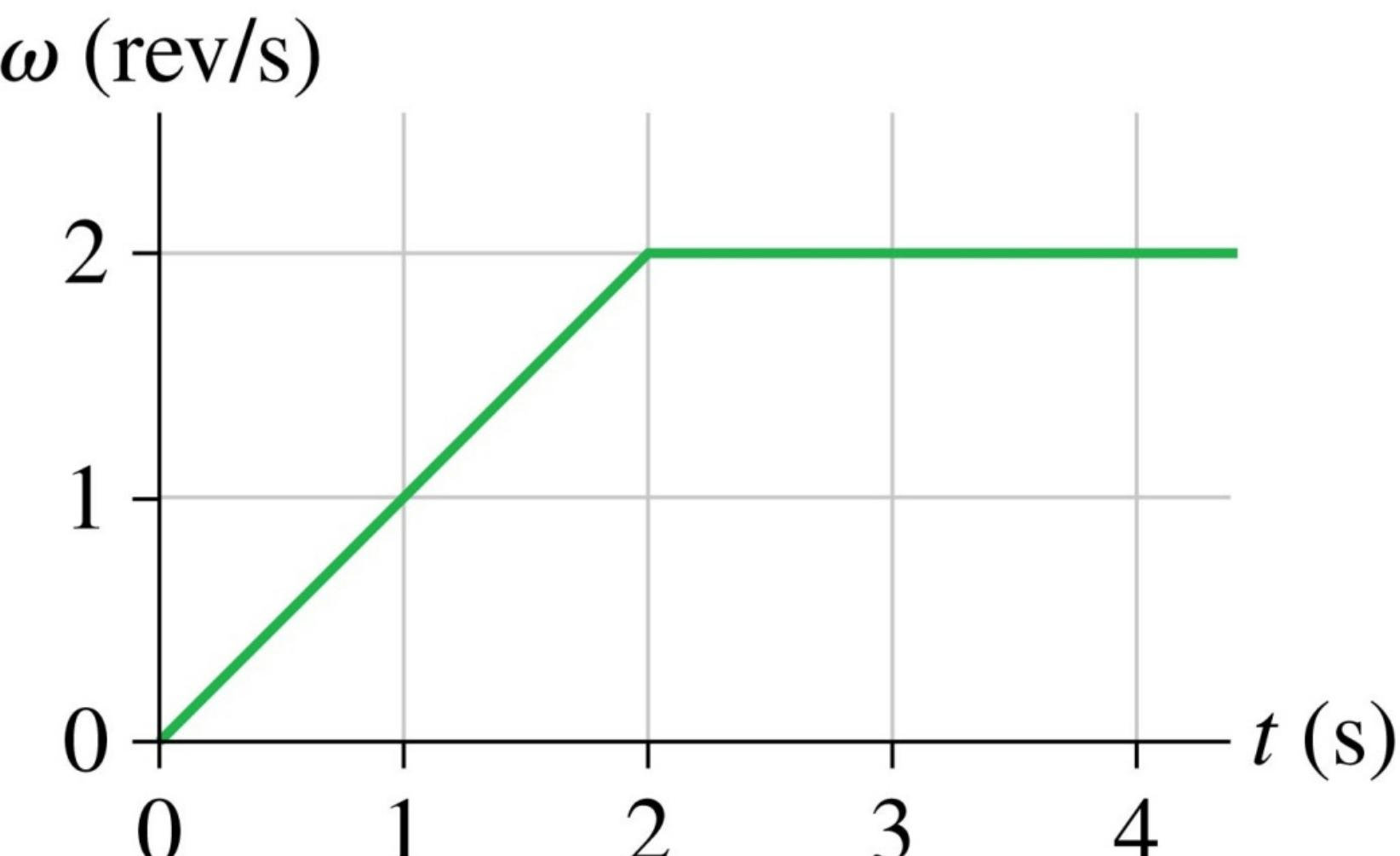


- A. Projectile 1 hits first.
- B. Projectile 2 hits first.
- C. They hit at the same time.
- D. There's not enough information to tell.

L4.Q3 - QuickCheck 4.7

This is the angular velocity graph of a wheel. How many revolutions does the wheel make in the first 4 s?

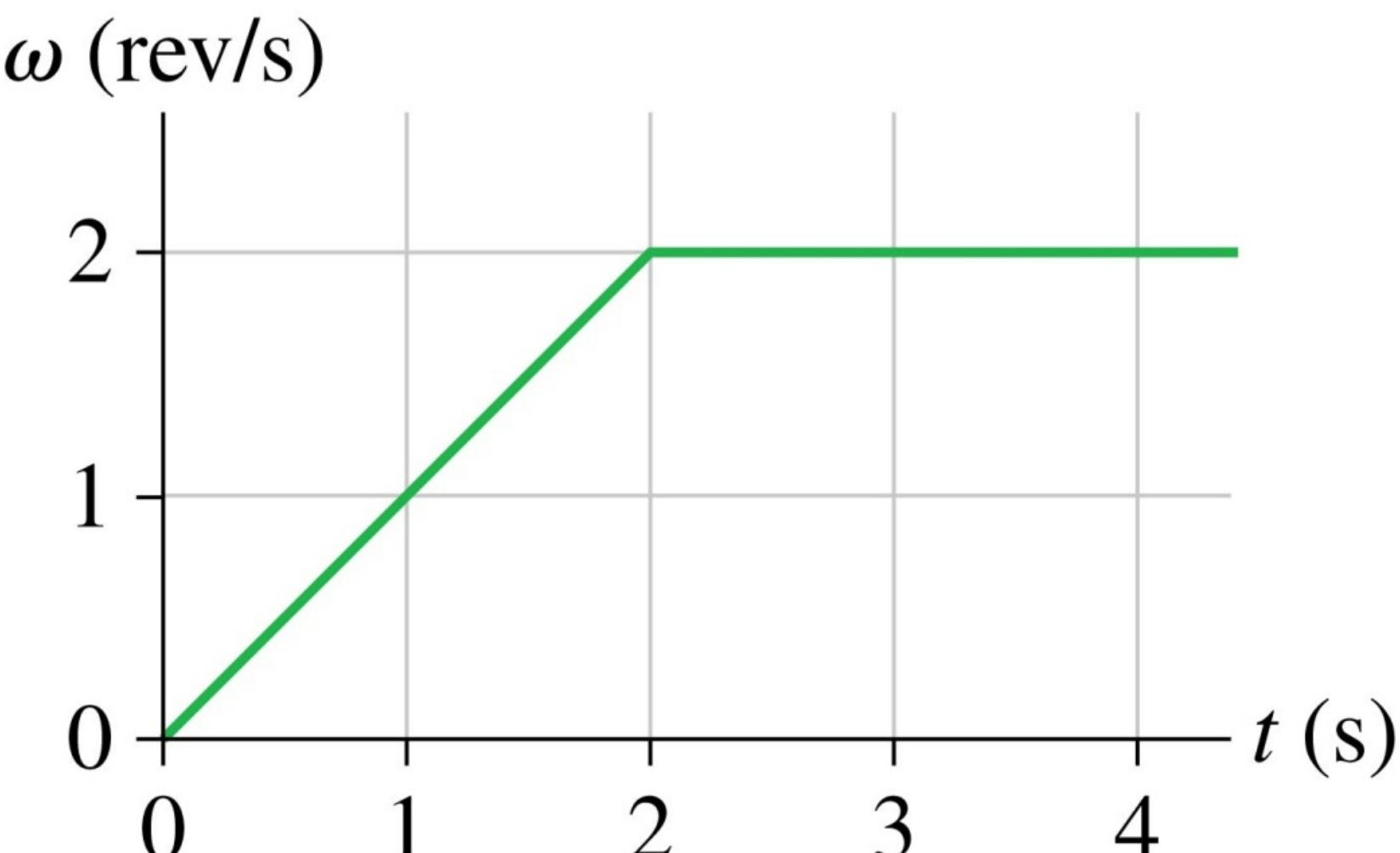
- A. 1
- B. 2
- C. 4
- D. 6
- E. 8



L4.Q3 - QuickCheck 4.7

This is the angular velocity graph of a wheel. How many revolutions does the wheel make in the first 4 s?

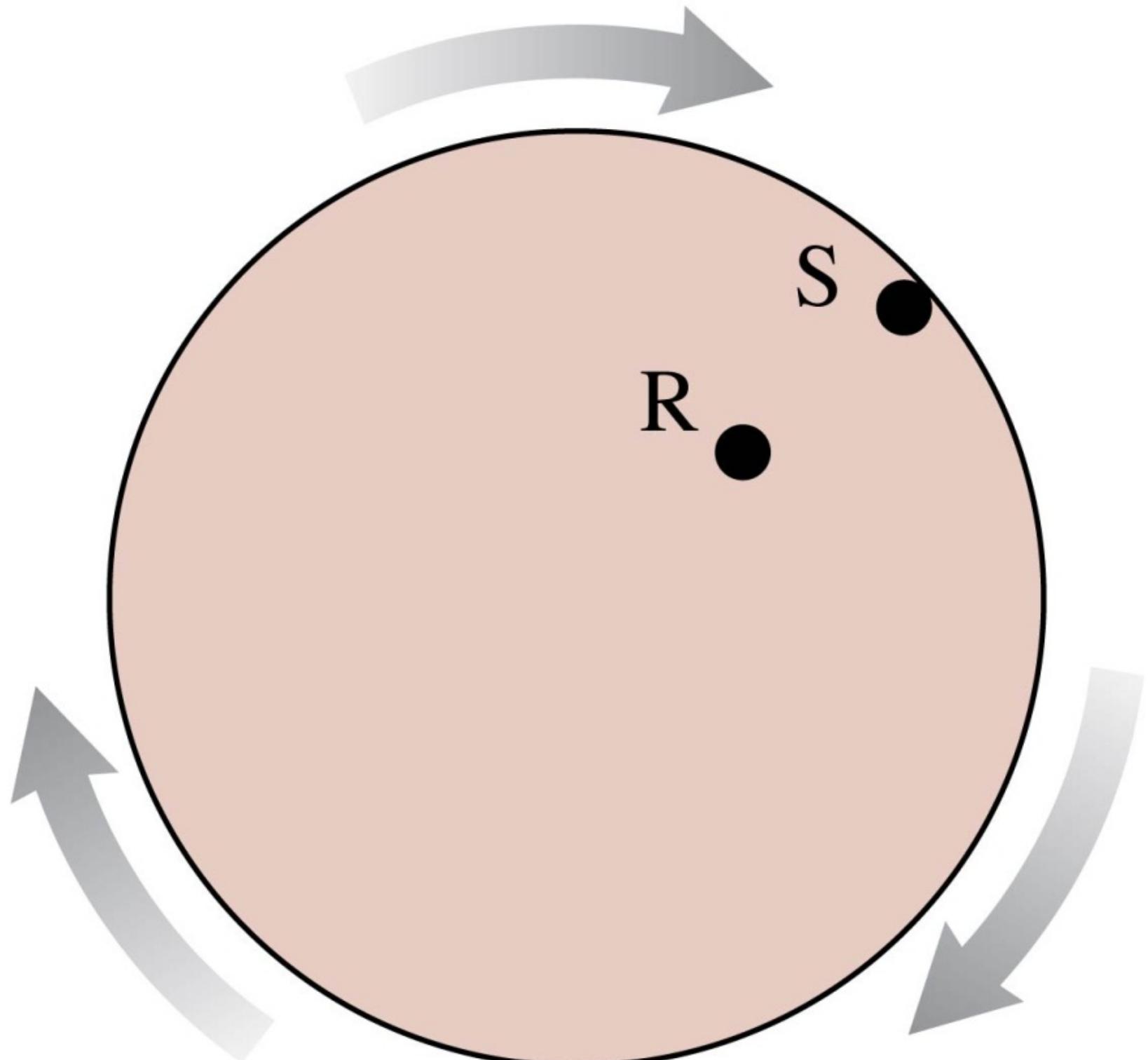
- A. 1
- B. 2
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- E. 8



L4.Q4A - QuickCheck 4.12

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's angular velocity is _____ that of Rasheed.

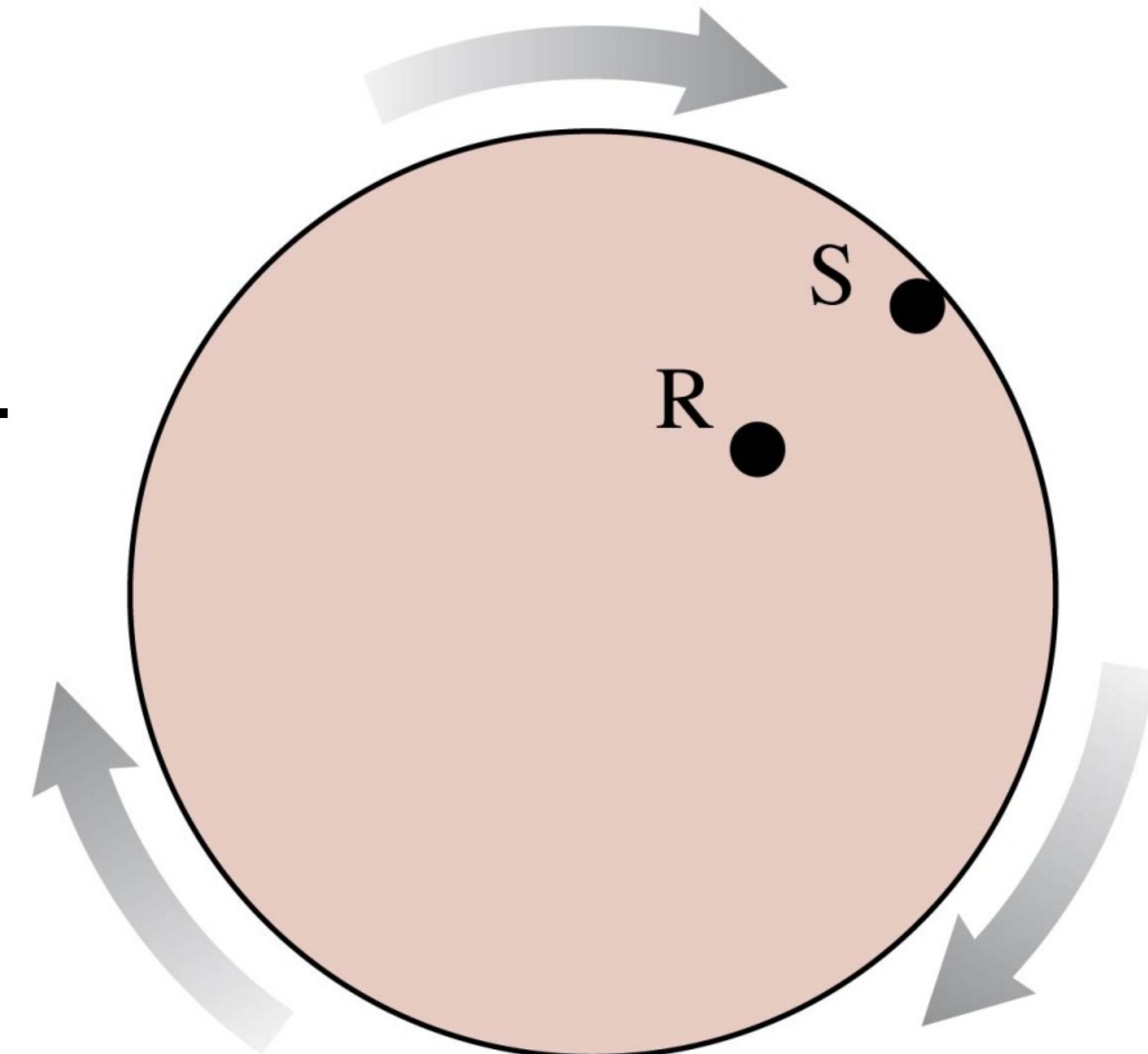
- A. half
- B. the same as
- C. twice
- D. four times
- E. We can't say without knowing their radii.



L4.Q4B - QuickCheck 4.13

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's speed is _____ that of Rasheed.

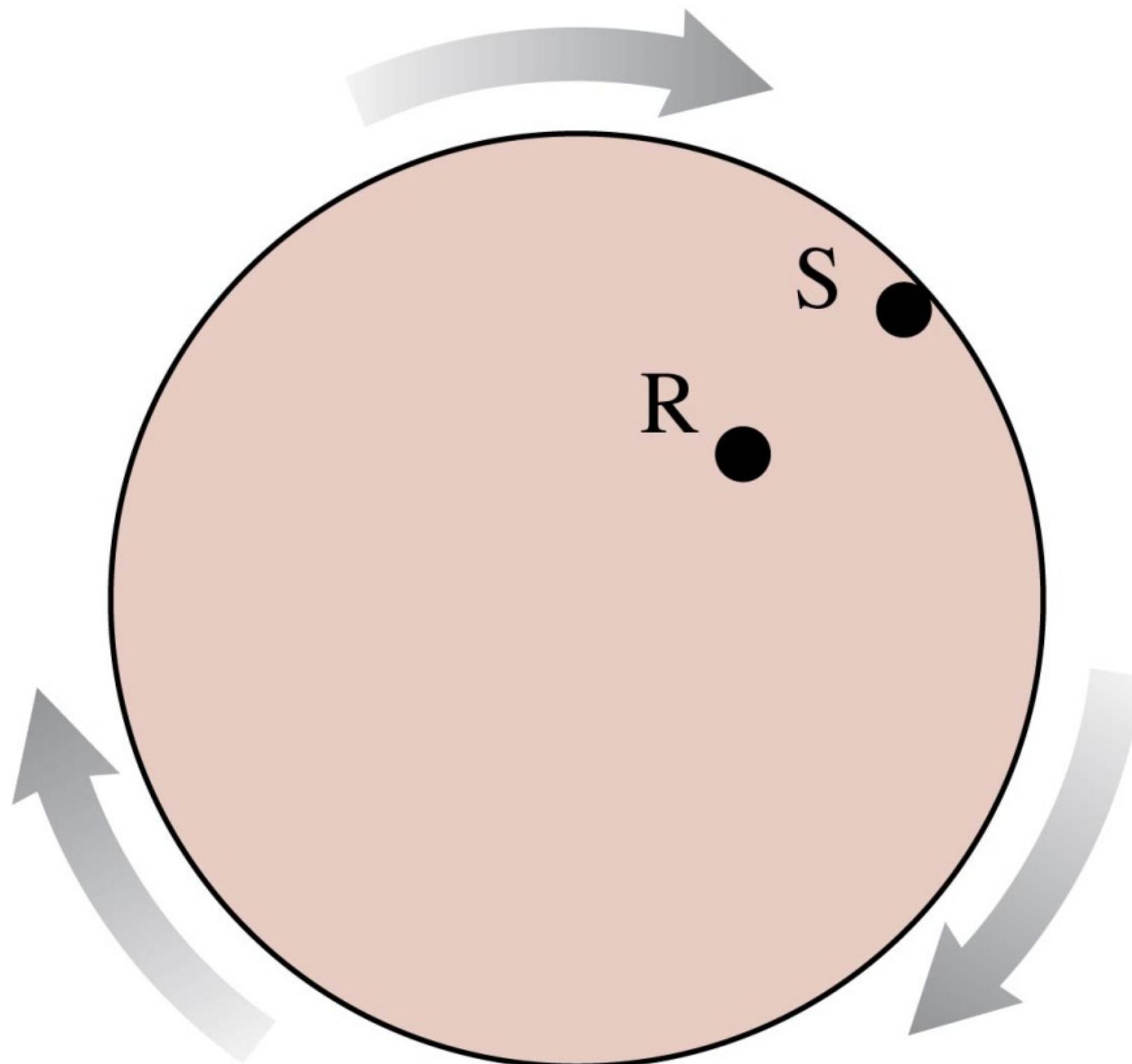
- A. half
- B. the same as
- C. twice
- D. four times
- E. We can't say without knowing their radii.



L4.Q4C - QuickCheck 4.14

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's acceleration is _____ that of Rasheed.

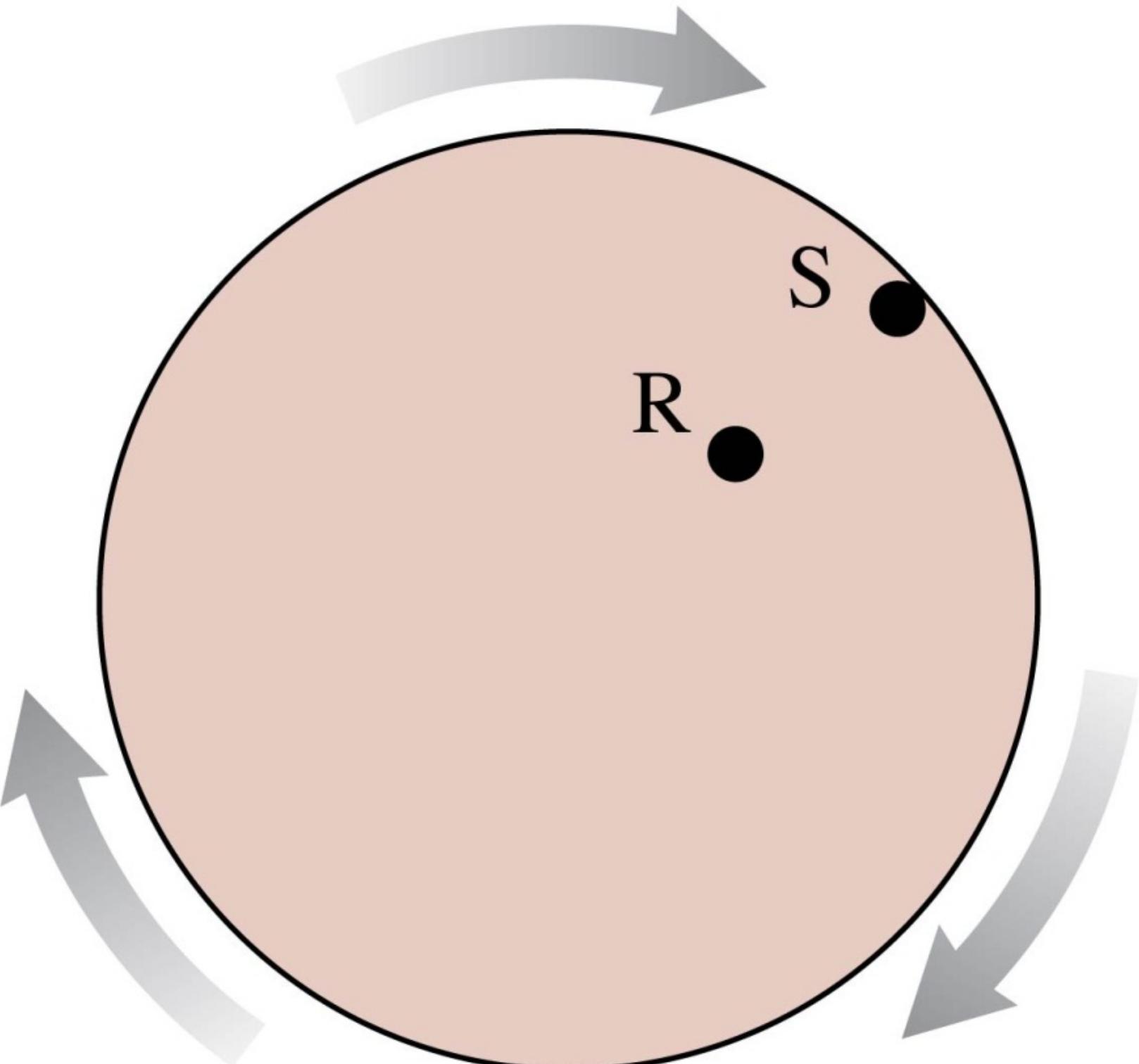
- A. half
- B. the same as
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L4.Q4A - QuickCheck 4.12

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's angular velocity is _____ that of Rasheed.

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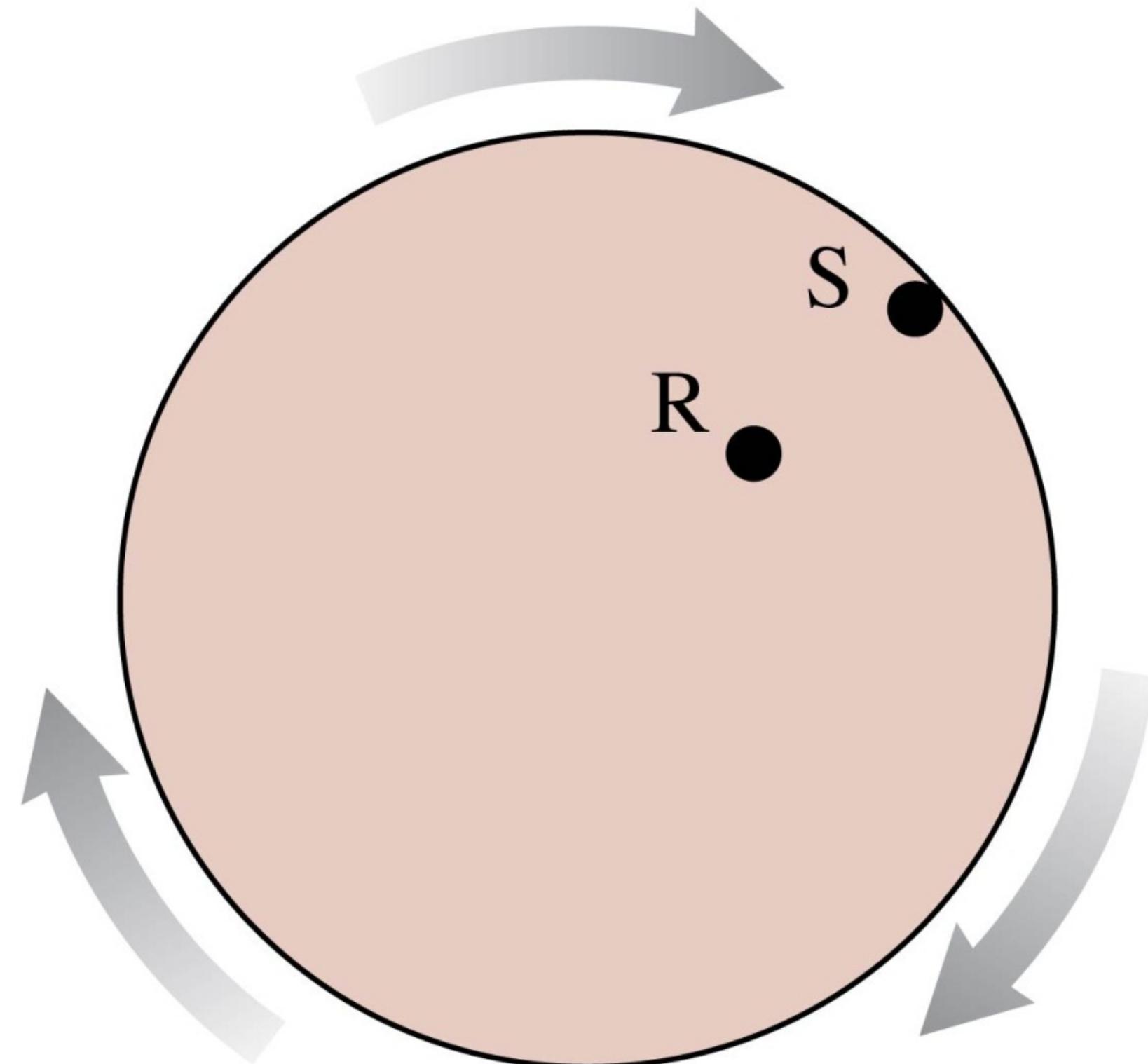


L4.Q4B - QuickCheck 4.13

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's speed is _____ that of Rasheed.

- A. half
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- E. We can't say without knowing their radii.

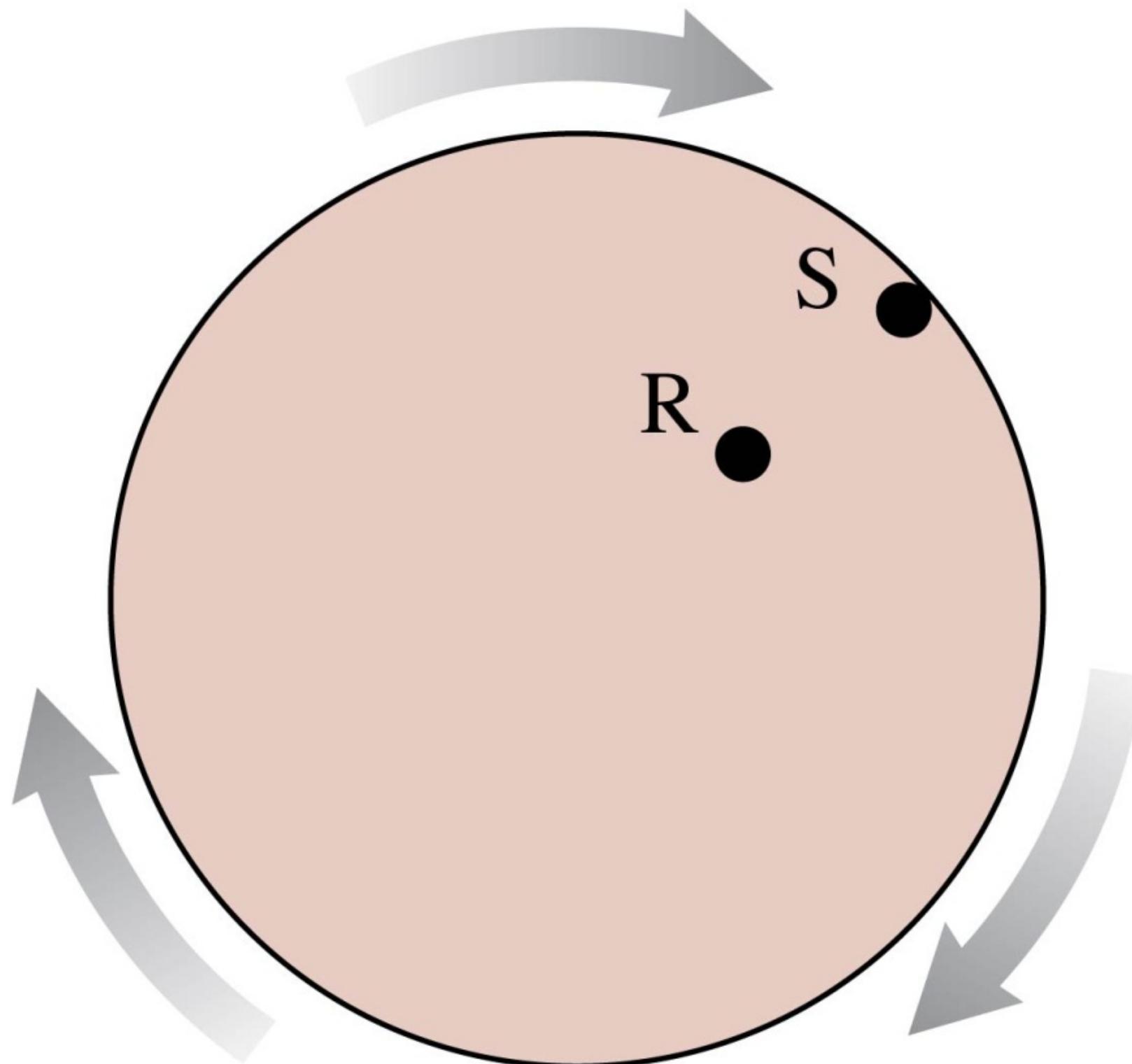
$$v = \omega r$$



L4.Q4C - QuickCheck 4.14

Rasheed and Sofia are riding a merry-go-round that is spinning steadily. Sofia is twice as far from the axis as is Rasheed. Sofia's acceleration is _____ that of Rasheed.

- A. half
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- D. four times
- E. We can't say without knowing their radii.



$$\text{Centripetal acceleration } a = \frac{v^2}{r} = \omega^2 r$$

Chapter 4

Important Concepts

Important Concepts

Kinematics in two dimensions

If \vec{a} is constant, then the x - and y -components of motion are independent of each other.

$$x_f = x_i + v_{ix} \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$y_f = y_i + v_{iy} \Delta t + \frac{1}{2} a_y (\Delta t)^2$$

$$v_{fx} = v_{ix} + a_x \Delta t$$

$$v_{fy} = v_{iy} + a_y \Delta t$$

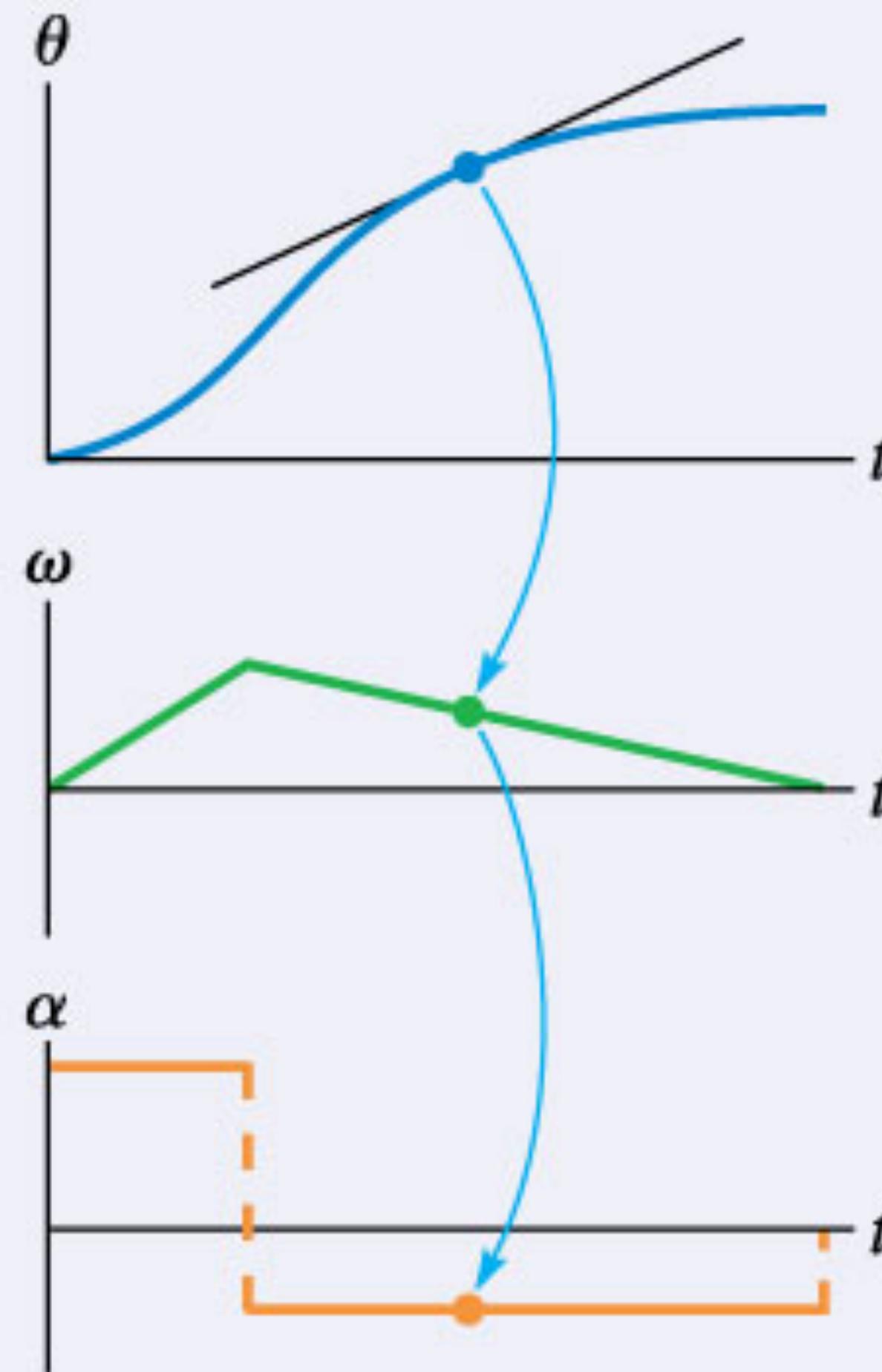
Important Concepts

Circular motion kinematics

Circular motion graphs and kinematics are analogous to linear motion with constant acceleration.

Angle, angular velocity, and angular acceleration are related graphically.

- The angular velocity is the slope of the angular position graph.
- The angular acceleration is the slope of the angular velocity graph.



Important Concepts

The **instantaneous velocity**

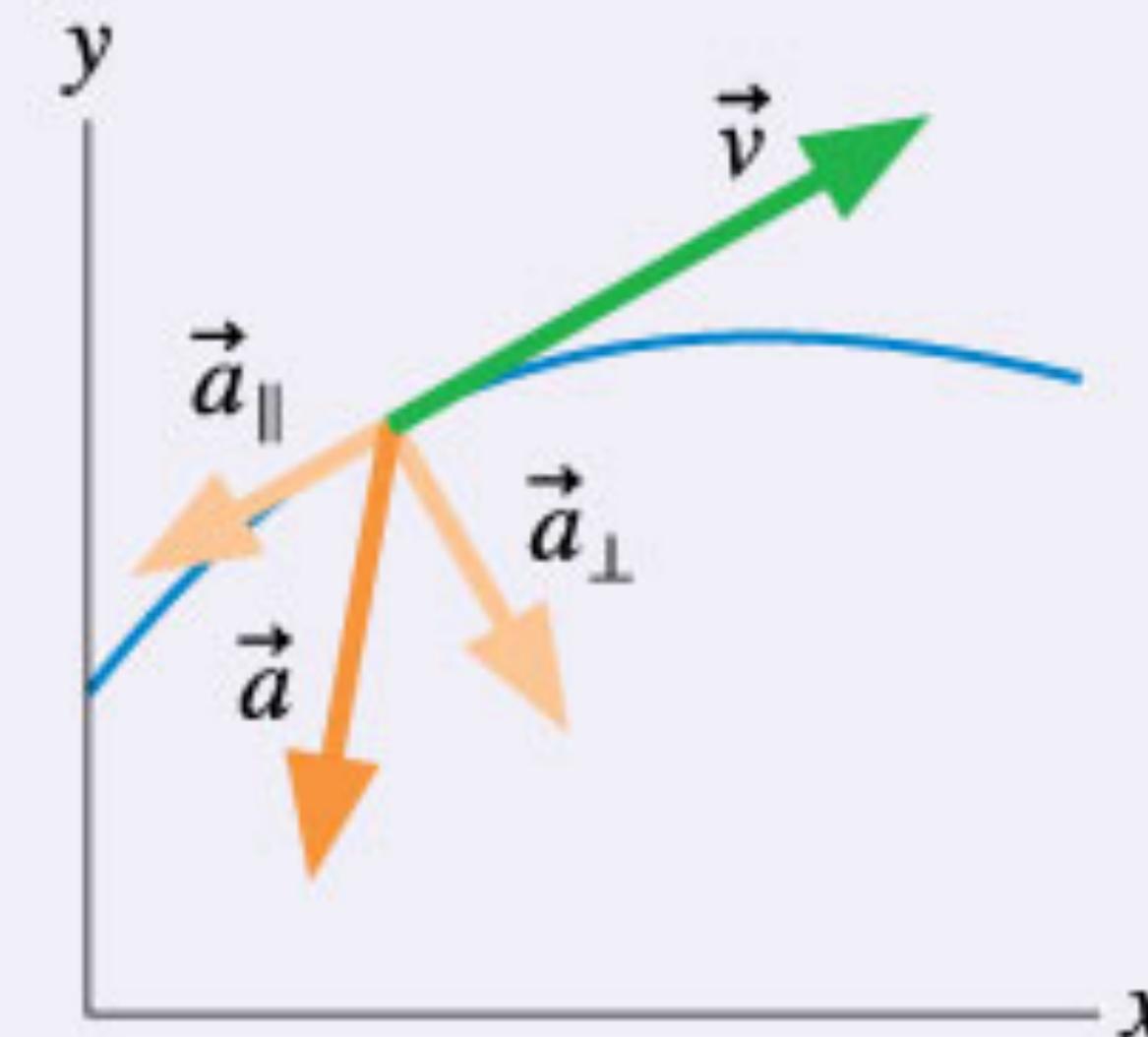
$$\vec{v} = d\vec{r}/dt$$

is a vector tangent to the trajectory.

The **instantaneous acceleration** is

$$\vec{a} = d\vec{v}/dt$$

$\vec{a}_{||}$, the component of \vec{a} parallel to \vec{v} , is responsible for change of *speed*. \vec{a}_{\perp} , the component of \vec{a} perpendicular to \vec{v} , is responsible for change of *direction*.



Important Concepts

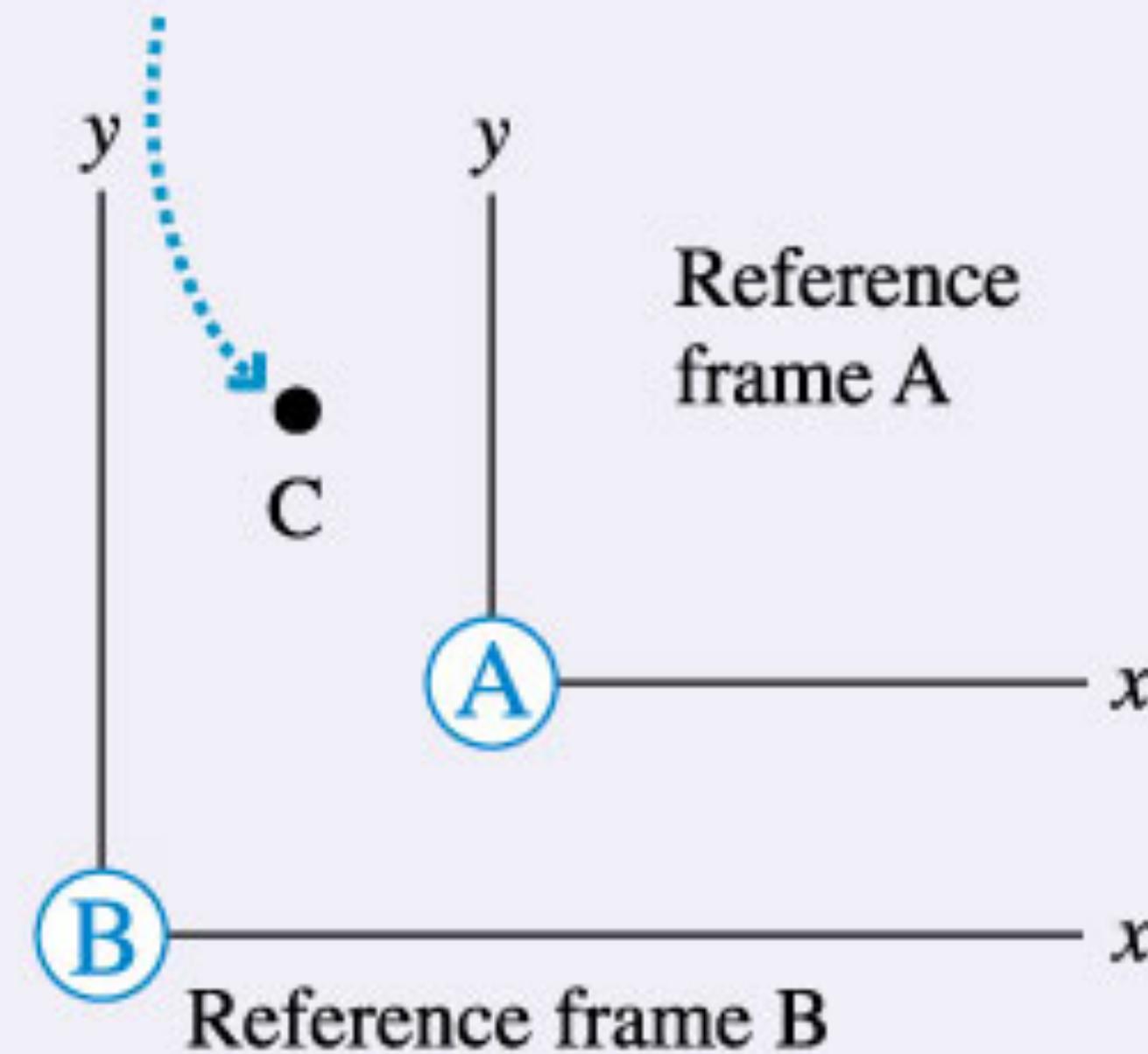
Relative Motion

If object C moves relative to reference frame A with velocity \vec{v}_{CA} , then it moves relative to a different reference frame B with velocity

$$\vec{v}_{CB} = \vec{v}_{CA} + \vec{v}_{AB}$$

where \vec{v}_{AB} is the velocity of A relative to B. This is the Galilean transformation of velocity.

Object C moves relative to both A and B.



Important Concepts

Uniform Circular Motion

Angular velocity $\omega = d\theta/dt$.

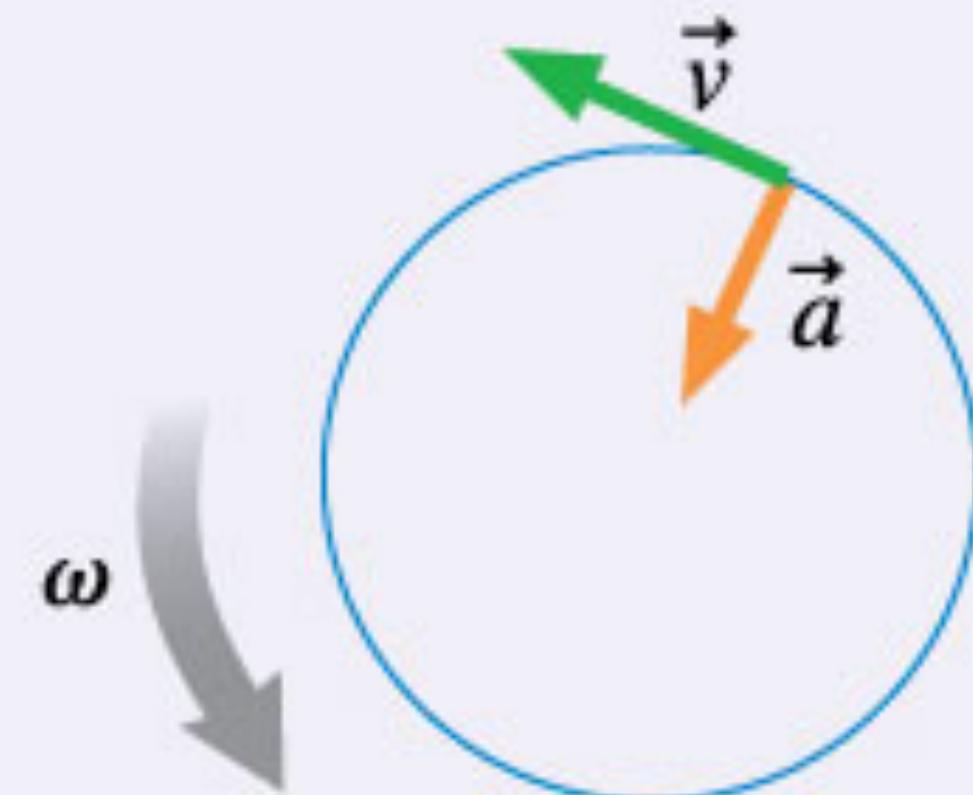
v_t and ω are constant:

$$v_t = \omega r$$

The centripetal acceleration points toward the center of the circle:

$$a = \frac{v^2}{r} = \omega^2 r$$

It changes the particle's direction but not its speed.



Important Concepts

Circular motion kinematics

$$\text{Period } T = \frac{2\pi r}{v} = \frac{2\pi}{\omega}$$

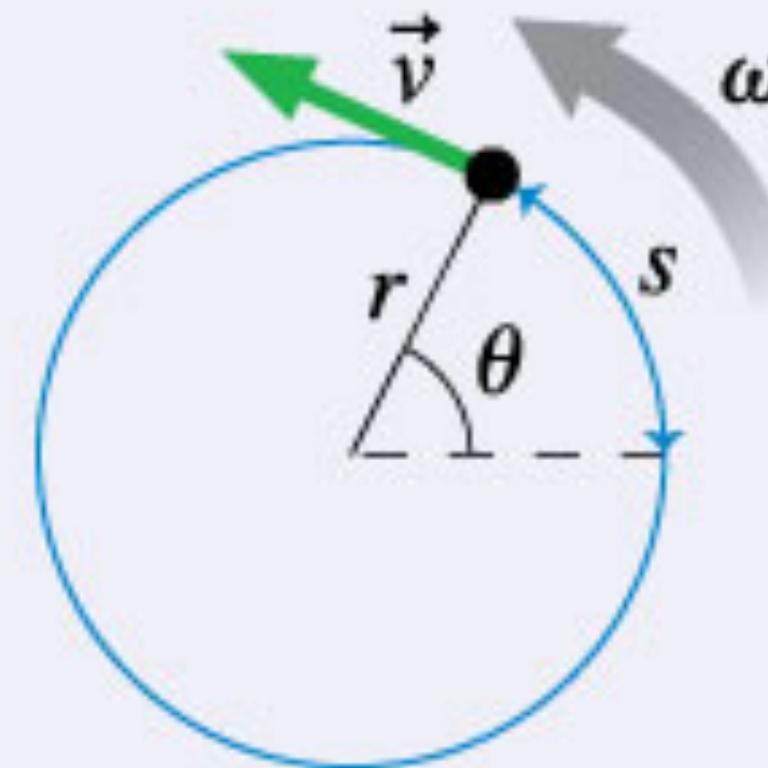
$$\text{Angular position } \theta = \frac{s}{r}$$

Constant angular acceleration

$$\omega_f = \omega_i + \alpha \Delta t$$

$$\theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2$$

$$\omega_f^2 = \omega_i^2 + 2\alpha \Delta \theta$$



Important Concepts

Nonuniform Circular Motion

Angular acceleration $\alpha = d\omega/dt$.

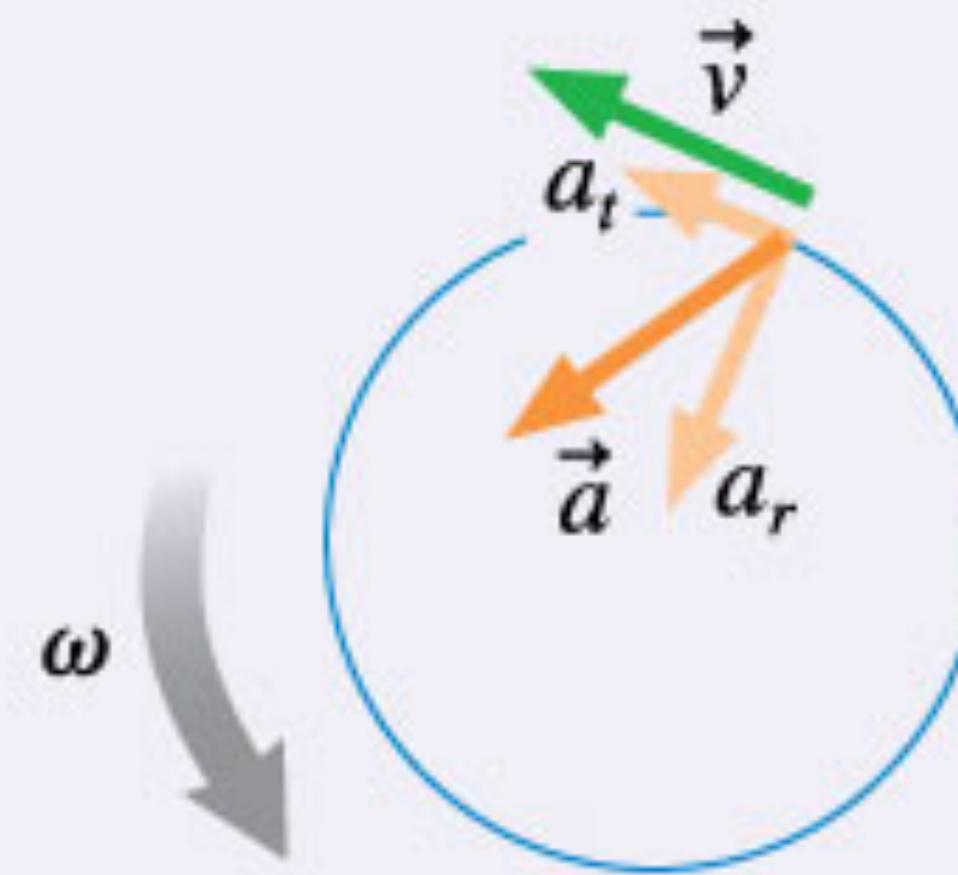
The radial acceleration

$$a_r = \frac{v^2}{r} = \omega^2 r$$

changes the particle's direction. The tangential component

$$a_t = \alpha r$$

changes the particle's speed.



Important Concepts

Projectile motion is motion under the influence of only gravity.

MODEL Model as a particle launched with speed v_0 at angle θ .

VISUALIZE Use coordinates with the x -axis horizontal and the y -axis vertical.

SOLVE The horizontal motion is uniform with $v_x = v_0 \cos \theta$. The vertical motion is free fall with $a_y = -g$. The x and y kinematic equations have the *same* value for Δt .

