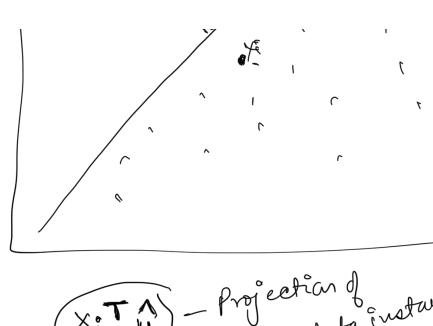
Principal Component Analysis.
Dimensionality Reduction
Latent variable Modeling (Hidden)
xi → one data instance xi € RD
Zi -> hidden/latent unknown variable.
J Zi € { 1,, K} clustering G Mixture of models
Y zi $\in \mathbb{R}^d$ where $d << D$
Ly This is a dimensionality reduction problem.
Civen X: [x,] find Z: [z,]

Such that "Some property is preserved.

0.20,0.10 0.35,0.40 0.50,0.20 0.65,0.10 0.70,0.60

Si vector



(XiTu) - Projection of instance

Let us assume that the data

has O mean.

has 0 mean.

$$\Rightarrow \sum_{i=1}^{N} x_i = 0$$

$$\text{var: } \sum_{i=1}^{N} (x_i T_u)^2$$

. N AT

This is the sample covariance

matrix of

$$S = \frac{1}{N} \sum_{i=1}^{N} x_i x_i^{T}$$

$$= \frac{1}{N} \sum_{i=1}^{N} x_i^{T} \sum_{i=1}^{N} x_i^{T}$$

$$= \frac{1}{N} \sum_{i=1}^{N} x_i^{T} \sum_{i=1}^{N} x_i^{T}$$

$$= \frac{1}{N} \sum_{i=1}^{N} x_i^{T} \sum_{i=1}^{N} x_i^{T} \sum_{i=1}^{N} x_i^{T}$$

$$= \frac{1}{N} \sum_{i=1}^{N} x_i^{T} \sum_{i=1}^{N} x_i$$

Wed May 05 PA3 due

PA3 due on May 9th (Sunday) at 11.59 PM

final exam for MPS Batch *
is on May 13th at 4.00 PM
4.00 - 6.00 PM

The state of the s

(Dx1) (Dx1)

(DxI) $\int \sum_{N \in I} (X_i^T u)^2$ $= \int \sum_{i=1}^{N} (u^T X_i^* x_i^* u)$

=
$$\frac{1}{1}$$
 $\frac{1}{1}$ $\frac{1$

Variance of projected data = Ü'Sü $= u^{\tau} \lambda u^{\eta}$ ニンガザか Variance along any eigenvector of S will be equal to the corresponding eigen value. First eigen vector gives the direction of maximum variance > First principal companent. For top L PCs:

$$Z = XW$$

$$(NXL) (NXD) (DXL)$$

$$X3 \begin{bmatrix} 7 & 3 \\ 2 & 4 \\ 1 & 8 \end{bmatrix}$$

$$X3 \begin{bmatrix} 10/3 & 5 \\ -1 & 3 \\ -7 & 3 \end{bmatrix}$$

$$R = 2 \cdot (L \times 1)$$

$$R = 2 \cdot (L \times 1)$$

Alhane Zi (LXI) $\hat{x}_i = WZ_i^i$ (DXI)

Fri May 7
Total
Variance
Variance

#PCs