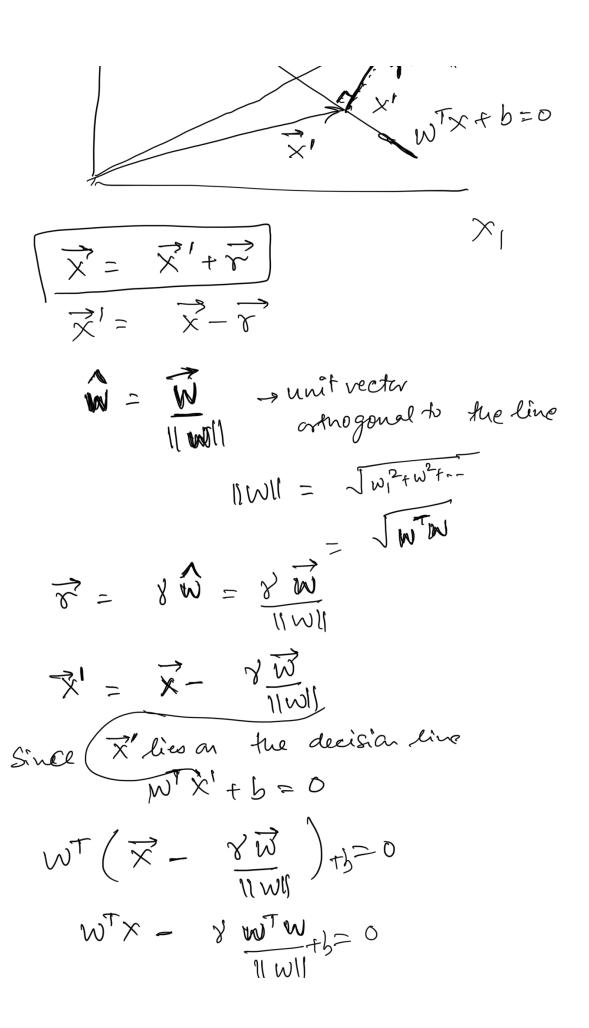
Support Vector Machines Mon Feb 22

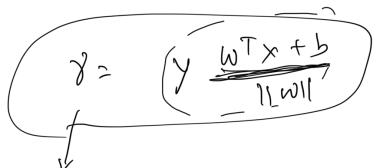
$$y = Sign(w^{T}x+1)$$

$$P(y=+1) = \frac{1}{1 + \exp(w^{T}x)}$$

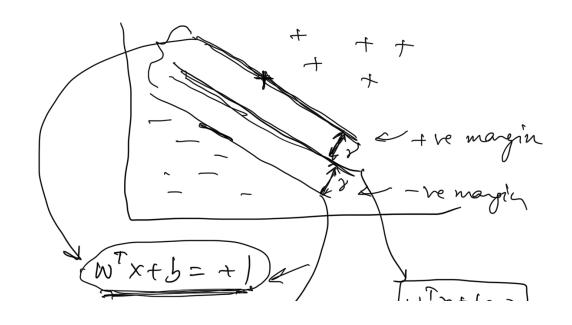
$$P(9=+1) \geq 0.5$$

$$P(y=+1) \geq 0.95$$





This is margin of an example.

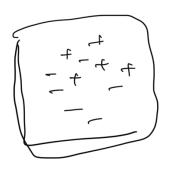




Distance between two margins:

will be





ith Praining example: Xi, Yi

If w, b has to correctly classify two instance

y: (wTx; +b) 20

If w, b have to be on the correct side of the margin;

Yi(w1xi+b) 21

Opt with equality constaints.

$$f(x,y) = x^{2} + 2y^{2} - 2$$

$$h(x,y) = x^{2} + 2y^{2} - 2 + \beta(x+y-1) = 0$$

$$2(x,y,\beta) = x^{2} + 2y^{2} - 2 + \beta(x+y-1) = 0$$

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$$x = x^{2} + 2y^{2} - 2 + \beta(x+y-1) = 0$$

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Wednesday Feb 24

$$\nabla f(w_1, w_2) = \lambda \nabla g(w_1, w_2)$$

$$g(w_1, w_2) = 0$$

$$V = f(w_1, w_2) + \lambda g(w_1, w_2)$$

$$\nabla f(w_1, w_2) + \lambda \nabla \xi g(w_1 w_2)$$

$$= 0$$

$$\nabla f(w_1, w_2) = 0$$

$$f(x,y) = x^{3} + y^{2}$$

$$g(x): x^{2} - 1 \le 0$$

$$L(x,y,x) = f(x,y) + \alpha f(x,y)$$

$$= x^{3} + y^{2} + \alpha (x^{2} - 1)$$

/ /

$$W = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$
win
$$W_1, w_2$$

$$S : t = (-1) \left(w_1 + w_2 + t_3 \right) < 0 \quad \forall i = 1$$

$$= 1 + w_1 + w_2 + t_3 \le 0 \quad \forall i = 1$$

$$1 - (ti) \left(2w_1 + 2w_2 + t_3 \right) \le 0 \quad \forall i = 1$$

$$1 - 2w_1 - 2w_2 - t_3 \le 0$$

$$1 - 2w_1 - 2w_2 - t_3 \le 0$$

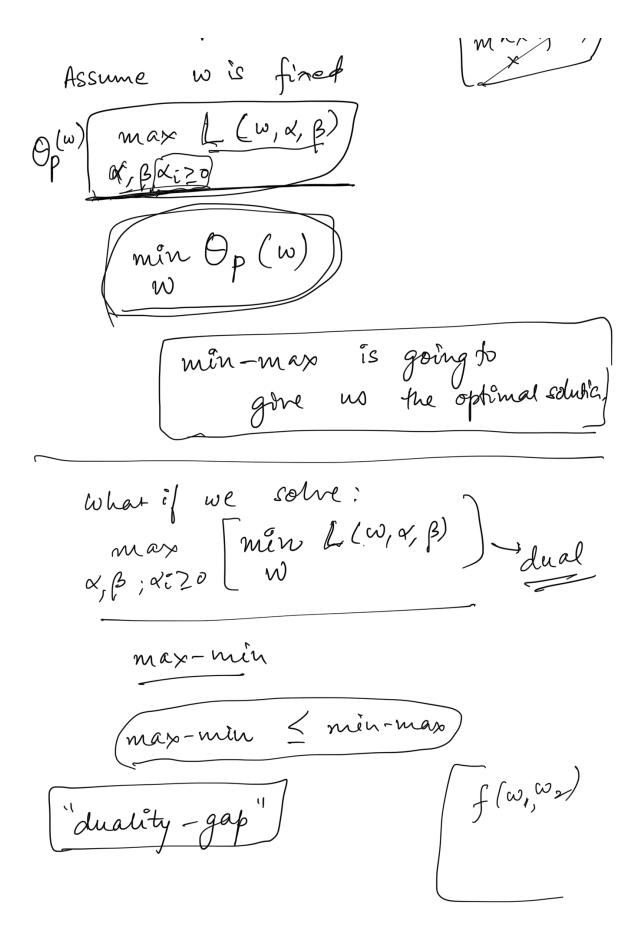
$$2L$$

$$2L$$

$$2w_1 - 2w_2 - t_3 \le 0$$

[(w, x, B)

I am ECA)



$$L_{p} = \frac{\|\mathbf{w}\|^{2}}{2} + \sum_{i=1}^{N} \mathbf{x}_{i}^{*} \underbrace{\{ [-y_{i}^{*}(\mathbf{w}^{T}\mathbf{x}_{i}^{*} + b) \}}]}_{i=1}^{N}$$

$$= \mathbf{w} - \sum_{i=1}^{N} \mathbf{x}_{i}^{*} \mathbf{x}_{i}^{*}$$

$$= \mathbf{w} - \sum_{i=1}^{N} \mathbf{x}_{i}^{*} \mathbf{x}_{i}^{*}$$

$$= \mathbf{w} - \sum_{i=1}^{N} \mathbf{x}_{i}^{*} \mathbf{x}_{i}^{*}$$

$$= \sum_{i=1}^{N} \mathbf{x}_{i}^{*} \mathbf{y}_{i}^{*} \mathbf{x}_{i}^{*}$$

$$Lp = \frac{||w||^2}{2} + \sum_{i=1}^{2} \frac{1 - y_i (w^{7}x_i + b)^2}{2}$$

$$= \frac{1}{2} w^{7}w + \sum_{i=1}^{2} \frac{1 - y_i (w^{7}x_i + b)^2}{2}$$
Replace w with $\sum_{i=1}^{2} x_i y_i x_i$

Solve the dual to get wish and freed the x's to get W

Friday Feb 26 $(\omega^T x + b)$ $J(w) \text{ min.} \frac{||w||^2}{2}$ $w, b \qquad 2$ $s.t \quad 1 - \left[y_i(\omega^T x_i + b)\right] \leq 0 \text{ i.e.} N$

$$\frac{1}{2} \left[\sum_{i=1}^{N} (w_{i}, b_{i}, \mathbf{x})^{2} + \sum_{i=1}^{N} x_{i}^{2} \left\{ 1 - y_{i}^{2} (w_{i}^{T} x_{i}^{2} + b_{i}) \right\} \right]$$

$$S. + \left[x_{i}^{2} \geq 0 \right] = 1, ..., N$$

Primal

 $W = \sum_{i=1}^{N} \langle i \rangle_i \times_i^{\circ}$

$$\begin{array}{c} \left(\begin{array}{c} x_{1} & , y_{1} \\ x_{2} & , y_{2} \end{array}\right) & N=2 \\ \left(\begin{array}{c} x_{1} & x_{1} & y_{1} & y_{1} & x_{1} \\ x_{2} & x_{1} & y_{1} & y_{2} & x_{1} \\ & + & x_{2} & x_{1} & y_{2} & y_{2} & x_{2} \\ & + & x_{2} & x_{1} & y_{2} & x_{2} \end{array}\right) \\ & S. t & x_{1} & y_{1} + x_{2} & y_{2} = 0 \\ & \text{and} & x_{1} & x_{2} & 0 \\ & \text{and} & x_{2} & x_{2} & 0 \end{array}$$

$$\begin{array}{c} x_{1} & x_{1} & x_{1} & x_{2} \\ & + & x_{2} & x_{1} & x_{2} \\ & x_{2} & x_{2} & x_{2} & x_{2} \end{array}$$

$$S. t & x_{1} & y_{1} + x_{2} & y_{2} = 0 \\ & \text{and} & x_{1} & x_{2} & 0 \\ & \text{and} & x_{2} & x_{2} & 0 \end{array}$$

Find &, and & hat maximize LD(X) $\alpha_{i}^{*}, \alpha_{v}^{*}$ $W = \mathbb{Z}_{1}^{*} \mathbb{Y}_{1} \mathbb{X}_{1} + \mathbb{Z}_{2}^{*} \mathbb{Y}_{2} \mathbb{X}_{2}$

$$b^2 = \frac{w^T x_1 + w^T x_2}{2}$$

For a test instance x^* y^*-9 $y^*= \text{Sign}(w^{T}x^*+b)$ $= \text{Sign}((\sum \alpha_i \gamma_i x_i)^{T}x^*+b)$ $= \text{Sign}((\sum \alpha_i \gamma_i x_i)^{T}x^*+b)$

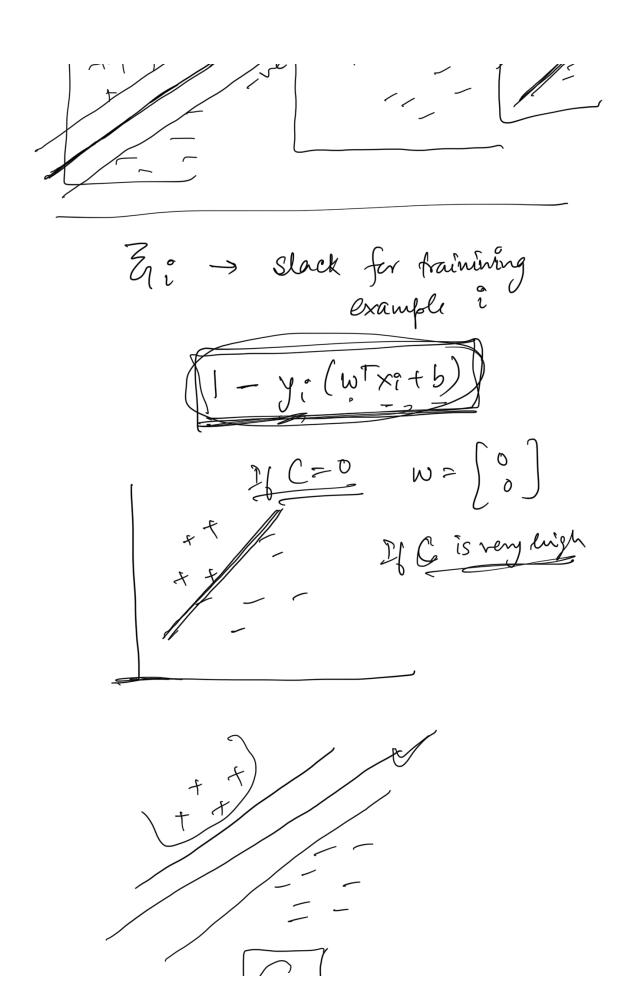
J(w,b) Lp(w,b,x) Lp(X)

KKT#5 X: (1-y: \(\omega \omega \tau \right) = 0

For any xi that lies on one the

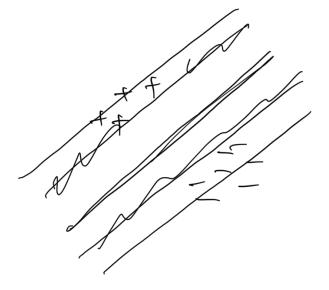
margins. Yi & WTXi+bb= and for any xi that does not lie on the margin;

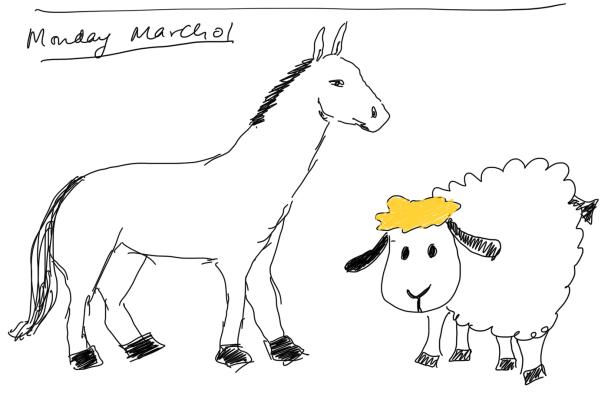
Yi & will be 0 y = sign(WTx = b) = Sign ((\(\int \times i \) \(\int \times i \) \(\int \times i \) = Sign (\(\sum_{\text{N}} \times_{\text{N}} \t) *= sign (\(\int x_i \tau_i





(Bias-Variance Tradeoff)





min L(W,6) = || W||2+ C\frac{N}{3}i

Sheep

Sit Si(WTXi+b) > 1- Zi;

Zi 20

Sheep

Sheep

bias-vaniance fradeoff