

# Physics 111 - Class 7A

## Force Applications

October 17, 2022

# Class Outline

- Logistics / Announcements
- Mid-course Feedback Results
- Introduction to Chapter 6
- Clicker Questions
- Activity: Worked Problems

# Logistics/Announcements

- Lab this week: Lab 4
- HW6 due this week on Thursday at 6 PM
- Learning Log 6 due on Saturday at 6 PM
- HW and LL deadlines have a 48 hour grace period
- Test/Bonus Test: Bonus Test 2 available this week (Chapters 3 & 4)
- Additional Student Hours from Tutorial TAs for more 1:1 help via Zoom

# Mid-course Feedback Results

## Phys 111 2022WT1 Mid-course feedback

### Default Question Block

Q2

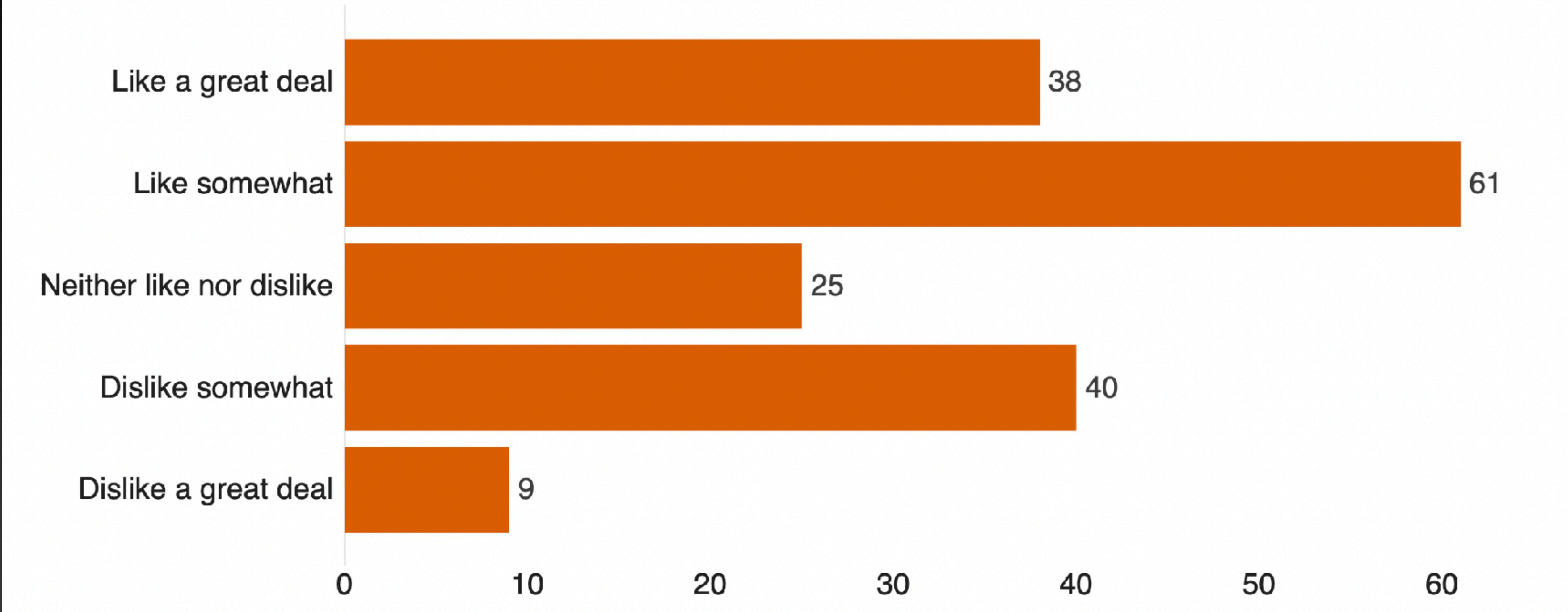
What do you think of the course structure so far?

*Reminder: the course structure is: Watch videos before class, attempt HW problems throughout the week, in Lectures you practice working with the most complex topics, and learn some practical skills during lab. Tests and Bonus Tests are held every two weeks keeps the content fresh in your mind, and reflections in Learning Logs cap off the week of learning.*

- 173 respondents ~ 60% response rate (class of 289)
- Thank you for taking the time to submit the feedback!

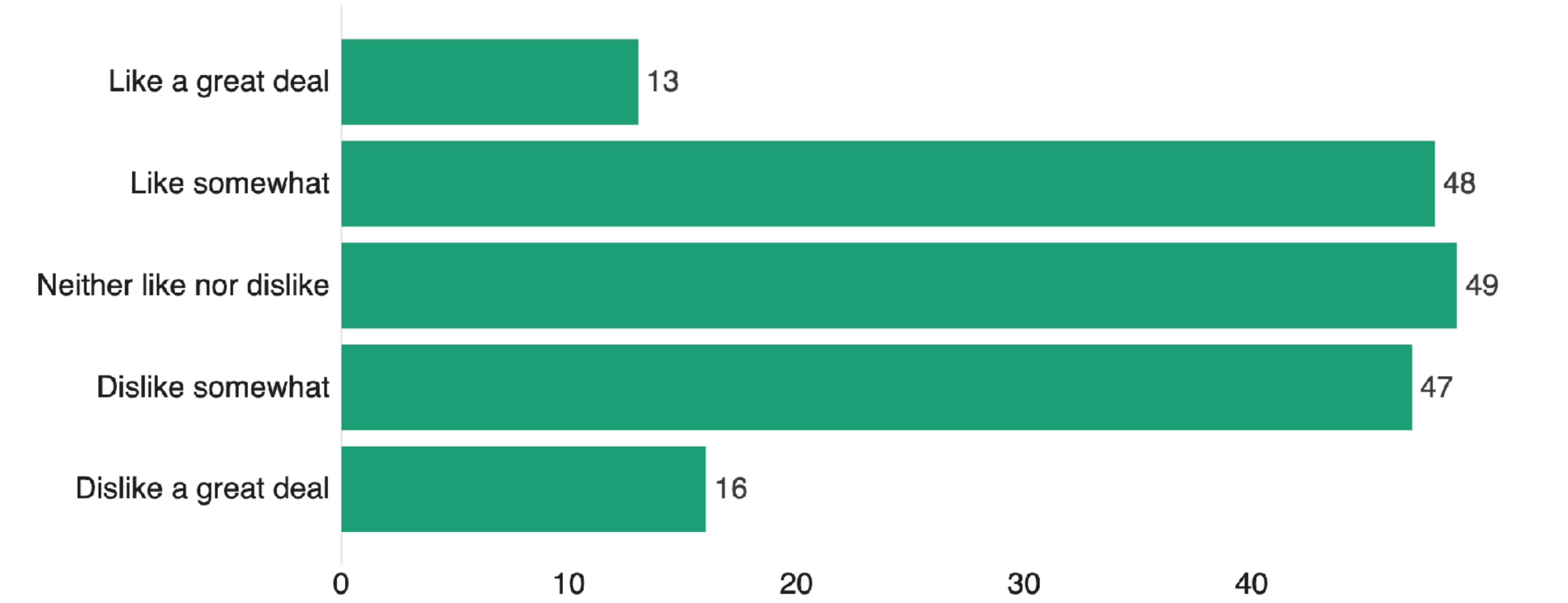
# Mid-course Feedback Results

What do you think of the course Structure so far?



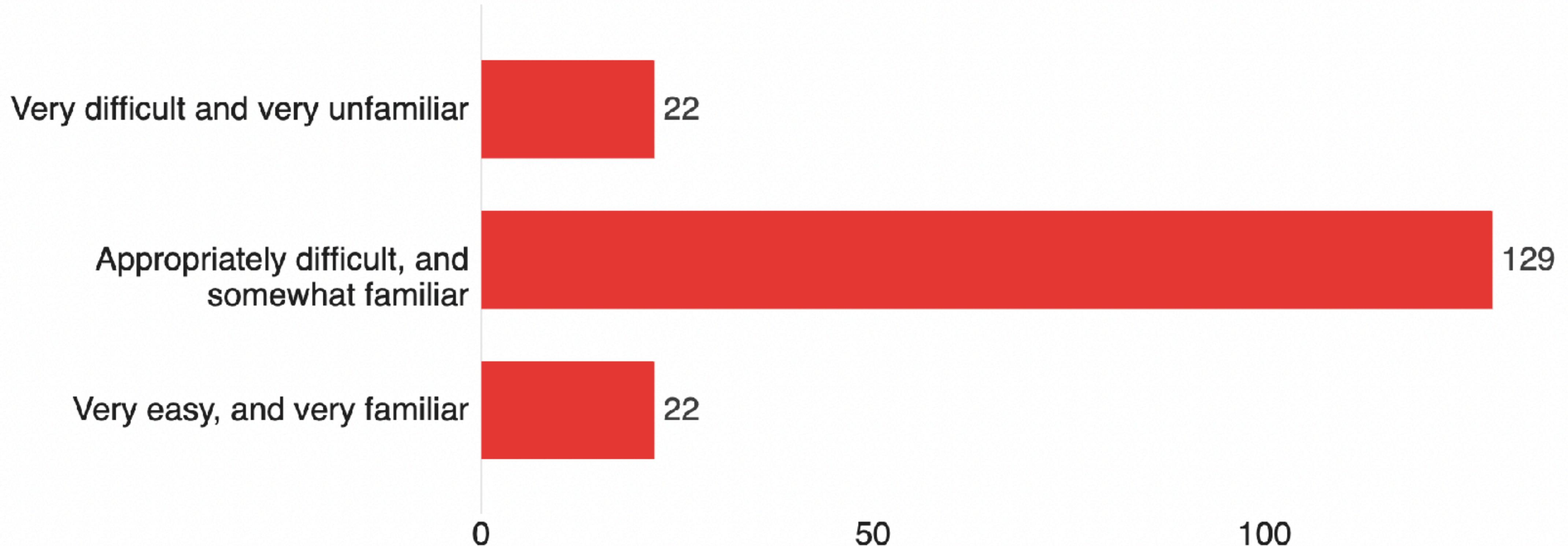
# Mid-course Feedback Results

What do you think about the course Lectures so far?



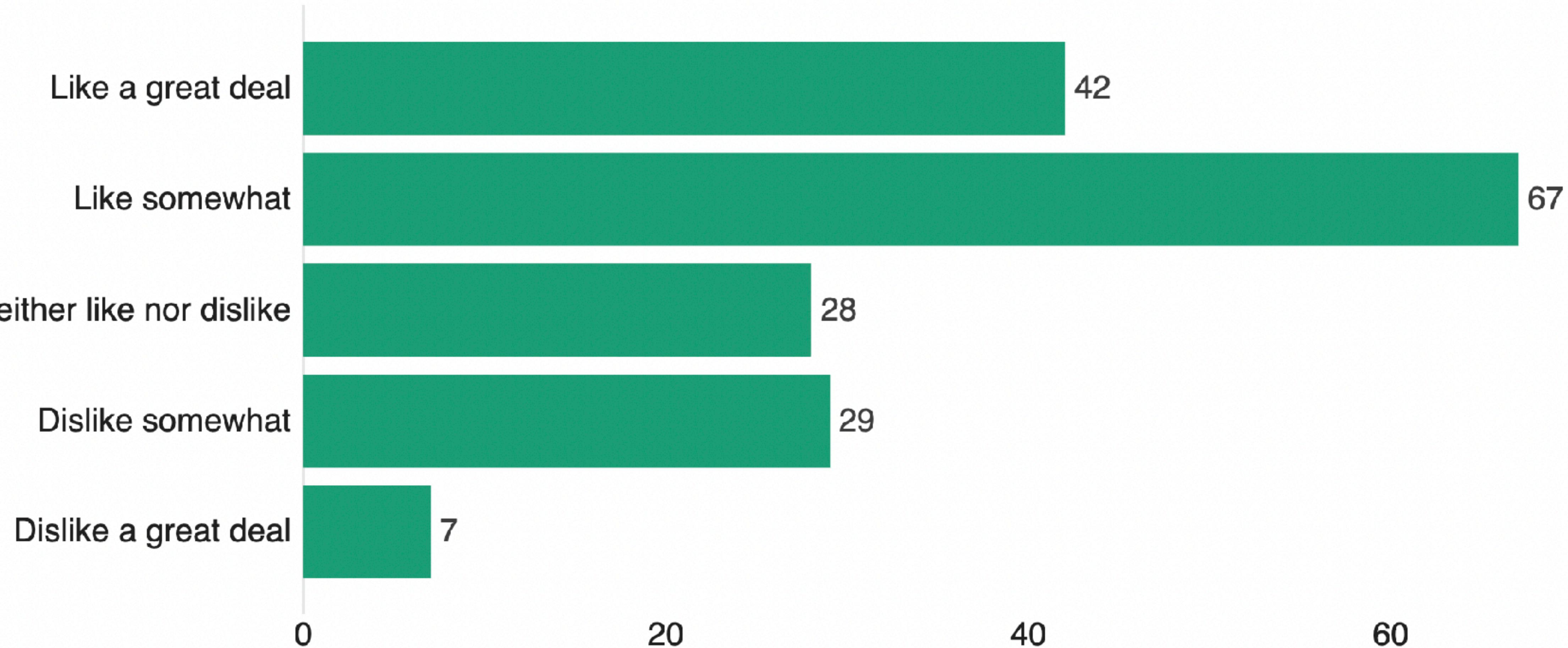
# Mid-course Feedback Results

How difficult are you finding the content we cover in lecture?



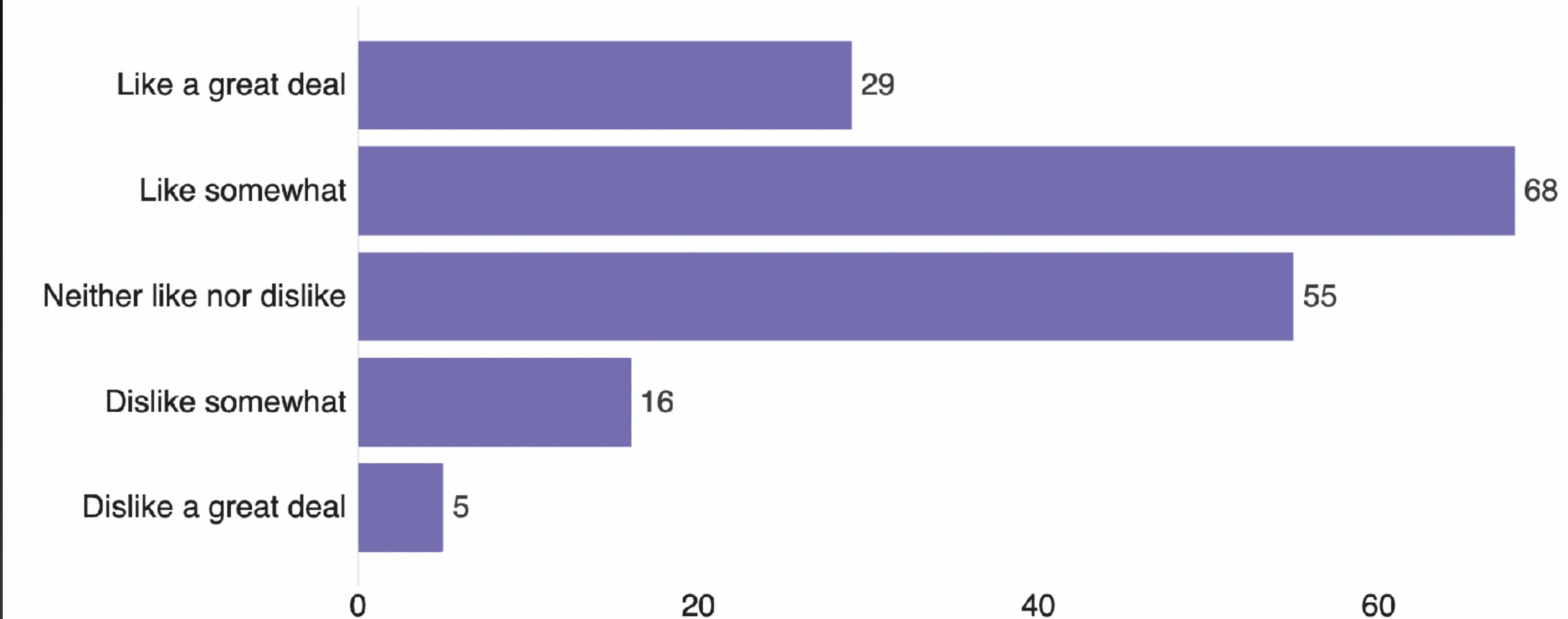
# Mid-course Feedback Results

What do you think about the course Labs so far?



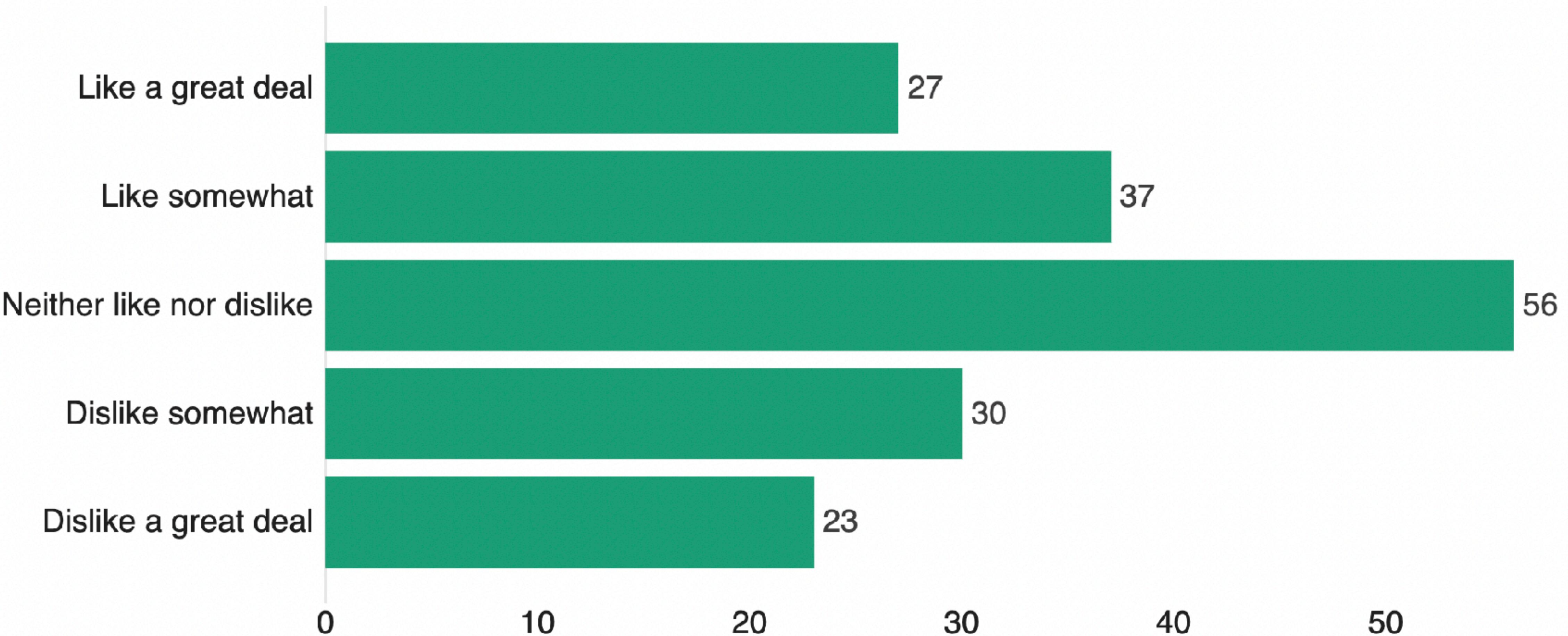
# Mid-course Feedback Results

What do you think of the course Homework so far?



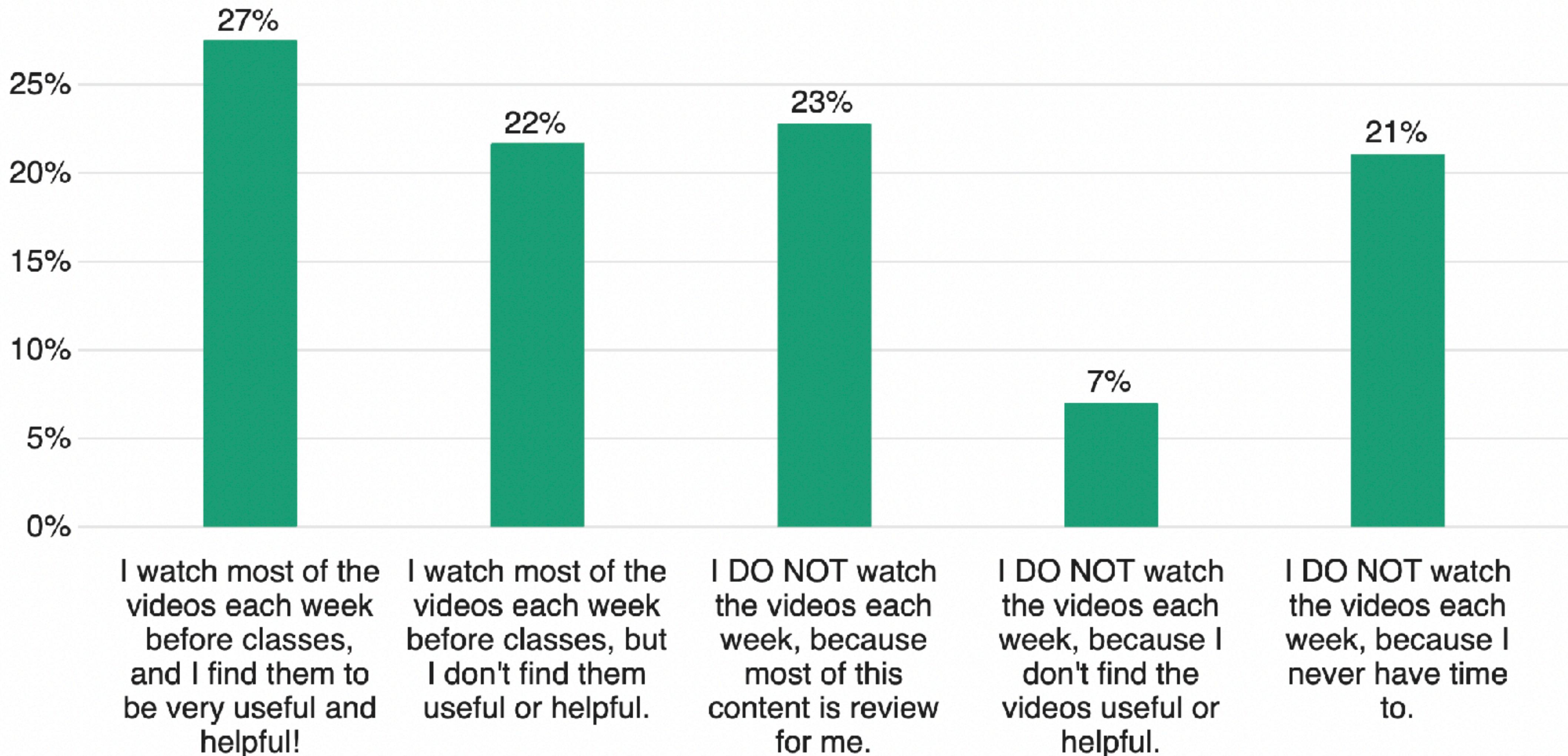
# Mid-course Feedback Results

What do you think of the course Learning Logs so far?



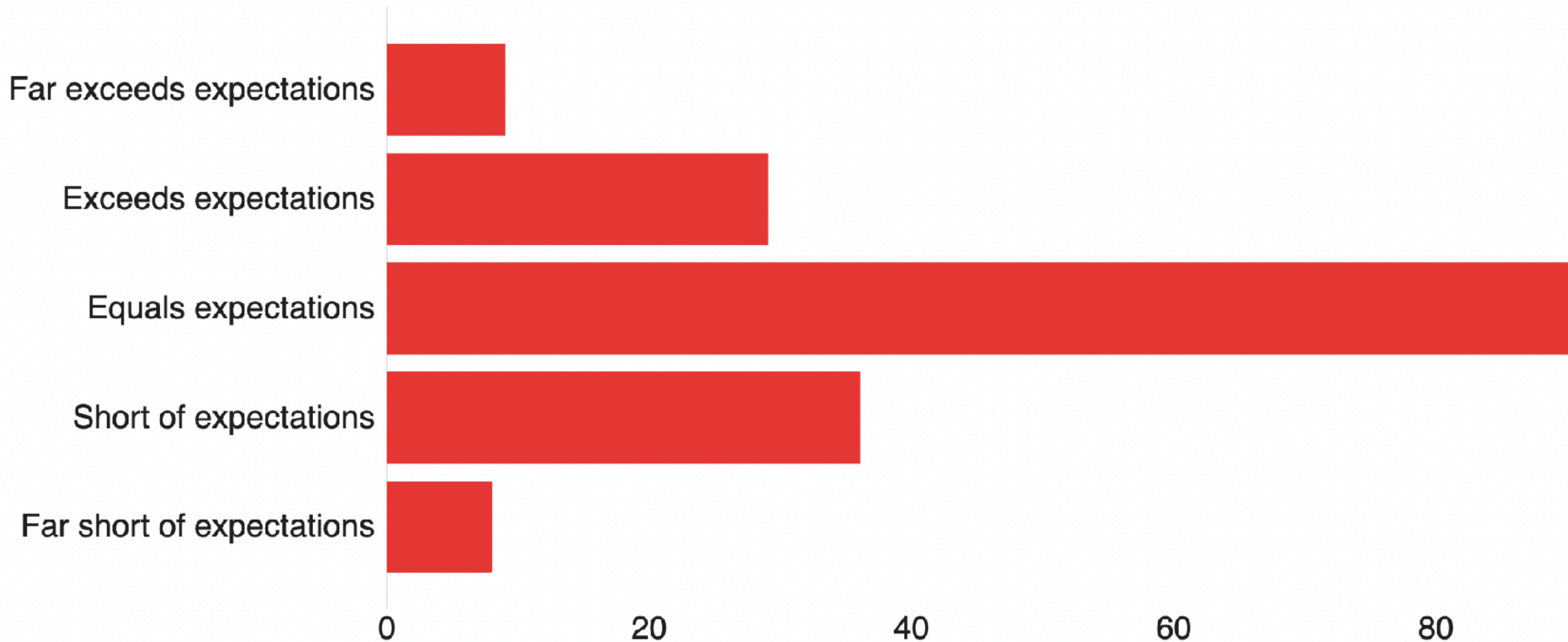
# Mid-course Feedback Results

Q12 - What do you think about the assigned videos by Flipping Physics?



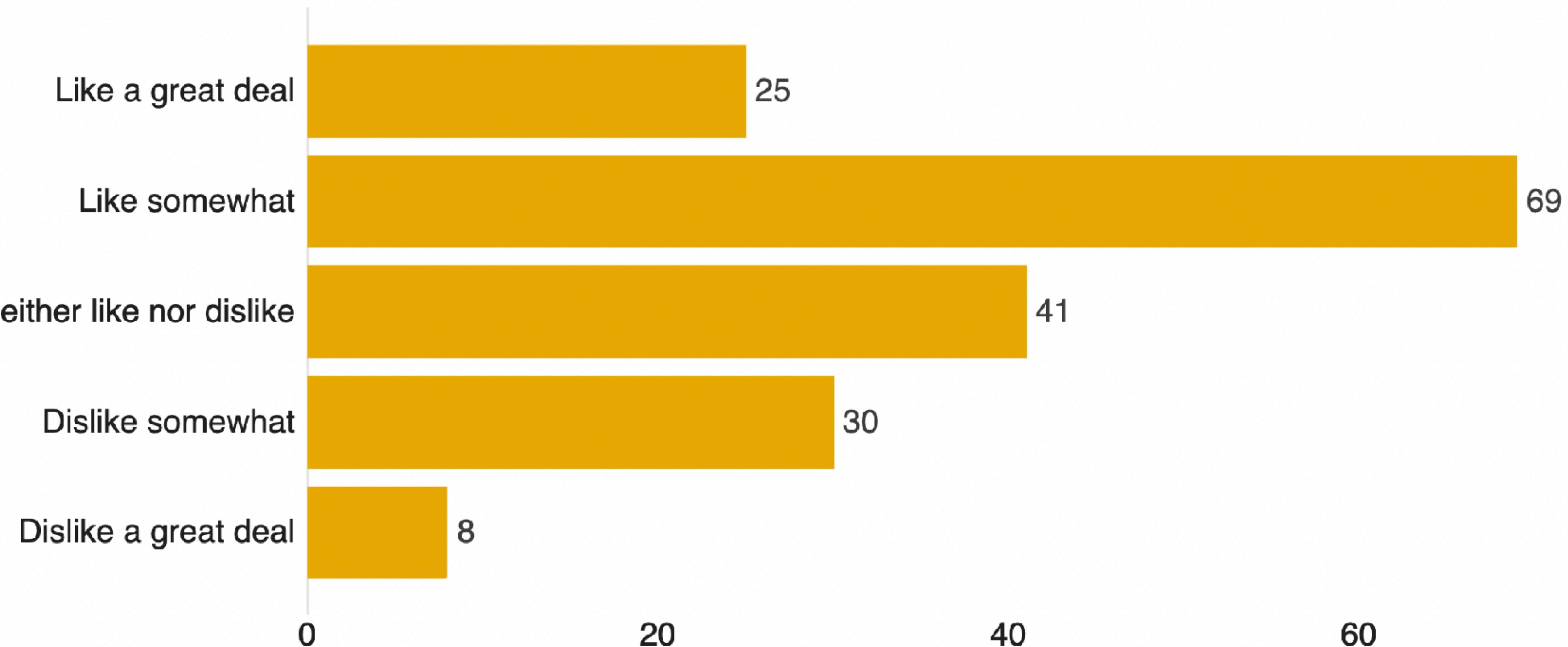
# Mid-course Feedback Results

Do you feel that you are getting sufficient feedback in the course so far?



# Mid-course Feedback Results

Overall, How do you think the course is going so far ?



# Mid-course Feedback Results

Start	My response
Doing more questions in class...	<i>I'll try, but the classes are pretty jam-packed already and many students are asking to complete the full examples, rather than leave it in algebra...</i>
Finish all the examples you do in class.  (AKA Do fewer questions in class...)	<i>This will just take up too much time! I think it's more useful to "set-up" the problem and then provide a full worked solution at the end of class like I started doing in Week 5. I'll keep this going.</i>
Teaching the introductory concepts we need for the HW (lecturing)	<i>Unfortunately, this cannot happen. This is a flipped classroom and it would just waste too many of the students' times to ask them to watch videos and then go through it again in class. <b>You need to teach yourself the concepts outside of class</b> and come to class to practice them, and I'll highlight the trickiest things.</i>
Review HW problems in class	<i>Good idea. I will ask the TAs to go over some of the most challenging problem from the HW that week during the Tutorials.</i>

# Mid-course Feedback Results

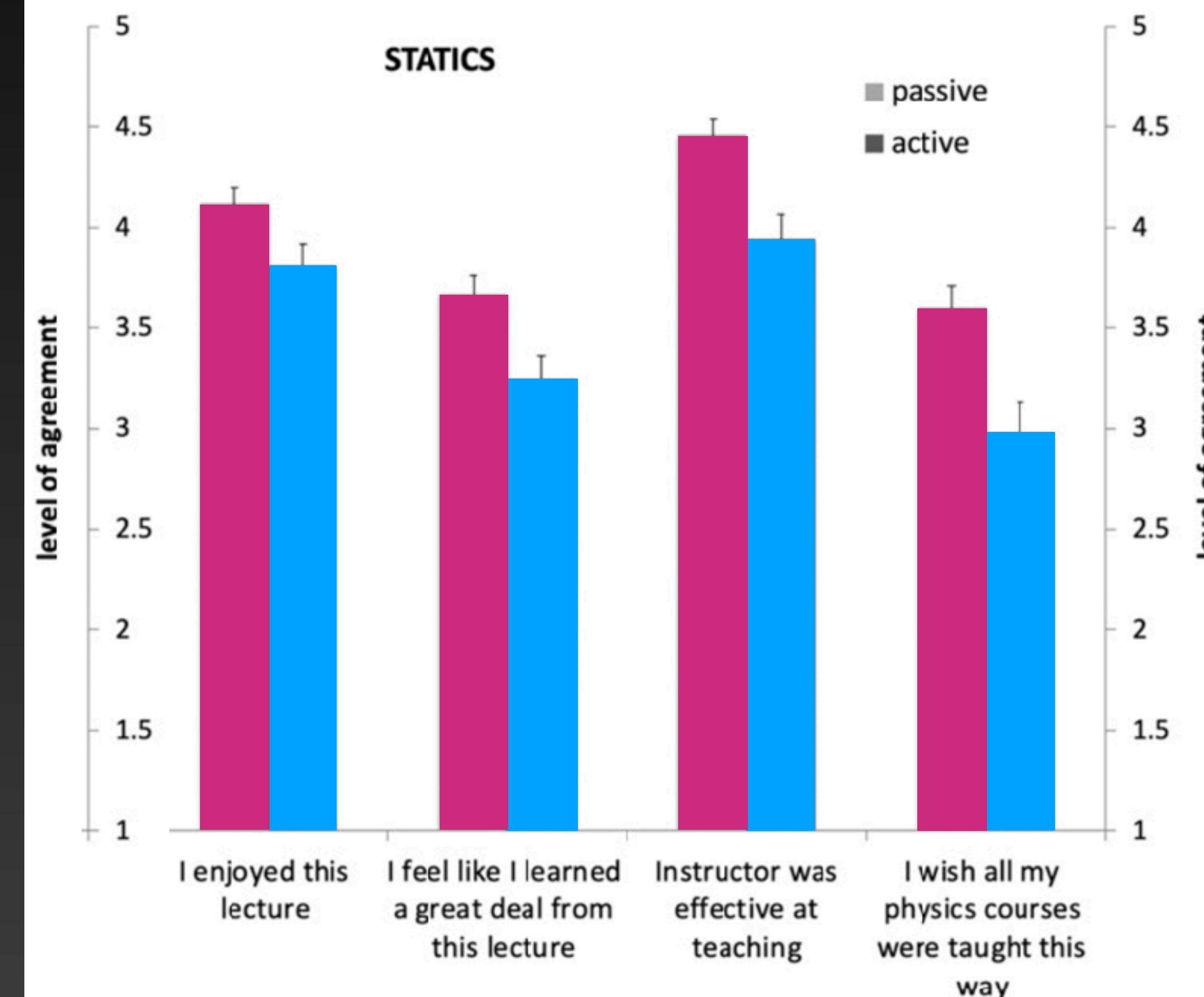
Stop	My response
Doing harder problems in class	This is controversial...
Doing easier problems in class	This is controversial...
Learning Logs nice, but very repetitive.	<p>Okay - I don't want the Learning Logs to be a "chore" so I will reduce the time it takes out of your lives by removing Question 2 (what grade you deserve and justify it).</p> <p>The other questions will remain as they're more directly tied to your learning and your well-being.</p>
Making the tests so long (and hard)!	Sorry! Test 2, admittedly, was longer than I wanted it to be!
(Making us teach ourselves the course material!) x 1000	See next slides...

# Measuring actual learning versus feeling of learning in response to being actively engaged in the classroom

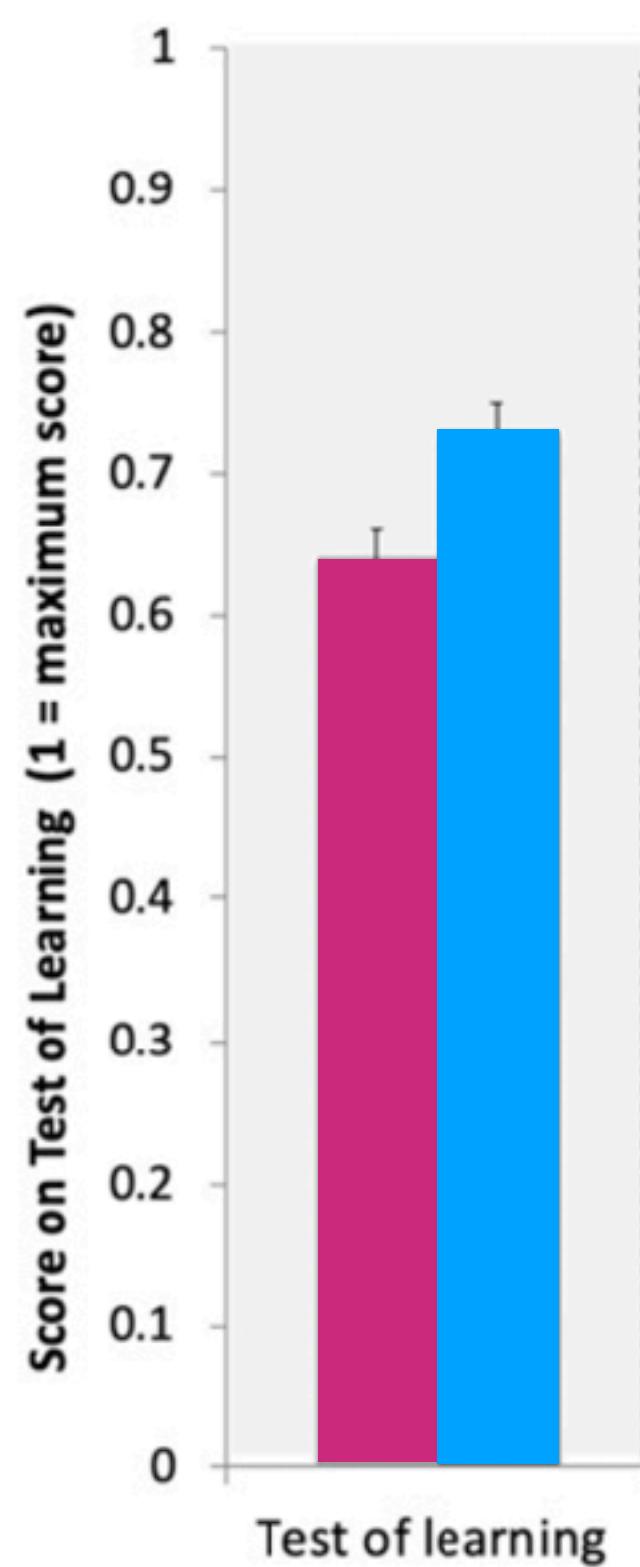
Louis Deslauriers<sup>a,1</sup>, Logan S. McCarty<sup>a,b</sup>, Kelly Miller<sup>c</sup>, Kristina Callaghan<sup>a</sup>, and Greg Kestin<sup>a</sup>

<sup>a</sup>Department of Physics, Harvard University, Cambridge, MA 02138; <sup>b</sup>Department of Chemistry and Chemical Biology, Harvard University, Cambridge, MA 02138; and <sup>c</sup>School of Engineering and Applied Sciences, Harvard University, Cambridge, MA 02138

## “Feeling” of Learning



## “Test” of Learning



# Twilight of the Lecture: Peer Instruction for Active Learning

- Dr. Eric Mazur

**campus**

**sense-making**

**instructor-led  
synchronous  
peer instruction**

**home**

**information  
transfer**

**self-paced  
asynchronous  
pre-class reading**

# Mid-course Feedback Results

Continue	My response
using intuitive easy-to-use platforms like Ed Discussion, PrairieLearn, Course Website.	<i>Glad you like them, I love them!!</i>
building and encouraging the excellent community on Ed Discussion, it's very helpful	<i>I am so proud of all of you helping each other on Ed Discussion! This is what learning is all about :-)</i>
asking students for feedback and acting on it.	<i>Thanks for recognizing this! This is my M.O.</i>
using learning logs to reflect on the week's content.	<i>I love learning Logs too, and reading your responses weekly.</i>
Energy and enthusiasm in class!	<i>Thank you! I love having students in class again!!</i>
Music before and during class!	

# Changes moving forward...

- **Full worked solutions posted after class (Started in Week 5)**
- **Adjustment to Learning Logs**
  - Question 2 will not be required (though I still encourage you to do it)
- **Review HW problems in class**
  - In Tutorials, I will ask Ishanka and Siddharth to do a quick poll before every tutorial and spend 5 minutes with the strategy on one HW problem
  - In class, I will **try** to give some hints on one HW problem (may not happen every week)

# Changes moving forward...

- **More opportunities for 1:1 help:** Three hours of additional time/week on Zoom
- Siddharth (TA): Tuesdays 3:00 - 4:30 PM on Zoom
- Ishanka (TA): Thursdays 2:00 - 3:30 on Zoom

## Contact Us

Team Member	Pronounce		
	as	Contact	Student Hours
Dr. Firas Moosvi (he/his/him); Instructor	Fur-az Moose-vee	Contact via <a href="#">Ed Discussion</a>	Wednesdays and Fridays 3:30-4:00 PM and 5:00 - 5:30 in COM 201
Siddharth Perera	<a href="#">Pronunciation</a>	Contact via <a href="#">Ed Discussion</a>	Tuesdays 3:00 - 4:30 on Zoom
Ishanka Banerjee	<a href="#">Pronunciation</a>	Contact via <a href="#">Ed Discussion</a>	Thursdays 2:00 - 3:30 on Zoom
Skyler Alderson	<a href="#">Pronunciation</a>	Contact via <a href="#">Ed Discussion</a>	N/A

# Monday's Class

**6.1 Solving problems with Newton's Laws**

**6.2 Friction**

**Preface****▼ Mechanics**

- ▶ 1 Units and Measurement
- ▶ 2 Vectors
- ▶ 3 Motion Along a Straight Line
- ▶ 4 Motion in Two and Three Dimensions
- ▶ 5 Newton's Laws of Motion
- ▶ 6 Applications of Newton's Laws
  - Introduction**
    - 6.1 Solving Problems with Newton's Laws
    - 6.2 Friction
    - 6.3 Centripetal Force
    - 6.4 Drag Force and Terminal Speed
  - ▶ Chapter Review
- ▶ 7 Work and Kinetic Energy
- ▶ 8 Potential Energy and Conservation of Energy
- ▶ 9 Linear Momentum and Collisions
- ▶ 10 Fixed-Axis Rotation
- ▶ 11 Angular Momentum
- ▶ 12 Static Equilibrium and Elasticity



**Figure 6.1** Stock cars racing in the Grand National Divisional race at Iowa Speedway in May, 2015. Cars often reach speeds of 200 mph (320 km/h).  
(credit: modification of work by Erik Schneider/U.S. Navy)

## Chapter Outline

- [6.1 Solving Problems with Newton's Laws](#)
- [6.2 Friction](#)
- [6.3 Centripetal Force](#)
- [6.4 Drag Force and Terminal Speed](#)

Car racing has grown in popularity in recent years. As each car moves in a curved path around the turn, its wheels also spin rapidly. The wheels complete many revolutions while the car makes only part of one (a circular arc). How



## Physics 111

Search this book...

Unsyllabus

### ABOUT THIS COURSE

- Course Syllabus (Official)
- Course Schedule
- Accommodations
- How to do well in this course

### GETTING STARTED

- Before the Term starts
- After the first class
- In the first week
- Week 1 - Introductions!

### PART 1 - KINEMATICS

- Week 2 - Chapter 2
- Week 3 - Chapter 3
- Week 4 - Chapter 4

### PART 2 - DYNAMICS

- Week 5 - Chapter 5
- Week 6 - Week Off !!

### Week 7 - Chapter 6

- Readings
- Videos**
- Homework
- Tutorial

## Friction

Friction: Crash Course Physics #6

Copy link

Watch on YouTube

- Video 2
- Video 3
- Video 4
- Video 5
- Video 6
- Video 7
- Video 8
- Video 9
- Video 10
- Video 11
- Video 12

## Required Videos

### 1. Introduction to Equilibrium

Introduction to Equilibrium

Copy link

# Applications of Newton's Laws

- Before the break, we discussed Newton's Three Laws, the concept of a "Free Body Diagram", and splitting forces into its vector components.
- This week, we will look at solving some physics problems with those concepts!
- It's important to note that there is no "new physics" this week! All of the problems we solve will just be applying Newton's Laws in different contexts

# Components of Forces

$$\sum F_{net,x} = ma_x$$

$$\sum F_{net,y} = ma_y$$

No matter how complex the problem seems,  
this always holds true!

## CQ7.0A - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

*Elevator at rest*

$$\vec{a} = 0$$

$$\vec{v} = 0$$



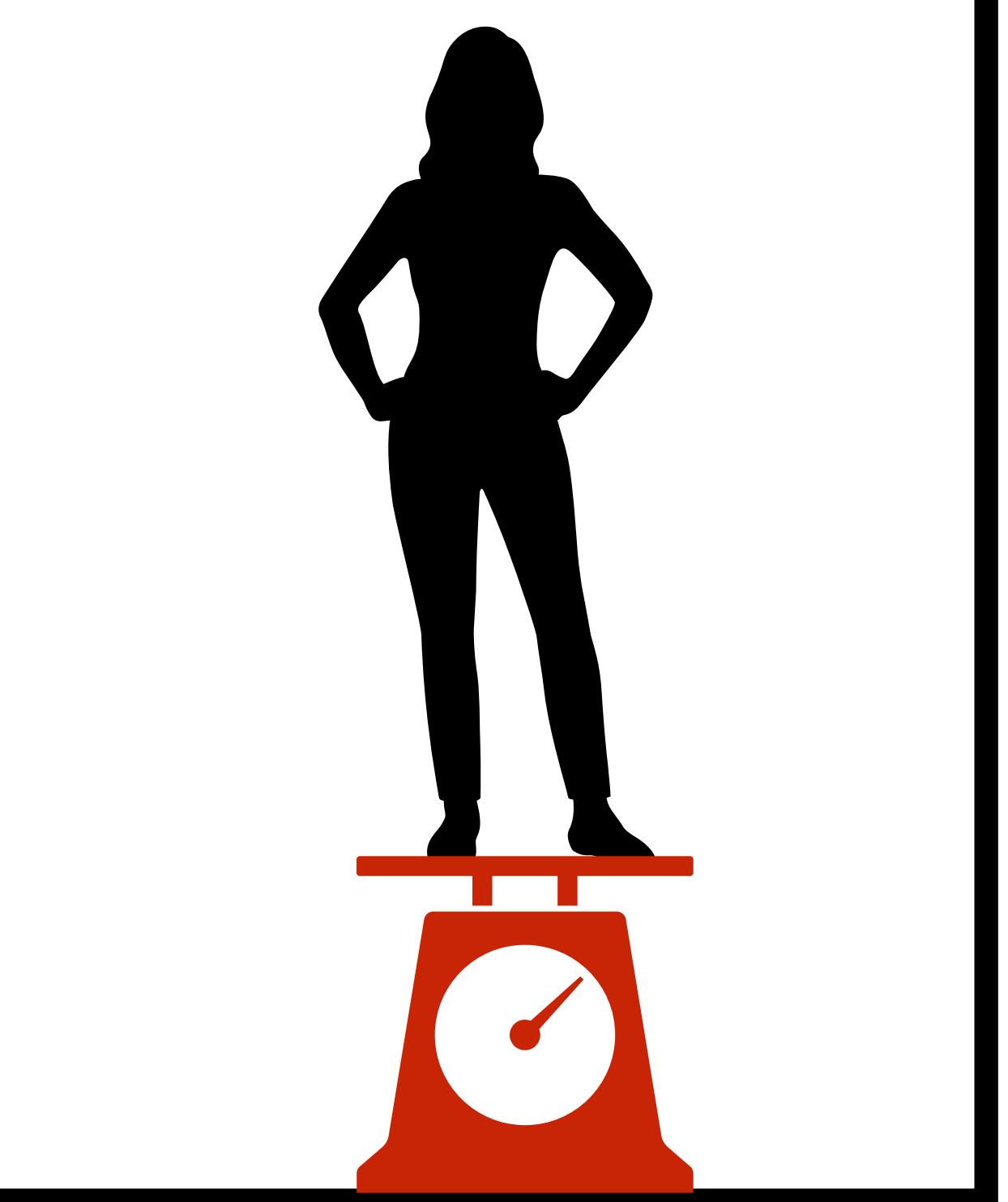
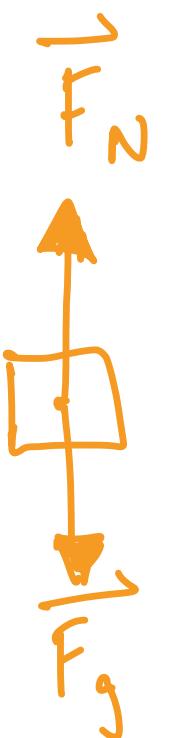
## CQ7.0A - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

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- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

$$\begin{aligned}\sum \vec{F}_y &= \vec{F}_N - \vec{F}_g = m\vec{a}_y \\ m\vec{a}_y &= \vec{F}_N - \vec{F}_g \\ \vec{F}_N &= m\vec{a}_y + m\vec{g} \\ \boxed{\vec{F}_N = m(a_y + g)} \\ a_y &= 0\end{aligned}$$



*Elevator at rest*

$$\vec{a} = 0$$
$$\vec{v} = 0$$

## CQ7.0B - Classic Elevator Problems

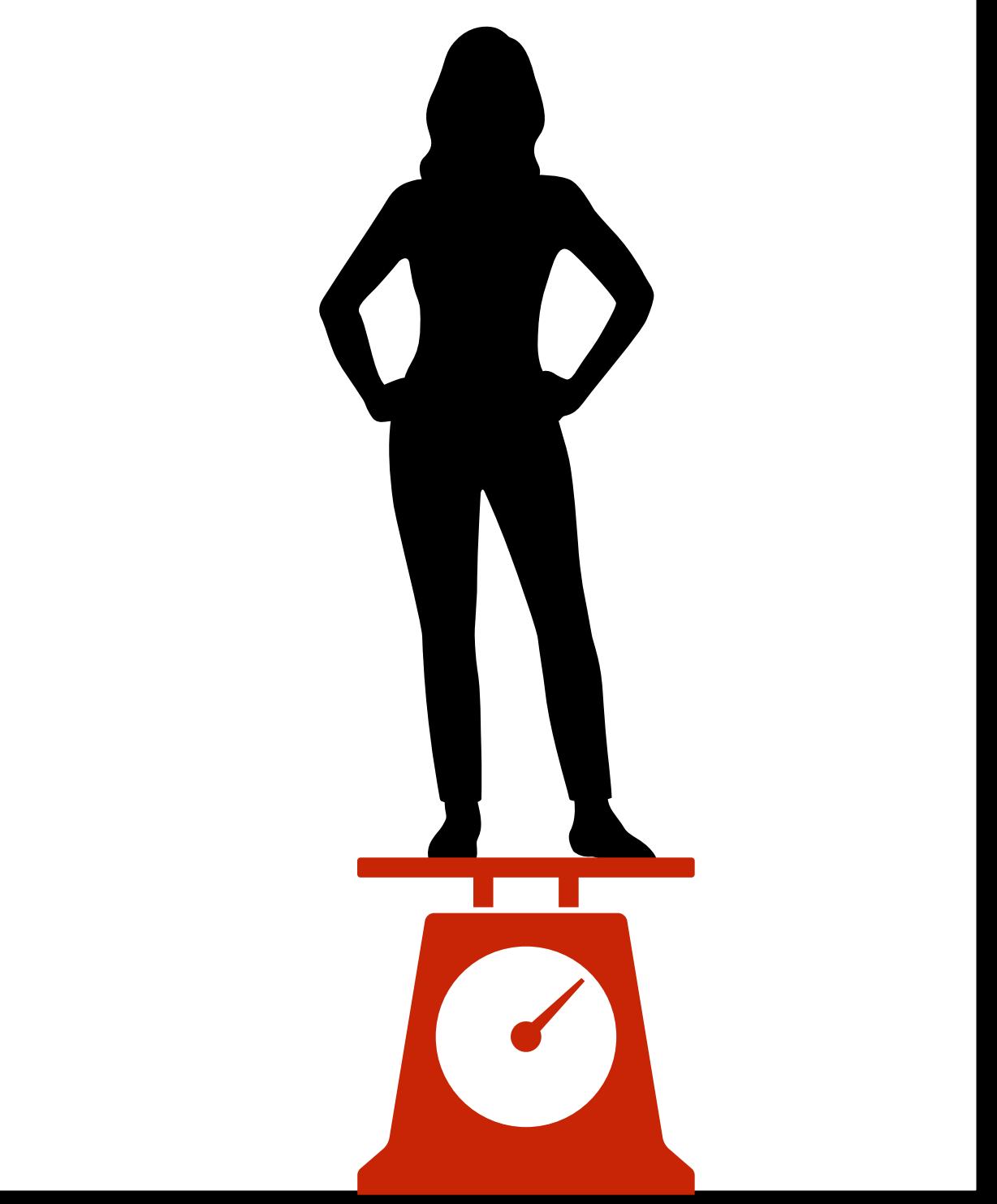
A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

Elevator moving up  
 $\vec{a} = 0$

$\vec{v} = 3\text{m/s}$



## CQ7.0B - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

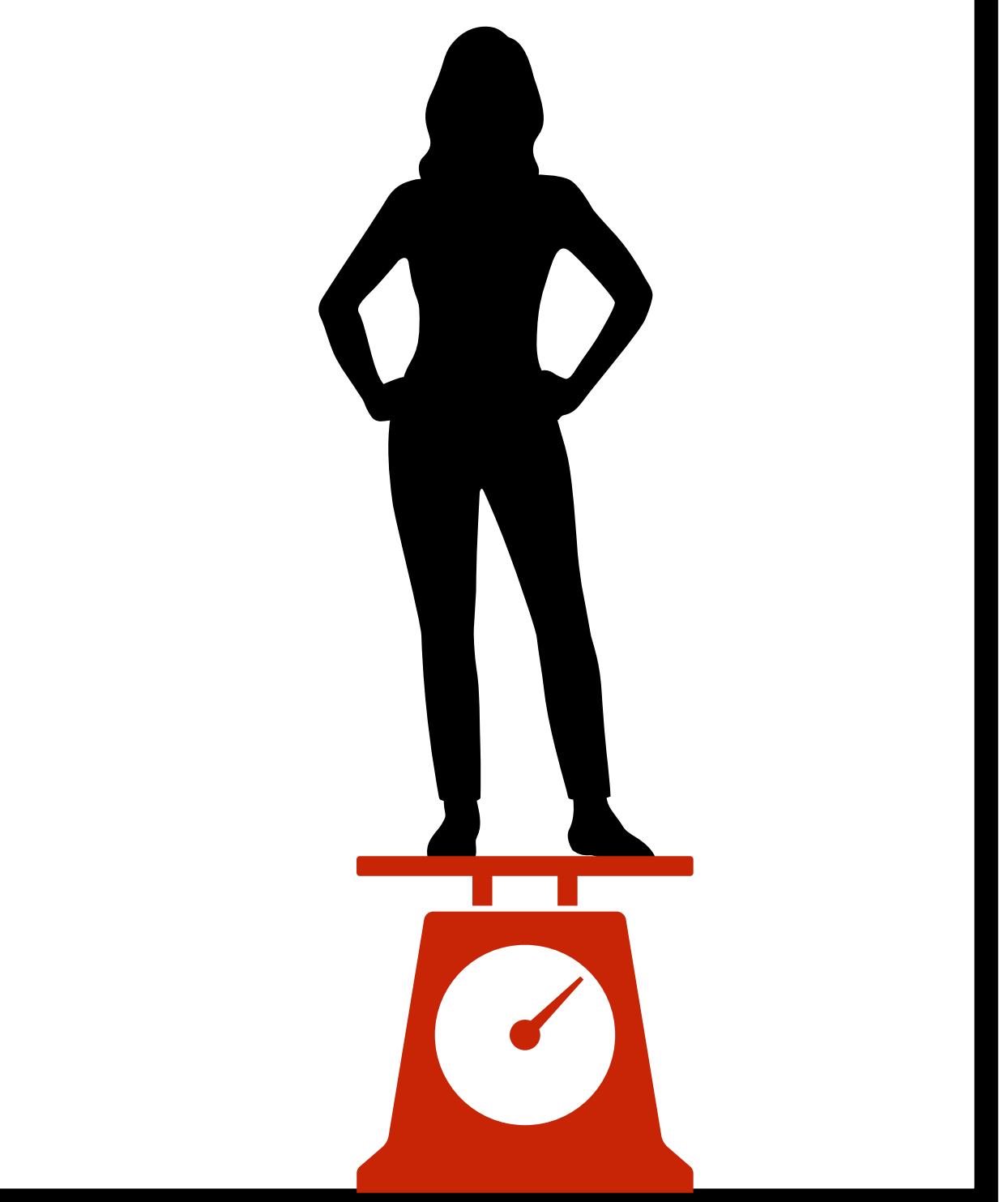
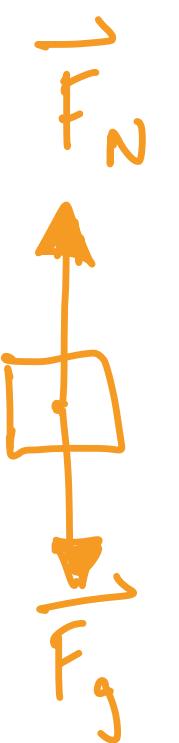
$$\sum \vec{F}_y = \vec{F}_N - \vec{F}_g = m\vec{a}_y$$

$$m\vec{a}_y = \vec{F}_N - \vec{F}_g$$

$$\vec{F}_N = m\vec{a}_y + \vec{F}_g$$

$$\boxed{\vec{F}_N = m(a_y + g)}$$

$$a_y = 0$$



## CQ7.0C - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

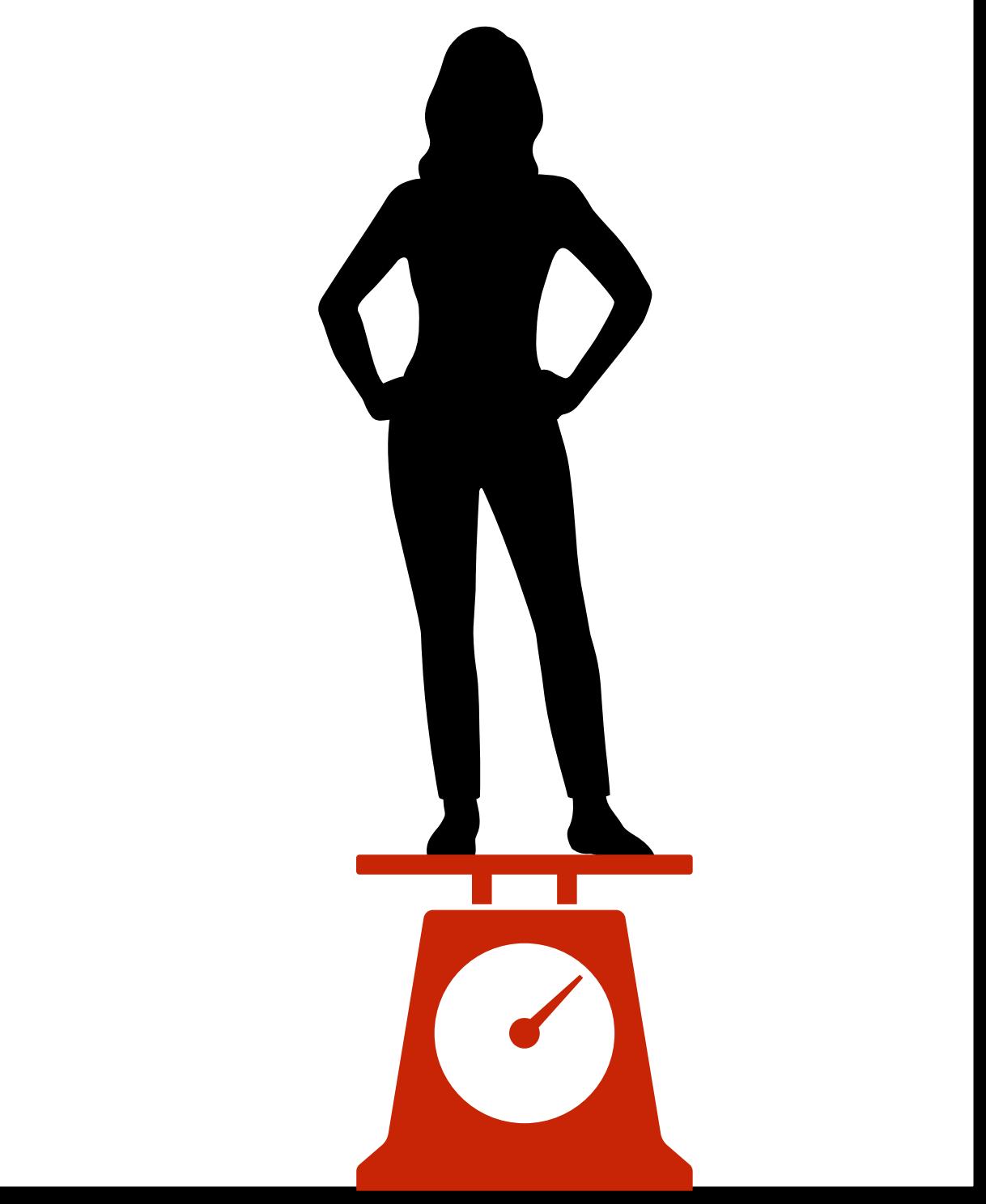
What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

*Elevator accelerating UP*

$$\vec{a} = 2 \text{ m/s}^2$$

$$\vec{v} = \text{variable}$$



## CQ7.0C - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

A) 720 N

B) 600 N

C) 480 N

D) 400 N

E) 0 N

F) I don't know

Elevator accelerating UP

$$\vec{a} = 2 \text{ m/s}^2$$

$$\vec{v} = \text{variable}$$

$$\sum \vec{F}_y = \vec{F}_N - \vec{F}_g = m\vec{a}_y$$

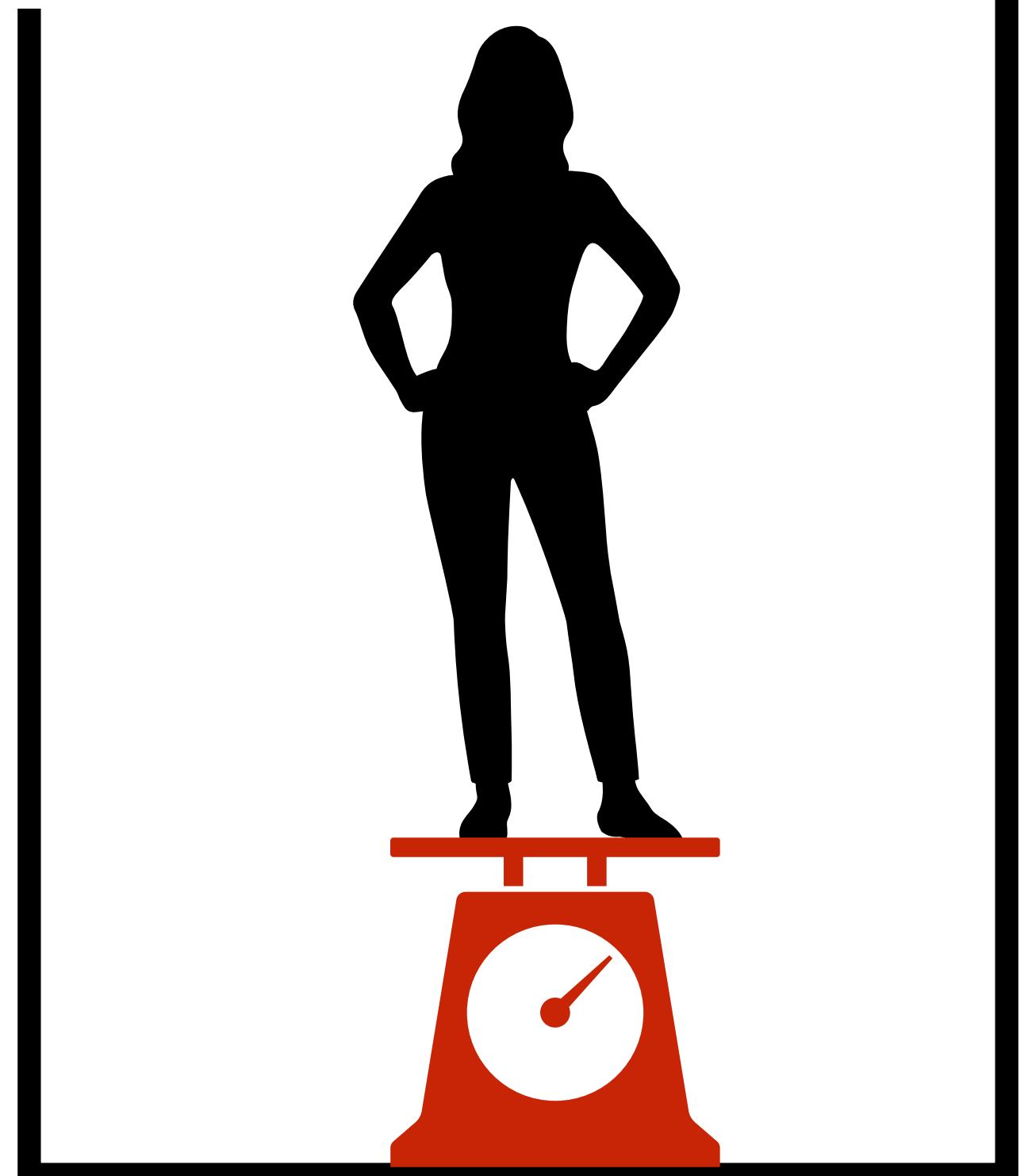
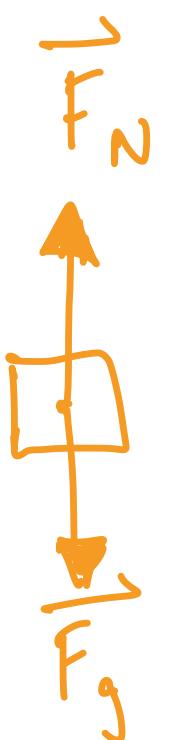
$$m\vec{a}_y = \vec{F}_N - \vec{F}_g$$

$$\vec{F}_N = m\vec{a}_y + m\vec{g}$$

$$\boxed{\vec{F}_N = m(a_y + g)}$$

$$a_y = 2 \text{ m/s}^2$$

$$g = 10 \text{ m/s}^2$$



## CQ7.0D - Classic Elevator Problems

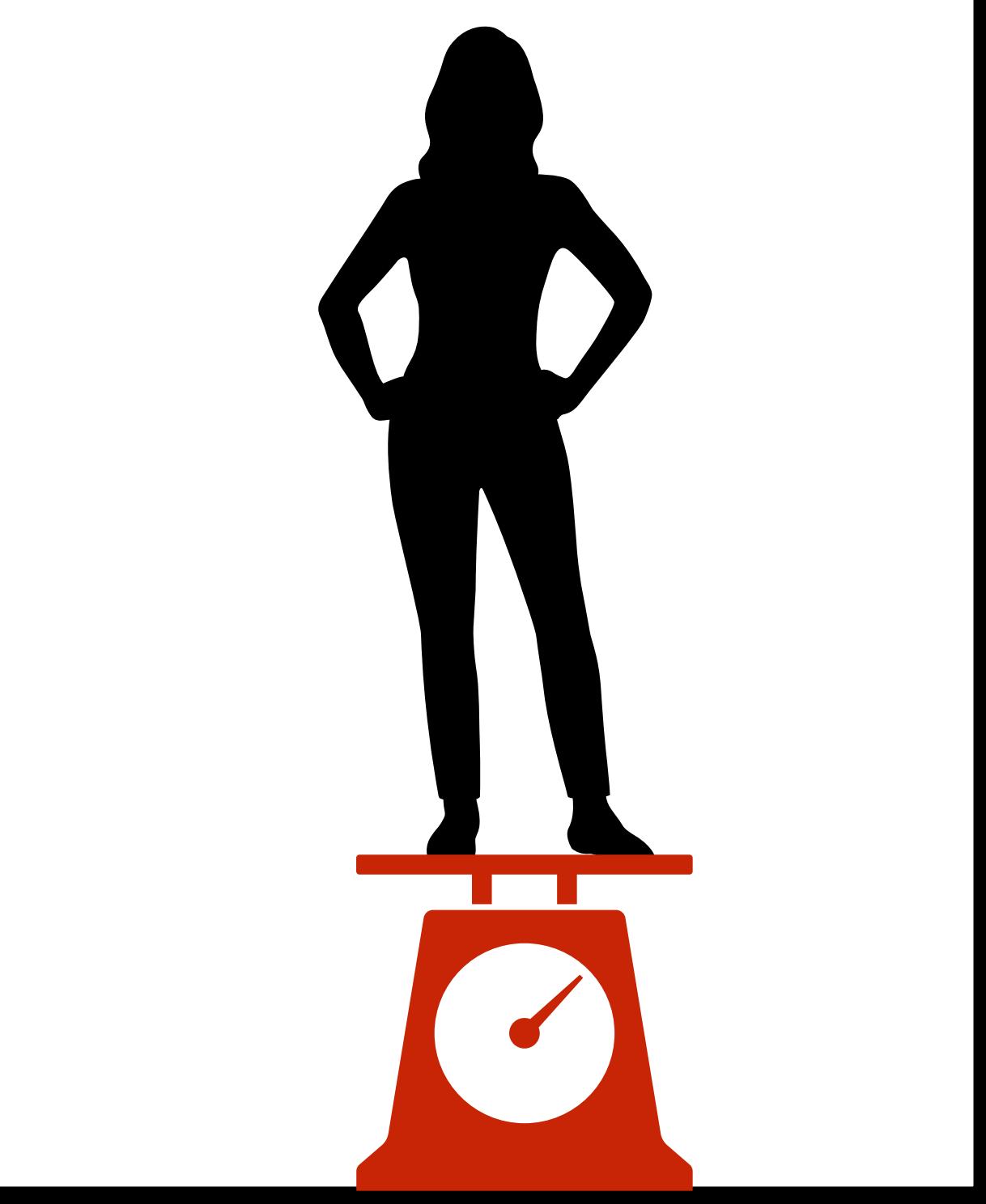
A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know

*Elevator accelerating down*

$$\vec{a} = 2\text{m/s}^2$$
$$\vec{v} = \text{variable}$$



## CQ7.0D - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

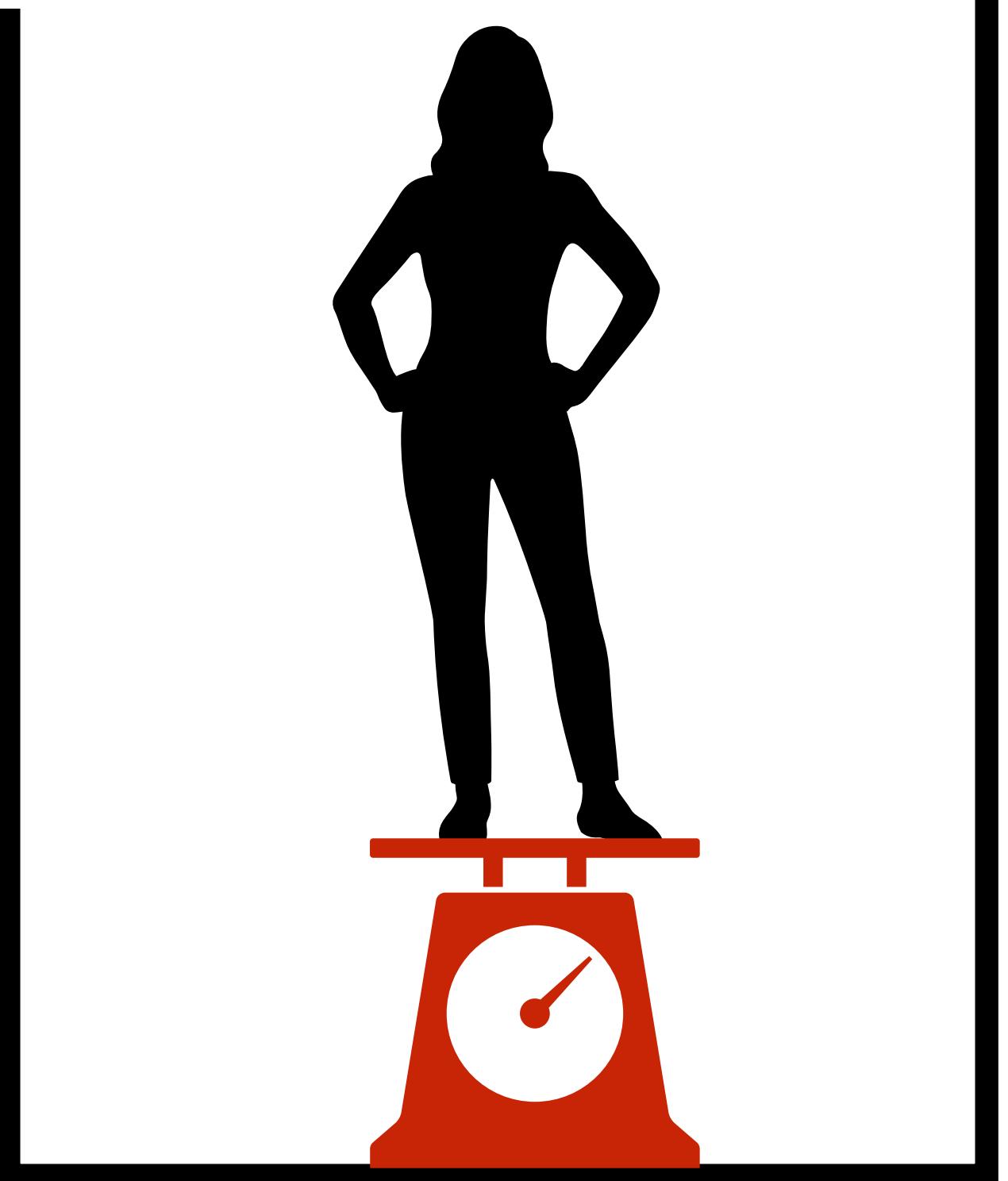
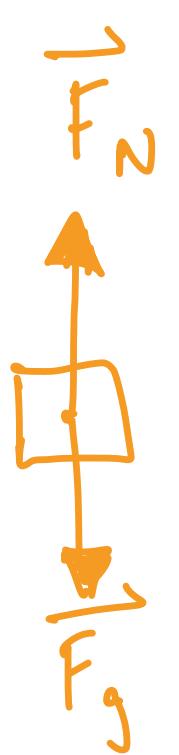
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Elevator accelerating down

$$\begin{aligned} \vec{a} &= 2\text{m/s}^2 \\ \vec{v} &= \text{variable} \end{aligned}$$

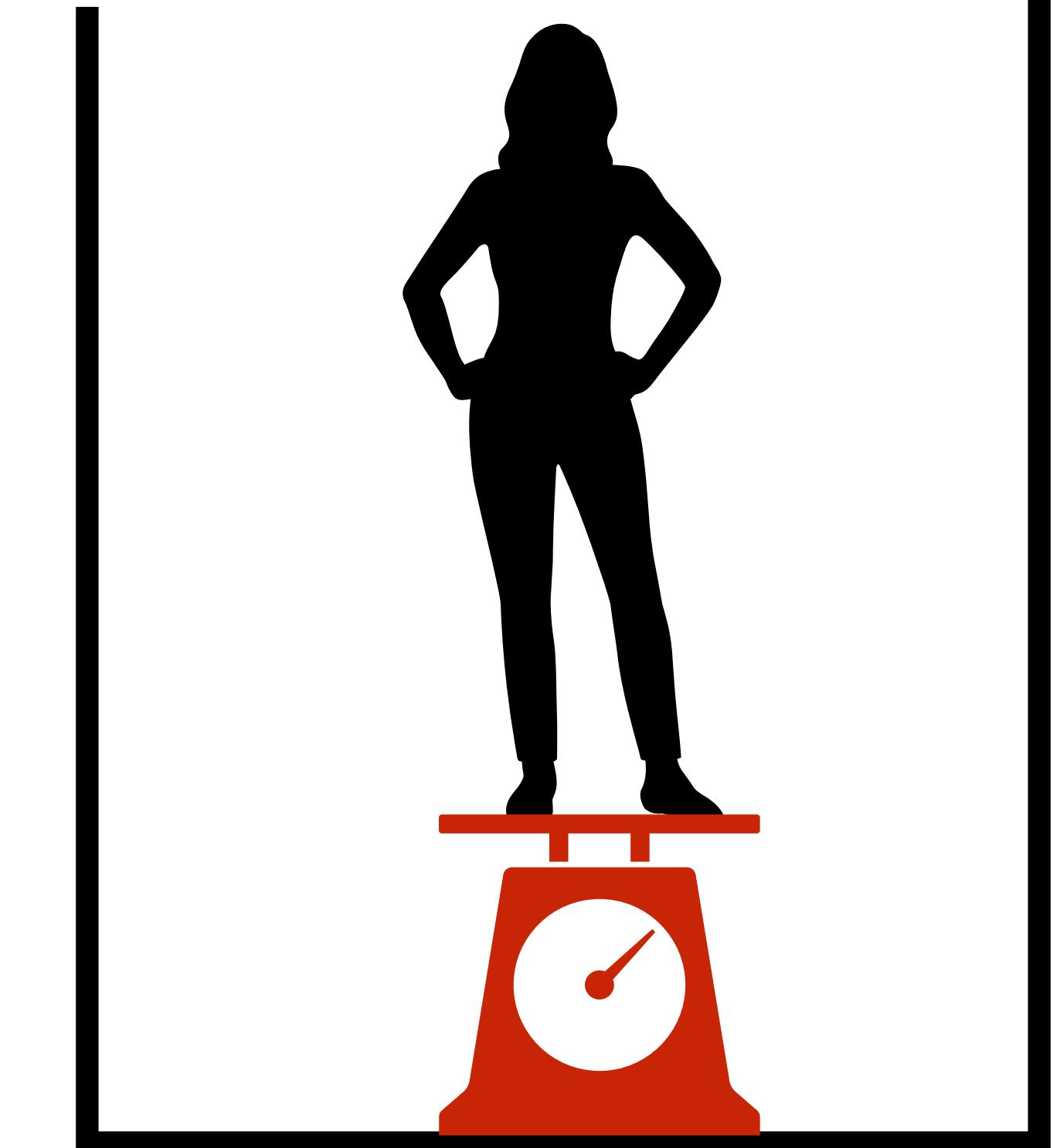


## CQ7.0E - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

- A) 720 N
- B) 600 N
- C) 480 N
- D) 400 N
- E) 0 N
- F) I don't know



*Elevator cable is cut!*

$$\vec{a} = ?(\text{pain})$$

$$\vec{v} = ?(\text{fast})$$

## CQ7.0E - Classic Elevator Problems

A person is standing in an elevator on top of a weighing scale. The person has a mass of 60kg. Assume  $g = 10\text{m/s}^2$

What is the reading on the scale (in N)?

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- D) 400 N
- E) 0 N
- F) I don't know

$$\begin{cases} \sum \vec{F}_y = \vec{F}_N - \vec{F}_g = m\vec{a}_y \\ m\vec{a}_y = \vec{F}_N - \vec{F}_g = \emptyset \end{cases}$$
$$\boxed{\vec{F}_N = \vec{F}_g}$$



*Elevator cable is cut!*

$$\begin{aligned} \vec{a} &= ?(\text{pain}) \\ \vec{v} &= ?(\text{fast}) \end{aligned}$$



# Textbook Examples

## EXAMPLE 6.1

Different Tensions at Different Angles

## EXAMPLE 6.2

Drag Force on a Barge

## EXAMPLE 6.3

What Does the Bathroom Scale Read in an Elevator?

## EXAMPLE 6.4

Two Attached Blocks

## EXAMPLE 6.5

Atwood Machine

## EXAMPLE 6.6

What Force Must a Soccer Player Exert to Reach Top Speed?

## EXAMPLE 6.7

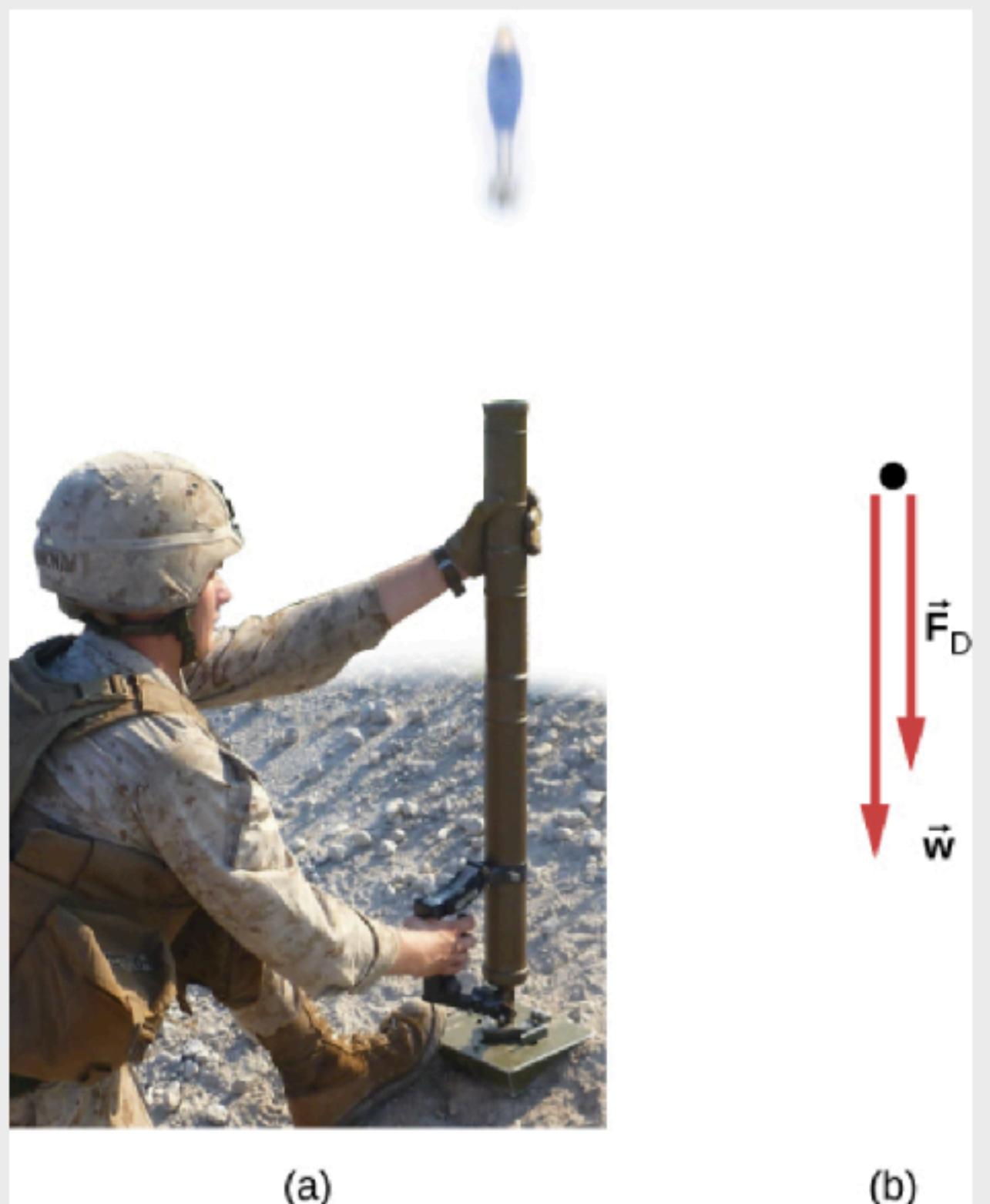
What Force Acts on a Model Helicopter?

# Textbook Examples (requires Integration)

## EXAMPLE 6.9

### Motion of a Projectile Fired Vertically

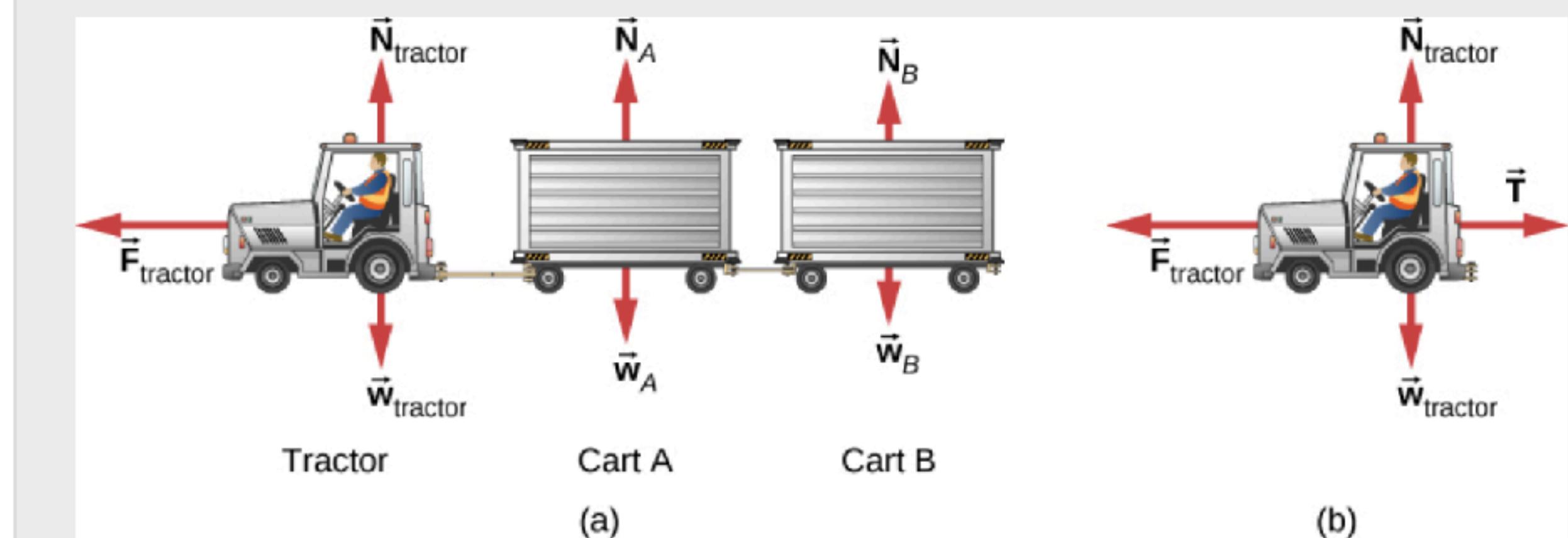
A 10.0-kg mortar shell is fired vertically upward from the ground, with an initial velocity of 50.0 m/s (see [Figure 6.9](#)). Determine the maximum height it will travel if atmospheric resistance is measured as  $F_D = (0.0100v^2) \text{ N}$ , where  $v$  is the speed at any instant.



## EXAMPLE 6.8

### Baggage Tractor

[Figure 6.8\(a\)](#) shows a baggage tractor pulling luggage carts from an airplane. The tractor has mass 650.0 kg, while cart A has mass 250.0 kg and cart B has mass 150.0 kg. The driving force acting for a brief period of time accelerates the system from rest and acts for 3.00 s. (a) If this driving force is given by  $F = (820.0t) \text{ N}$ , find the speed after 3.00 seconds. (b) What is the horizontal force acting on the connecting cable between the tractor and cart A at this instant?



**Figure 6.8** (a) A free-body diagram is shown, which indicates all the external forces on the system consisting of the tractor and baggage carts for carrying airline luggage. (b) A free-body diagram of the tractor only is shown isolated in order to calculate the tension in the cable to the carts.

# Friction

## FRICITION

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Friction is a force that opposes relative motion between systems in contact.

## STATIC AND KINETIC FRICTION

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If two systems are in contact and stationary relative to one another, then the friction between them is called **static friction**. If two systems are in contact and moving relative to one another, then the friction between them is called **kinetic friction**.

# Friction

## MAGNITUDE OF STATIC FRICTION

The magnitude of static friction  $f_s$  is

$$f_s \leq \mu_s N,$$

6.1

where  $\mu_s$  is the coefficient of static friction and  $N$  is the magnitude of the normal force.

The symbol  $\leq$  means *less than or equal to*, implying that static friction can have a maximum value of  $\mu_s N$ . Static friction is a responsive force that increases to be equal and opposite to whatever force is exerted, up to its maximum limit. Once the applied force exceeds

$f_s(\max)$ , the object moves. Thus,

$$f_s(\max) = \mu_s N.$$

## MAGNITUDE OF STATIC FRICTION

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$$f_s(\text{max}) = \mu_s N.$$

## MAGNITUDE OF KINETIC FRICTION

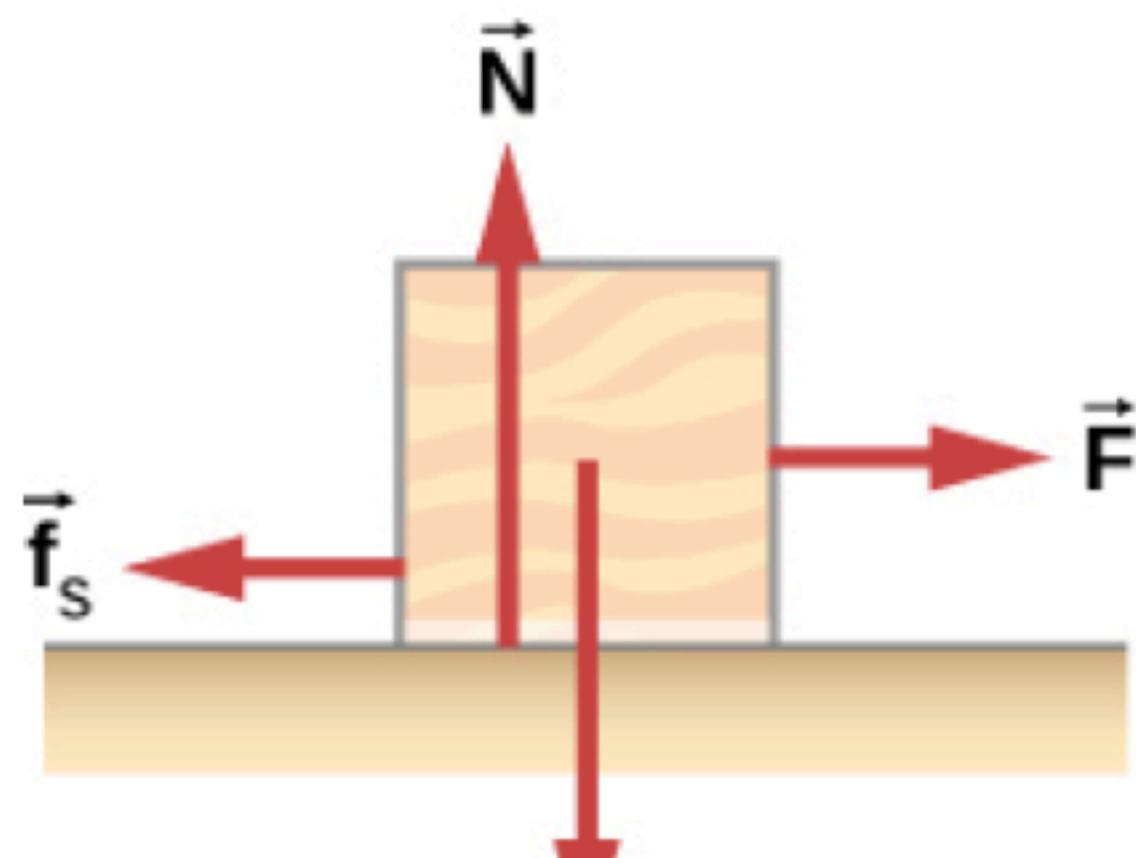
The magnitude of kinetic friction  $f_k$  is given by

$$f_k = \mu_k N,$$

6.2

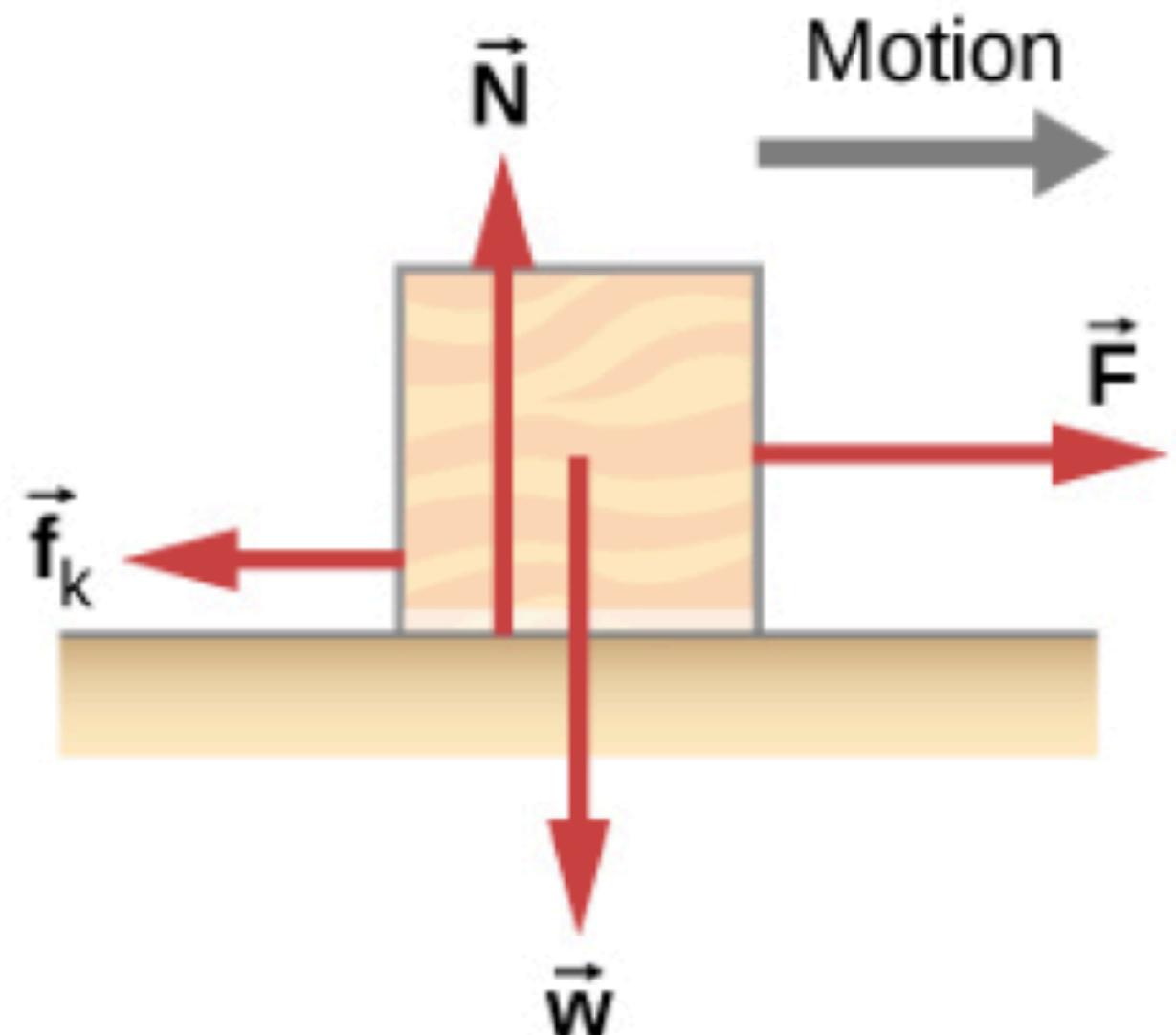
where  $\mu_k$  is the coefficient of kinetic friction.

# Friction



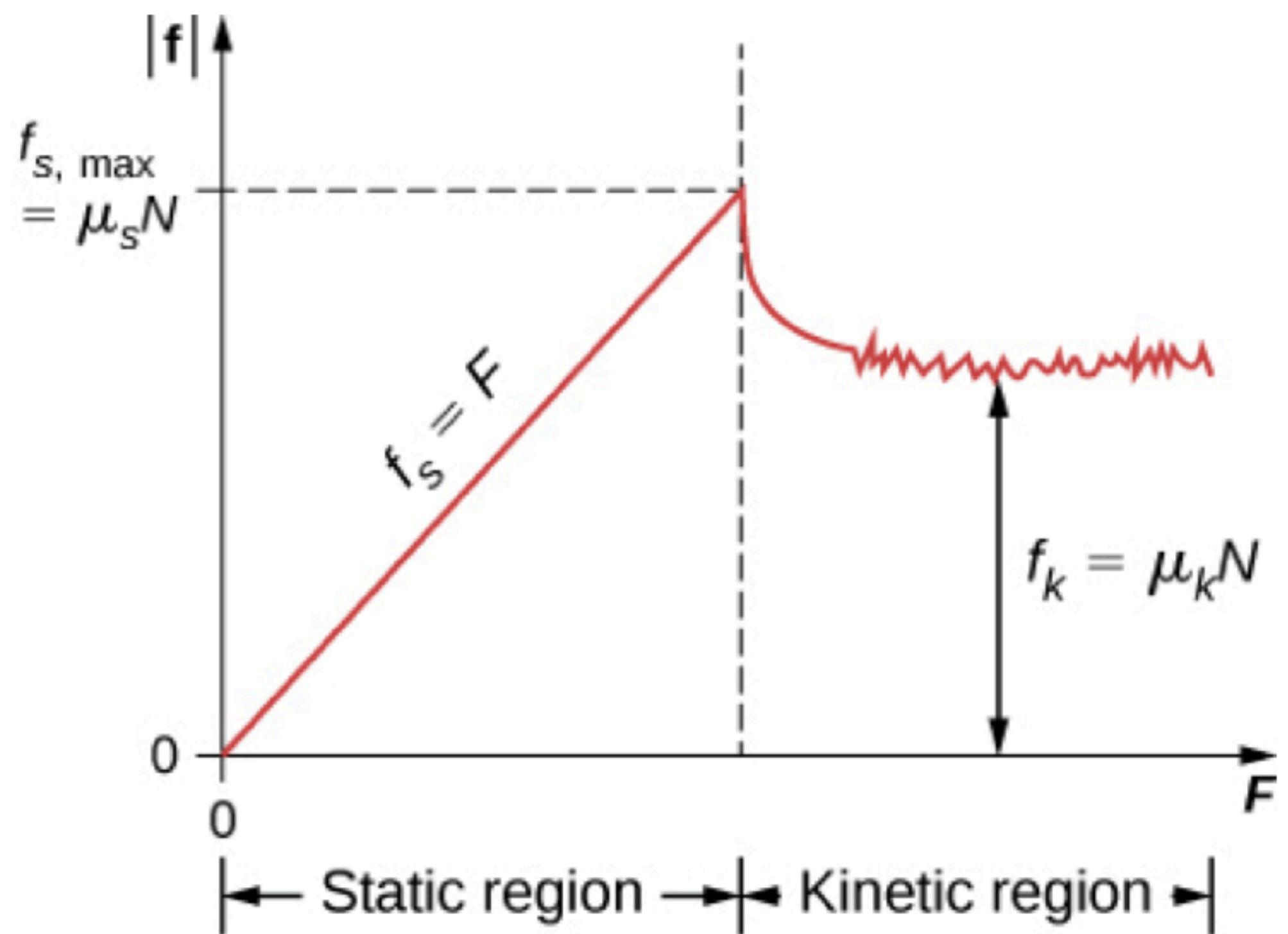
(a)

Impending motion



(b)

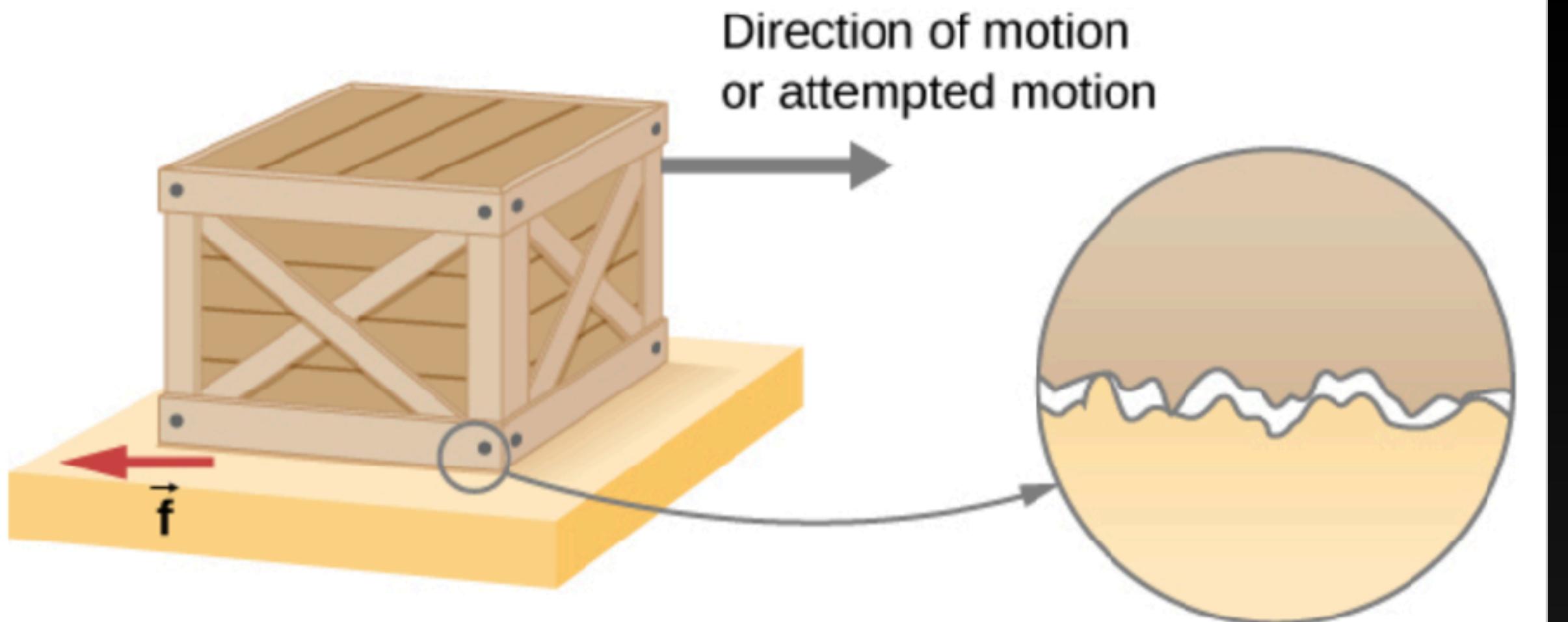
Object moves



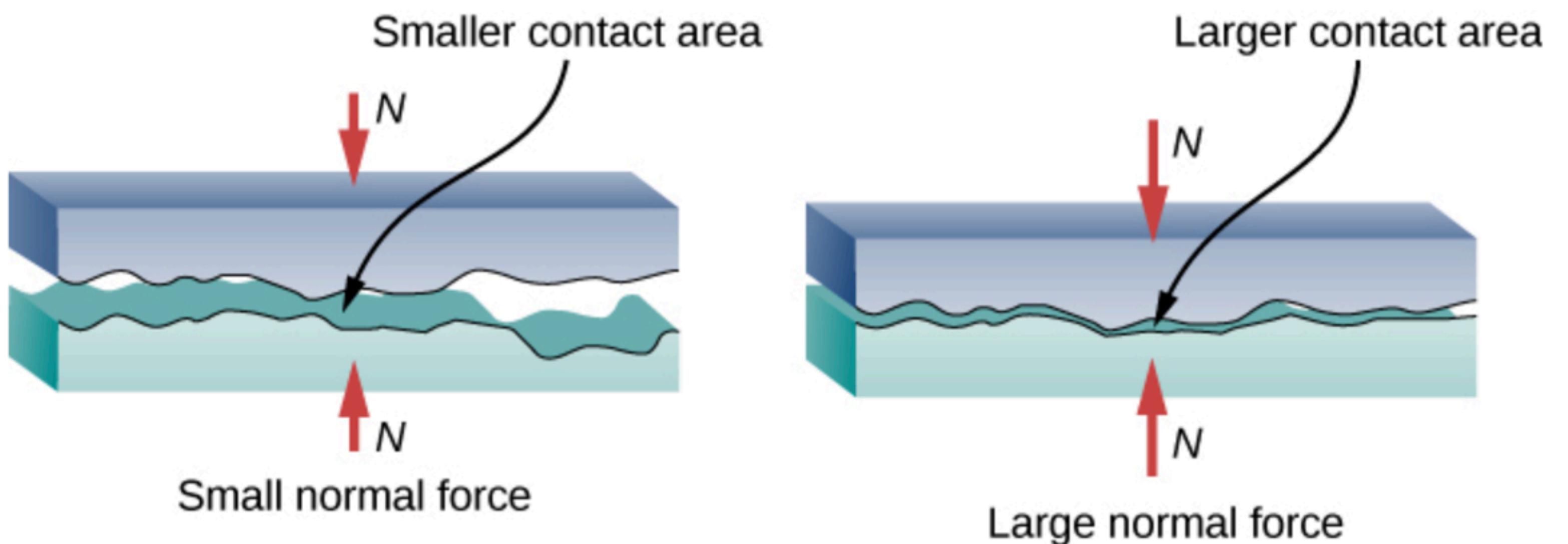
(c)

**Figure 6.11** (a) The force of friction  $\vec{f}$  between the block and the rough surface opposes the direction of the applied force  $\vec{F}$ . The magnitude of the static friction balances that of the applied force. This is shown in the left side of the graph in (c). (b) At some point, the magnitude of the applied force is greater than the force of kinetic friction, and the block moves to the right. This is shown in the right side of the graph. (c) The graph of the frictional force versus the applied force; note that  $f_s(\text{max}) > f_k$ . This means that  $\mu_s > \mu_k$ .

# Friction



**Figure 6.10** Frictional forces, such as  $\vec{f}$ , always oppose motion or attempted motion between objects in contact. Friction arises in part because of the roughness of the surfaces in contact, as seen in the expanded view. For the object to move, it must rise to where the peaks of the top surface can skip along the bottom surface. Thus, a force is required just to set the object in motion. Some of the peaks will be broken off, also requiring a force to maintain motion. Much of the friction is actually due to attractive forces between molecules making up the two objects, so that even perfectly smooth surfaces are not friction-free. (In fact, perfectly smooth, clean surfaces of similar materials would adhere, forming a bond called a “cold weld.”)



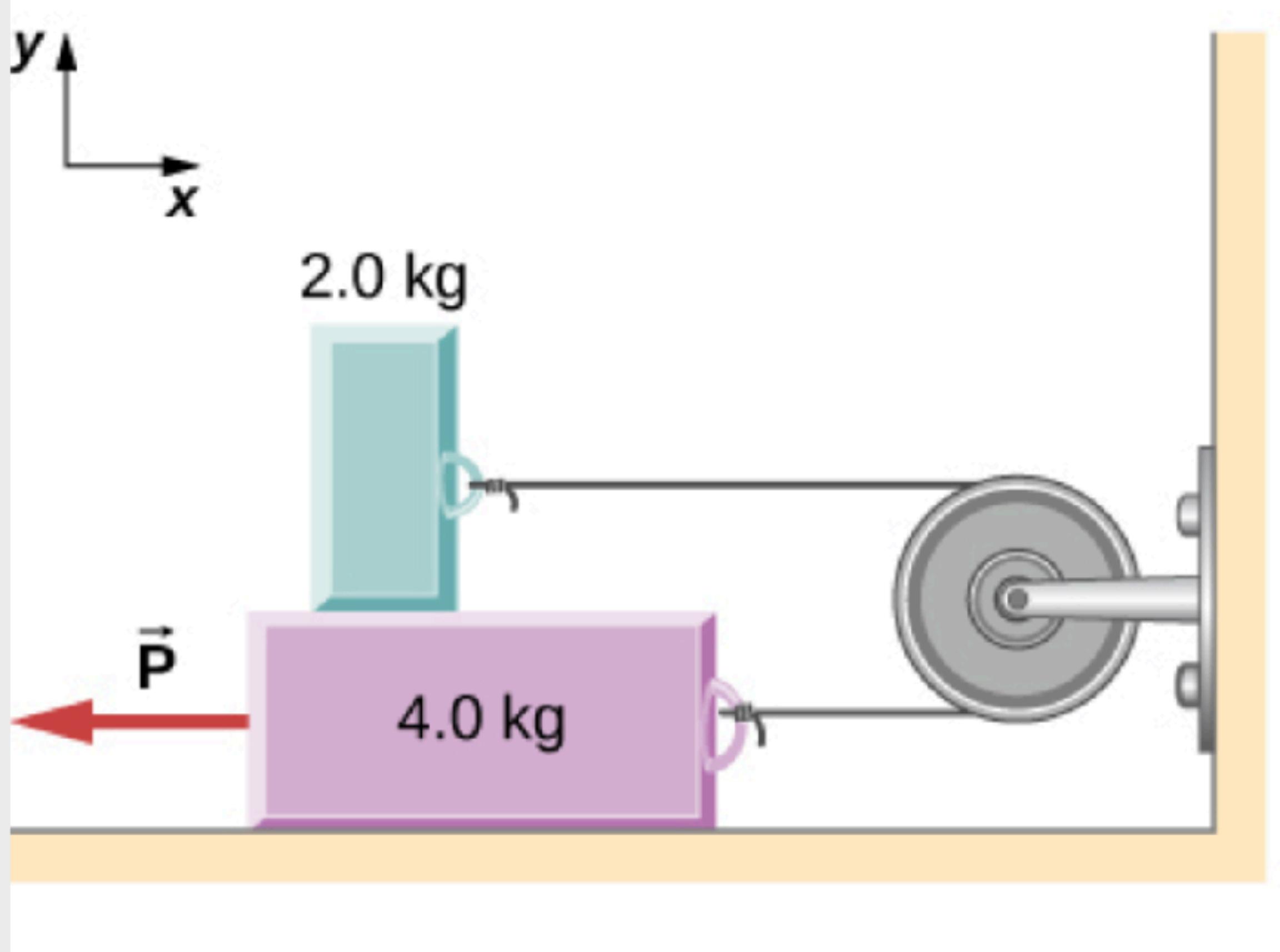
**Figure 6.15** Two rough surfaces in contact have a much smaller area of actual contact than their total area. When the normal force is larger as a result of a larger applied force, the area of actual contact increases, as does friction.

# Friction

## EXAMPLE 6.12

### Sliding Blocks

The two blocks of [Figure 6.17](#) are attached to each other by a massless string that is wrapped around a frictionless pulley. When the bottom 4.00-kg block is pulled to the left by the constant force  $\vec{P}$ , the top 2.00-kg block slides across it to the right. Find the magnitude of the force necessary to move the blocks at constant speed. Assume that the coefficient of kinetic friction between all surfaces is 0.400.

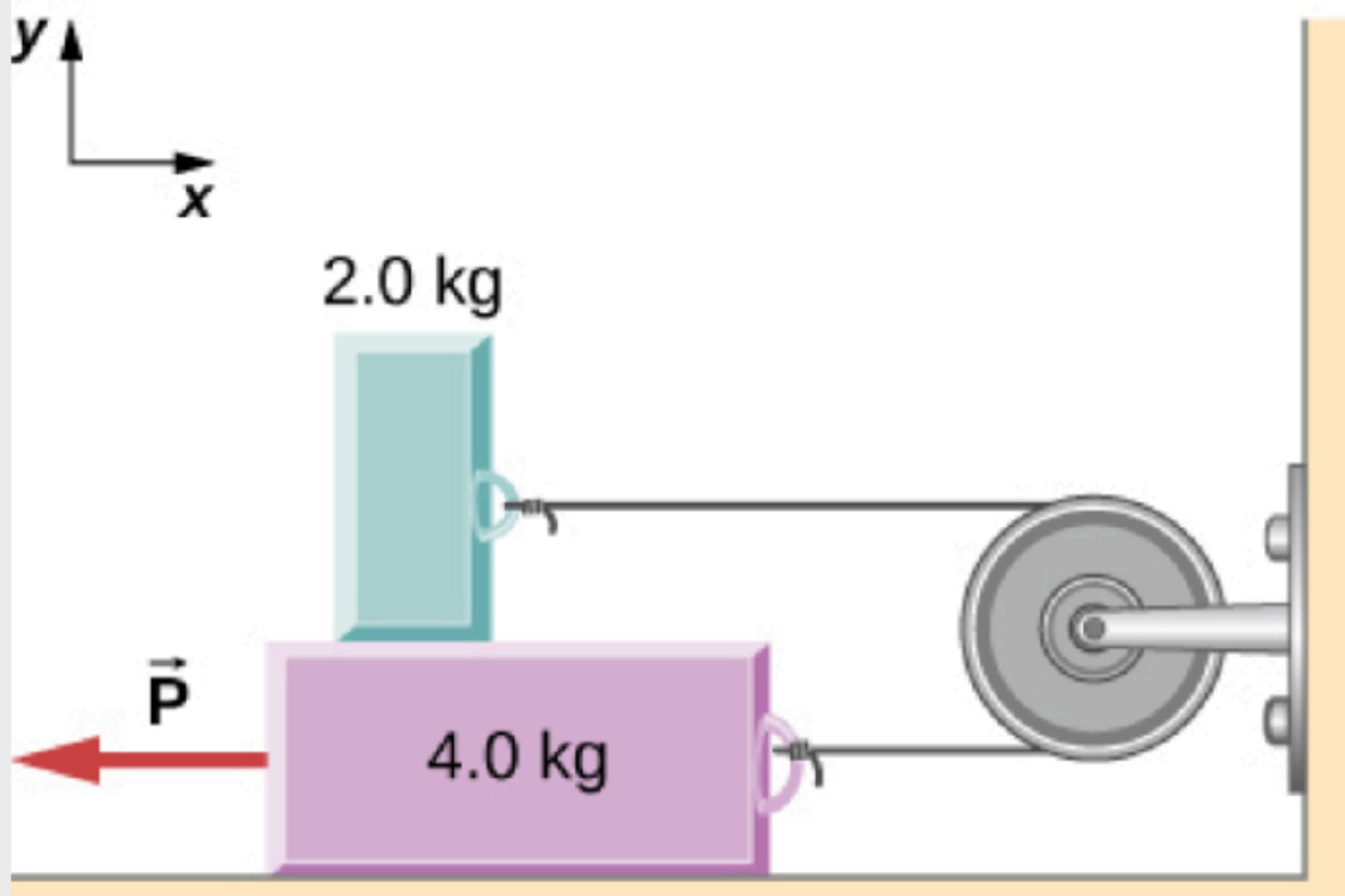


# Friction

## EXAMPLE 6.12

### Sliding Blocks

The two blocks of Figure 6.17 are attached to each other by a massless string that is wrapped around a frictionless pulley. When the bottom 4.00-kg block is pulled to the left by the constant force  $\vec{P}$ , the top 2.00-kg block slides across it to the right. Find the magnitude of the force necessary to move the blocks at constant speed. Assume that the coefficient of kinetic friction between all surfaces is 0.400.



### Strategy

We analyze the motions of the two blocks separately. The top block is subjected to a contact force exerted by the bottom block. The components of this force are the normal force  $N_1$  and the frictional force  $-0.400N_1$ . Other forces on the top block are the tension  $T_1$  in the string and the weight of the top block itself, 19.6 N. The bottom block is subjected to contact forces due to the top block and due to the floor. The first contact force has components  $-N_1$  and  $0.400N_1$ , which are simply reaction forces to the contact forces that the bottom block exerts on the top block. The components of the contact force of the floor are  $N_2$  and  $0.400N_2$ . Other forces on this block are  $-P$ , the tension  $T_1$ , and the weight -39.2 N.

### Solution

Since the top block is moving horizontally to the right at constant velocity, its acceleration is zero in both the horizontal and the vertical directions. From Newton's second law,

$$\begin{aligned}\sum F_x &= m_1 a_x & \sum F_y &= m_1 a_y \\ T - 0.400N_1 &= 0 & N_1 - 19.6 \text{ N} &= 0.\end{aligned}$$

Solving for the two unknowns, we obtain  $N_1 = 19.6 \text{ N}$  and  $T = 0.40N_1 = 7.84 \text{ N}$ . The bottom block is also not accelerating, so the application of Newton's second law to this block gives

$$\begin{aligned}\sum F_x &= m_2 a_x & \sum F_y &= m_2 a_y \\ T - P + 0.400N_1 + 0.400N_2 &= 0 & N_2 - 39.2 \text{ N} - N_1 &= 0.\end{aligned}$$

The values of  $N_1$  and  $T$  were found with the first set of equations. When these values are substituted into the second set of equations, we can determine  $N_2$  and  $P$ . They are

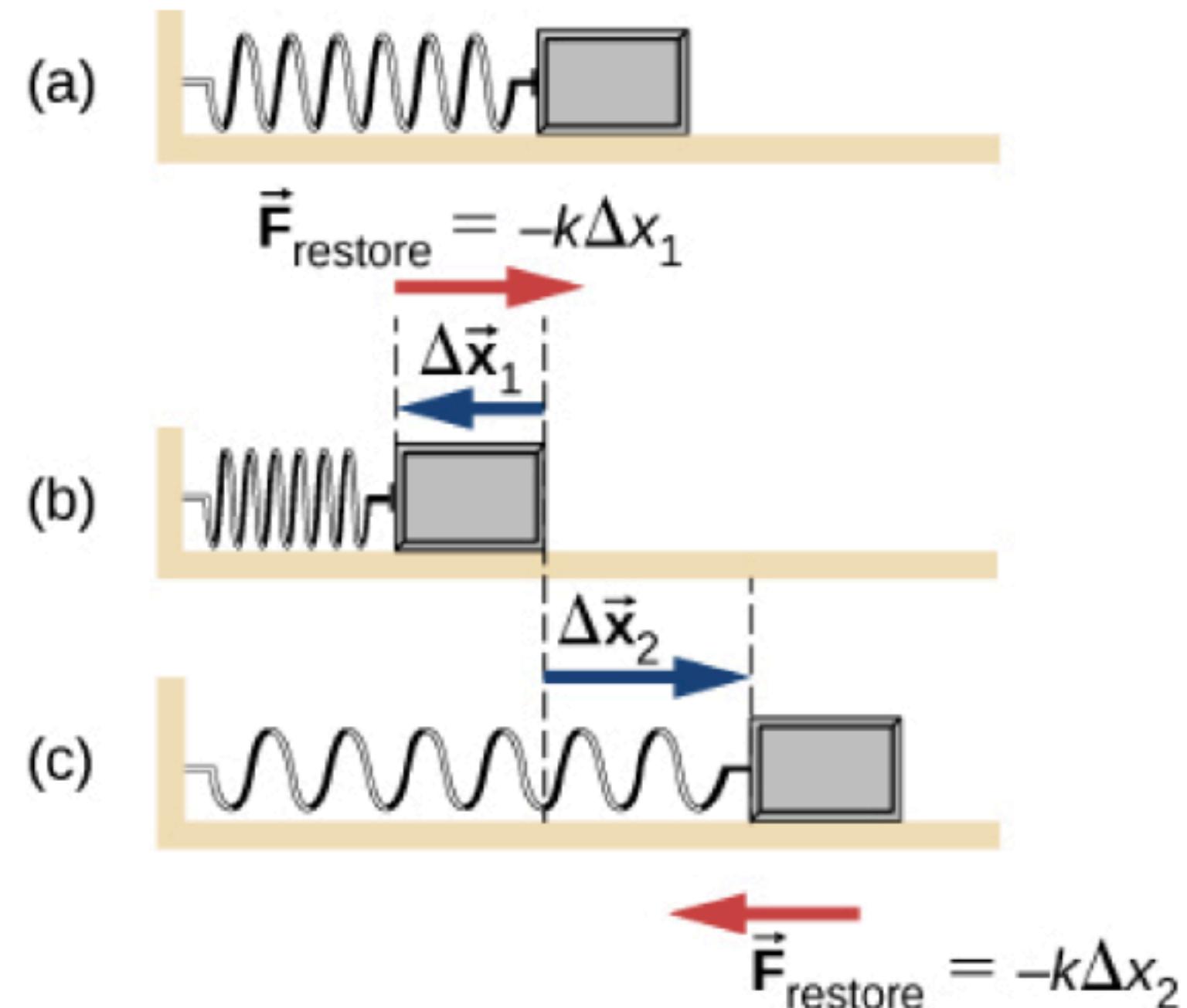
$$N_2 = 58.8 \text{ N} \text{ and } P = 39.2 \text{ N}.$$

## Spring force

A spring is a special medium with a specific atomic structure that has the ability to restore its shape, if deformed. To restore its shape, a spring exerts a restoring force that is proportional to and in the opposite direction in which it is stretched or compressed. This is the statement of a law known as Hooke's law, which has the mathematical form

$$\vec{F} = -k\vec{x}.$$

The constant of proportionality  $k$  is a measure of the spring's stiffness. The line of action of this force is parallel to the spring axis, and the sense of the force is in the opposite direction of the displacement vector ([Figure 5.29](#)). The displacement must be measured from the relaxed position;  $x = 0$  when the spring is relaxed.



**Figure 5.29** A spring exerts its force proportional to a displacement, whether it is compressed or stretched. (a) The spring is in a relaxed position and exerts no force on the block. (b) The spring is compressed by displacement  $\Delta\vec{x}_1$  of the object and exerts restoring force  $-k\Delta\vec{x}_1$ . (c) The spring is stretched by displacement  $\Delta\vec{x}_2$  of the object and exerts restoring force  $-k\Delta\vec{x}_2$ .

# Spring Force

# Key Equations

Magnitude of static friction

$$f_s \leq \mu_s N$$

Magnitude of kinetic friction

$$f_k = \mu_k N$$

Centripetal force

$$F_c = m \frac{v^2}{r} \text{ or } F_c = mr\omega^2$$

Ideal angle of a banked curve

$$\tan \theta = \frac{v^2}{rg}$$

Drag force

$$F_D = \frac{1}{2} C \rho A v^2$$

Stokes' law

$$F_s = 6\pi r \eta v$$

# Clicker Questions

# CQ.7.1

A 1100-kg car pulls a boat on a trailer.

**What total frictional force resists the motion of the car, boat, and trailer, if the car exerts a 1900-N force on the road and produces an acceleration of  $0.550 \text{ m/s}^2$ ? The mass of the boat plus trailer is 700kg.**

a) 1300 N

b) 1900 N

c) 1520 N

d) 910 N

A

B

C

D

E

# CQ.7.1

A 1100-kg car pulls a boat on a trailer.

**What total frictional force resists the motion of the car, boat, and trailer, if the car exerts a 1900-N force on the road and produces an acceleration of  $0.550 \text{ m/s}^2$ ? The mass of the boat plus trailer is 700 kg.**

a) 1300 N

b) 1900 N

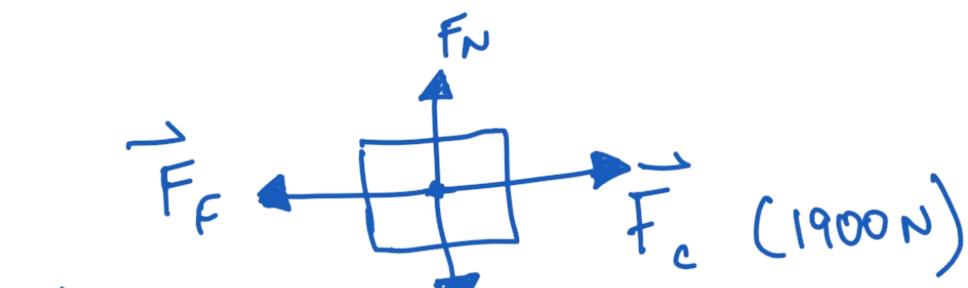
c) 1520 N

✓ d) 910 N

$$M_T = 700 \text{ kg} \quad m_c = 1100 \text{ kg}$$



Car exerts a force of 1900 N on the road, road exerts a force 1900N on the car. This is the force the trailer (+boat) is pulled at. Let's treat everything as one "object".



$$\vec{F}_{NETx} = \vec{F}_c - \vec{F}_F$$

$$M \cdot a_x = \vec{F}_c - \vec{F}_F$$

$$\vec{F}_F = \vec{F}_c - M \cdot a_x$$

$$= 1900 \text{ N} - (1100 + 700) \cdot 0.550 \text{ m/s}^2$$

$$|F_F| = 910 \text{ N} \quad \text{to the left}$$

A

B

C

D

E

# CQ.7.2

A flea jumps by exerting a force of  $1.20 \times 10^{-5}$  N straight down on the ground. A breeze blowing on the flea parallel to the ground exerts a force of  $0.500 \times 10^{-6}$  N on the flea. Find the direction and magnitude of the acceleration of the flea if its mass is  $6.00 \times 10^{-7}$  kg. Do not neglect the gravitational force.

- a)  $20.0 \text{ m/s}^2$ ,  $2.39^\circ$  from vertical
- b)  $10.2 \text{ m/s}^2$ ,  $2.39^\circ$  above horizontal
- c)  $10.2 \text{ m/s}^2$ ,  $4.67^\circ$  from vertical
- d)  $20.0 \text{ m/s}^2$ ,  $4.67^\circ$  from vertical

A

B

C

D

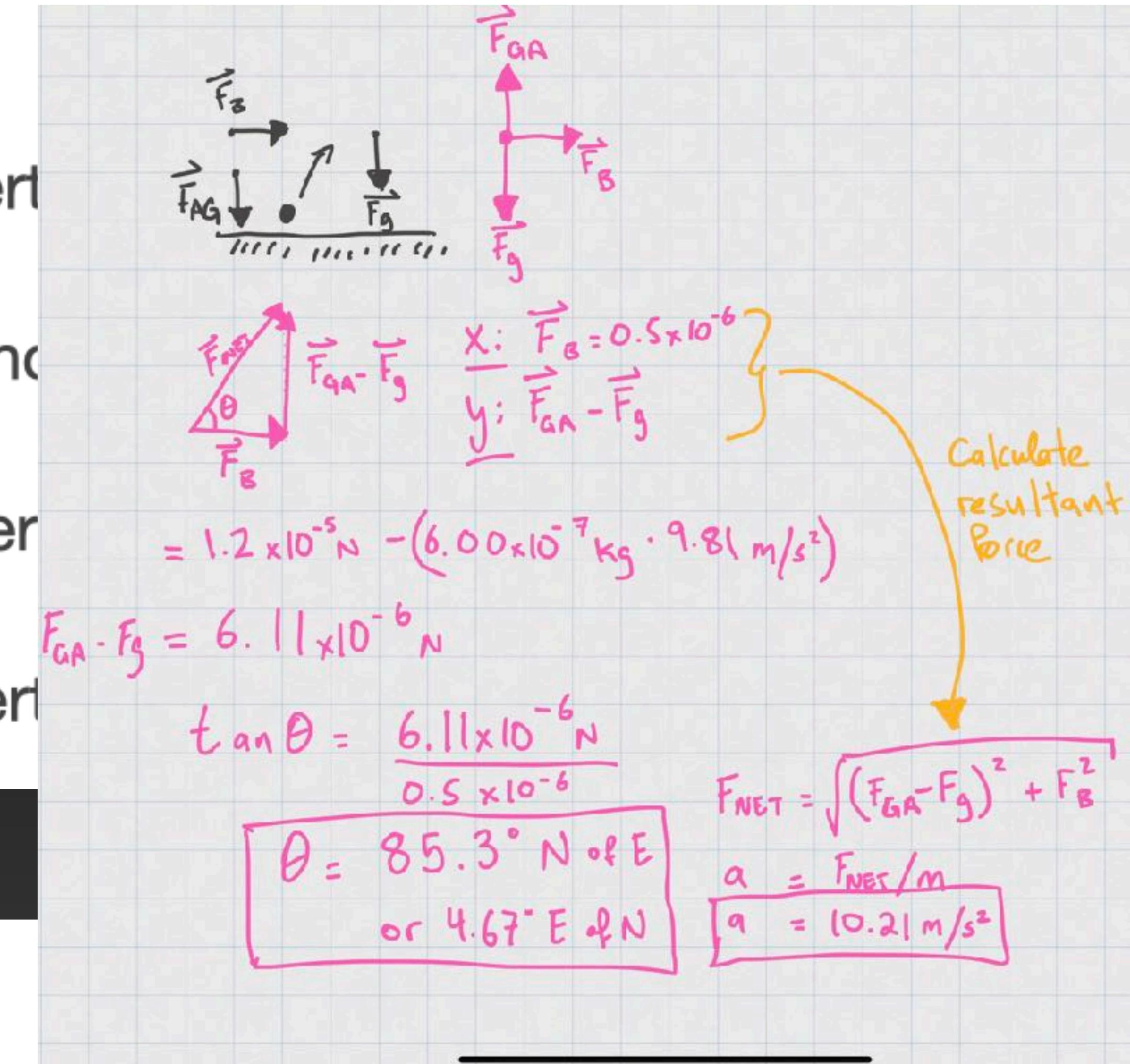
E

# CQ.7.2

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- a)  $20.0 \text{ m/s}^2$ ,  $2.39^\circ$  from vertical
- b)  $10.2 \text{ m/s}^2$ ,  $2.39^\circ$  above horizontal
- c)  $10.2 \text{ m/s}^2$ ,  $4.67^\circ$  from vertical
- d)  $20.0 \text{ m/s}^2$ ,  $4.67^\circ$  from vertical

**A      B      C      D      E**



# CQ.7.3

A skier with a mass of 67 kg is skiing down a snowy slope with an incline of  $37^\circ$ . Find the friction if the coefficient of kinetic friction ( $\mu_k$ ) is 0.07. (Take Earth's gravity as  $9.8 \text{ m/s}^2$ )

a) 27.7 N

b) 34.7 N

c) 36.7 N

d) 46.0 N

A

B

C

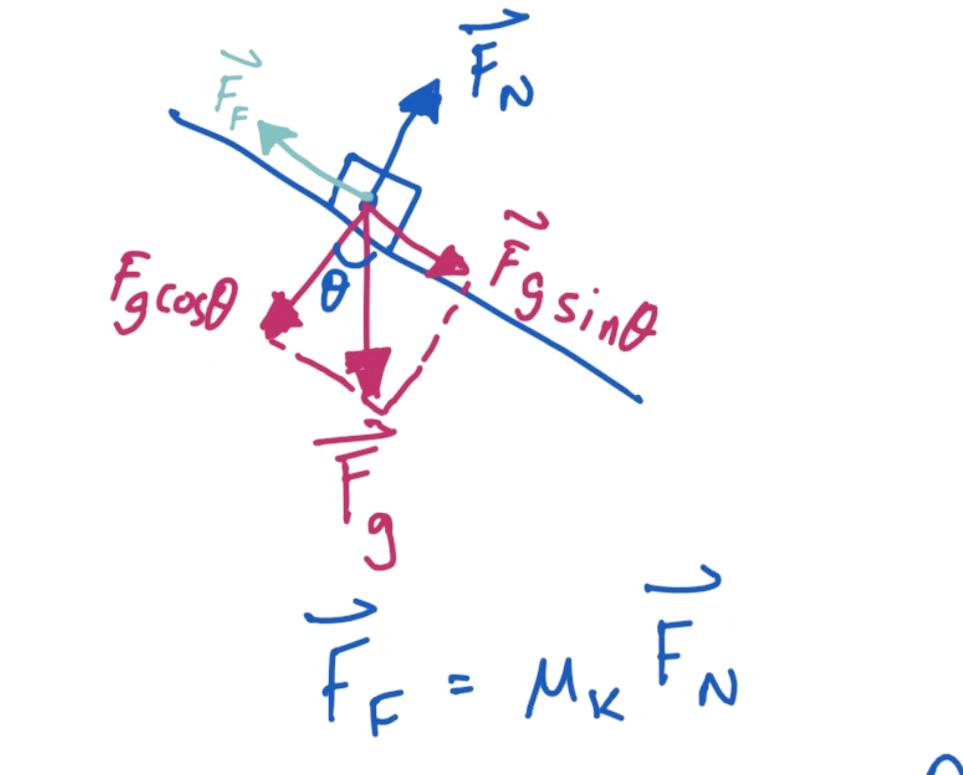
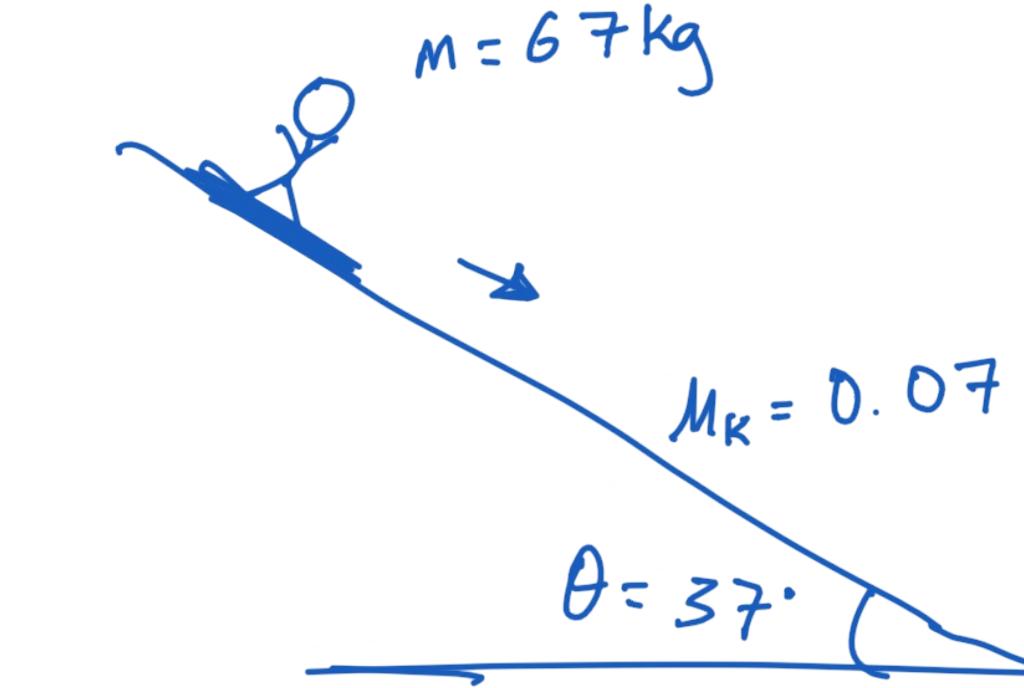
D

E

# CQ.7.3

A skier with a mass of 67 kg is skiing down a snowy slope with an incline of  $37^\circ$ . Find the friction if the coefficient of kinetic friction ( $\mu_k$ ) is 0.07. (Take Earth's gravity as  $9.8 \text{ m/s}^2$ )

- a) 27.7 N
- b) 34.7 N
- c) 36.7 N
- d) 46.0 N



to :  $\vec{F}_{NET} = 0 = \vec{F}_N - \vec{F}_g \cos \theta$

Down Ramp :  $\vec{F}_{NET} = \vec{F}_g \sin \theta - \vec{F}_F$   
 $Ma = mg \sin \theta - \mu_k mg \cos \theta$

$$\boxed{\vec{F}_F = 36.7 \text{ N}}$$

To get acceleration 'a', apply Newton's second law.

Detailed solution:  $f_k = \mu_k mg \cos \theta = 36.7 \text{ N}$

A

B

C

D

E

# CQ.7.4

Two springs are attached to two hooks. Spring A has a greater force constant than spring B. Equal weights are suspended from both. Which of the following statements is true?

- a) Spring A will have more extension than spring B.
- b) Spring B will have more extension than spring A.
- c) Both springs will have same extension.
- d) Both springs are equally stiff.

A

B

C

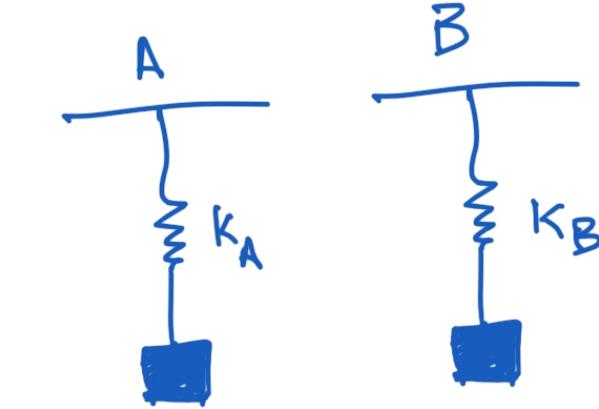
D

E

# CQ.7.4

Two springs are attached to two hooks. Spring A has a greater force constant than spring B. Equal weights are suspended from both. Which of the following statements is true?

- a) Spring A will have more extension than spring B.
- b) Spring B will have more extension than spring A.
- c) Both springs will have same extension.
- d) Both springs are equally stiff.



$k_A > k_B$ , so from Hooke's Law:

$$\text{In equilibrium, } \vec{F}_{\text{NETY}} = 0$$

$$\vec{F}_g - \vec{F}_R = 0$$

$$mg + k\Delta x = 0$$

$$\boxed{\Delta x = -\frac{mg}{k}}$$

Inversely proportional relationship, so  
 $\Delta x_B > \Delta x_A$  if  
 $k_A > k_B$ !

**Detailed solution:** The greater the force constant, the stiffer the spring. Therefore, spring B will have more extension than spring A.

A

B

C

D

E

# CQ.7.5

A team of six dogs pulls a sled with waxed wood runners on wet snow ( $\mu_k = 0.08$ ). The loaded sled with its rider has a mass of 210 kg.

If each dog exerts an average force of 35 N applied force, what is the acceleration of the sled? (Take Earth's gravity as  $9.8 \text{ m/s}^2$ )

- a)  $0.22 \text{ m/s}^2$
- b)  $0.46 \text{ m/s}^2$
- c)  $0.78 \text{ m/s}^2$
- d)  $1.00 \text{ m/s}^2$

A

B

C

D

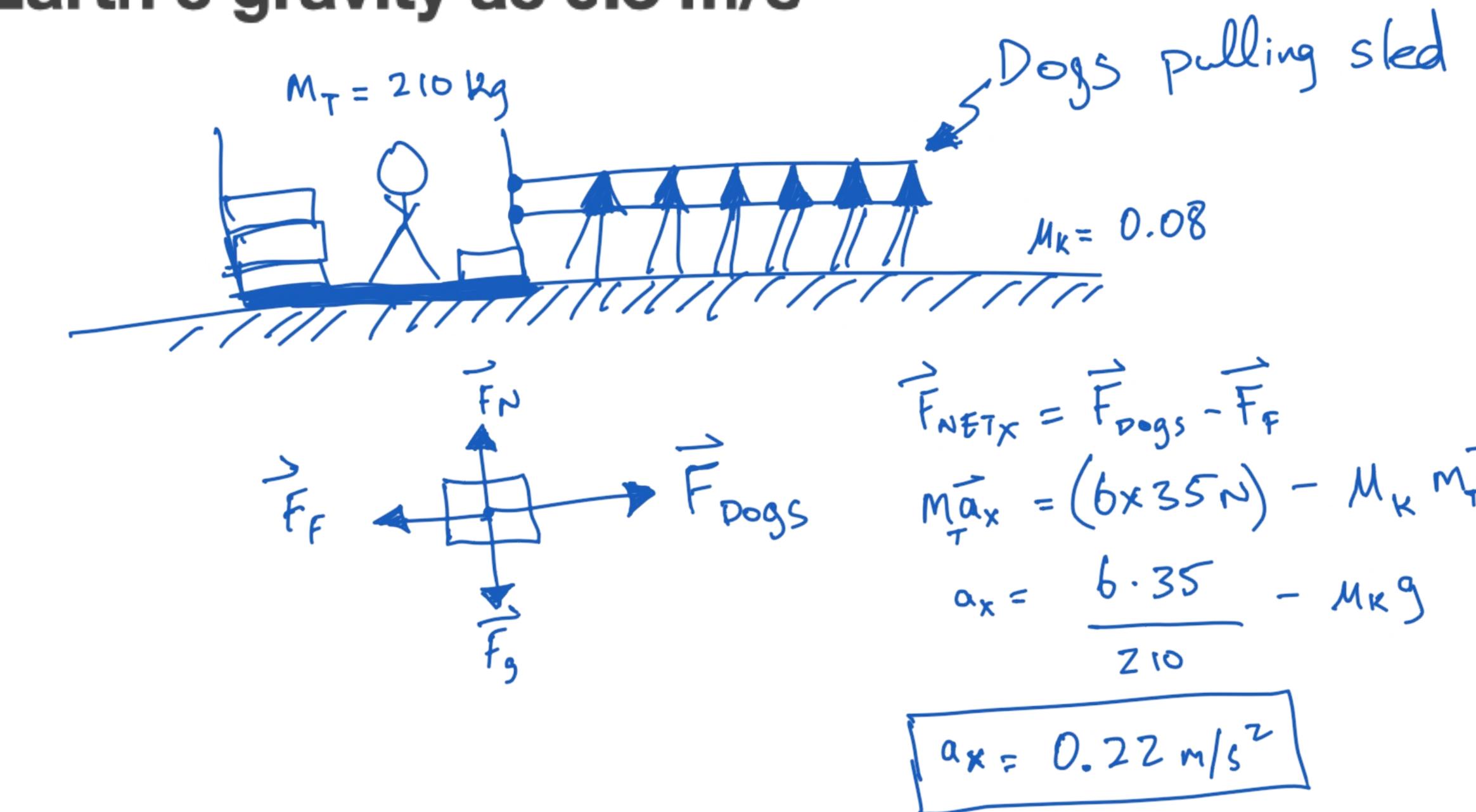
E

# CQ.7.5

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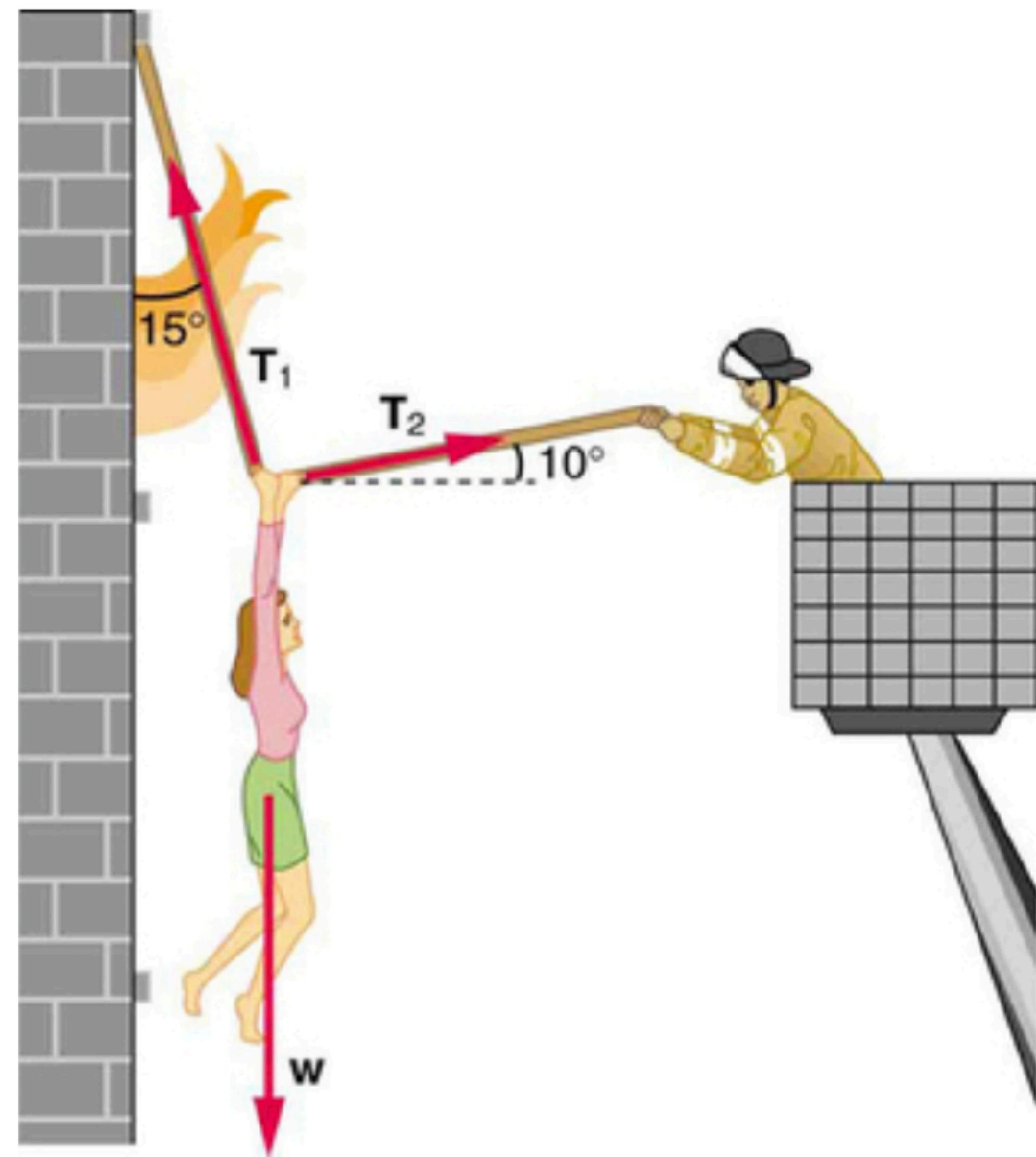


A      B      C      D      E

# Activity: Worked Problems

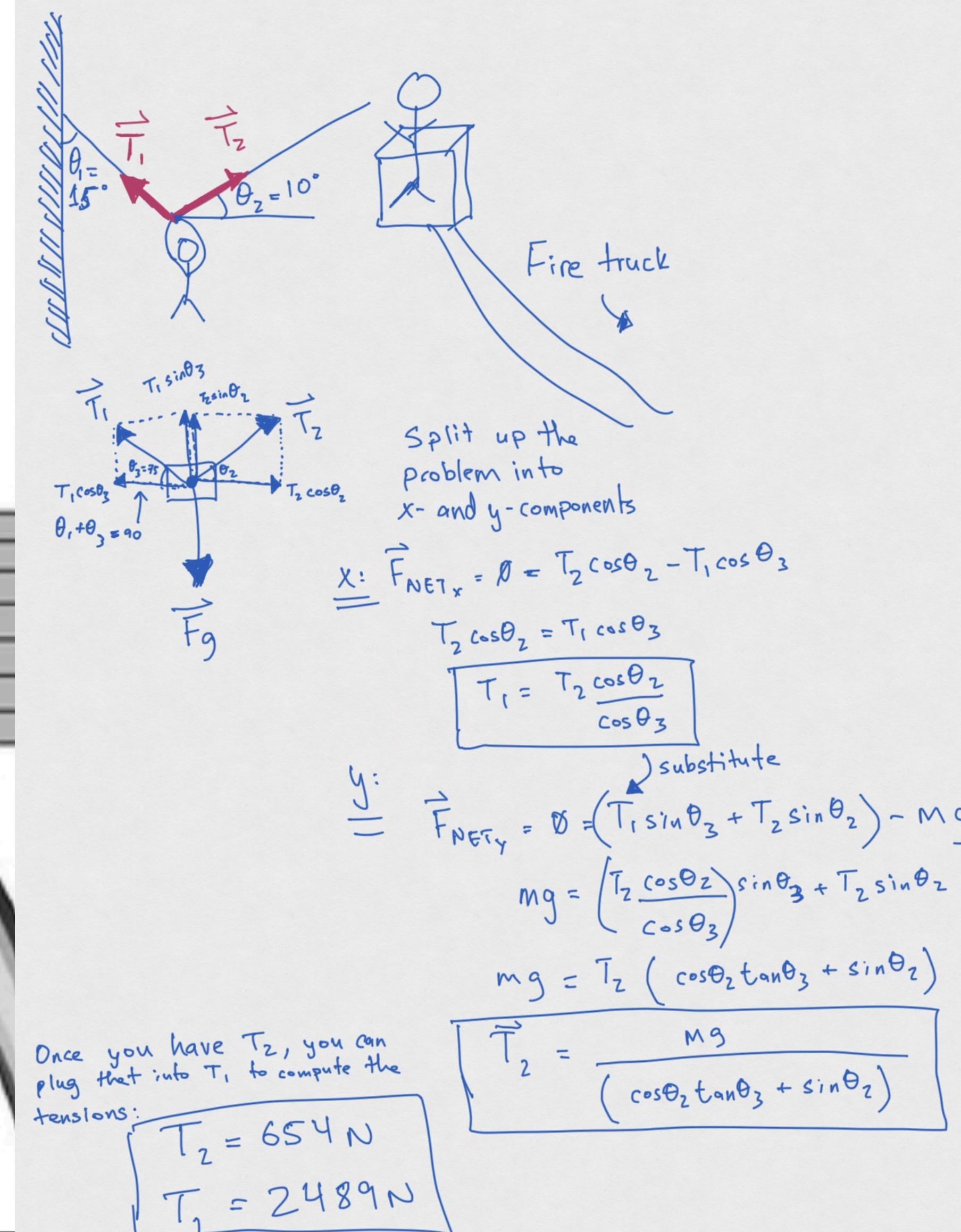
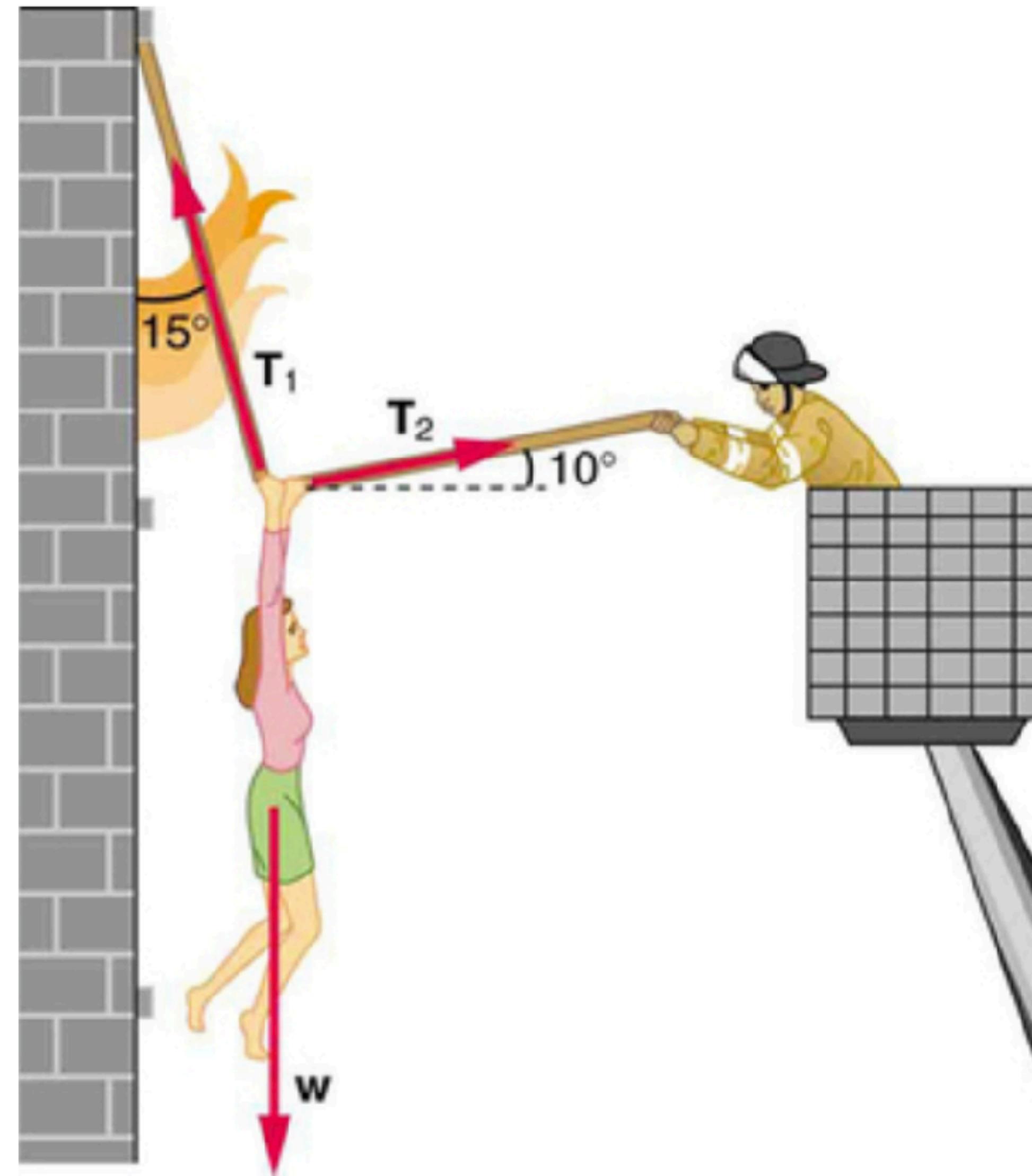
# WP 7.1

A 76.0-kg person is being pulled away from a burning building as shown in the figure. Calculate the tension in the two ropes if the person is momentarily motionless. Include a free-body diagram in your solution.



# WP 7.1

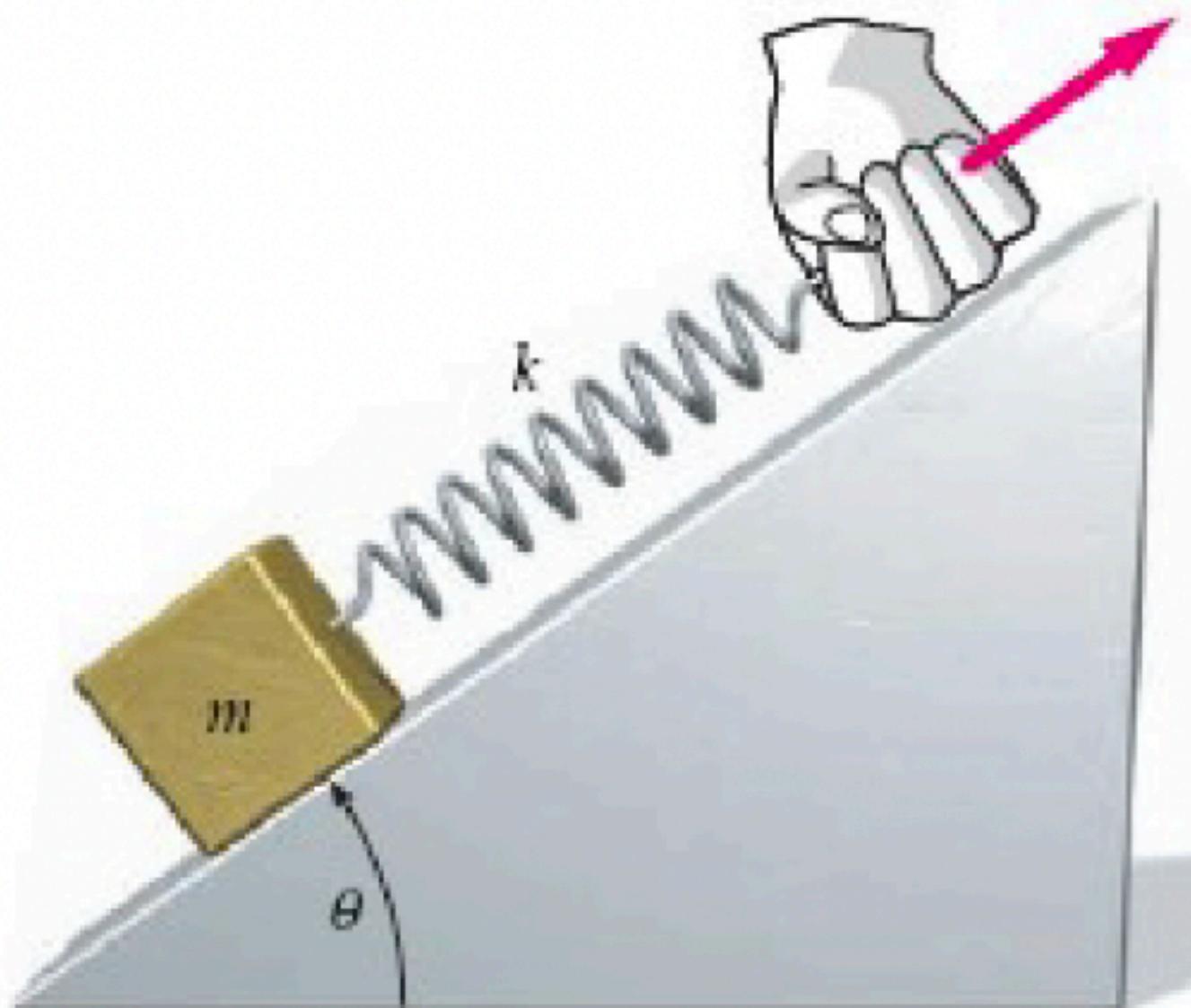
A 76.0-kg person is being pulled away from a burning building as shown in the figure. Calculate the tension in the two ropes if the person is momentarily motionless. Include a free-body diagram in your solution.



# HW 6.8

## HW6.8. Spring on Ramp

In the figure below  $m = 7 \text{ kg}$ ,  $\theta = 30^\circ$ , and  $k = 100 \text{ N/m}$ . In this problem assume that the ramp never moves and that there is friction between the block and the ramp.



**Part 1**

If the coefficient of static friction between the block and the ramp is  $\mu_s = 0.7$ , what is the maximum amount that the spring can be stretched beyond its equilibrium length before the block begins to slide up the ramp?

$x =$  number (rtol=0.05, atol=1e-08)      m ?

**Part 2**

Suppose now that the block is sliding up the ramp at a constant velocity. By what length is the spring stretched? Assume that the coefficient of kinetic friction is  $\mu_k = 0.39$ .

$x =$  number (rtol=0.05, atol=1e-08)      m ?

TIPS :

- Pay attention to signs!
- Force of spring-on-block is equal in magnitude, opposite in sign to the restoring force  $\vec{F}_r = -k\Delta\vec{x}$
- Draw the FBD accounting for all forces:
  - 1 Friction (down ramp)
  - 2 gravity
  - 3 spring on block
  - 4 Normal force

More tips :

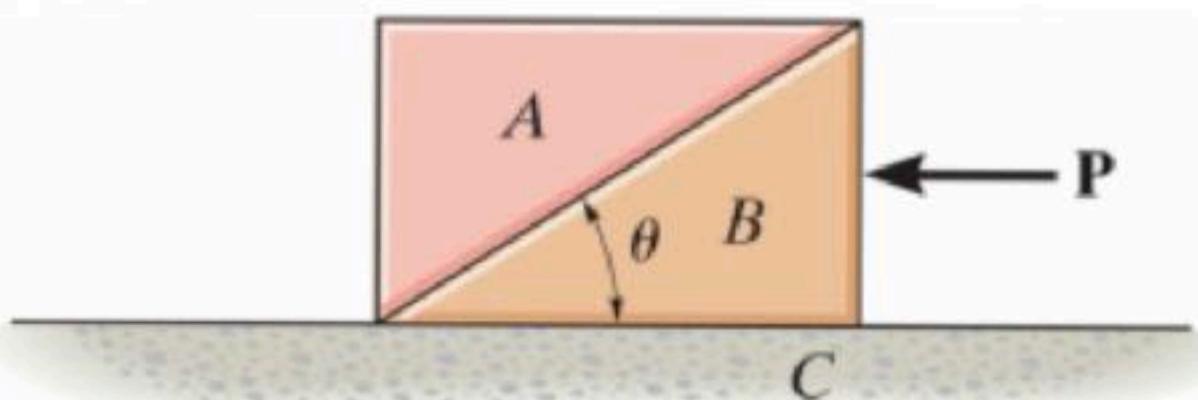
- The block will begin sliding up when  $\vec{F}_{NET} \neq 0$  so just before that, look at when  $\vec{F}_{NET} = 0$
- Constant velocity means no acceleration.
- Remember the difference between static and kinetic friction.

# HW 6.8

# HW 6.7

## HW6.8. Two Blocks Stacked

Blocks A and B each have a mass  $m = 10 \text{ kg}$ . The coefficient of static friction between A and B is  $\mu_s = 0.38$ . The angle shown is  $\theta = 33^\circ$ . Neglect any friction between B and C.



Determine the largest horizontal force  $\vec{P}$  that can be applied so that A will not slip on B.

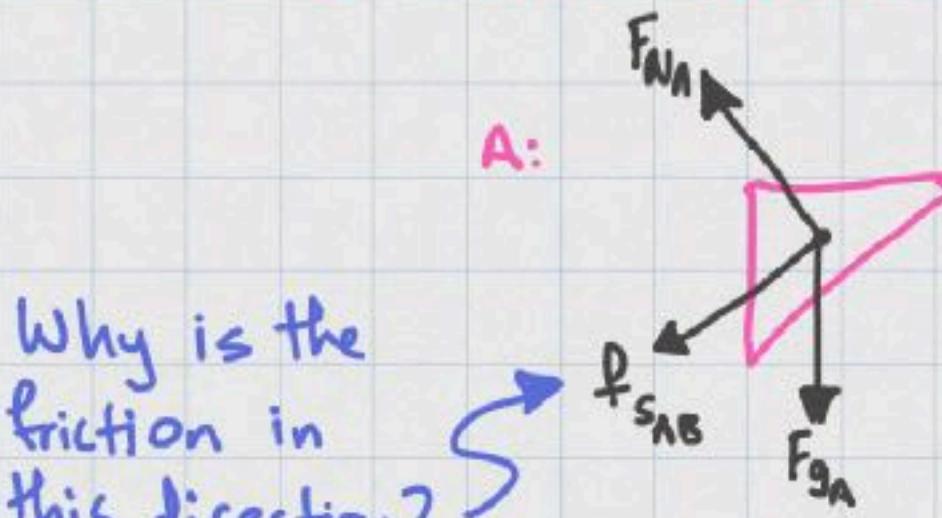
$$\vec{P} = 37.28$$

N

?

x 0%

① Draw separate FBDs for each Block



Why is the  
friction in  
this direction?

If Block B is  
pushed to the  
left, Block A  
will slide up  
the ramp if

$P$  is large enough!



Where did these  
forces come from?  
Ans: These are the  
Newton's 3rd Law  
Force Pairs

Remember  $F_{NA}$  is the  
force that changes  
as  $P$  increases (or decreases)

③ Consider the case where forces  
balance such that  $a_A = a_B = a$

**See you next class!**

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